Hierarchical Discrete Event Supervisory Control of Aircraft Propulsion Systems

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This paper presents a hierarchical application of Discrete Event Supervisory (DES) control theory for intelligent decision and control of a twin-engine aircraft propulsion system. A dual layer hierarchical DES controller is designed to supervise and coordinate the operation of two engines of the propulsion system. The two engines are individually controlled to achieve enhanced performance and reliability, necessary for fulfilling the mission objectives. Each engine is operated under a continuously varying control system that maintains the specified performance and a local discrete-event supervisor for condition monitoring and life extending control. A global upper level DES controller is designed for load balancing and overall health management of the propulsion system.

I. Introduction

Discrete-event dynamic behavior of physical plants is often modeled as regular languages\(^1,2\) that can be realized by finite-state automata.\(^3\) This paper focuses on the development of intelligent decision and control algorithms based on the theory of Discrete Event Supervisory (DES) control on twin-engine aircraft propulsion systems. This work extends the research in the DES field and adds validity to its theory.

The DES control system is designed to be hierarchically structured. Each engine’s continuously varying controller interacts with its own local DES controller for detailed health monitoring and intelligent control. The operational information is abstracted and reported to the coordinator for propulsion or mission level DES control of the two engines. Furthermore, the propulsion level DES controller allows for interaction with external inputs such as those from a pilot, aircraft components (e.g. flight control, etc.), and other vehicle management systems, resulting in flexibility for making on-line modifications in the mission objectives. The uniqueness of this DES control approach is that the control policy can be adaptively updated on-line at both the engine and propulsion coordinator levels, and the system is tolerant of small components faults.

Although DES control has been developed for quite some time, there are only a few application examples.\(^4,5\) It is primarily because no quantitative analytical tool has been established to help design and evaluate the DES controllers. This research is the first time hierarchical DES control is used on a complex non-linear dynamical system, such as an aircraft.
The objective of the paper is to apply hierarchical Discrete Event Supervisory (DES) control theory for intelligent decision and control of a twin-engine aircraft propulsion system. In this paper, the following has been demonstrated:

1. DES control can be used for intelligent decision and control of twin-engine aircraft propulsion systems e.g. the problem of load balancing between various engines.
2. Implementation of DES control can reduce the accumulated engine damage and thus extend the life of the aircraft engine.
3. DES control is helpful in improving the overall mission success and operational behavior.

In this paper the terms controller and supervisor are used interchangeably, also the phrases “Upper Level” and “Propulsion Level” are synonymous and similarly the phrases “Lower Level” and “Engine Level” are synonymous. The paper is organized in six sections including the present one. Section II describes the simulation setup. Section III summarizes the DES control techniques. Section IV discusses the design of the engine level and propulsion level DES controller. The simulation results are examined in section V, and the paper is concluded in section VI.

II. Simulation Setup

In this section the implementation of Discrete Event Supervisory (DES) control on a commercial turbofan engine model simulation is discussed. The objective of such an application is to validate the hierarchical DES control technique with a real world complex non-linear dynamical system. The overall system structure will be explained first, followed by a description of the two hierarchical levels of the system including their internal components.

A. Overall Simulation Testbed Architecture

A hierarchical DES controlled propulsion system has been designed and tested on a simulation test bed that consists of three networked computers using the client/server concept, refer to Figure 1. Computer 1 is the upper level propulsion system coordinator responsible for load balancing, intelligent decision making and health monitoring of the engines. Each of the other two computers, Computer 2 and Computer 3, runs its own copy of a gas turbine engine simulation (differing from each other only through such performance-related parameters as component efficiencies, etc.), including its continuously varying control system and a local discrete-event supervisor. Each of the engine simulators integrates the event-driven discrete dynamics modeled by a finite-state automaton as well as time-driven continuous dynamics modeled by ordinary differential equations through continuous-discrete and discrete-continuous interfaces. The test bed is capable of simulating different dynamics for each individual engine based on performance-related parameters and operating conditions.

As can be seen in Figure 1, the simulation architecture can be expanded to include more engines that would run in parallel with Computers 2 and 3. It could also be expanded to include higher levels of control. For example, there could be a level above Computer 1 that controls propulsion in parallel with flight control. In this sense, hierarchical DES could be applied to any number of complex systems and missions.
B. Engine Level DES Control

Figure 2 shows the architecture of the engine level plant and DES controller implementation, which is replicated on Computer 2 and Computer 3. This section will briefly address the main points. For more detailed explanations, refer to reference 6.

In order to implement the DES control in tandem with the gas turbine engine simulation program (written in FORTRAN), a C++ interface was written. The C++ wrapper interfaces the major inputs/outputs of the engine simulation and makes it function just like a simulation running in the C++ environment.

The turbofan engine simulation was designed for full flight envelope operation. With the proper inputs such as power lever angle (PLA or pilot throttle input), and ambient condition (altitude and speed or temperature and pressure), the FORTRAN simulation program simulates the complex operation of the engine from transient to some steady state running condition with large order differential and difference equations. This simulation is a stand-alone program with its own continuous time gain scheduled controller. From the engine simulation, important sensor data such as combustion chamber temperature and high-pressure turbine speed, together with other important information, such as the simulation step size and the simulation cycle number are collected by the C++ wrapper program exchanged with the DES controller through the Message API (Application Programming Interface) communication routine.

The engine level DES controller design has two important components, refer to Figure 2. One is the Event Generator and the other is the Action Generator (which resides on the Server). The Event Generator is the module which receives continuous time sensor data from the plant. This data along with other information, such as estimated state and external inputs are used by this module to generate events, which in turn are inputs to an open-loop DES model of engine operation. The open-loop DES model is constructed based on the operating scenario. The details of the modeling are discussed in section IV. The state-based Deterministic Finite State Automata (DFSA) model serves as state estimator and provides important state and event (both controllable and uncontrollable) information for the discrete-event supervisor to take proper action. Event behavior in the state-based DFSA model only depends on the state where the event is defined and does not depend on the history of how the state was reached.

The DES controller represents the control policy applied to the DFSA model of engine operation, and it could be an ad hoc DES controller based on experience or a discrete-event supervisor designed by the control techniques discussed in section III and IV. The DES controller takes the estimated state as input and generates control commands (controllable event disabling or enabling) as outputs. The control commands are sent through a Message API communication routine to the Action Generator. The primary task of Action Generator is to convert control commands from the supervisor into necessary simulation input for the continuously varying plant (altitude and mach).

C. Propulsion Level DES Control

Figure 3 shows the structure of the propulsion level DES controller together with its own Event Generator. This structure is implemented on a separate computer (Computer 1) which uses the messaging interface to communicate with the other two computers. The Higher Level Supervisor is a DES controller. If expanded graphically, it would be similar to the Client on the Engine Level design.

The software architecture of the simulation test bed is flexible to adapt arbitrary DFSA models and controller designs which make it portable to other complex dynamic systems.
III. Review of Language Measure Concepts

This section reviews the previous work on language measure. It provides the background information necessary to develop a performance index.

Let the dynamical behavior of a physical plant be modeled as a deterministic finite state automaton (DFSA) \( G_i \equiv (Q, \Sigma, \delta, q_i, Q_m) \) with \( |Q| = n \) and \( |\Sigma| = m \). Here \( Q = \{q_0, q_1, \ldots, q_n\} \) is a finite set of states with \( q_0 \) the initial state; \( \Sigma \) is a finite alphabet of events; \( \delta \) is a function from \( Q \times \Sigma \) to \( Q \) (the transition function); and \( Q_m \subseteq Q \) is the set of marked states. Additionally, \( \Sigma^* \) is the set of all strings over \( \Sigma \).

**Definition 1**: A DFSA \( G_i \), initialized at \( q_i \in Q \), generates the language \( L(G_i) \equiv \{s \in \Sigma^*: \delta^*(q_i, s) \in Q\} \) and its marked sublanguage \( L_m(G_i) \equiv \{s \in \Sigma^*: \delta^*(q_i, s) \in Q_m\} \).

**Definition 2**: The language of all strings that, starting at \( q_i \in Q \), and terminating at \( q_j \in Q \), is denoted as \( L(q_i, q_j) \).

**Definition 3**: The characteristic function that assigns a signed real weight to state-partitioned sublanguages \( L(q_i, q_j) \) is defined as: \( \chi: Q \rightarrow [-1, 1] \) such that

\[
\chi_j = \chi(q_j) = \begin{cases} 
-1, & \text{if } q_j \in Q_m^- \\
0, & \text{if } q_j \in Q_m^+ \text{ independent of } q_i \\
0, & \text{if } q_j \in Q_m^+ 
\end{cases}
\]

The \((n \times 1)\) characteristic vector is denoted as:

\[
\vec{\chi} = [\chi_1 \chi_2 \cdots \chi_n]^T.
\]

**Definition 4**: The event cost is defined as \( \tilde{\pi}: \Sigma^* \times Q \rightarrow [0,1) \) such that \( \forall q_j \in Q, \forall \sigma_k \in \Sigma, \forall s \in \Sigma^* \),

- \( \tilde{\pi} [\sigma_k | q_j] = 0 \) if \( \delta(q_j, \sigma_k) \) is undefined; \( \tilde{\pi} [ \varepsilon | q_j] = 1 \), where \( \varepsilon \) is the empty (zero length) string;
- \( \tilde{\pi} [\sigma_k | q_j] = \tilde{\pi}_{jk} \in [0,1); \sum_k \tilde{\pi}_{jk} < 1; \)
- \( \tilde{\pi} [\sigma_k s | q_j] = \tilde{\pi} [\sigma_k | q_j] \tilde{\pi} [s | \delta(q_j, \sigma_k)] \).

The \((n \times m)\) event cost matrix is denoted as: \( \tilde{\Pi} \equiv [\tilde{\pi}_{ij}] \).

**Definition 5**: The state transition cost of the DFSA is defined as a function \( \pi: Q \times Q \rightarrow [0,1) \) such that \( \forall q_j, q_k \in Q \), \( \pi(q_k | q_j) = \sum_{\sigma \in \Sigma: \delta(q_j, \sigma) = q_k} \tilde{\pi}(\sigma | q_j) \equiv \pi_{jk} \) and \( \pi_{jk} = 0 \) if \( \{\sigma \in \Sigma: \delta(q_j, \sigma)\} = \emptyset \).

The \(n \times n\) state transition cost matrix, denoted as \( \Pi \), is defined as:

\[
\Pi = \begin{bmatrix}
\pi_{11} & \pi_{12} & \cdots & \pi_{1n} \\
\pi_{21} & \pi_{22} & \cdots & \pi_{2n} \\
\vdots & \ddots & \ddots & \vdots \\
\pi_{n1} & \pi_{n2} & \cdots & \pi_{nn}
\end{bmatrix}
\]
**Definition 6:** The signed real measure $\mu$ of a singleton string set $\{s\}$ is defined as:

$$\mu(\{s\}) \equiv \chi(q_i) \pi_i(s | q_i) \quad \forall s \in L(q_i, q_j) \subseteq L(G_i).$$

The signed real measure of $L(q_i, q_j)$ is defined as:

$$\mu(L(q_i, q_j)) \equiv \left( \sum_{s \in L(q_i, q_j)} \mu(\{s\}) \right).$$

The signed real measure of a DFSA $G_i$, initialized at the state $q_i \in Q$, is defined as

$$\mu_i \equiv \mu(L(G_i)) = \sum_{j} \mu(L(q_i, q_j)).$$

The $n \times 1$ real signed measure vector is denoted as:

$$\mu \equiv [\mu_1 \quad \mu_2 \quad \ldots \quad \mu_n]^T$$

In reference 5, it has been shown that the measure of the language $L(G_i)$, where $G_i = (Q, \Sigma, \delta, q_i, O_m)$ can be expressed as: $\mu_i = \sum_j \pi ij \mu_j + \chi i$. Equivalently, in vector notation: $\mu = \Pi \mu + \chi$. Since $\Pi$ is a contraction operator, the measure vector $\mu$ is uniquely determined as:

$$\mu = (I - \Pi)^{-1} \chi$$

(1)
IV. DES controllers

One of the major tasks of this paper is fusion of the (possibly) redundant, conflicting and incomplete information to make timely decisions. Such information can be derived from different types of sensor data as well as operational history and the knowledge base generated from pilots’ personal experience. Computer-based advanced analytical techniques are necessary for fusion of the time series data available from multiple sensors and the relevant non-sensor-based information (e.g. weather data, analytical damage model data) to make specific inferences that could not be achieved by the use of single sensors alone. However, improved performance may not result simply from an increased volume of sensor data and engine information unless the ensemble of information is systematically processed in the context of the engine operational conditions and mission objectives. In essence, fusion of the heterogeneous information is necessary to:

1. Guarantee improvement of resolution and reduction of ambiguity in decision and control.
2. Make advantageous trade-offs between probability of false alarms and missed detections.

The open-loop discrete event dynamics are modeled as a Discrete Finite State Automaton (DFSA) based on the postulated engine operating scenario. The model may vary for different mission scenarios. The DFSA plant model assumes that an aircraft equipped with twin turbofan engines is carrying out a routine surveillance mission. Abortion of the mission is allowed at certain states when an anomaly is detected in the engine. Each engine of the aircraft is equipped with a continuous time controller which is supervised by a local DES controller. The primary objective of the local Engine level DES controller is to strike the right balance between the conflicting demands of higher performance from a higher level DES and limiting the damage (stress-related damage modes) to the engine. The upper Propulsion level DES controller redistributes the load depending on the health of the engine and thrust demand of the pilot.

A. Engine Level DES control

Figure 4 presents the DFSA model of the engine operation discrete-event supervisory control for an individual engine, whereas Figure 5 shows the associated DES controller, which is derived from the engine model. The state and the event list are presented as tables A-1 through A-4 in the appendix of the paper (C denotes controllable events and UC denotes uncontrollable events). The engine can operate in two regimes, one is a high performance regime (state q3) where the damage rate is high, and the other is a low performance regime (state q5) where the damage rate is low. In the high performance regime the engine has a tendency of going to state q4 where state variables like combustor temperature have been observed to have oscillatory behavior. This is extremely harmful in terms of engine health and must be avoided. The engine level controller chooses the regime of operation (q3 or q5) depending on two factors: (1) Thrust demand from upper level DES, and (2) Health of the engine (as formulated below).

In the context of this paper, “health” specifically refers to structural health, i.e. the remaining life of the engine or its components. Life is consumed by thermal and/or structural loads that result in engine “damage.” The health of the engine is determined by the damage accumulated over the period of operation.

Figure 4.—Engine Level DES plant model.

Figure 5.—Engine Level DES controller model.
Damage accumulation has two components. It is formulated as a function of high-pressure turbine gas inlet temperature and shaft speed. In addition, at random time intervals, damage spikes (sudden jumps) are introduced to simulate sudden events of unspecified cause resulting in damage accumulation in the engine.

B. Propulsion level DES Control

The main task of the upper level DES controller is to redistribute the load between two engines depending on the current health of each engine and the thrust demand of the pilot. The states and the event list are presented in table A-3 and A-4 of the appendix. A graphical representation for the propulsion level DES controller, such as Figure 5 for the engine level controller, is provided in the appendix as Figure A-1. Due to the complexity of the propulsion level system, the figure is not fully labeled.

V. Simulation Experiments: Results and Discussion

The experimentation setup for the DES simulator is designed on the engine simulation test bed to validate the DES control concept. Upon successful implementation of the software modules (discussed in section II) on the client and server computers, two sets of experiments were performed. The first set of experiments was performed on the engine level DES controller to validate that implementation of DES control reduces the engine damage and thus extends engine life. The second set of experiments was performed on the Propulsion Level DES to validate that it judiciously balances engine load for the two engines. Afterwards, the DES controller performance is analyzed.

A. Engine Level DES Test

Both unsupervised and supervised plants are excited by the same predetermined fixed input shown in Figure 6. To make a comparison between the supervised and the unsupervised cases several outputs (Combustor temperature, high pressure turbine speed, net thrust of the engine and fuel flow through the main burner) of the engine simulation were observed over a period of 12 minutes. Figures 7 and 8 show the simulation outputs for the unsupervised and supervised cases respectively.

![Figure 6.—Power Lever Angle input.](image-url)
The comparison of two figures indicates that the DES controller applied in the engine level eliminates the high frequency oscillations which are observed in the unsupervised case. High frequency oscillations are modeled as the primary source of damage to the turbine blades and adversely affect the overall health of the engine.

B. Propulsion Level DES Test

The propulsion level DES controller has two main tasks. One is the intelligent decision making and control of twin-engine aircraft propulsion systems and the second is to improve the overall mission and operational behavior so that engine health is maintained. These can be demonstrated through intelligent load balancing. The issue of load balancing becomes especially important when the health conditions of two engines are significantly different (one can be called in “bad” condition and in “good” condition). For this scenario, the aim of the DES controller is judicious redistribution of the load between two engines such that the “bad” engine carries lower load than the “good” one, subject to the condition that the total thrust output of the engines remains same. Figures 9 and 10 show the simulation inputs/outputs of each of the two engines. Initially in region (1), both engines are in “good” condition. As the mission progresses, Engine 2 suffers a sudden damage-inducing event, i.e. the condition of Engine 2 becomes “bad” (as indicated by the discrete damage increment spike at approx 325s; this unexplained event facilitates the demonstration of the Propulsion level DES). At this point (entering region (2)), the propulsion level DES redistributes the load such that Engine 1 carries a higher load than the damaged Engine 2, (as can be seen by comparing Figures 9 and 10). At approx 625s, Engine 1 goes “bad” (as indicated by the discrete damage increment spike on Figure 9). Entering region (3), both Engine 1 and Engine 2 are considered to be in “bad” condition, thus the propulsion level DES controller balances the load approximately equally between the two.
C. DES Controller Performance Measure

To observe the impact of the propulsion level DES controller on the overall mission, the concept of “language measure,” described in section III is used. Language measure gives a theoretical performance measure (equation (1) from section III) of the controllers, given the state weights ($\gamma$) and the state transition probabilities ($\Pi$). To form the state transition probability matrix $\Pi$, 50 experimental runs were conducted for both supervised and unsupervised cases. The $\Pi$ matrices for the engine level and propulsion level DES controllers are presented in the appendix as Table A-5 and A-6.
Given the vector for the state weights of the engine level as \( \chi = [0 \ 0 \ 0.2 \ -0.1 \ 0.2 \ -0.5] \) (designed by the control engineer), the theoretical language measure for the unsupervised plant and supervised plant are computed from equation (1) to be:

\[
\mu_{\text{unsupervised}} = 4.603 \quad \text{and} \quad \mu_{\text{supervised}} = 6.3678.
\]

Improved performance is a positive gain in the language measure. Therefore, the engine level DES controller improves the performance of the open loop plant.

For the propulsion level DES controller the weights of the states are selected according to their importance to the mission management as \( \chi = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ -1 \ -0.2 \ 0.2 \ 0 \ 0] \). Table 1 shows the experimental results of the number of visits to the states which have weights other than 0. These are State 8: Plane destroyed, State 9: Mission abort, State 10: Mission successful. They have relative weights of -1, -0.2 and 0.2 respectively. The language measures, i.e. the theoretical performance of the controllers are calculated as:

\[
\mu_{\text{unsupervised}} = -2.7999 \quad \text{and} \quad \mu_{\text{supervised}} = -1.6003,
\]

which indicate that the propulsion level DES controller improves mission performance.

Experimental outcomes, shown in Table 1, can also be used to evaluate the DES controller performance directly by multiplying each state visit with the relative weight of the state. The experimental performances of the propulsion level controllers are:

- Unsupervised: \( 1 \times (-1) + 15 \times (-0.2) + 34 \times (0.2) = 2.8 \)
- Supervised: \( 1 \times (-1) + 8 \times (-0.2) + 41 \times (0.2) = 5.6 \)

Once again, a positive gain is observed, which confirms that the supervised plant performs better than the unsupervised plant, indicating an overall improvement of the mission performance. A similar experimental calculation for the engine level controllers is not shown because there is no mission behavior element in the engine level.

### VI. Conclusions

This paper presents a quantitative approach to synthesis of a hierarchical discrete-event supervisory (DES) control of an aircraft propulsion system. The DES control law has been validated on a networked simulation test bed. The plant dynamics in the simulation test bed are built upon the model of a generic gas turbine engine. The software architecture of the simulation test bed is flexible to adapt arbitrary DFSA models and controller designs and to fit other complex systems. The supervisory control laws are quantitatively analyzed using a language measure.\(^7,8\)

The long-term objectives of the proposed approach are to achieve: (i) intelligent decision and control of distributed propulsion management systems, where each of the engines has its own local DES control; (ii) structural damage reduction and life extension of aircraft engines without any significant loss of the system performance; and (iii) decision making and mission planning modifications through a high-level DES coordinator; (iv) extension of this work to other complex dynamic systems such as Rotorcraft, power plants, and spacecraft simulation test-beds. Future work includes incorporation of optimal control laws.\(^5\)
## Appendix

Table A-1.—State List for the engine level DES supervisor.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>Status</th>
</tr>
</thead>
<tbody>
<tr>
<td>q₁</td>
<td>Engine Start</td>
<td></td>
</tr>
<tr>
<td>q₂</td>
<td>Engine Warm up</td>
<td></td>
</tr>
<tr>
<td>q₃</td>
<td>High Performance/ High damage rate</td>
<td>Marked (good)</td>
</tr>
<tr>
<td>q₄</td>
<td>Oscillations</td>
<td>Marked (bad)</td>
</tr>
<tr>
<td>q₅</td>
<td>Low Performance/ low damage rate</td>
<td>Marked (good)</td>
</tr>
<tr>
<td>q₆</td>
<td>Engine inoperable</td>
<td>Marked (worst)</td>
</tr>
<tr>
<td>q₇</td>
<td>Low Performance/ high damage rate</td>
<td>Marked (bad)</td>
</tr>
</tbody>
</table>

Table A-2.—Event List for the engine level DES supervisor.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>Status</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>Start</td>
<td>C</td>
</tr>
<tr>
<td>b</td>
<td>Warm up complete</td>
<td>UC</td>
</tr>
<tr>
<td>c</td>
<td>Shut down the engine</td>
<td>UC</td>
</tr>
<tr>
<td>d</td>
<td>Detection of oscillations</td>
<td>UC</td>
</tr>
<tr>
<td>e</td>
<td>Nozzle area reduction</td>
<td>C</td>
</tr>
<tr>
<td>f</td>
<td>Engine fails</td>
<td>UC</td>
</tr>
<tr>
<td>g</td>
<td>Reduce performance /reduce damage</td>
<td>C</td>
</tr>
<tr>
<td>h</td>
<td>Increase performance/ increase damage</td>
<td>C</td>
</tr>
<tr>
<td>i</td>
<td>Remain in the state</td>
<td>C</td>
</tr>
<tr>
<td>j</td>
<td>Reduce performance</td>
<td>C</td>
</tr>
<tr>
<td>k</td>
<td>Increase performance</td>
<td>C</td>
</tr>
<tr>
<td>l</td>
<td>Increase damage rate</td>
<td>C</td>
</tr>
<tr>
<td>m</td>
<td>Decrease damage rate</td>
<td>C</td>
</tr>
</tbody>
</table>
Table A-3.—State List for the propulsion level DES supervisor.

<table>
<thead>
<tr>
<th>State</th>
<th>Description</th>
<th>Status</th>
</tr>
</thead>
<tbody>
<tr>
<td>q₁</td>
<td>Engines on ground</td>
<td></td>
</tr>
<tr>
<td>q₂</td>
<td>Engines warming up</td>
<td></td>
</tr>
<tr>
<td>q₃</td>
<td>Both engines in High Performance operation</td>
<td></td>
</tr>
<tr>
<td>q₄</td>
<td>One engine in High one engine in Low Performance</td>
<td></td>
</tr>
<tr>
<td>q₅</td>
<td>Both engines in Low Performance operation</td>
<td></td>
</tr>
<tr>
<td>q₆</td>
<td>One engine stopped one engine in High Performance</td>
<td></td>
</tr>
<tr>
<td>q₇</td>
<td>One engine stopped one engine in Low Performance</td>
<td></td>
</tr>
<tr>
<td>q₈</td>
<td>Both engines failed</td>
<td>bad</td>
</tr>
<tr>
<td>q₉</td>
<td>Decision for abort mission</td>
<td>bad</td>
</tr>
<tr>
<td>q₁₀</td>
<td>Mission successful</td>
<td>good</td>
</tr>
<tr>
<td>q₁₁</td>
<td>High damage detected for one engine</td>
<td></td>
</tr>
<tr>
<td>q₁₂</td>
<td>High damage detected for both engines</td>
<td></td>
</tr>
</tbody>
</table>
Table A-4.—Event List for the propulsion level DES supervisor.

<table>
<thead>
<tr>
<th>Event</th>
<th>Description</th>
<th>Status</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Start engine</td>
<td>C</td>
</tr>
<tr>
<td>B</td>
<td>Warm up complete</td>
<td>UC</td>
</tr>
<tr>
<td>C</td>
<td>One engine deteriorates</td>
<td>UC</td>
</tr>
<tr>
<td>D</td>
<td>Redistribute the load</td>
<td>C</td>
</tr>
<tr>
<td>E</td>
<td>Both engines deteriorate</td>
<td>UC</td>
</tr>
<tr>
<td>F</td>
<td>One good engine fails</td>
<td>UC</td>
</tr>
<tr>
<td>G</td>
<td>Both engines fail</td>
<td>UC</td>
</tr>
<tr>
<td>H</td>
<td>Increase performance</td>
<td>C</td>
</tr>
<tr>
<td>I</td>
<td>Reduce performance</td>
<td>C</td>
</tr>
<tr>
<td>J</td>
<td>Request to abort mission</td>
<td>C</td>
</tr>
<tr>
<td>K</td>
<td>Request accepted</td>
<td>UC</td>
</tr>
<tr>
<td>L</td>
<td>Request rejected</td>
<td>UC</td>
</tr>
<tr>
<td>M</td>
<td>Mission accomplished</td>
<td>UC</td>
</tr>
<tr>
<td>N</td>
<td>Turn off engines</td>
<td>UC</td>
</tr>
<tr>
<td>O</td>
<td>Redistribute load</td>
<td>C</td>
</tr>
<tr>
<td>P</td>
<td>Redistribute load</td>
<td>C</td>
</tr>
<tr>
<td>Q</td>
<td>Request rejected</td>
<td>UC</td>
</tr>
<tr>
<td>R</td>
<td>One bad engine fails</td>
<td>UC</td>
</tr>
</tbody>
</table>
Table A-5.—Engine Level D{\small{E}}S matrix.

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<tr>
<th>q_i</th>
<th>a</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
<th>G</th>
<th>H</th>
<th>I</th>
<th>J</th>
<th>K</th>
<th>L</th>
<th>M</th>
<th>N</th>
<th>O</th>
<th>P</th>
<th>Q</th>
<th>R</th>
</tr>
</thead>
<tbody>
<tr>
<td>q_1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
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<td>0</td>
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<td>0</td>
<td>0</td>
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</tr>
<tr>
<td>q_2</td>
<td>0</td>
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<td>0</td>
<td>0</td>
<td>0</td>
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<td>0</td>
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<td>0</td>
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<tr>
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<td>0</td>
<td>0.091</td>
<td>0</td>
<td>0</td>
<td>0.045</td>
<td>0</td>
<td>0</td>
<td>0.864</td>
<td>0</td>
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<td>0</td>
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<td>0</td>
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</tr>
<tr>
<td>q_4</td>
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<td></td>
</tr>
<tr>
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<td>0</td>
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<td>0</td>
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</tr>
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<td></td>
</tr>
</tbody>
</table>

Table A-6.—Propulsion Level D{\small{E}}S matrix.

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
<th>G</th>
<th>H</th>
<th>I</th>
<th>J</th>
<th>K</th>
<th>L</th>
<th>M</th>
<th>N</th>
<th>O</th>
<th>P</th>
<th>Q</th>
<th>R</th>
</tr>
</thead>
<tbody>
<tr>
<td>q_1</td>
<td>1</td>
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<td>0</td>
<td>0</td>
<td>0</td>
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<td>0</td>
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<td></td>
</tr>
<tr>
<td>q_2</td>
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<td>0</td>
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<td></td>
</tr>
<tr>
<td>q_4</td>
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<td>0</td>
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<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>q_5</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
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<td>0</td>
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<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
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</tr>
<tr>
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<td>0</td>
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<td>0</td>
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<td></td>
</tr>
</tbody>
</table>

Figure A-1.—Propulsion Level D{\small{E}}S controller
(NOTE: not all state transitions are labeled due to complexity).
References

## Title and Subtitle

Hierarchical Discrete Event Supervisory Control of Aircraft Propulsion Systems

## Authors

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## Abstract

This paper presents a hierarchical application of Discrete Event Supervisory (DES) control theory for intelligent decision and control of a twin-engine aircraft propulsion system. A dual layer hierarchical DES controller is designed to supervise and coordinate the operation of two engines of the propulsion system. The two engines are individually controlled to achieve enhanced performance and reliability, necessary for fulfilling the mission objectives. Each engine is operated under a continuously varying control system that maintains the specified performance and a local discrete-event supervisor for condition monitoring and life extending control. A global upper level DES controller is designed for load balancing and overall health management of the propulsion system.