Trailing Edge Blowing on a Two-Dimensional Six-Percent Thick Elliptical Circulation Control Airfoil Up to Transonic Conditions

Michael G. Alexander, Scott G. Anders, Stuart K. Johnson, Jennifer P. Florance, and Donald F. Keller
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Abstract

A wind tunnel test was conducted in the NASA Langley Transonic Dynamics Tunnel (TDT) on a six percent thick slightly cambered elliptical circulation control airfoil with both upper and lower surface blowing capability. Parametric evaluations of jet slot heights and Coanda surface shapes were conducted at momentum coefficients ($C_\mu$) from 0.0 to 0.12. Test data were acquired at Mach numbers of 0.3, 0.5, 0.7, 0.8, and 0.84 at Reynolds numbers per foot of $2.43 \times 10^5$ to $1.05 \times 10^6$. For a transonic condition, (Mach = 0.8 at $\alpha = 3^\circ$), it was generally found the smaller slot and larger Coanda surface combination was overall more effective than other slot/Coanda surface combinations. Lower surface blowing was not as effective in producing lift and pitching moment increments at transonic conditions as the upper surface blowing over the same range of momentum coefficients. No appreciable Coanda surface, slot height, or slot blowing position preference was indicated transonically with the dual slot blowing. Subsonically (Mach = 0.3 at $\alpha = 6^\circ$), it was generally found the smaller slot and smaller Coanda surface combination was more effective overall than other slot/Coanda surface combinations. At Mach = 0.3 and $\alpha = 6^\circ$, the 1.78:1 Coanda with the upper slot blowing position with a slot height of $h/c = 0.0012$ gave the maximum $\Delta Cl$ generated of 0.75 at a $C_\mu = 0.085$. At Mach = 0.8 and $\alpha = 3^\circ$, the 2.98:1 Coanda with the upper slot blowing position having a slot height of $h/c = 0.001$, slightly outperformed the lower slot position, with the upper slot generating a maximum $\Delta Cl$ of 0.25 at a $C_\mu = 0.008$. Both subsonic and transonic trailing edge blowing influenced the flow field upstream of the slot.

Introduction

Circulation control is considered one of the most efficient methods for lift augmentation at low Mach numbers (ref. 1). The device augments an airfoil's lifting capability by tangentially ejecting a thin jet of high momentum air over a rounded trailing edge (ref. 2). When the jet sheet velocity is greater than the local external flow, the jet sheet remains attached over the curved surface by means of the Coanda effect (ref. 3-5). The Coanda effect is created when a tangentially blowing slot ejects a jet sheet of air over a curved or “Coanda surface” and remains attached to the surface due to a balance between the low static pressures generated by the jet and the centrifugal force acting on the curving jet (ref. 6) (figure 1). The jet not only moves the separation point around the trailing edge toward the lower surface of the wing, but also entrains the external flow field to follow the jet. This entrainment and separation point movement produces a net increase in the circulation of the wing resulting in lift augmentation (ref. 7).

Numerous experimental circulation control tests using the Coanda effect to enhance lift have been conducted at subsonic velocities on thick airfoils sections (ref. 8-14). However, a void exists for transonic data on thin circulation control airfoils. Therefore, it is the focus of this experiment to evaluate the effectiveness of trailing edge circulation control on a thin airfoil section at transonic Mach numbers. A wind tunnel test was conducted on a six percent thick slightly cambered elliptical airfoil with both upper and lower surface slot blowing capability. Parametric evaluations of slot heights and Coanda surface shapes...
were conducted at momentum coefficients ($C_\mu$) ranging from 0.0 to 0.12. Test data were acquired in the Langley Transonic Dynamics Tunnel at multiple Mach numbers and angles of attack at Reynolds numbers per foot ranging from 2.43 x $10^5$ to 1.05 x $10^6$.

### Symbols

- $\alpha$ angle of attack (degrees)
- $\Delta$ delta (incremental change)
- $\rho$ density (lbm/ft$^3$)
- $\gamma$ ratio of specific heat
- $A$ area (ft$^2$)
- $b$ model span (inch)
- $c$ chord (inch)
- cref reference chord (30 inch)
- CCA circulation control airfoil
- CD discharge coefficient
- $C_d$ sectional drag coefficient
- $C_{d,\text{rake}}$ uncorrected drag measured at the wake rake
- $C_l$ sectional lift coefficient
- $C_{l,\alpha}$ lift curve slope
- $C_m$ or $C_{m,\text{ref}}$ sectional 0.25cref pitching moment coefficient
- $C_{m,\alpha}$ pitching moment independent of angle of attack
- $C_{m,\alpha}$ pitching moment curve slope
- $C_p$ pressure coefficient
- CP center of pressure ($x_{cp}/c$)
- $C_{p,*}$ critical pressure coefficient
- $C_\mu$ momentum coefficient
- $\Delta C_l/C_\mu$ lift augmentation ratio
- $\Delta C_l/C_\mu = \frac{C_l - C_{l,\mu = 0}}{C_\mu}$
- DAS data acquisition system
- ESP electronically scanned pressures
- gc gravitation constant

### Subscripts

- jet airflow exiting nozzle
- l lower
- max maximum value
- s slot
- TE trailing edge
- u upper
- $\infty$ freestream


Model Description

The configuration tested in this experimental investigation was a semi-span circulation control airfoil (CCA) having zero leading and trailing edge sweep and an end plate on its tip (figure 2). The model was mounted in the TDT on a splitter plate located approximately 3 feet from the tunnel wall. The model incorporated circulation control by blowing tangentially from a full span rectangular slot located upstream of a trailing edge "Coanda surface". The rectangular slot exit is located at x/c_{ref} = 0.9 and extends full width (60 inches) of the model. The model has two separate and isolated internal plenums that provide air to either the upper or lower rectangular slot. The model is instrumented with a total of 157 static and total pressure taps, one accelerometer, and a type J thermocouple located in each plenum. The model has a surface finish of 32μ inch, and the Coanda surface finish from upper slot exit to lower slot exit is 16μ inch finish.

A wake rake was placed one reference chord length (30 inches) downstream of the CCA trailing edge and was used to acquire the CCA wake total and static pressures. The wake pressures were then integrated to determine drag.

![Figure 2 - CCA wind tunnel model mounted in the TDT (looking downstream).](image)

Circulation Control Airfoil (CCA)

The CCA was derived from a baseline elliptical airfoil truncated at x/c_{ref} = 0.90 where the nozzle of the rectangular slot occurred. All other baseline airfoil attributes remained the same.

Baseline Airfoil

In determining an airfoil to use in this experimental effort, a NACA-64A series was initially considered. However, an elliptical section was chosen based on discussions in reference 15 which examine desirable pressure distributions for transonic circulation control airfoils. A 6 percent thick section with 0.75 percent camber was chosen based primarily on reference 5 that indicates this would nearly achieve an optimum thickness to generate maximum ΔC'l’s at Mach numbers from 0.8 to 0.85.
Reference Chord

The CCA sectional profile was sized with a 30 inch chord length without a Coanda surface. In order to have a consistent non dimensional nozzle height parameter (h/c), it was decided to establish the chord length of each CCA trailing edge configuration as seen in table 1.

<table>
<thead>
<tr>
<th>Coanda</th>
<th>y/b</th>
<th>1.78:1</th>
<th>2.38:1</th>
<th>2.98:1</th>
</tr>
</thead>
<tbody>
<tr>
<td>x/cref</td>
<td>0.5</td>
<td>27.82-in.</td>
<td>28.09-in.</td>
<td>28.36-in.</td>
</tr>
</tbody>
</table>

Table 1 - CCA chord lengths for each Coanda surface.

CCA Planform Characteristics

The CCA section is a simple six percent thick elliptical airfoil having 0.75 percent camber (figure 4). The model span (b) is 60 inches with zero leading and trailing edge sweep. A reference chord (cref) of 30 inches gave the model an aspect ratio of two and a taper ratio of one. Common practice for testing semispan models on a reflection plane is to refer to this as an aspect ratio four wing. To accommodate the trailing edge Coanda surfaces, the reference airfoil was truncated at x/cref = 0.90 (27 inches). The CCA model tip was capable of accommodating either a 30 inch diameter circular end plate to promote two dimensional flow or a "t/2" tip used to evaluate three dimensional effects.

Coanda Surface Definition

Three elliptical trailing edge surfaces (referred to as Coanda surfaces) were manufactured with length to height ratios of 1.78:1, 2.38:1, and 2.98:1 (as illustrated in figure 5) and installed on the CCA model shown in figure 6. The minor axis of the Coanda surface was aligned with the slot exit to ensure the minimum exit area occurred at the exit (x/cref = 0.9). The horizontal axis of the ellipse was mapped to the camber line of the elliptical airfoil and formed a 5 degree converging nozzle at the exit. The Coanda surface spanned the entire model (60 inches). Table 2 lists the Coanda surface characteristics.
Suggested guidelines from reference 15 for Coanda surface radii of curvatures are listed in table 2. It was not possible to meet the entire guideline radius of curvatures on a six percent thick airfoil, and it was decided preference would be given to the slot radius of curvature in an effort to achieve initial attachment of the jet flow. For this reason, a family of elliptical Coanda surfaces was chosen which has larger slot radii of curvature and small trailing edge radii of curvature.

<table>
<thead>
<tr>
<th>Coanda</th>
<th>Chord (in.)</th>
<th>1.78 : 1</th>
<th>2.38 : 1</th>
<th>2.98 : 1</th>
</tr>
</thead>
<tbody>
<tr>
<td>h1/r</td>
<td>0.024</td>
<td>0.014</td>
<td>0.009</td>
<td></td>
</tr>
<tr>
<td>h2/r</td>
<td>0.039</td>
<td>0.022</td>
<td>0.014</td>
<td></td>
</tr>
<tr>
<td>h3/r</td>
<td>0.051</td>
<td>0.028</td>
<td>0.018</td>
<td></td>
</tr>
<tr>
<td>h1/rTE</td>
<td>0.14</td>
<td>0.18</td>
<td>0.23</td>
<td></td>
</tr>
<tr>
<td>h2/rTE</td>
<td>0.22</td>
<td>0.30</td>
<td>0.37</td>
<td></td>
</tr>
<tr>
<td>h3/rTE</td>
<td>0.29</td>
<td>0.38</td>
<td>0.48</td>
<td></td>
</tr>
</tbody>
</table>

| Guidelines | h/r | 0.01 to 0.08 |

Table 2 - Coanda Radius and Slot Height Dimensions.

**Slot Definition**

Three upper and lower slot heights for each Coanda surface were possible for this wind tunnel investigation. The aft upper and lower removable surfaces were designed to set the slot heights by varying the internal mold line while not disturbing the outer mold line of the model. Average measured slot height
(h) and chord lengths were used to determine the height to chord ratio (h/c) of each slot. Table 3 below lists the measured average slot height and the resulting h/c. Actual measurements are recorded in Appendix A.

<table>
<thead>
<tr>
<th>Slot</th>
<th>h(avg) (inch)</th>
<th>h/c</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.035</td>
<td>0.0012</td>
</tr>
<tr>
<td>2</td>
<td>0.056</td>
<td>0.0020</td>
</tr>
<tr>
<td>3</td>
<td>0.073</td>
<td>0.0026</td>
</tr>
<tr>
<td>4</td>
<td>0.021</td>
<td>0.0007</td>
</tr>
</tbody>
</table>

Table 3 - Slot and Chord Measurements.

**Half Height Slot**

A fourth slot height (4, table 3) was constructed during the test using the upper surface small slot (h/c = 0.0012) aft skin by applying four layers of tape at 0.0035 inches per layer for a total thickness of 0.014 inches (figure 7). The resulting "half height" slot was used with the 2.98:1 Coanda, resulting in an exit h = 0.021 inches or h/c = 0.0007.

![Figure 7 – Half height slot.](image)

**Aft Surfaces**

Three sets of aft surfaces were manufactured and attached to the main airfoil body to form the upper and lower external airfoil contour as well as the internal convergent nozzle contour (figure 8). The aft skins also contained chordwise surface static pressure taps at y/b = 0.5. Any aft surface in combination with any Coanda surface ensured the minimum nozzle area was located at the nozzle exit. Each aft surface also established a discrete slot height above the Coanda surface.

![Figure 8 - Aft surface identification.](image)
End Plate

The purpose of the circular end plate was to promote two dimensional flow across the span so the chordwise pressure measurements at mid chord would represent the performance of a two dimensional, infinite span airfoil. As seen in figure 9, the end plate is a 30 inch diameter circular plate constructed from a 0.25 inch thick aluminum plate with the outside edge beveled. The forward edge of the end plate was flush with the airfoil leading edge and centered vertically with the airfoil. This resulted in the end plate extending past the trailing edge of the airfoil by 1.7 to 2.3 inches, depending on which Coanda surface was installed. A removable cutout located at its trailing edge was used to allow Coanda surface removal and replacement. The design of the end plate was based on sizing criteria found in reference 16.

![Figure 9 - CCA end plate.](image)

**t/2 Tip**

A “t/2 tip” was designed to close out the airfoil in a manner representative of a three dimensional wing (figure 10). The rounded tip had a radius equal to one half the local thickness and is referred to as the “t/2 tip” configuration. The data acquired from this configuration were used to evaluate the effects of the end plate.

![Figure 10 - CCA "t/2 tip".](image)

**Internal Plenum**

As seen in figure 11, the airfoil section is divided into contiguous, separate, and isolated upper and lower plenums. The ratio of the slot height to plenum height ranged from 3.8 to 12.8 depending on the slot
height. This ensured low flow velocities in the plenum that helped maintain uniform plenum pressures. Each plenum has the capability of accepting three high loss screens to promote flow uniformity. This test used only the most aft screen that ran full span and parallel to the slot nozzle.

![Figure 11 - CCA internal plenum section cut.](image)

**Internal Screens**

The model has the capability to hold six removable, 0.050 inch thick, high pressure loss screens (figure 12). The screens were fastened to the model center plate and extended to the plenum ceiling. Each screen has a porosity of 30 percent and was sized using the method described in reference 17. It was determined through bench testing to use only one screen in each plenum in the aft most position. The aft screen was located approximately $x/\text{cref} = 0.72$ and ran full spanwise, parallel to the slot.

![Figure 12 - Center body internal screen and upper plenum layout.](image)

**Boundary Layer Trip**

A boundary layer trip strip (ref. 18) was located 1.5 inches (measured along the surface) aft of the leading edge on both the upper and lower surfaces. The trip strip used epoxy dots with a diameter of 0.038 inch, a thickness of 0.015 inch, and an edge to edge spacing distance between the epoxy dots of 0.098 inch.
Facility

This wind tunnel investigation was conducted in the Langley Transonic Dynamics Tunnel (TDT) (ref. 19). The TDT is a closed circuit, continuous flow, variable pressure wind tunnel with a 16 foot square test section with cropped corners (figure 13). The tunnel has the capability of using either air or R134a gas as the test medium. The current investigation was conducted in air. The tunnel can operate up to Mach 1.2 and is capable of maximum Reynolds numbers of approximately three million per foot and dynamic pressures up to 2.29 psi in air. Tunnel stagnation pressure can be varied from near vacuum to atmosphere.

![Figure 13 - TDT schematic.](image)

Model Support

The TDT model support systems used for this test were a sidewall turntable and splitter plate as seen in figure 14. The splitter plate was located approximately 3 feet from the tunnel walls using wall standoffs. The rigid support and the model instrumentation were placed inside an aerodynamic shape or "canoe" located between the splitter plate and the tunnel sidewall.

![Figure 14 - CCA model installed on splitter plate (looking downstream).](image)
Data Acquisition and Processing

The TDT open architecture dynamic data acquisition system (DAS) allowed real time acquisition and display of measured static and dynamic data as well as online analysis of the acquired data.

The DAS hardware is comprised of three subsystems with each switch connectable to a subset of four NEFF "front ends". Each NEFF provides signal conditioning, filtering, and sample and hold analog to digital conversion for 64 channels for a total capability of 256 channels. Data can be sampled at an aggregate rate approaching 300,000 samples per second, which typically provides data acquisition at a rate of at least 1000 samples per second for all available model instrumentation. The computer systems supporting the DAS perform basic data acquisition, archiving, and continuous buffering necessary to provide high quality dynamic data during tests. All computers and terminals are connected, via networks, to workstations at the TDT or at remote sites, which provide a distributed real time data display capability.

For this test, the DAS handled typical model instrumentation arrangements such as strain gage balances, potentiometers for position indication, and electronically scanned pressure (ESP) transducers.

Labview that resided on a personal computer in the TDT control room further processed data. Labview acquired the raw data from the tunnel data acquisition computer, reduced the data, and presented near real-time force and pressure information in a graphical format as well as data files.

Air Supply

Air was supplied to the model via two 1 inch high pressure flex lines delivering a maximum of 1 lbm/sec at 200 psia. The supply total temperature to the model was uncontrolled and ranged from -13°F to 70°F. Each supply line was attached to a control valve that regulated total pressure to the CCA model (figure 15). A manually operated crossover line located upstream of the control valve allowed mass flow to be diverted from one line to another. After the control valve, the supply air went through its dedicated critical flow venturi and then entered the model plenum.

![Figure 15 - Air supply.](image)

Critical Flow Venturi

The two critical flow venturis, serial numbers 47 and 48, were used in this wind tunnel test and can be seen in table 4. They required 1 inch diameter input/exit lines and have a venturi throat diameter of 0.505 inch. Each venturi had a total pressure keel probe located upstream of the venturi throat and a static
pressure and a total temperature probe located at the venturi throat. Located upstream of the venturi was the remotely operated control valve that controlled the upstream total pressure prior to entering the venturi. Further information about the venturis and their calibration can be found in Appendix B.

<table>
<thead>
<tr>
<th>Venturi Serial Number</th>
<th>47 (upper plenum)</th>
<th>48 (lower plenum)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Throat Area (ft²)</td>
<td>0.0014</td>
<td>0.0014</td>
</tr>
<tr>
<td>Discharge Coefficient</td>
<td>0.971</td>
<td>0.982</td>
</tr>
</tbody>
</table>

Table 4 - Critical flow venturi information

**Burst Disk**

To ensure safe operations with high pressure air, a 1 inch diameter burst disk was located downstream of each venturi. The burst disks were rated to 112 psia with a five percent uncertainty band (106.4 to 112 psia) and were placed in line on a 1 inch carbon steel safety holder.

**CCA Instrumentation**

**Static Pressures**

Eighty-three (42 upper and 41 lower) external static surface pressure taps were located at y/b = 0.5 on the upper and lower airfoil surface. There were two spanwise rows of ten static pressures taps located at x/cref = 0.5 and 0.8 on the upper and lower airfoil surface.

**Coanda Surface Static Pressures**

Each Coanda has 19 surface static pressure taps located at approximately y/b = 0.5 (figure 16). Some taps were slightly offset in span from y/b = 0.5 to accommodate manufacturability.

Figure 16 - Coanda surface static pressure tap locations.
Plenum Total Pressures

Each plenum had six total pressure taps with five taps located behind the high loss screens as seen in figure 17. Pressure taps two through six were located upstream of the slot, and tap one was used to determine the total pressure entering the plenum from the intake nozzle. Total pressure taps two through six were averaged together to obtain the nozzle exit total pressure.

CCA Wake Pressures

The wake rake was mounted in the tunnel using a tripod mounting arrangement (figures 2 and 18) with two of the legs attaching to the splitter plate and the aft leg attaching to the tunnel wall. The fixed rake is 48 inches in length and was used to obtain the total and the static pressure distributions in the model wake on the model centerline. The measured pressures were integrated to determine the drag. The plane of the total pressure tubes was located 30 inches or one reference chord length from the baseline airfoil’s trailing edge. The wake rake has a total of 87 pressures with 79 total pressures and eight static pressures taps. The total pressure tubing was stainless steel tubing having a 0.062 inch outside diameter with a wall thickness of 0.010 inch. The static pressure probes used a four hole system that provided an integrated static pressure from each probe. The static probes were manufactured using the criteria found in reference 20.
Plenum Thermocouples

The plenum has 2 iron constantan, type J thermocouples located in each plenum to measure plenum total temperature.

Test Procedures and Conditions

Lift and Pitching Moment

The sectional lift coefficient (equation 1) and quarter-chord pitching moment coefficient (equation 2) were obtained by numerically integrating (using the trapezoidal method) the local pressure coefficient at each y/b = 0.5 chordwise orifice from the upper and lower surface of the model.

\[
C_L = \int_0^1 \left( C_{p_l} - C_{p_u} \right) d\left( \frac{x}{c} \right) \cos \alpha
\]

\[
C_{m_{0.25}} = \int_0^1 \left( C_{p_l} - C_{p_u} \right) \left( 0.25 - \left( \frac{x}{c} \right) \right) d\left( \frac{x}{c} \right)
\]

Momentum Coefficient

The momentum coefficient was calculated using equation 3.

\[
C_\mu = \frac{m U_{jet}}{q_{\infty} S}
\]

The ideal jet velocity (U_{jet}) (ft/s) was calculated (ref. 21) based on the assumption that the slot jet flow expands isentropically to the free stream static pressure (equation 4).

\[
U_{jet} = \sqrt{2 R T_o \gamma \left( \frac{\gamma}{\gamma-1} \right) \left[ 1 - \left( \frac{p_{\infty}}{P_{\text{plenum}}} \right)^{\gamma-1} \right]}
\]

Mass flow was determined using equation 5. The discharge coefficient (CD) was obtained from critical flow venturi calibrations conducted in the Langley Jet Exit Test Facility (Appendix B).

\[
\dot{m} = CD (AV \rho)_{\text{throat}}
\]
Drag

The sectional drag coefficient was obtained by numerically integrating (using the trapezoidal method) the rake total pressures to solve for the momentum loss across the deficit in the wake. The wake deficit integration used the procedure of Baals and Mourhess (ref. 22). This method, however, fails to account for the additional momentum introduced in the control volume by the jet at the trailing edge. To correct the drag for the added momentum, the term $\frac{V_{\infty}}{U_{jet}}$ was subtracted from the drag coefficient (ref. 21) (equations 6 & 7).

$$C_{d_{rake}} = \text{uncorrected integrated drag from rake}$$

**Single Slot**

$$C_d = C_{d_{rake}} - C\mu \left( \frac{V_{\infty}}{U_{jet}} \right) \quad (6)$$

**Dual Slots**

$$C_d = C_{d_{rake}} - C\mu \left( \frac{V_{\infty}}{U_{jet_{up\_slot}}} \right) - C\mu \left( \frac{V_{\infty}}{U_{jet_{low\_slot}}} \right) \quad (7)$$

The drag term used for developing $l/d$ came from reference 21 and is seen in equation 8 below. This drag equation takes into consideration the additional penalty for mass intake (ram drag).

$$C_d = C_{d_{rake}} + C\mu \left( \frac{U_{jet}}{2V_{\infty}} \right) + C\mu \left( \frac{V_{\infty}}{U_{jet}} \right) \quad (8)$$

**Test Conditions**

The test conditions and ranges are presented in table 5 below.

<table>
<thead>
<tr>
<th>Mach</th>
<th>$P_o$ (psia)</th>
<th>$P_s$ (psia)</th>
<th>$T_o$ (°F)</th>
<th>Rn/ft</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.3</td>
<td>2.7 – 4.1</td>
<td>2.6 – 3.8</td>
<td>67 – 94</td>
<td>3.6x10^5 – 5.5 x 10^5</td>
</tr>
<tr>
<td>0.5</td>
<td>3.3 – 3.5</td>
<td>2.8 – 2.9</td>
<td>82 – 85</td>
<td>6.8x10^5 – 7.2 x 10^5</td>
</tr>
<tr>
<td>0.7</td>
<td>3.3 – 4.0</td>
<td>2.3 – 2.9</td>
<td>90 – 113</td>
<td>8.2 x 10^5 – 1.0 x 10^6</td>
</tr>
<tr>
<td>0.8</td>
<td>3.0 – 4.1</td>
<td>2.0 – 2.7</td>
<td>95 – 125</td>
<td>7.8 x 10^5 – 1.0 x 10^6</td>
</tr>
<tr>
<td>0.84</td>
<td>2.1 – 2.7</td>
<td>1.3 – 1.7</td>
<td>102 – 117</td>
<td>5.8 x 10^5 – 7.4 x 10^5</td>
</tr>
</tbody>
</table>

Table 5 - Range of Test Conditions
Data Corrections

No corrections were applied to the data to account for tunnel flow angularity, wall interference, thrust, or end plate effects.

Discussion of Results

Baseline Airfoil Aerodynamic Performance (No Blowing)

Figure 19 presents the no blowing longitudinal aerodynamic coefficients for the baseline airfoil. The baseline trailing edge configuration includes the 2.98:1 Coanda surface, having the upper and lower slot height (h/c) of 0.0012. Due to an unexplained data anomaly in the no blowing Mach = 0.3 data, the Mach = 0.3 data presented in figure 19 are from the model configuration having a slot height of h/c = 0.0020.

The angle of attack range was limited to +10° due to model stress analysis; therefore, a Cl_{max} was not observed. In figure 19(a), the slope of the $C_L - \alpha$ graph, $Cl_\alpha$, is linear from $-5^\circ$ to $+8^\circ$ at all Mach numbers with $C_l_0$ occurring at a slightly negative angle of attack. Typical two dimensional airfoil subsonic Mach number effects on $Cl_\alpha$ are observed which show an increasing $Cl_\alpha$ with increasing Mach number.

In figures 19(b) and 19(c), from Mach numbers 0.3 to 0.7, the baseline airfoil is statically unstable with a $Cm_0$ occurring at $\alpha = 5^\circ$ ($C_l \sim 0.7$). At Mach = 0.8, no $Cm_0$ is observed, but $Cm_\alpha$ indicates a slight statically unstable airfoil until a reversal is encountered at $\alpha = 5^\circ$ ($C_l \sim 0.7$). At Mach = 0.84, $Cm_\alpha$ indicates a statically stable airfoil up to $\alpha = 6^\circ$ ($C_l \sim 0.9$) where $Cm_\alpha$ reverses and indicates an unstable airfoil. The $Cm_0$ at this Mach number occurs at $\alpha \sim -4^\circ$. Seen in figure 19(d), a maximum l/d of 44 occurs at a lift coefficient of 0.5 at Mach = 0.7. At Mach numbers above 0.7, l/d_{max} diminishes which may be in part due to the transonic drag rise.

A drag increase associated with increasing angle of attack, Mach number, and $C_l$ is observed in figures 19(e), and 19(f). The transonic drag rise can also be seen in figure 19(g) beginning at approximately Mach = 0.7.

Chordwise Pressure Distribution

The no blowing chordwise pressure distributions are observed in figure 20. Subsonic Mach numbers (0.3 and 0.5) display a very strong leading edge pressure spike that is followed by an equally strong pressure recovery over a very short chordwise distance. The first presence of an upper surface shock is seen at Mach = 0.7 at $\alpha = 5^\circ$ and gains further strength and moves aft with increasing angles of attack and Mach numbers. However, the shock is seen to move forward on the upper surface for $\alpha > 8^\circ$ at Mach = 0.8 and $\alpha > 6^\circ$ at Mach = 0.84. It is also noted the chordwise pressures at $\alpha = 0^\circ$ remain mostly positive throughout the angle of attack and Mach number range. With the chordwise pressure distributions seen in figure 20 and the center of pressure data in figure 21, it is conjectured the airfoil shock system is gaining strength with increasing angle of attack and Mach number which allow for the center of pressure to move further aft until a large region of separated flow occurs at the trailing edge. This is possibly due to a shock interaction or a stall causing the $Cm_\alpha$ reversals seen in figure 19(b).
Comparison of End Plate and t/2 Tip Configurations

Several runs were made with the tip configuration as shown in figure 10. Runs with the t/2 tip configuration were made with the 2.98:1 Coanda surface and the h/c = 0.0012 slot only. Comparisons are presented in Figures 22 and 23 for unblown and blown data taken at Mach = 0.3 at α = 6° and at Mach = 0.8 at α = 3°. Based on C_l, the endplate does not produce a strong effect.

Mach 0.3

The unblown airfoil performance at Mach = 0.3 is shown in figure 22(a). A jump in the C_l - α curve occurs between 1° and 3°. McLachlan (ref. 23) found a similar jump in their blowing data which was attributed to the state of the boundary layer proceeding the slot location. It is assumed the shift shown here is also due to Reynolds number. The Reynolds number based on chord was 1x10^6. The C_l - α slope before and after the jump appears to be nearly the same. In spite of the jump, the results show the end plate did little to affect the C_l - α curve. The slope of the t/2 tip curve is only slightly less than the end plate slope, but the difference is too small to make any strong conclusions.

The ΔC_l - C_μ performance at Mach = 0.3 for α = 6.0° is shown in figure 22(b). The slope of the ΔC_l - C_μ graph, typically referred to as the augmentation ratio, is 27 up to C_μ = 0.01. Abramson and Rogers (ref. 6) report augmentation ratios of up to 72. Typical good circulation airfoils should achieve augmentation ratios in the 50 to 70 range. In contrast, jet flaps attain augmentation ratios of approximately 14. The augmentation ratio of 27 indicates the airfoil lift control performing between the two regimes. The control method found for this experiment might be more accurately described as a Coanda jet flap. The ΔC_l - C_μ slope falls off to 4.3 for C_μ > 0.03, and the last datum point indicates the peak ΔC_l may be 0.66.

Mach 0.8

The unblown airfoil performance at Mach = 0.8 is shown in figure 23(a). The slope of the end plate C_l - α curve is higher than the t/2 tip slope. The lower slope occurs because of the upper and lower flowfield communication allowed by the t/2 tip configuration. Table 6 lists several C_l - α slopes for comparison. The empirical values from Raymer (ref. 24) are for wing lift curve slopes (per radian) for preliminary aircraft design purposes. The experimental values do not quite reach the empirical values but are close considering the approximation. The empirical values also give insight to how much improvement might be expected from the end plate.

<table>
<thead>
<tr>
<th>Theoretical: 2π/(1-M^2)^1/2</th>
<th>M=0.3</th>
<th>M=0.8</th>
</tr>
</thead>
<tbody>
<tr>
<td>Subsonic 2D Ideal</td>
<td>6.6</td>
<td>10.5</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Empirical Results:</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>End Plate</td>
<td>4.5</td>
<td>6.9</td>
</tr>
<tr>
<td>T/2 Tip</td>
<td>4.1</td>
<td>5.9</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>From Experiment:</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>End Plate</td>
<td>4</td>
<td>6.3</td>
</tr>
<tr>
<td>T/2 Tip</td>
<td>3.8</td>
<td>5.6</td>
</tr>
</tbody>
</table>

Table 6 - Lift Curve Slopes (Per Radian) for Circulation Control Airfoil for C_μ = 0
The \( \Delta C_l - C_\mu \) performance at Mach = 0.8 for \( \alpha = 3.0^\circ \) is shown in figure 23(b). The \( \Delta C_l - C_\mu \) slope remains constant at a value of 37 up to near the maximum \( \Delta C_l \) point. The augmentation ratio is actually increased over the Mach = 0.3 results. However, it is still below what has historically been considered characteristic of circulation control performance (\( \Delta C_l / C_\mu > 50 \)). Abramson and Rogers (ref. 6) achieved augmentation ratios of 58 at Mach = 0.6 for one of their 16% thick airfoil configurations. They found the augmentation ratio dropped to 27 for Mach = 0.7. The only slope available from their data set at Mach = 0.8 was 10.

**Blowing Performance**

*Mach = 0.3 at \( \alpha = 6^\circ \)*

**Coanda Surface Effect**

In figures 24, 25, and 26, incremental lift and pitching moment data for Coanda surface effects are presented for the upper, lower, and dual slot blowing, respectively. Each Coanda surface at this Mach number and angle of attack is capable of generating incremental lift and pitching moment at each blowing condition with the exception of dual slot blowing. Dual slot blowing negates the contributions of the upper and lower slot blowing configurations and does not create any appreciable forces and moments. Increasing \( C_\mu \) during upper slot blowing creates positive lift increments and negative pitching moment increments. Conversely, increasing \( C_\mu \) during lower slot blowing creates negative lift and positive pitching moment increments. Upper and lower slot blowing data trends for each Coanda surface appear to be somewhat asymptotic, and the Coanda surfaces may even decrease in effectiveness at higher blowing rates. The trend generally observed in figures 24, 25, and 26 is the smaller the Coanda surface, the greater the lift and pitching moment increment. Also observed in figure 24 and somewhat in figure 25 data, a preferred Coanda surface configuration changes with slot exit height by increasing the slot exit h/c. In figure 24, at a slot h/c = 0.0012, the apparent preferred Coanda is the smaller Coanda surface (1.78:1). As the slot size increases from h/c = 0.0012 to h/c = 0.0020, the data indicate all three Coanda surfaces are essentially equivocal. By increasing the slot height to h/c = 0.0026 from 0.0020, the larger Coanda surface (2.98:1) generates the larger magnitudes at the larger slot exit h/c, albeit overall still smaller than Coanda surface size of 1.78:1 and a slot height of 0.0012. In figure 25 at h/c = 0.0026, the 2.98:1 and 2:38:1 Coanda surfaces are essentially equivocal in effectiveness. Using the upper slot blowing position with a slot height of h/c = 0.0012, the maximum \( \Delta C_l \) generated is 0.75 at a \( C_\mu \) of 0.085.

The Coanda surface effect is observed in the lift augmentation ratio as seen in figures 27 and 28 for upper slot blowing and figures 29 and 30 for lower slot blowing. Dual slot blowing is not presented since it was not effective at generating appreciable lift increments. Data are presented in the above figures as \( \Delta C_l / C_\mu \) versus \( C_\mu \) or versus \( U_{jet} / V_\infty \). The data in these plots suggest that with increasing \( C_\mu \) or velocity ratio, the lift augmentation diminishes. The data also indicate the smaller the Coanda surface and slot size (h/c), the greater the augmentation. Generally seen in figures 27 and 28 in the lower \( C_\mu \) values of the h/c = 0.0020 or 0.0026 data, the 2.98:1 Coanda surface values typically increase in magnitude over a small \( C_\mu \) range, while at the same \( C_\mu \) range, the lift augmentation of smaller Coanda surfaces decreases in value.

A Coanda surface effect is observed in figure 31, \( \Delta C_l \) versus nozzle pressure ratio (NPR), on upper slot blowing only. The same type of trends observed in figures 24, 25, and 26 is observed in figure 31.
Slot Height Effect

A slot height effect is observed in the incremental lift and pitching moment data shown in figures 32, 33, and 34 for the upper, lower, and dual blowing slots respectively. The trend generally indicates that the smaller the slot h/c, the greater the lift and moment increment generated. No appreciable slot preference is indicated with the dual slot blowing. Also observed is an apparent 'pinch down' in the h/c = 0.0012 and 0.0020 slot in the upper and lower blowing data from $C_\mu = 0.06$ to 0.08 that diminished as the Coanda surface size increased. This may indicate a jet reattachment (in the immediate region of the slot) followed by a lull where there is little flow turning with $C_\mu$ increment. The lull is followed by a period of flow turning around the Coanda bulb due to the increased $C_\mu$. Typically observed are no significant differences in upper or lower slot blowing, and they appear to be somewhat equivocal in force and moment generation with the expected differences in signs.

A slot height effect on the lift augmentation ratio is observed in figures 35 and 36 for upper slot blowing and figures 37 and 38 for lower slot blowing. Similar trends are observed as seen in the Coanda surface effects on the lift augmentation data. The data indicate the smaller slot height is preferred on any Coanda surface with the exception of h/c = 0.0007 on the 2.98:1 Coanda during upper slot blowing (figures 35 and 36). At this blowing configuration the slot height of h/c = 0.0007 performs no greater than the larger slot height. However, at the same blowing configuration for lower slot blowing (figures 37 and 38), slot h/c = 0.0007 is the better performer, and the trend of the smallest slot for any Coanda surface holds true for lower slot blowing.

Slot Blowing Position Effect

The effect of slot blowing position on the 1.78:1 Coanda using the h/c = 0.0012 slot at two Mach numbers and angles of attack can be observed in figure 39. At these Mach numbers and angles of attack, the upper slot blowing position generated the largest $\Delta Cl$ of all the slot positions.

Pressure Distributions

Main Airfoil Body

The effect on the upper and lower surface pressure distribution due to upper, lower, and dual slot blowing can be observed in figure 40. In figure 40(a), a $C_\mu$ effect from upper slot blowing is observed on the upper surface leading edge suction peak of the airfoil. As $C_\mu$ increases, the pressure footprint grows and moves aft up to a $C_\mu$ value of 0.046 where the remaining values of $C_\mu$ have no further effect on the leading edge suction peak. Little $C_\mu$ effect on the leading edge pressure peak is observed during lower slot blowing (figure 40(b)) and none for dual slot blowing (figure 40(c)). In figures 40(a) and 40(b), it appears the surface flow near 80-90% x/c accelerates due to flow entrainment caused by the trailing edge blowing jet that result in a decrease of the surface static pressures near the nozzle exit. No induced shocks due to blowing are observed at this Mach number (M = 0.3).

Coanda Bulb

Figures 41 and 42 display the Coanda bulb surface static pressures generated by upper and lower slot blowing (figure 41) and dual slot blowing (figure 42). An expansion at the slot is immediately followed by a compression before the flow accelerates again. Also observed in each figure is the aft movement of the shock with increasing $C_\mu$. 

18
$Mach = 0.8$ at $\alpha = 3^\circ$

Coanda Surface Effect

The incremental lift and pitching moments shown in figures 43, 44, and 45 are presented for the upper, lower, and dual slot blowing respectively. Increasing incremental lift and moments are observed with increasing blowing rates with upper slot blowing generating positive lift increments and negative pitching moment increments. Lower slot blowing generates negative lift and positive pitching moment increments. Dual slot blowing seen in figure 45 follows the Mach = 0.3 data trends, producing no appreciable incremental lift or pitching moments at any Coanda surface type. Generally, the data in figure 43 (upper slot blowing) display three distinct regions with the first region characterized by an increasing lift increment with further increasing $C_\mu$. As the Coanda surfaces lengthened, the regions were stretched out further with increasing $C_\mu$. The Coanda surface effect observed in this data indicates the larger Coanda surface is more effective over the mid to high $C_\mu$ range, while all three Coanda surfaces are equivocal in the low $C_\mu$ range. The data suggest the jet on the longer Coanda surface remains attached longer over a larger range of momentum coefficients while conversely, the jet separates much sooner on the smaller Coanda surfaces. This data trend is generally followed in figure 44 for lower slot blowing. However, the lower slot blowing is not as effective in producing lift and pitching moment increments as the upper slot blowing over the same range of momentum coefficients. Also, as seen in figure 44, none of the Coanda surfaces tested were capable of generating incremental lift or pitching moment for $h/c = 0.0026$. Note the contrast to this in figure 43 at $h/c = 0.0026$, for the 2.98:1 Coanda surface which shows that it does not diminish in effectiveness but appears to be somewhat asymptotic, reaching a maximum increment and maintaining that increment over the upper $C_\mu$ range. At Mach = 0.8 at $\alpha = 3^\circ$, the upper slot position slightly outperformed the lower slot position, with the upper slot generating a maximum $\Delta Cl$ of 0.25 at a $C_\mu$ of 0.008.

The Coanda surface effect using the lift augmentation ratio is observed in figures 46 and 47 for upper slot blowing and figures 48 and 49 for lower slot blowing. Dual slot blowing data are not presented since no appreciable increments were generated. Data are presented in the above figures as $\Delta Cl / C_\mu$ versus $C_\mu$ or versus $U_{jet} / V_\infty$. The data generally follow the same trend as the Mach 0.3 data where with increasing $C_\mu$ or velocity ratio values, the lift augmentation diminishes. In figure 46, at very low $C_\mu$ values, the 1.78:1 Coanda surface initially generates the largest lift augmentation values, but its effectiveness rapidly diminishes as $C_\mu$ and slot heights are increased where the apparent preferred Coanda surface becomes the larger 2.98:1 Coanda surface. It is also observed as the slot $h/c$ increases, the maximum lift augmentation value attained decreases for each Coanda surface. Similar trends are observed in figure 47. In figures 48 and 49 for lower slot blowing, generally no significant Coanda effects are observed, with each Coanda surface essentially equivocal.

A Coanda surface effect is observed in figure 50, $\Delta Cl$ versus nozzle pressure ratio (NPR), on upper slot blowing only. Figure 50 generally follows the same trends as reported above in figures 43, 44, and 45.

Slot Height Effect

A slot height effect using incremental lift and pitching moments due to upper, lower, and dual slot blowing can be observed in figures 51, 52, and 53 respectively. The same type of data regions found in the Coanda effect (figure 43) is also observed in the slot height effect data. The data in figures 51 and 52 indicate that the smaller slot sizes are more effective over the Coanda surface range. On the 2.98:1 Coanda surface, the data indicate that the $h/c = 0.0007$ slot is equivocal in effectiveness as the $h/c = 0.0012$ slot. It can be seen in the aforementioned figures that as the Coanda surface size increases, the $C_\mu$ value where...
incremental lift and pitching moments are equal to zero increases in magnitude. Dual slot blowing, seen in figure 53, follows previously shown dual slot blowing trends, which display the inability for it to produce appreciable incremental lift or pitching moments at any slot height.

A slot height effect using the lift augmentation ratio for upper slot blowing is observed in figures 54 and 55 and for lower slot blowing in figures 56 and 57. On upper and lower slot blowing, generally the data indicate the smaller the slot height the greater the increment magnitude. Additionally, the data in figure 56, lower slot blowing, also suggest that at $C_{\mu} > 0.02$ on any given Coanda, the slots are equivocal in effectiveness. Similar trends are observed in figure 49.

2.98:1 Coanda with $h/c = 0.0012$ Slot

It was demonstrated for transonic conditions that the 2.98:1 Coanda surface using the $h/c = 0.0012$ slot was the preferred trailing edge circulation control configuration of all possible combinations. This section expands the results specifically for this preferred trailing edge configuration for upper and lower slot blowing operations. Due to the large $C_{\mu}$ range at Mach = 0.3, some of its incremental data was truncated in an effort to show the effects at lower $C_{\mu}$ ranges.

Mach Number Effect

The Mach number effect can be observed in figures 58 and 59, for upper and lower slot blowing respectively. In figures 58 and 59, the data suggest that generally this trailing edge configuration becomes less effective as the Mach number and $C_{\mu}$ is increased. This is in agreement with the data from reference 6. The corresponding lift augmentation ratios are observed in figures 60 and 61.

Mach number effects on the center of pressure location can be observed in figure 62 for upper and lower slot blowing. The large shift in the center of pressure at higher blowing rates is attributed to the jet detaching from the Coanda bulb surface.

Angle of Attack Effect

Figures 63 and 64 display an angle of attack effect for upper and lower slot blowing respectively. In figure 63 at Mach = 0.3 and 0.84, it appears the lower the angles of attack, the greater the slot effectiveness is. However, at Mach = 0.7 and 0.8, at higher $C_{\mu}$ values the opposite appears to be true, with the higher angles of attack appearing to be more effective than the lower angles of attack. For the lower slot blowing cases shown in figure 64, for Mach = 0.3 and 0.84, the effectiveness of the slot increases as angle of attack increases to $\alpha = 3$. However, at larger angles of attack, the slot becomes less effective. This may be due to an increased flow separation on the wing. But at Mach 0.7 and 0.8, the data generally indicate that as the angle of attack increases, the slot effectiveness decreases. However, it is noted in both figures 63 and 64 the performance differences between the angles of attack are very marginal, and in some cases the effectiveness across the angles of attack could be considered equivocal.

The angle of attack effect on the lift augmentation ratio can be observed in figures 65 and 66, upper and lower slot blowing respectively. Similar angle of attack effect trends that were observed in figures 63 and 64 are observed in figures 65 and 66.

In figures 67 and 68, an angle of attack effect can be observed on the lift coefficient ($C_{l}$) using upper and lower slot blowing. In these figures, as the Mach number increases, the lift increases with increasing angles of attack. Beginning at Mach = 0.8, $C_{l}$ reaches a maximum magnitude and remains somewhat
constant over a discrete $C_U$ range, and then diminishes as $C_U$ increases. Similar trends are observed in figures 69 and 70 with the velocity ratio ($U_{jet} / V_{∞}$) on the independent axis.

**Slot Blowing Position Effect**

In figure 71, at Mach = 0.3 and $\alpha = 3°$, the upper and lower slots are essentially equivocal in performance. However as angle of attack is increased to 6° (Mach = 0.3), the upper slot blowing is slightly more effective than the lower slot blowing. As the Mach number is increased, the upper slot blowing becomes slightly more effective than lower slot blowing.

**Pressure Distributions**

**Main Airfoil Body**

The effect of upper, lower, and dual slot blowing on the upper and lower surface pressures at $\alpha = 3°$ is observed in figures 72 (upper slot blowing), 73 (lower slot blowing), and 74 (dual slot blowing). In figure 72 at Mach = 0.3 and 0.7, a slight blowing effect can be seen across the upper airfoil surface. As the flow nears the slot exit, the pressure data indicate the flow accelerates and lowers the upper surface pressures resulting in an aft loading of the airfoil. At the same Mach numbers in figure 73, lower slot blowing, a different trend is seen. In lieu of decreasing the upper surface pressures as the upper slot blowing did, the lower slot blowing increased those pressures suggesting that lower slot blowing may enhance the environment to promote separated flow on the upper surface. In figures 72, 73, and 74, at Mach = 0.84, the overall trend for the upper surface pressures is to slightly decrease with increasing $C_U$. In figure 72, Mach = 0.84, upper slot blowing, initially with increasing $C_U$, the aft shock tends to move aft towards the Coanda surface, and as $C_U$ increases further, the shock reverses and moves forward towards the leading edge of the airfoil. This shock movement is caused by the slot blowing influencing the flow field upstream of the slot. In figure 73, lower slot blowing, the opposite is observed at Mach = 0.84 where initially the shock moves forward towards the leading edge, then as $C_U$ increases further, the shock reverses and moves aft towards the Coanda surface. For dual slot blowing at Mach = 0.84, as seen in figure 74, the shock moves forward towards the leading edge of the airfoil with increasing $C_U$.

In figure 72, upper slot blowing, at Mach = 0.8, what appears to be a leading edge shock tends to weaken with increasing $C_U$. However, in figure 73, lower slot blowing, this possible leading edge shock seems to slightly increase in strength with increasing $C_U$. In figure 74, as anticipated, dual slot blowing had no apparent blowing effect on the shock. In figures 72, 73, and 74, no significant blowing effects are observed on the leading edge below Mach = 0.7.

**Coanda Bulb**

Figures 75 and 76 are the pressure distributions at $\alpha = 3°$ of the upper and lower surface of the 2.98:1 Coanda bulb using the h/c = 0.0012 slot at various Mach numbers. In figure 75 (upper slot blowing) with increasing $C_U$, a shock is observed on the bulb just aft of the slot exit. Once the shock forms, generally as $C_U$ increases, the shock appears to move aft on the bulb. At $C_U$ values greater than or equal to 0.017 and Mach numbers ≥ 0.8, the jet appears to detach from the bulb, and the pressures generally recover near to its no blowing static pressure values. No such jet detachment is observed in the Mach = 0.7 and 0.3 data. These same trends and Mach numbers are observed in figure 58 (lower slot blowing). The dual slot blowing data are seen in figures 77 through 80. At Mach = 0.84 (figure 77), increasing $C_U > 0.019$ apparently has the effect of detaching the jet from the bulb surface, and then the bulb surface pressure recovers to near its no blowing static pressure values.
**Drag**

**Dual Slot Blowing**

Dual slot blowing is where the upper and lower slots had the same slot h/c value and were blown simultaneously at the same $C_\mu$. Dual slot blowing tests were conducted primarily to evaluate drag reduction effects obtained by using the jet to eliminate separation and fill the wake for the blunt Coanda trailing edges. Drag measurements were acquired by integrating the wake rake pressures and accounting for the additional momentum introduced into the test section, making them equivocal to what a balance would measure if induced effects could be eliminated (ref. 26).

Presented in figure 81 are dual slot blowing drag coefficient plots at two Mach numbers at different angles of attack. The $C_\mu = 0$ drag coefficient at both Mach = 0.3 at $\alpha = 6^\circ$ and Mach = 0.8 at $\alpha = 3^\circ$ is approximately 0.012. Ideal thrust curves are also provided in figure 81 for reference to indicate the thrust only effects of dual blowing. At Mach = 0.3, the dual slot blowing decreases the drag along the ideal thrust curve, indicating a net 100% thrust efficiency. This net efficiency is a result of the slot nozzle losses being offset by reduced drag of the baseline airfoil due to blowing. At Mach = 0.8, the dual slot blowing decreases the drag below the ideal thrust curve (greater than 100% efficiency), clearly indicating the baseline drag is reduced by dual blowing. This effect is greatest at $C_\mu = 0.005$ and is most likely caused by the elimination of flow separation on the blunt trailing edge. In figure 82, an angle of attack effect is observed in both Mach numbers with $\alpha = 10^\circ$ displaying the greater drag.

**Slot Blowing Position Effect**

*Coanda 1.78:1 with h/c = 0.0012 Slot*

In figure 83 a slot blowing position effect on drag can be observed at two different Mach numbers and angles of attack. The data in figure 83 at Mach = 0.3 suggest when compared to the ideal thrust curve, over the $C_\mu$ range, no loss or gain in drag is observed in the dual slot blowing, and only a marginal decrease in drag is observed using just the lower slot. However, a rise in drag from upper slot blowing is observed over the $C_\mu$ range. At Mach = 0.8, the data indicate dual slot blowing decreases the drag along the ideal thrust curve up to a $C_\mu = 0.015$ where it increases the drag for all $C_\mu$'s > 0.015. In relationship to the ideal thrust curve, the upper and lower slots generally increase the drag at Mach = 0.8.

*Coanda 2.98:1 with h/c = 0.0012 Slot*

In figure 84 a slot position effect on drag can be observed at two different Mach numbers and angles of attack. The data at Mach = 0.3 and 0.8 follow the same trends seen in figure 83 (Coanda 1.78:1, h/c = 0.0012) with the exception of dual slot blowing at Mach = 0.8, where the data indicate dual slot blowing marginally reduces the drag over the $C_\mu$ range when compared against the ideal thrust curve.

**Angle of Attack Effect**

*Coanda 2.98:1 with h/c = 0.0012 Slot*

Presented in figures 85 and 86 is an angle of attack effect on upper and lower slot blowing respectively, on the drag coefficient at Mach = 0.3 and Mach = 0.8. The data generally indicate that at both
slot positions and over the $C_\mu$ range, higher angles of attack result in larger drag. Also seen in figures 85 and 86, as $C_\mu$ increases, the drag diminishes.

Summary of Results

1. A wind tunnel experiment was conducted in the NASA Langley Transonic Dynamics Tunnel (TDT) at Mach numbers of 0.3, 0.5, 0.7, 0.8, and 0.84 on a two dimensional, six percent thick airfoil with a modified trailing edge used to enhance the Coanda effect by tangential jet slot blowing.

2. The endplate does not produce a strong effect on the results.

3. The Mach = 0.3 and 0.5 data trend generally indicated that the smaller the Coanda surface and slot h/c, greater were the lift and pitching moment increments.

4. The Mach 0.7, 0.8, and 0.84 data trend generally indicated that the larger the Coanda surface and slot h/c, greater were the lift and pitching moment increments.

5. Increasing incremental lift and moments are observed with increasing blowing rate, with upper slot blowing creating positive lift increments and negative pitching moment increments, while lower slot blowing creates negative lift and positive pitching moment increments.

6. Lower slot blowing was not as effective in producing lift and pitching moment increments at transonic velocities as the upper slot blowing over the same range of momentum coefficients.

7. At Mach = 0.3 and $\alpha = 6^\circ$, the 1.78:1 Coanda with the upper slot blowing position having a slot height of h/c = 0.0012 gave the maximum $\Delta Cl$ generated of 0.75 at a $C_\mu$ of 0.085.

8. At Mach = 0.8 and $\alpha = 3^\circ$, the 2.98:1 Coanda with the upper slot blowing position having a slot height of h/c = 0.0012 slightly outperformed the lower slot position, with the upper slot generating a maximum $\Delta Cl$ of 0.25 at a $C_\mu$ of 0.008.

9. Trailing edge blowing influenced the flow field upstream of the slot.

10. The pressure distribution on all Coanda bulbs at Mach $\geq 0.8$ suggests the jet detached from the bulb surface at the higher blowing rates, indicating a limit to the amount of blowing that can be accomplished without losing effectiveness.

11. At Mach 0.84, the trailing edge shock at the higher blowing rates moves forward possibly creating an area of flow separation thereby affecting the center of pressure location.

12. Based upon the $\Delta Cl$ and $\Delta Cm$ data, no appreciable Coanda surface and slot height preference were found with dual slot blowing.

13. Dual slot blowing resulted in the reduction of the airfoil’s baseline drag at Mach = 0.8 and yielded near ideal slot thrust recovery at Mach = 0.3 and 0.8.

14. The movement of the airfoil shock (typically Mach = 0.84) at higher blowing rates is due to the flow field responding to the jet attachment and detachment on the Coanda bulb.
Appendix A

Gap and Chord Length Measurements

Below are gap height and chord length measurements at specific locations on the model.

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Half-Height (h4) 4-layers of tape @ 0.0035-in per layer taped on ‘small’ slot

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Appendix B

Critical Flow Venturi Calibration

Test Facility

The NASA Langley Jet Exit Facility is an indoor nozzle test stand which combines multiple flow air propulsion simulation with high pressure and high mass flow capabilities. Two individually controlled 1800 psia air lines supply the test model system(s), and each can provide flow rates up to 23 lbm per second. Supply air is heated to maintain room temperature conditions at critical model measurement stations. The mass flow rate of each air line is measured using a system of multiple critical venturi meters. Such systems allow accurate mass flow computations over a large range of flow rates. Pressurized air from one or both supply lines is directed through a selected model interface system into the propulsion simulation geometry and vented to atmosphere in the large test bay area. Exhaust flow is drawn outside the facility through two roof mounted ventilation systems, keeping the test bay conditions at atmospheric pressure.

The dual flow propulsion simulation system is designed for supply and control of two separate flow fields: a primary (core) flow and a secondary flow. It incorporates a 6 component strain gage force and moment balance with maximum axial force capacity of 1200 lbf. A nozzle installed to this rig can be tested at charging station total pressures up to 350 psi and total temperatures up to 90°F. Such conditions provide nozzle pressure ratios in excess of 20.

Venturi Description and Instrumentation

The two critical flow venturis, serial numbers 47 and 48, are identical and were assembled as shown in figure B1. They require 1 inch diameter input/exit lines and have a venturi throat diameter of 0.505 inch. Each venturi has a total pressure keel probe located upstream of the venturi throat and a static pressure and a total temperature probe located at the venturi throat. Located upstream of the venturi (figure B1) is the control valve which controlled the airflow to the venturi and was operated remotely from within the control room.

Typical Venturi Cross Section

![Typical Venturi Cross-section](image)

Figure B1 - Typical Venturi cross section and its assembly.
The in line venturi assemblies were attached to the Jet Exit Facility's secondary flow system that supplied a known quantity of mass flow measured by the upstream multiple critical venturi meters. The test venturi assemblies were attached to the secondary system’s alternate cover plate as shown in figure B2. Thus, controlled and metered airflow was supplied to each venturi system for calibration of flow rate as a function of internal pressure.

The test venturis’ total pressure and temperature measurements were correlated with the known mass flow and temperature from the secondary flow system to obtain the venturi calibrations. This test did not utilize the balance.

![Figure B2 - Venturis s/n 47 & 48 installation.](image)

**Experimental Instrumentation**

Upstream total pressure was acquired using a total pressure keel probe for each venturi. Throat static pressure and total temperature were also acquired. A Type J thermocouple was used to acquire the total temperature at the throat.

**Calibration Conditions**

The venturis were calibrated at two different air temperatures of 75° F and 55° F over a mass flow range from 0.6 to 2.0 lbms/sec at total pressures ranging from 0 psi to 400 psi. Mass flow data points were gathered in 0.1 lbms/sec increments to capture any unexpected non lineairities from the venturis. Repeat points were taken at the end of each run to ensure data integrity.

**Data Reduction**

Jet Exit Facility data were reduced in accordance with reference 25. Venturi mass flow was determined from flow conditions at the facility Multiple Critical Venturis (MCV) according to the following relationships (equation B1).
For choked conditions
\[
\left( \frac{p_\infty}{p_{o_s}} \right) \leq 0.5283
\]

\[
mdot = \left( A_{4,4} \right. \left. * P_{o_s} * \sqrt{\frac{g_c}{R T_o}} * \left( \frac{2}{\gamma + 1} \right) \right)^{\gamma + 1} \left( \frac{2}{\gamma - 1} \right) lbms / sec
\]

where
\[
A_1 = MCV1_Throat_Area (0.00019 ft^2)
\]
\[
A_4 = MCV4_Throat_Area (0.00076 ft^2)
\]
\[
P_{o_s} = Total_Pressure_of_Supply_Air (psf)
\]
\[
p_\infty = Atmospheric_Static_Pressure (psf)
\]
\[
\gamma = 1.4
\]
\[
g_c = 32.174 \left( \frac{lbm - ft}{lbf - s^2} \right)
\]
\[
R = 53.34 \left( \frac{ft - lbf}{lbm - R} \right)
\]
\[
T_o = Supply_Air_Temperature (Rankine)
\]
Temperature Effect
Left Venturi S/N 47

55 deg. (F)  
75 deg. (F)

System Mass Flow (lbm/sec)

Mdot 55 = 0.00176 + 0.00448x  R = 0.9997
Mdot 75 = 0.00129 + 0.00459x  R = 0.9998

Right Venturi S/N 48

Figure B3 – Temperature effects plot.
Results

The test venturi calibrations are presented as curve fits to the system mass flow vs venturi total pressure as found in figure B3. Since the curve fits are very nearly linear, the calibration are expressed as a discharge coefficients as seen in equation B2.

\[ CD = \left( \frac{w_{p_{\text{actual}}}}{w_{p_{\text{ideal}}}} \right) = \text{discharge coefficient} \quad (B2) \]

where:

\[ w_{p_{\text{actual}}} = \text{flow rate in lbm/sec from facility Multiple Critical Venturi (MCV) system.} \]

\[ w_{p_{\text{ideal}}} = \text{flow rate in lbm/sec calculated using 1-D flow equation using total pressure, total temperature and area at the test venturi.} \]

As seen in figure B3 and table B1, negligible temperature effects are observed in the venturi discharge coefficients. The discharge coefficients determined at 75°F were used for this experiment and were 0.971 and 0.982 for venturis S/N 47 and S/N 48, respectively.

<table>
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<th>Venturi Serial Number (S/N)</th>
<th>55°F</th>
<th>75°F</th>
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<tr>
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<td>0.974</td>
<td>0.971</td>
</tr>
<tr>
<td>48</td>
<td>0.984</td>
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Table B1 – Discharge Coefficients
References


Figure 19 – Airfoil performance, Mach number effect, no blowing.
Figure 19 – Continued.
Figure 19 – Continued.
Figure 19 – Concluded.
Figure 20 – Chordwise pressure distribution, angle of attack effect, no blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 20 – Concluded.
Figure 21 – Center of pressure versus angle of attack, Mach number effect, no blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 22 – End plate effects, Mach = 0.3.
Figure 23 – End plate effects, Mach = 0.8.
Figure 24 – ΔC_l & ΔC_m versus C_μ, Coanda surface effect, upper slot blowing, Mach = 0.3, α = 6°.
Figure 25 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, Coanda surface effect, lower slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 
Figure 26 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, Coanda surface effect, dual slot blowing, Mach = 0.3, $\alpha$ = 6°.
Figure 27 – Lift augmentation ratio versus $C_\mu$, Coanda surface effect, upper slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 
Figure 28 – Lift augmentation ratio versus velocity ratio, Coanda surface effect, upper slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 
Figure 29 – Lift augmentation ratio versus $C_\mu$, Coanda surface effect, lower slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 

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Figure 30 – Lift augmentation ratio versus velocity ratio, Coanda surface effect, lower slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 
Figure 31 – $\Delta C_l$ versus nozzle pressure ratio, Coanda surface effect, upper slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 
Figure 32 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, slot height effect, upper slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 
Figure 33 – $\Delta C_1$ & $\Delta C_m$ versus $C_{\mu}$, slot height effect, lower slot blowing, $Mach = 0.3$, $\alpha = 6^\circ$. 
Figure 34 – $\Delta C_1$ & $\Delta C_m$ versus $C_{\mu}$, slot height effect, dual slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 
Figure 35 – Lift augmentation ratio versus $C_\mu$, slot height effect, upper slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 
Figure 36 – Lift augmentation ratio versus velocity ratio, slot height effect, upper slot blowing, Mach = 0.3, \( \alpha = 6^\circ \).
Figure 37 – Lift augmentation ratio versus $C_{\mu}$, slot height effect, lower slot blowing, Mach = 0.3, $\alpha = 6^\circ$. 

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Figure 38 – Lift augmentation ratio versus velocity ratio, slot height effect, lower slot blowing, Mach = 0.3, α = 6°.
Figure 39 – ΔC_l & ΔC_m versus C_μ, slot position effect, Coanda (1.78:1), slot (h/c = 0.0012).
Figure 40 – Upper and lower chordwise pressure distribution, Coanda (1.78:1), slot (h/c = 0.0012), Mach = 0.3, $\alpha = 6^\circ$. 
Dual Slot Blowing

\[ C_{\mu} = \text{No blowing} \]
\[ C_{\mu} = 0.016 \]
\[ C_{\mu} = 0.07 \]
\[ C_{\mu} = 0.09 \]
\[ C_{\mu} = 0.02 \]

Figure 40 – Concluded.
Figure 41 – Upper and lower surface Coanda bulb pressure distribution, Coanda (1.78:1), slot (h/c = 0.0012), Mach = 0.3, $\alpha = 6^\circ$. 

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Figure 42 - Coanda bulb pressure distribution, dual slot blowing
Coanda (1.78:1), slot (h/c = 0.0012), Mach = 0.3, $\alpha = 6^\circ$. 
Figure 43 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, Coanda surface effect, upper slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 44 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, Coanda surface effect, lower slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 45 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, Coanda surface effect, dual slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 46 – Lift augmentation ratio versus $C_\mu$, Coanda surface effect, upper slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 47 – Lift augmentation ratio versus velocity ratio, Coanda surface effect, upper slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 48 – Lift augmentation ratio versus $C_\mu$, Coanda surface effect, lower slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 

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Figure 49 – Lift augmentation ratio versus velocity ratio, Coanda surface effect, lower slot blowing, Mach = 0.8, $\alpha = 3^\circ$.  

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Figure 50 – $\Delta C_1$ versus nozzle pressure ratio, Coanda surface effect, upper slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 51 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, slot height effect, upper slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 52 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, slot height effect, lower slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 53 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, slot height effect, dual slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 

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Figure 54 – Lift augmentation ratio versus C_μ, slot height effect, upper slot blowing, Mach = 0.8, α = 3°.
Figure 55 – Lift augmentation ratio versus velocity ratio, slot height effect, upper slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 56 – Lift augmentation ratio versus $C_\mu$, slot height effect, lower slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 
Figure 57 – Lift augmentation ratio versus velocity ratio, slot height effect, lower slot blowing, Mach = 0.8, $\alpha = 3^\circ$. 

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Figure 58 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, Mach number effect, upper slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 58 – Continued.
Figure 58 – Concluded.
Figure 59 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, Mach number effect, lower slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 59 – Continued.
Figure 59 – Concluded.
Figure 60 – Lift augmentation ratio versus $C_\mu$ or velocity ratio, Mach number effect, upper slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 60 – Continued.
Figure 60 – Concluded.
Figure 61 – Lift augmentation ratio versus $C_\mu$ or velocity ratio, Mach number effect, lower slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 61 – Continued.
Figure 61 – Concluded.
Figure 62 – Center of pressure location versus $C_\mu$, Mach number effect, Coanda (2.98:1), slot ($h/c = 0.0012$).
Figure 63 – $\Delta C_l$ & $\Delta C_m$ versus $C_\mu$, angle of attack effect, upper slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 63 – Concluded.
Figure 64 – $\Delta C_1$ & $\Delta C_m$ versus $C_\mu$, angle of attack effect, lower slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 64 – Concluded.
Figure 65 – Lift augmentation ratio versus $C_\mu$ or velocity ratio, angle of attack effect, upper slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 65 – Concluded.
Figure 66 – Lift augmentation ratio versus $C_\mu$ or velocity ratio, angle of attack effect, lower slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
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Figure 67 – $C_l$ versus $C_\mu$, angle of attack effect, upper slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 67 – Concluded.
Figure 68 – $C_l$ versus $C_\mu$, angle of attack effect, lower slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 68 – Concluded.
Figure 69 – $C_l$ versus velocity ratio, angle of attack effect, upper slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 69 - Concluded.
Figure 70 – $C_l$ versus velocity ratio, angle of attack effect, lower slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 70 – Concluded.
Figure 71 – $\Delta C_1$ & $\Delta C_m$ versus $C_\mu$, slot position effect, Coanda (2.98:1), slot ($h/c = 0.0012$).
Figure 71 – Concluded.
Figure 72 – Upper and lower chordwise surface pressure distribution, $C_\mu$ effect, upper slot blowing, Coanda (2.98:1), slot (h/c = 0.0012), $\alpha = 3^\circ$. 

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Figure 73 – Upper and lower chordwise surface pressure distribution, $C_\mu$ effect, lower slot blowing, Coanda (2.98:1), slot (h/c = 0.0012), $\alpha = 3^\circ$. 
Figure 74 – Upper and lower chordwise surface pressure distribution, $C_\mu$ effect, dual slot blowing, Coanda (2.98:1), slot ($h/c = 0.0012$), $\alpha = 3^\circ$. 
Figure 75 – Upper surface Coanda bulb pressure distribution, $C_\mu$ effect, upper slot blowing, Coanda (2.98:1), slot (h/c = 0.0012), $\alpha = 3^\circ$. 
Figure 76 – Lower surface Coanda bulb pressure distribution, $C_\mu$ effect, lower slot blowing, Coanda (2.98:1), slot (h/c = 0.0012), $\alpha = 3^\circ$. 

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Figure 77 – Coanda bulb pressure distribution, dual slot blowing, Coanda (2.98:1), slot (h/c = 0.0012), Mach = 0.84, $\alpha = 3^\circ$. 
Figure 78 – Coanda bulb pressure distribution, dual slot blowing, Coanda (2.98:1), slot (h/c = 0.0012), Mach = 0.8, $\alpha = 3^\circ$. 
Figure 79 – Coanda bulb pressure distribution, dual slot blowing, Coanda (2.98:1), slot (h/c = 0.0012), Mach = 0.7, α = 3°.
Figure 80 – Coanda bulb pressure distribution, dual slot blowing, Coanda (2.98:1), slot (h/c = 0.0012), Mach = 0.3, $\alpha = 3^\circ$. 
Mach = 0.3
$\alpha = +6^\circ$

Mach = 0.8
$\alpha = +3^\circ$

Figure 81 – $C_d$ versus $C_\mu$, Coanda surface effect, dual slot blowing, slot (h/c = 0.0012).
Figure 82 – $C_d$ versus $C_\mu$, angle of attack effect, dual slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 83 – $C_d$ versus $C\mu$, slot position effect, Coanda (1.78:1), slot (h/c = 0.0012).
Figure 84 – $C_d$ versus $C_\mu$, slot position effect, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 85 – $C_d$ versus $C_\mu$, angle of attack effect, upper slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
Figure 86 – $C_d$ versus $C_\mu$, angle of attack effect, lower slot blowing, Coanda (2.98:1), slot (h/c = 0.0012).
A wind tunnel test was conducted in the NASA Langley Transonic Dynamics Tunnel (TDT) on a six percent thick slightly cambered elliptical circulation control airfoil with both upper and lower surface blowing capability. Parametric evaluations of jet slot heights and Coanda surface shapes were conducted at momentum coefficients (Cm) from 0.0 to 0.12. Test data were acquired at Mach numbers of 0.3, 0.5, 0.7, 0.8, and 0.84 at Reynolds numbers per foot of 2.43 x 10^5 to 1.05 x 10^6. For a transonic condition, (Mach = 0.8 at $\alpha = 3^\circ$), it was generally found the smaller slot and larger Coanda surface combination was overall more effective than other slot/Coanda surface combinations. Lower surface blowing was not as effective as the upper surface blowing over the same range of momentum coefficients. No appreciable Coanda surface, slot height, or slot blowing position preference was indicated transonically with the dual slot blowing.