Assessments of Fracture Toughness of Monolithic Ceramics—SEPB Versus SEVNB Methods

Sung R. Choi
University of Toledo, Toledo, Ohio

John P. Gyekenyesi
Glenn Research Center, Cleveland, Ohio

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University of Toledo, Toledo, Ohio

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Sung R. Choi
University of Toledo
Toledo, Ohio 43606

John P. Gyekenyesi
National Aeronautics and Space Administration
Cleveland, Ohio 44135

Abstract

Fracture toughness of a total of 13 advanced monolithic ceramics including silicon nitrides, silicon carbide, aluminas, and glass ceramic was determined at ambient temperature by using both single edge precracked beam (SEPB) and single edge v-notched beam (SEVNB) methods. Relatively good agreement in fracture toughness between the two methods was observed for advanced ceramics with flat R-curves; whereas, poor agreement in fracture toughness was seen for materials with rising R-curves. The discrepancy in fracture toughness between the two methods was due to stable crack growth with crack closure forces acting in the wake region of cracks even in SEVNB test specimens. The effect of discrepancy in fracture toughness was analyzed in terms of microstructural feature (grain size and shape), toughening exponent in R-curve, and stable crack growth determined using back-face strain gaging.

1. Introduction

There are several methods to determine fracture toughness of brittle materials such as glasses, glass ceramics, and advanced monolithic ceramics. These includes indentation techniques such as indentation fracture (IF) (ref. 1), indentation strength (IS) (ref. 2), surface crack in flexure (SCF) (ref. 3), chevron notch technique (ref. 3), single edge precracked beam (SEPB) technique (ref. 3), and single edge v-notched beam (SEVNB) technique (ref. 4). Both indentation fracture (IF) and indentation strength (IS) methods are based on the empirical calibration constants to determine fracture toughness; hence, they are less rigorous theoretically from a fracture-mechanics perspective than the other methods.

The SEVNB technique (ref. 4) has been introduced recently, in which a final sharp v-notch with its radius ranging from 10 to 20 μm was introduced by polishing a pre-notched section with razor blade in conjunction with diamond paste. This technique has shown to be in good agreement with other techniques. A previous round robin on fracture toughness (ref. 4) was dedicated to use the SEVNB method to determine fracture toughness of five
different ceramic materials. It was shown that certain ceramics exhibited significant difference in fracture toughness between the SEVNB and SEPB methods: the SEVNB estimated lower fracture toughness than the SEPB. The plausible reason for this discrepancy was presumed to be attributed to R-curve behavior of the materials.

This study, as motivated from the previous round robin, determined fracture toughness of a total of 13 advanced ceramics using both SEVNB and SEPB methods. The difference in fracture toughness between the two methods was carefully analyzed based on R-curve estimations and back-face strain measurements. The effect of major microstructural feature - grain size and its shape - was also taken into account.

2. Experimental Techniques

Flexure test specimens typically measuring $b = 3.0 \text{ mm}$, $W = 4.0 \text{ mm}$, and $L$ (length) = 25 or 50 mm, were used in fracture toughness testing at room temperature in air. In the SEVNB method, a razor blade with diamond paste with grain size of 1 $\mu\text{m}$ was used to generate a final sharp notch with a root radius ranging from 10 to 20 $\mu\text{m}$ by tapering a saw notch (ref. 4). The final notch depth thus produced ranged from 1.0 to 2.0 mm. A typical example of a SEVNB test specimen thus v-notched is presented in figure 1. In the SEPB method (ref. 3), a starting indent crack was placed at the center of the 3.0 mm side of each test specimen. The indented test specimen was then placed onto a specially designed precracking fixture and then loaded via a test frame until the indent crack popped-in to form a sharp through-the-thickness precrack (refs. 3 and 5). The precrack size was typically around 2 mm.
A four-point flexure fixture with 20 (or 10) mm-inner and 40 (or 20) mm-outer spans was used to determine fracture load. A test rate of 0.5 mm/min was used via an electromechanical test frame (Model 8562, Instron) with a load cell with a capacity of 1000 N. Crack sizes were optically determined from fracture surfaces of tested specimens. Typically, five test specimens were used for each material in each test method. Fracture toughness was calculated based on the formula by Srawley and Gross (ref. 6). Load versus back-face strain curves were also determined for some ceramics to better understand stable crack propagation. R-curve of each material was estimated using an indentation technique (ref. 7). A total of 13 advanced ceramics and glass ceramic were used: seven silicon nitrides (NC132, AS800 (’94), SN282, N3208, AS800 (’99), NCX34, and NKK), one silicon carbide (α-SiC; Hexoloy), four aluminas (AD998 (Coors), AD998 (VAMAS) (ref. 4), AD999 (VAMAS) (ref. 4), and 96% alumina), and one glass ceramic (Pyroceram 9606). Many properties of these materials including strength and slow crack growth at elevated temperatures have been evaluated previously by the authors and others (refs. 8 and 13). Some properties such as density, elastic 1modulus and flexure strength at ambient temperature, together with fracture toughness values by SEPB and SEVNB methods determined in this work, are summarized in table 1.

### TABLE 1.—PROPERTIES AND FRACTURE TOUGHNESS OF CERAMIC MATERIAL USED IN THIS WORK

<table>
<thead>
<tr>
<th>Material a</th>
<th>Density (g/cm³)</th>
<th>Elastic modulus, E (GPa)</th>
<th>Flexure strength b (MPa)</th>
<th>By SEPB</th>
<th>By SEVNB</th>
</tr>
</thead>
<tbody>
<tr>
<td>NC132 Si₃N₄ (ref. 8)</td>
<td>3.20</td>
<td>315</td>
<td>1018(35)</td>
<td>4.6(0.4)</td>
<td>4.3(0.1)</td>
</tr>
<tr>
<td>α-SiC (Hexoloy) (ref. 8)</td>
<td>3.13</td>
<td>415</td>
<td>335(35)</td>
<td>2.4(0.1)</td>
<td>2.5(0.1)</td>
</tr>
<tr>
<td>AS800 Si₃N₄ (’94) (ref. 8)</td>
<td>3.27</td>
<td>308</td>
<td>778(39)</td>
<td>7.2(0.2)</td>
<td>6.5(0.3)</td>
</tr>
<tr>
<td>SN282 Si₃N₄ (refs. 9 and 10)</td>
<td>3.32</td>
<td>304</td>
<td>595(64)</td>
<td>5.5(0.2)</td>
<td>4.5(0.2)</td>
</tr>
<tr>
<td>AD998 Al₂O₃ (ref. 8)</td>
<td>3.85</td>
<td>372</td>
<td>303(7)</td>
<td>4.6(0.4)</td>
<td>3.4(0.1)</td>
</tr>
<tr>
<td>Glass ceramic (Pyroceram) (ref. 11)</td>
<td>2.59</td>
<td>122</td>
<td>303(7)</td>
<td>2.3(0.1)</td>
<td>2.4(0.1)</td>
</tr>
<tr>
<td>AD998 Al₂O₃ (VAMAS) b (ref. 4)</td>
<td>3.86</td>
<td>386</td>
<td>342</td>
<td>4.4(0.1)</td>
<td>3.6(0.1)</td>
</tr>
<tr>
<td>AS800 Si₃N₄ (’99) (ref. 9 and 10)</td>
<td>3.27</td>
<td>309</td>
<td>775(45)</td>
<td>8.1(0.3)</td>
<td>6.7(0.1)</td>
</tr>
<tr>
<td>NCX34 Si₃N₄ (ref. 8)</td>
<td>3.37</td>
<td>296</td>
<td>805(50)</td>
<td>6.9(0.6)</td>
<td>4.3(0.2)</td>
</tr>
<tr>
<td>NKK Si₃N₄ (ref. 12)</td>
<td>3.26</td>
<td>307</td>
<td>774(38)</td>
<td>10.2(0.7)</td>
<td>7.4</td>
</tr>
<tr>
<td>96% Al₂O₃ (ref. 8)</td>
<td>3.67</td>
<td>309</td>
<td>344(15)</td>
<td>3.4(0.1)</td>
<td>3.1(0.1)</td>
</tr>
<tr>
<td>AD999 Al₂O₃ (VAMAS) b (ref. 4)</td>
<td>3.97</td>
<td>386</td>
<td>350</td>
<td>3.5(0.2)</td>
<td>3.6(0.2)</td>
</tr>
</tbody>
</table>

a NC132, Norton Advanced Ceramics, Northboro, MA; α-SiC (Hexoloy), Saint-Gobain Advanced Ceramics, Niagara Falls, NY; AS800; Honeywell, Torrance, CA; SN282, Kyocera, Vancouver, WA; AD998, Coors, Golden, CO; N3208, Bayer-CFI, Germany; Pyroceram 9606, Corning, Corning, NY; AD998 (VAMAS) and AD999 (VAMAS), Metoxit, Switzerland; NCX34, Norton, Worcester, MA; NKK, NKK Corp., Japan; 96% Al₂O₃, General Electrical Ceramics, Laurens, SC.

b Materials and their strength and density data from the VAMAS report (ref. 4).

c Strength determined at ambient temperature in four-point flexure typically with 20 to 40 mm spans. The numbers in parentheses indicate ±1.0 standard deviation.
3. Results and Discussion

Typical fracture surfaces of both SEPB and SEVNB silicon nitride specimens are shown in figure 2. Precracked or notched region is evident for each specimen. Note that the precrack front of the SEPB specimen is curved, which represents a unique feature of a pop-in event from a micro-indentation crack to form a precrack. A summary of fracture toughness of a total of 13 advanced ceramics used in this work by both SEVNB and SEPB methods is presented in figure 3 and table 1 as well. The figure compares the values of fracture toughness for each test material. As can be seen, agreement in fracture toughness between the two methods was good at lower fracture toughness, but poor at higher fracture toughness with a deviation becoming significant. This deviation can be seen more readily in terms of microstructural features -grain size and its shape- of test materials. Figure 4 depicts $K_{ic}$ ratio [$=(K_{ic} \text{ by SEVNB})/(K_{ic} \text{ by SEPB})$] with respect to a range of grain size. Fine grained ceramics and glass ceramic, such as $\alpha$-SiC, AD999 alumina, NC132 and N3208 silicon nitrides, and Pyroceram, exhibited little difference in fracture toughness with $K_{ic}$ ratio close to unity. By contrast, coarse grained and elongated grained ceramics exhibited consistently lower $K_{ic}$ ratio ranging from 0.6 to 0.9 with an average of about 0.8. This indicates clearly that the two methods are in good agreement for fine-grained materials but in poor agreement with coarse or elongated grained materials.

It has been known that increase in fracture toughness for coarse or elongated grain-structured ceramics was due to mechanisms such as grain pullouts, grain bridging, and/or crack deflection, thereby generating crack closure stresses in the wake region of a crack. It has been also observed by the authors for a long time that these coarse and elongated grained ceramics revealed rising R-curve behavior with its degree depending on material.

![Typical fracture surfaces of silicon nitride specimens showing a precracked region by SEPB method (a) and a notched region by SEVNB method (b).](image)

Figure 2.—Typical fracture surfaces of silicon nitride specimens showing a precracked region by SEPB method (a) and a notched region by SEVNB method (b).
Figure 3.—Fracture toughness determined by SEVNB and SEPB methods for various ceramics.

Figure 4.—$K_{ic}$ ratio (=SEVNB/SEPB) with respect to range of grain sizes for various ceramics.
Figure 5.—A typical example of indent crack propagation in coarse grained NKK silicon nitride. A tortuous crack path with interactions such as grain bridging and pullout is noted.

![Indent Crack Propagation](image)

Figure 6.—Crack growth resistance curves of some brittle materials, determined by indent techniques.

![Crack Growth Resistance Curves](image)

A typical example showing a microstructural feature of a coarse and elongated grained NKK silicon nitride associated with tortuous indent crack propagation is shown in figure 5 (ref. 12). Based on the authors’ experience, this material exhibited the highest value of fracture toughness \((K_{IC} = 10.2 \pm 0.7 \text{ MPam}^{1/2})\) of monolithic ceramic materials and a rising R-curve as well (ref. 12). Typical examples of R-curves of some materials evaluated by the indentation technique (ref. 7), are shown in figure 6. Note that fine-grained NC132 silicon
nitride (grain size <1 μm) and soda-lime glass showed flat R-curve behavior; whereas, coarse-grained AD998 alumina (grain size >10 μm) and elongated grained NKK and AS800 silicon nitrides (elongated grain size >20 μm) exhibited significant rising R-curves. The degree and size of grain elongation were greater in NKK than in AS800. The R-curve in figure 6 was formulated using the following expression (ref. 7)

\[ K_R = k[a]^m \] (1)

where \( K_R \) is crack growth resistance, \( a \) is crack size (crack extension), \( k \) is a parameter, and \( m \) is toughening exponent. With the estimated \( m \) parameter for each test material, \( K_Ic \) ratio was plotted as a function of \( m \), as shown in figure 7. A clear trend can be seen from the figure such that \( K_Ic \) ratio remained close to unity for lower \( m \) values (\( m < 0.02 \)) but decreased appreciably (or dropped) at higher \( m \) values (\( m = 0.1 \) to 0.14), giving rise to a following approximation

\[ \frac{K_{Ic/SEVNB}}{K_{Ic/SEPB}} \approx -1.9 m + 1 \] (2)

This, although not based on theoretical consideration, implies that the toughening exponent \( m \) could be an important parameter to quantify the degree of discrepancy in fracture toughness between the SEVNB and SEPB methods.

![Figure 7.—\( K_Ic \) ratio as a function of toughening exponent (\( m \)) for various ceramics.](attachment:figure7.png)
Typical load versus back-face strain curves of SEVNB test specimens of several ceramics are shown in figure 8 (Note that back-face strain was in compression but was expressed in tension for simplicity). Both fine-grained ceramics such as N3208 silicon nitride and AD998 alumina showed linearity in their load-versus-strain curves. However, the coarse-grained AD998 alumina and the elongated-grained AS800 silicon nitride exhibited nonlinearity at the region close to the final fracture, resulting in stable crack growth prior to instability. This stable crack growth was determined analytically in conjunction with the results of figure 8. The analytical solution was expressed as follows:

$$\alpha = 1 - \left[ \frac{dP}{d\varepsilon} \right]^{1/2} f(L_o, L_i, b, W, E)$$  \hspace{1cm} (3)$$

where $\alpha = a/W$ with $a$ and $W$ being crack size and specimen depth, $P$ is applied load, $\varepsilon$ is backside strain, and the function $f$ depends on fixture spans, and width and elastic modulus of test specimen.

The crack growth resistance $K_R$, corresponding to crack size ($\alpha$) and applied load in the stable crack-growth region, was determined using equation (3) and the results are shown in figure 9. For N3208 and AD999 materials, no or negligible stable crack growth occurred. By contrast, AS800 material exhibited a significant stable crack growth, resulting in a considerable increase in fracture toughness by about 35 percent. Also, AD998 material resulted in fracture-toughness increase by about 25 percent. It is interesting to note from the figure that fracture toughness started from the values determined by the SEVNB method and ended up with the values determined by the SEPB method. This indicates that the discrepancy in fracture toughness between the two methods, particularly for coarse and
Figure 9.—Crack growth resistance curves determined by back-face strain gaging based on the results in figure 6.

elongated grained ceramics, is due to the fact that the calculation of $K_I$ in SEVNB specimens did not consider the stable crack growth in their final crack sizes, which is hardly discernable from fracture surfaces in many cases. Although this extension by sable crack growth is small in the order of a few hundred micrometers and the measurement imposes a great difficulty, the effect on fracture toughness is still significant. Stable crack growth occurring via grain bridging and pullouts together with crack closure stresses acting in the wake region is the most plausible, physical explanation for the discrepancy in fracture toughness between the two methods.

4. Conclusions

The discrepancy in fracture toughness between the SEVNB and SEPB methods was attributed to R-curve behavior of ceramic materials, in which stable crack growth through grain pullouts and/or bridging takes place, imposing crack closure forces in the wake region of a propagating crack even for SEVNB specimens. The discrepancy increased for materials with stronger rising R-curve and was quantified with a toughening exponent ($m$). It is recommended that both SEVNB and SEPB methods be used together to evaluate fracture toughness of any materials unknown in microstructural features and/or R-curve behavior. Any appropriate method to monitor stable crack growth in SEVNB specimens is also recommended.
References

13. S.R. Choi, various previous publications not quoted here.
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**AUTHOR(S)**
Sung R. Choi and John P. Gyekenyesi

**PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)**
National Aeronautics and Space Administration
John H. Glenn Research Center at Lewis Field
Cleveland, Ohio 44135–3191

**SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)**
National Aeronautics and Space Administration
Washington, DC 20546–0001

**ABSTRACT (Maximum 200 words)**
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