Afterbody Heating Predictions for a Mars Science Laboratory Entry Vehicle

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The Mars Science Laboratory mission intends to deliver a large rover to the Martian surface within 10 km of its target site. One candidate entry vehicle aeroshell consists of a 3.75-m diameter, 70-deg sphere-cone forebody and a biconic afterbody similar to that of Viking. This paper presents computational fluid dynamics predictions of laminar afterbody heating rates for this configuration and a 2010 arrival at Mars. Computational solutions at flight conditions used an 8-species Mars gas model in chemical and thermal non-equilibrium. A grid resolution study examined the effects of mesh spacing on afterbody heating rates and resulted in grids used for heating predictions on a reference entry trajectory. Afterbody heating rate reaches its maximum value near 0.6 W/cm² on the first windward afterbody cone at the time of peak freestream dynamic pressure. Predicted afterbody heating rates generally are below 3% of the forebody laminar nose cap heating rate throughout the design trajectory. The heating rates integrated over time provide total heat load during entry, which drives thermal protection material thickness.

Nomenclature

- \( a \) speed of sound (m/sec)
- \( C_D \) drag coefficient, \( D^{1/2} \rho V_c r S_{ref} \)
- \( CG \) center of gravity
- \( h \) altitude above ground level (km)
- \( L/D \) lift-to-drag ratio
- \( M \) Mach number
- \( MSL \) Mars Science Laboratory
- \( m \) aeroshell entry mass (kg)
- \( m/C_D S_{ref} \) ballistic coefficient (kg/m²)
- \( Q \) total heat load (J/cm²)
- \( q \) heating rate (W/cm²)
- \( Re \) Reynolds number, \( \rho u L_{ref}/\mu \)
- \( S_{ref} \) reference area, \( \pi D^2/4 \) (m²)
- \( T \) temperature (K)
- \( TPS \) Thermal Protection System
- \( t \) time from atmospheric interface (sec)
- \( V \) velocity relative to atmosphere (km/sec)
- \( X \) radial coordinate measured from nose (m)
- \( Z \) axial coordinate measured from nose (m)
- \( \alpha \) angle of attack (deg)
- \( \varepsilon \) surface emissivity
- \( \Delta \eta \) grid cell height at wall (m)
- \( \mu \) viscosity (kg/m²·sec)
- \( \rho \) density (kg/m³)
- \( \sigma \) Stefan’s constant (5.67 x 10⁻⁸ W/m²/K⁴)

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The Viking, Pathfinder, and Mars Exploration Rover missions successfully used ballistic entry trajectories to land on Mars with target accuracy on the order of 100 km. Second generation landers, such as the proposed Mars Science Laboratory (MSL), will be designed to land with 10 km or smaller footprints that are of particular scientific interest\textsuperscript{1,2}. MSL will achieve 10 km landing accuracy through the use of lift via an offset radial center of gravity (CG). Controlling the entry vehicle lift mitigates uncertainties in predicted entry states, atmospheric properties, aerodynamics, etc. that cause an unguided entry to have a large landing footprint. A hypersonic lift-to-drag ratio \((L/D)\) of 0.18 at a trim angle of attack \((\alpha)\) of 11 degrees and ballistic coefficient \((m/C_D S_{ref})\) less than 120 kg/m\(^2\) are the desired entry conditions for a 2010 arrival. References 3-8 contain computational and experimental aeroheating analyses for various MSL entry vehicle configurations. Topics include predictions on alternative aeroshell shapes\textsuperscript{3}, turbulent transition and heating augmentation\textsuperscript{4}, and experimental studies in perfect gas and high-enthalpy facilities to augment and validate the computational results\textsuperscript{5-8}. This paper presents computed MSL laminar flight afterbody heating predictions and comparisons to perfect gas wind tunnel data. The prediction of afterbody heating rates is a difficult problem, even with improvements in computational tools and resources. Consequently, the uncertainties in predicted flight environments are typically much larger than those on the forebody. Even though afterbody heating rates are low, generally only a few percent of forebody heating levels, improvement in their prediction would help reduce entry mass. For Viking, the peak afterbody heating rate was predicted to be 3\% (including a 1.5 factor of safety) of the nose laminar heating rate\textsuperscript{9}. Post-flight analysis of the temperature data showed that the heating rates were as high as 4.2\% of the nose laminar heating level. Since Viking, there have been few efforts to measure flight afterbody heating levels for Mars entry vehicles or compare modern computational methods to existing data\textsuperscript{10}. The current effort is the first step in using high-fidelity computational tools to predict MSL afterbody heating environments and estimate the uncertainties in those predictions.

II. Analysis

A. Aeroshell Geometry

Figure 1 shows the candidate entry vehicle aeroshell geometry and dimensions. The vehicle is a 3.75-m scaled version of the Viking 3.5-m 70-deg sphere-cone aeroshell\textsuperscript{11}, with a blunter shoulder radius. A 70-deg sphere-cone has been the forebody shape of choice for all previous Mars entry aeroshells. Figure 2 shows a comparison of the MSL and Viking aeroshell shapes. The Viking entry vehicle also was designed to trim at \(\alpha = 11\) deg using an offset CG. The MSL afterbody cone angles are identical to those of Viking. The MSL aeroshell accommodates a larger rover than did Viking.

Figure 1. Aeroshell Geometry and Dimensions
B. Computational Method

Computational Fluid Dynamics (CFD) modeling is combined with an experimental test program to predict the MSL flight vehicle aerothermodynamic environments. Hypersonic flight conditions in a reacting Mars atmosphere cannot be recreated in ground-based facilities, so the use of numerical tools is a critical element of the MSL aerothermodynamic analysis. The continued improvement of grid generation methods, flow solvers, and computational resources makes it possible to solve three-dimensional, chemically-reacting flowfields that once were prohibitive. The present analysis represents such an approach to predict afterbody flight aerothermodynamics that cannot be duplicated in ground-based facilities. When available, ground-based data are used to validate the CFD models for perfect gas conditions.

1. LAURA CFD Code

Aerothermodynamic calculations at flight conditions were performed using the Langley Aerothermodynamic Upwind Relaxation Algorithm (LAURA)\textsuperscript{12} CFD code. LAURA has been used previously to predict the aerothermodynamic environments for other Mars applications\textsuperscript{13,14}. For Mars flight conditions, LAURA models an 8-species Mars gas (CO\textsubscript{2}, CO, N\textsubscript{2}, O\textsubscript{2}, NO, C, N, O) in chemical and thermal non-equilibrium using the Park-94\textsuperscript{15} reaction rates. A finite-volume approach is used to solve the full Navier-Stokes flowfield equations for all calculations presented here. The code uses Roe’s averaging\textsuperscript{16} for the inviscid fluxes with second-order corrections using Yee’s symmetric total variation diminishing (TVD) scheme\textsuperscript{17}.

A super-catalytic wall boundary condition fixes the species mass fractions for CO\textsubscript{2} and N\textsubscript{2} at their freestream values of 0.97 and 0.03, respectively. This boundary condition results in conservative heating rate predictions in flight. A radiative-equilibrium wall temperature was specified to satisfy the following relation:

$$ q_\text{w} = \varepsilon \sigma T_w^4 $$

A fixed surface emissivity ($\varepsilon$) of 0.9 was used for all solutions. The wall is assumed to radiate to a temperature of absolute zero.

2. Computational Grid

LAURA solutions used a singularity-free structured volume grid of the reference configuration. Figure 3 shows the baseline surface and symmetry plane mesh distributions. Pitch plane symmetry allows modeling of only half of the aeroshell. The forebody nose cap and afterbody base meshes do not have a singularity pole boundary that could otherwise introduce artificial discontinuities into the flowfield. The finest streamwise grid resolution occurs at the shoulder and is necessary to resolve the rapidly expanding flow in that region.

The grids were built using GridGen\textsuperscript{18} to construct the topology and surface distribution, 3DGRAPE/AL\textsuperscript{19} to generate the volume grid, and the Volume Grid Manipulator (VGM)\textsuperscript{20} to enhance grid quality and impose boundary conditions along block interfaces. The baseline 56-block grid has 3280 surface cells and 64 cells in the surface normal direction. A grid resolution study examined meshes with finer resolution in all three coordinate directions.
3. Grid Adaptation

LAURA possesses the capability to adapt the computational mesh to the boundary layer and bow shock through user-defined parameters. Proper mesh resolution at the wall is especially important for reliable heating predictions. In LAURA, a user-specified cell Reynolds number controls the grid spacing at the wall:

$$Re_w = \left( \frac{\rho a \Delta \eta}{\mu} \right)_w$$  \hspace{1cm} (2)

Experience has shown that reliable laminar heating predictions can be achieved with $Re_w = O(1)$. Grid adaptations are executed throughout the solution process until further adaptations do not significantly change the heating rate.

C. Atmospheric Entry Trajectory

The MSL aeroheating analysis presented here is based on the 99.87% heat load trajectory for a 2010 arrival at Mars. The design trajectory was obtained through a Monte Carlo analysis of the entry system using Program to Optimize Simulated Trajectories (POST)\(^3\). The analysis included uncertainties in navigation, mass properties, atmospheric density, and entry vehicle aerodynamics. Entry conditions for the specified trajectory are a 5.5 km/sec...
atmosphere-relative velocity and a ** deg inertial flight path angle, The reference trajectory’s integrated heat load was the 3-sigma high case (99.87 percentile) of all cases run. Thermal protection system (TPS) material thickness, and thus mass, is proportional to the integrated heat load.

The MSL atmosphere-relative entry velocity is higher than Viking (4.5 km/sec, entry from orbit), lower than Pathfinder (7.47 km/sec, direct entry), and similar to the Mars Exploration Rovers (5.5 km/sec, direct entry).

Figure 4 shows the velocity-altitude map for the design trajectory. Reference heating rate, dynamic pressure, and Reynolds number based on aeroshell diameter (ReD) are shown in Figure 5. Atmospheric density perturbations included in the Monte Carlo analysis result in the plot line irregularities. The heating rate is based on the Sutton-Graves formula for a sphere having the same radius of curvature as the forebody nose. The peak heating rate occurs 89 seconds after atmospheric entry, followed by peak dynamic pressure at 110 seconds, and peak ReD at 120 seconds. LAURA solutions were obtained at eight time points along the trajectory, with freestream conditions summarized in Table 1.

<table>
<thead>
<tr>
<th>t (sec)</th>
<th>h (km)</th>
<th>V (km/sec)</th>
<th>ρ (kg/m³)</th>
<th>T (K)</th>
<th>M</th>
<th>ReD</th>
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<tr>
<td>50</td>
<td>68.3</td>
<td>5.54</td>
<td>4.71 x 10⁻⁶</td>
<td>145</td>
<td>29.1</td>
<td>1.37 x 10⁴</td>
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<td>70</td>
<td>47.7</td>
<td>5.48</td>
<td>7.63 x 10⁻⁵</td>
<td>149</td>
<td>29.3</td>
<td>2.11 x 10⁵</td>
</tr>
<tr>
<td>80</td>
<td>38.3</td>
<td>5.31</td>
<td>2.10 x 10⁻⁵</td>
<td>162</td>
<td>26.3</td>
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<td>89</td>
<td>31.0</td>
<td>4.98</td>
<td>4.74 x 10⁻⁴</td>
<td>179</td>
<td>24.4</td>
<td>9.82 x 10⁵</td>
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<td>4.10</td>
<td>1.05 x 10⁻³</td>
<td>189</td>
<td>18.9</td>
<td>1.68 x 10⁶</td>
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<tr>
<td>109</td>
<td>19.6</td>
<td>3.63</td>
<td>1.44 x 10⁻³</td>
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<td>17.0</td>
<td>2.03 x 10⁶</td>
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<td>137</td>
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<td>1.95</td>
<td>2.43 x 10⁻³</td>
<td>193</td>
<td>8.8</td>
<td>1.81 x 10⁶</td>
</tr>
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</table>

III. Results and Discussion

A grid resolution study was completed to determine the appropriate grid on which to compute flight predictions along the reference entry trajectory. The results of the grid study are shown along with afterbody heating rate predictions at various entry times and total integrated heat load.

1. Grid Resolution Study

Viscous CFD solutions require a large number of grid points and small spacing at wall boundaries in order to properly resolve the flowfield gradients. The complex features typical of blunt body wake flows make the grid requirements even more stringent for afterbody aeroheating predictions. The existence of unsteady flow, separation,
and turbulence further complicate the numerical prediction of wake flowfields. Consequently, uncertainties on the predicted afterbody heating environments are typically much larger than those on the forebody.

A blunt body CFD grid must capture the essential flowfield features in order to produce dependable heating results. Figure 6 shows a typical blunt body flowfield at a hypersonic Mach number. At such high speeds, the shock wave lies very close to the forebody. The wake flowfield is influenced by the shear layer evolution from the shoulder. It is critical to capture the shear layer with sufficient streamwise and normal grid points so that the effects on recirculation and detachment are properly captured further downstream.

The objective of the grid resolution study was to determine the appropriate wall spacing in the surface normal direction and the streamwise spacing at the aeroshell shoulder. Wall spacing determines the quality of the resolved boundary layer. Shoulder streamwise spacing impacts the location of the shear layer, which in turn determines the evolution of flow separation/impingement and recirculation further downstream. The grid resolution study consisted of running several LAURA solutions at the time of peak Sutton-Graves heating rate on the reference trajectory. Beginning with the baseline grid, the grid distribution was resolved to finer levels in all directions until the peak afterbody heating rate remain unchanged with further grid refinement. Solutions at the remaining trajectory times used two meshes resulting from the grid resolution study, one “coarse” and one “fine”; a full grid resolution study was not performed for each trajectory point.

Table 2 summarizes the grids used in the resolution study, beginning with the baseline mesh (Grid 1). Each subsequent grid possesses twice the number of cells in the streamwise, circumferential, and/or normal direction for at least a portion of the grid. Special attention was paid to the resolution at the shoulder and on the first afterbody cone where rapid flow expansion occurs. For each grid, the average streamwise resolution around the aeroshell shoulder is reflected by the number of degrees of turning per streamwise cell. Figures 7 and 8 show the surface mesh distribution for the first four grids in the resolution study. Each surface grid was run with 64 and 128 cells in the surface normal direction. Grids 3 and 4 (not shown) contained four and eight times, respectively, the streamwise surface grid resolution of Grid 1 on the shoulder and first afterbody cone (blocks 23-40 in Figure 8). Each grid was adapted to the boundary layer and bow shock within LAURA using the Re_w specified in Table 2.

Table 2. Grid Resolution Study

<table>
<thead>
<tr>
<th>Grid</th>
<th>Surface Cells</th>
<th>Normal Cells</th>
<th>Volume Cells</th>
<th>( \text{Re}_w )</th>
<th>Avg. Deg./Cell at Shoulder</th>
<th>Modification to Baseline Grid</th>
</tr>
</thead>
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<tr>
<td>1</td>
<td>3280</td>
<td>64</td>
<td>209,920</td>
<td>1</td>
<td>6.9</td>
<td>Baseline</td>
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<tr>
<td>1a</td>
<td>3280</td>
<td>128</td>
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<td>6.9</td>
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<tr>
<td>2</td>
<td>13120</td>
<td>64</td>
<td>839,680</td>
<td>1</td>
<td>3.5</td>
<td>4x Surface</td>
</tr>
<tr>
<td>2a</td>
<td>13120</td>
<td>128</td>
<td>1,679,360</td>
<td>0.5</td>
<td>3.5</td>
<td>4x Surface and 2x Normal</td>
</tr>
<tr>
<td>3</td>
<td>17360</td>
<td>64</td>
<td>1,111,040</td>
<td>1</td>
<td>1.7</td>
<td>4x Streamwise Shoulder</td>
</tr>
<tr>
<td>3a</td>
<td>17360</td>
<td>128</td>
<td>2,222,080</td>
<td>0.5</td>
<td>1.7</td>
<td>4x Streamwise Shoulder and 2x Normal</td>
</tr>
<tr>
<td>4</td>
<td>27440</td>
<td>64</td>
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<td>1</td>
<td>0.8</td>
<td>8x Streamwise Shoulder</td>
</tr>
<tr>
<td>4a</td>
<td>27440</td>
<td>128</td>
<td>3,512,320</td>
<td>0.5</td>
<td>0.8</td>
<td>8x Streamwise Shoulder and 2x Normal</td>
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</tbody>
</table>

Figure 6. Hypersonic Flowfield Streamlines and Contours of Normalized Velocity
Figures 9 and 10 show laminar windward afterbody heating rate, pressure, and shear stress as a function of radial coordinate for six of the eight grids in the resolution study. Figure 9 shows results for the first four grids. Peak afterbody heating rate occurs on the windward side of the first afterbody cone as the flow expands from the forebody. The predicted heating rate is nearly an order of magnitude lower at all other locations on the afterbody windward symmetry plane. The heating spikes at the windward shoulder (extreme left side) is ignored for the purposes of this study since it covers a relatively small area.

Figure 9 indicates that increasing normal and surface grid resolution separately (Grid 1a and 2) results in higher and lower heating rates, respectively, than the baseline level. The heating rates for Grid 1a and 2 are +13% and -11%, respectively, from the Grid 1 results on the first afterbody windward cone at X = -1.6 m. Simultaneously doubling the grid resolution in all three coordinate directions (Grid 2a) results in heating rates m those on Grid 1. The same trends are reflected in the pressure and shear stress predictions; the results on Grids 1a and 2 bound the Grid 1 results. The pressures for Grid 1a and 2 are +6% and -10%, respectively, from the Grid 1 results on the first afterbody windward cone at X = -1.6 m. The shear stress bounds at the same location are +5% and -4%. Grid 2a produces pressure and shear stress distributions matching those on Grid 1, which is consistent with the heating rate results. All four grids predict attached flow along the entire first afterbody cone. The grid effects are more noticeable on the second cone where flow separation occurs. Flow separation is located at the point where pressures increases and shear stress decreases. Grid 1a predicts the earliest separation, and Grid 2 the latest. Heating rate is least affected by flow separation.

Figure 10 show the effects of increased streamwise resolution at the shoulder on heating rate, pressure, and shear stress. Further streamwise grid refinement at the shoulder and first afterbody cone (Grid 3a and Grid 4a) does not change the predicted heating rate on the first windward afterbody cone from the results of Grid 1. The surface pressures and shear stress follow a similar trend. Again, there are small differences in the predicted flow separation point, with heating rate being the least affected. Grid 1 is the only grid with 64 normal cells that produces heating rates similar to those grids with 128 normal cells. It may be coincidental that the baseline grid resulted in the same heating rates on the first afterbody cone as the finest grids. Although Grid 1 produced grid independent heating on the first windward afterbody cone, both Grid 1 and Grid 2a were used for solutions at other time points to determine whether the finer grid produced significantly different results that did Grid 1 for other freestream conditions. The results are shown in the next section. Although not shown, increasing circumferential grid resolution does not affect predicted heating rate at α = 11 deg. Circumferential grid distribution may become more important if α increases and more crossflow is induced.
Figure 9. Effect of Grid Resolution on Computed Windward Afterbody Symmetry Plane Heating Rate (Top), Pressure (Middle), and Shear Stress (Bottom)

Figure 10. Effect of Streamwise Shoulder Grid Resolution on Computed Windward Afterbody Symmetry Plane Heating Rate (Top), Pressure (Middle), and Shear Stress (Bottom)
2. Flight Predictions

Figure 11 shows the Grid 1 laminar heating rate distribution on the forebody and afterbody at 89 seconds. At a trim angle of 11 degrees, the stagnation point moves to a location near the tangency point between the spherical nose cap and conical flank. However, the maximum forebody heating rate of 44 W/cm$^2$ is still located on the apex of the nose cap. Turbulent transition is predicted to augment forebody heating higher than the laminar level shown. The afterbody heating rates are two orders of magnitude lower than the forebody levels. As such, the backshell TPS thickness and mass are significantly smaller.

Computations at flight conditions were obtained on Grid 1 and Grid 2a to estimate peak afterbody heating rate and total integrated heat load for the reference trajectory. Figure 12 shows the streamlines and normalized velocity contours in the symmetry plane for each solution using Grid 1. The shock standoff distance is smallest at 89 seconds at a Mach number of 24.4. With increasing time, the extent of the wake decreases and the origin of the leeward shear layer moves forward along the afterbody until it reaches the aeroshell shoulder. The flow is predicted to remain attached on the first windward afterbody cone at all times. At 103 seconds, as Reynolds number increases, the flow starts to detach at the second windward afterbody cone and secondary recirculation regions appear. The sensitivity in predicted heating rate to each grid adaptation was larger at the higher Re$_D$, possibly because the flow is actually unsteady even though the CFD solutions assume a steady state flowfield. This was especially true near the base of the vehicle where the windward flow separation occurs on the second afterbody cone.

Figure 13 shows the afterbody heating rate distributions on Grid 1 at various times along the reference entry trajectory. The peak heating rate for each time occurs on the windward first cone (left side). Heating on the remaining afterbody regions is generally much lower, except at 109 and 113 seconds where the Reynolds number is approaching its peak value. The maximum heating rate occurs at the time of peak dynamic pressure (t = 109 sec) rather than the time of peak Sutton-Graves heating rate (t = 89 sec). Heating rate magnitudes on the bulk of the windward first cone vary between 0.2 W/cm$^2$ and 0.6 W/cm$^2$.

Afterbody heating rate normalized by computed laminar nose heating rate is shown in Figure 14. Heating rate prior to peak dynamic pressure (t = 109 sec) is predicted to be below 1% of forebody nose heating for most of the afterbody. Beginning at 109 sec, the non-dimensional heating rate is higher, but still generally less than 3% of the laminar forebody nose level. The predicted normalized heating rates are in line with general rules of thumb for afterbody heating (~2-5% of forebody heating). The predictions are also similar to Viking entry flight data, which showed windward afterbody heating rates on the afterbody first cone up to 4.2% of forebody heating.

Figure 15 shows afterbody heating rate at $X = -1.6$ m as a function of time, along with Sutton-Graves heating rate and dynamic pressure. Again, the afterbody heating rate more closely mirrors freestream dynamic pressure than it does the heating rate. The heating rates between the two grids are within 5% of one another at most times, with the largest difference of 19% occurring at 137 seconds. The heating rates in Figure 14 were integrated over time (0 to 250 seconds) to obtain the total heat load shown in Figure 15. Results from both Grid 1 and Grid 2a are shown. Grid 2a heat load is up to 6% lower on the first afterbody windward cone. The computed heat load is highest on the first windward cone, where it is generally between 40 and 100 J/cm$^2$. Heat load at other afterbody locations are lower, except for small regions near the aeroshell shoulder. The design heating environments will include uncertainties on the model predictions as well as uncertainties and margins for the TPS material response. Typical afterbody heating uncertainties are much larger than forebody heating uncertainties due to the complexity of wake flowfields, including unsteady flow and turbulence effects.
Figure 12. Computed Symmetry Plane Streamlines and Normalized Velocity Contours Along the Reference Trajectory (Grid 1)
IV. Summary and Conclusions

Computational afterbody heating predictions were obtained for a candidate Mars Science Laboratory entry aeroshell designed to fly at a trim angle of attack of 11 deg. The reference aeroshell is a 70-deg sphere-cone geometry with a biconic afterbody that is derived from the Viking entry vehicle. Flight predictions for a 2010 Mars arrival were computed with the LAURA code using an 8-species Mars gas in thermo-chemical non-equilibrium. Laminar solutions were obtained at several solutions along a reference trajectory resulting in the 3-sigma high integrated heat load. Afterbody heating rate reaches its maximum value near 0.6 W/cm² on the first windward afterbody cone at the time of peak freestream dynamic pressure. Computations on a baseline mesh and a mesh with double the resolution in each direction produce similar heating results. Afterbody heating rates are predicted to be generally less than 3% of the laminar heating rate on the forebody nose cap.
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References