Apollo Capsule Optimization for Improved Stability and Computational/Experimental Data Comparisons

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APOLLO CAPSULE OPTIMIZATION FOR
IMPROVED STABILITY
AND COMPUTATIONAL/EXPERIMENTAL
DATA COMPARISONS

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SUMMARY

Numerical optimization was employed on the Apollo Command Module to modify its external shape. The Apollo Command Module (CM) that was used on all NASA human spaceflights during the Apollo Space Program is stable and trimmed in an apex-forward (alpha of approximately 40 to 80 degrees) position. This poses a safety risk if the CM separates from the launch tower during abort. Optimization was employed on the Apollo CM to remedy the undesirable stability characteristics of the configuration. Geometric shape changes were limited to axisymmetric modifications that altered the radius of the apex ($R_A$), base radius ($R_O$), corner radius ($R_C$), and the cone half angle ($\theta$), while the maximum diameter of the CM was held constant. The results of multipoint optimization on the CM indicated that the cross-range performance can be improved while maintaining robust apex-aft stability with a single trim point. Navier–Stokes computations were performed on the baseline and optimized configurations and confirmed the Euler-based optimization results. Euler analysis of ten alternative CM vehicles with different values of the above four parameters are compared with the published experimental results of numerous wind tunnel tests during the late 1960s. These comparisons cover a wide Mach number range and a full 180-degree pitch range and show that the Euler methods are capable of fairly accurate force and moment computations and can separate the vehicle characteristics of these ten alternative configurations.

INTRODUCTION

An unstructured Euler method has undergone extensive validation with experimental data on numerous space vehicles with blunt-based aft bodies. The validation is over subsonic to hypersonic Mach numbers and includes high angles of attack. The accuracy of the method is well understood, and the method is superior to preliminary design methods in the subsonic to low supersonic Mach number range. (The data and geometries are proprietary). This Euler method is coupled to a constrained gradient-based optimization algorithm and is used for aerodynamic shape optimization (ASO). Performance increments/improvements over baseline configurations held through wind tunnel tests and Navier–Stokes comparisons on a previous crew transfer vehicle (CTV) design. The method has been successfully used for multipoint complete configuration optimization with performance and stability/trim objectives on Lockheed Martin CTV configurations.
With the recent NASA mandate for the development of a manned crew exploration vehicle and the likely change from winged configurations to capsule designs, the Euler solver used in the optimization package was evaluated by comparison with the extensive wind tunnel data obtained during the Apollo Space Program. During this investigation the baseline Apollo CM (employed on all flights) was found to have an undesirable characteristic in that it is both stable and trimmed in an apex-forward position that poses a safety risk if the CM separates from the launch tower during abort. The Euler-based optimization program that was used successfully on winged configurations seemed ideally suited to perform optimization of the CM to remedy this undesirable characteristic. Alterations and additional components that were developed to eliminate the dual trim point of the Apollo capsule were built during the Apollo program, and the aerodynamic quantities of these vehicles were obtained through extensive wind tunnel tests. Computational fluid dynamics (CFD) codes have proliferated since the late 1960s and have become the testbeds for aerodynamic-based design changes with typically only limited wind tunnel testing. The wealth of test data from the 1960s remains significant to the calibration of CFD methods and was therefore used to compare with the Euler code on a series of 10 parametric designs of the capsule with shape changes that altered the radius of the apex ($R_A$), base radius ($R_O$), corner radius ($R_C$), and the cone half angle ($\theta$), while holding the maximum diameter of the CM constant. Figure 1 depicts the variables used to change the capsule shape.

The four design parameters used were employed as design variables in a multipoint design optimization problem to eliminate the apex-forward trim point and improve the performance of the vehicle. Since the number of design variables was sufficiently small, a parametric study was also performed to find sets of parameters that were close to the optimum. This parametrically determined optimum is compared with the optimum found through the gradient-based optimization method.

The set of ten capsules (table 1) with experimental data are compared with the Euler solver at Mach numbers of 0.4, 0.7, 1.2, 1.65, 3.26, 3.27, and 5.0.

**PARAMETRIC STUDY AND RESULTS**

To properly assess an optimization of the Apollo capsule, a parametric study of the four design variables was initiated during the optimization of the Apollo capsule. The small number of geometric variables made a parametric study feasible. Each of the four design variables was altered over a range of reasonable values in equal increments to five different values and at three different angles of attack, requiring a total of 1875 ($3 \times 5^4$) flow solutions. The values of the variables are provided below:

<table>
<thead>
<tr>
<th>$\theta$ (degrees)</th>
<th>25.0</th>
<th>30.0</th>
<th>35.0</th>
<th>40.0</th>
<th>45.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_A$ (inches)</td>
<td>5.0</td>
<td>10.0</td>
<td>15.0</td>
<td>20.0</td>
<td>25.0</td>
</tr>
<tr>
<td>$R_C$ (inches)</td>
<td>0.0</td>
<td>7.5</td>
<td>15.0</td>
<td>22.5</td>
<td>30.0</td>
</tr>
<tr>
<td>$R_O$ (inches)</td>
<td>125.0</td>
<td>193.75</td>
<td>262.5</td>
<td>331.25</td>
<td>400.0</td>
</tr>
</tbody>
</table>

The capsule was assessed at Mach 3.26 and three angles of attack $\alpha = 75.0$, 130.0, and 143.0 degrees, representing design points 1, 2, and 3, respectively. This large volume of data was evaluated
by applying the objective function used in the optimization problem to lift, drag, and moment coefficient data from these runs. The reference area of the semispan model used in the computations is 9313.2514 in.\(^2\), the center of gravity (c.g.) was located at an axial location of 105.49 inches and a vertical location of –9.086 inches from the apex, and the average chord was 154 inches. This objective function comprises weighted terms involving forces and moment coefficient data from the three design points, as follows:

\[
\text{Objective} = \sigma_1 (CM_1 - 0.002)^2 + \sigma_2 |CD_2/CL_2| + \sigma_3 (CM_3)^2
\]

The subscripts on the force and moment terms represent the design point of the solution. The variables \(\sigma_1, \sigma_2,\) and \(\sigma_3\) were derived by finding the maximum value of each of the three terms in the parametric study, and scaling them such that:

\[
\begin{align*}
\sigma_1 &= 0.50 / \max [(CM_1 - 0.002)^2] \\
\sigma_2 &= 0.25 / \max [|CD_2/CL_2|] \\
\sigma_3 &= 0.25 / \max [(CM_3 - 0.0)^2]
\end{align*}
\]

This weights the first term, forcing a positive pitching moment of 0.002 at \(\alpha = 75\) degrees—to eliminate the trim point that occurs near this design point—as 50% of the objective function, with the other terms both weighted to 25% of the objective function.

The actual values of weighting terms determined from the parametric study are:

\[
\begin{align*}
\sigma_1 &= 9.36754242347172 \\
\sigma_2 &= 0.0424317664785264 \\
\sigma_3 &= 15.5260032173313
\end{align*}
\]

These weighting terms were then used in optimization. The starting objective function is set equal to 1.0 by the choice of the weighting terms described previously. Thus, the resulting weighted sum is expected to be of order 1 during optimization.

The parametric data can be visualized by multiplying the objective function at each of the 625 points of the four-dimensional matrix by 1000 and rounding its value to the nearest integer, as shown in table 2.

The data are shown as inner and outer matrix values where the outer matrix is for the half angle of the cone, \(\theta\), and apex radius, \(R_A\), and the inner matrix is for the corner radius (columns for \(R_C\) of 0.0, 7.5, 15.0, 22.5, and 30.0 inches plotted left to right, respectively) and the base radius (rows for \(R_O\) of 125.0, 193.75, 262.5, 331.25, and 400.0 inches plotted from top to bottom, respectively). Since the objective function is to be minimized, the smaller integers represent better solutions. The lowest value of objective function using these \(\sigma\) values is 49 (colored red in table 2) and appears at position (4, 5, 1, 4); that is, outer matrix position of column 4, row 5, and inner matrix position of column 1, row 4, where \(\theta = 40\), \(R_A = 25\), \(R_C = 0.0\), and \(R_O = 331.25\). This will be called the best parametric shape. The objective function value was about 0.04948 for this combination of design variables.
Note that the optimum occurs where \( R_C \) is zero (the corner between the cone and the base is sharp). This may not be desirable in a practical design problem for aerodynamic heating concerns. If the zero-radius solutions are not feasible there are several choices with objective function values of 58 with larger \( R_C \) values of 7.5 degrees. The design space can be readily viewed by assigning colors to the original values of the four-dimensional matrix (figure 2). The color assignment is based on the values of the objective function, rather than the values in table 2. Slight differences in value are seen in the colors for equivalent values shown in the table. For example, the positions for \( \theta = 35 \) degrees, \( R_A = 25 \) inches, \( R_C = 7.5 \) inches (row 2 of inner matrix), and \( R_O = 262.5, 331.25, \) and 400 inches (columns 3–5) have values of 58. But these objective function values are actually 0.58108, 0.57557, and 0.57553, respectively, so there are slightly different shades of cyan in the colored graphic of figure 2. The baseline Apollo capsule C01 has values of \( \theta = 33 \) degrees, \( R_A = 15.4 \) inches, \( R_C = 7.7 \) inches, and \( R_O = 184.8 \) inches with a base width of 154.0 inches. The closest parametric 4-tuple for this would correspond to \( \theta = 35 \) degrees, \( R_A = 15 \) inches, \( R_C = 7.5 \) inches, and \( R_O = 193.73 \) inches at position (3, 3, 2, 2), which corresponds to a value of 65 in the table.

**OPTIMIZATION DESCRIPTION**

An Euler unstructured-tetrahedral-grid-based CFD code, AIRPLANE (ref. 1), is coupled to a constrained gradient-based optimization algorithm, NPSOL (ref. 2), to provide an aerodynamic shape optimization technique for the Systems Analysis & Integration Branch at NASA Ames Research Center. NPSOL is a constrained quasi-Newton finite-difference optimization method. Several codes were developed to facilitate aerodynamic shape optimization. These include adding multigrid capability to AIRPLANE, developing surface grid perturbation methods, developing a variety of mesh movement techniques, and the parallelization of these methods. In this capsule design case, the surface grids were developed by a new process, described in the next paragraph, and the multigrid option in the flow solver was not used.

A four-tuple \((\theta, R_A, R_C, R_O)\) determines a generating curve \( y(x) \) in the symmetry plane, which then defines the capsule by rotation about the \( x \) axis. The capsule surface is made of a spherical apex, conical body, toroidal corner, and spherical base, with tangency at the connecting circles unless \( R_C \) is zero. Surface mesh generation is done by application of a special program named MKACM that creates strips of triangles from the waist (maximum diameter of the capsule), where \( y(x) = 77 \), marching to each axial extremity, driven by a maximum edge length requirement and a preference for equilateral triangles. For example, the baseline C01 surface mesh from minimum \( x = 12.88 \) to maximum \( x = 142.7 \) is defined by 9145 points, 18034 triangles, and 27178 edges, for which the average edge length is 1.85 inches with a standard deviation of 0.064. The whole surface mesh is shown in figure 3. Details of the apex, apex cone, cone corner base, and the corner base are shown in figures 4, 5, 6, and 7, respectively. The resulting surface mesh meets the Delaunay criterion, which is that the sphere balanced on each triangle contains no other mesh points than its vertices.

The optimization code has been successfully used in the recent past for the High-Performance Computing and Communication Program (HPCCP) by applying the method to the Ames Sharp CTV configurations. The resulting configurations were used for the approach and landing simulation database for the Virtual Flight Rapid Integration Test Environment (VF-RITE) project (ref. 3). These
methods more recently were used for the design of orbital space plane vehicles under a contract with Lockheed Martin Corporation, where improved stability characteristics and performance at multiple design points were attained.

Aerodynamic shape optimization is particularly amenable to unstructured-grid methods. Complete configuration multipoint numerical optimization can often begin within a few days for an unstructured method with the rapid generation of surface (triangles) and volume (tetrahedral) meshes of an unstructured method. A gradient approach was chosen since this tool is well suited for detailed aerodynamic design (the vehicle conceptual design was performed a priori). A gradient-based algorithm should require fewer function evaluations to find local minima or design improvements in contrast to non-gradient methods such as genetic algorithm techniques that are capable of finding the global minimum. However, the gradients calculated via finite differences are computationally expensive since they require at least two flow solutions for each design variable. Thus, a limited number of design variables is recommended to reduce the CPU time with the present method.

The AIRPLANE optimization process requires the user to supply a range of values for each design variable to limit the perturbations to those that are acceptable to the designer. The variable bounds are never exceeded since NPSOL is a constrained optimization method. The choice of variable bounds should be carefully considered before optimization begins. The ranges should be narrow enough to eliminate undesirable results, yet wide enough so that significant performance changes can be obtained by the optimizer. As the optimizer runs, it checks for stored solutions that may have already been computed, matching flow conditions and design variables. This is used to “restart” the optimization process because finding flow solutions is relatively time consuming—NPSOL itself executes very rapidly. If no existing solution is found, the code proceeds to create the surfaces of the vehicle, either through a body-of-revolution meshing method for capsule designs or through modification of the surfaces of the configurations using APSHAPER and APSHBODY (ref. 4). APSHAPER perturbs the triangulated surfaces of wing-type components, ensuring that the number of points and connectivity remain unchanged. It is capable of wing planform changes and dihedral in addition to wing sectional changes such as camber, thickness, and leading- and trailing-edge droop. It can also provide flap deflections as either true rotations or by shearing the wing for either leading- or trailing-edge flaps. APSHBODY is used to perturb “body-type” components. Perturbation on the fuselage can be applied vertically, spanwise, or radially. Fuselage camber and droop applied to either the fore or aft portion is also attainable.

When the surface mesh is established, the AIRPLANE volume mesh of tetrahedra is either deformed or regenerated. MESHMV (ref. 4), the mesh deformation package, preserves the number of points and connectivity of the original mesh and runs quickly. If this method inverts any tetrahedron, the whole mesh is automatically regenerated from scratch using MESH3D (ref. 5). In this capsule design effort, MESH3D was used to regenerate the volume meshes each time because the surface mesh generation program was allowed to change the number of surface points. Following this, AIRPLANE is run, and the aerodynamic lift coefficient (CL), drag coefficient (CD), and pitching moment coefficient (CM) are returned to NPSOL in order to compute the objective function.
APOLLO CAPSULE AERODYNAMIC CHARACTERISTICS

The Apollo capsule is known as the C01 configuration to distinguish it from the other nine capsules that were wind tunnel tested during the Apollo Program (table 1). The C01 configuration has these properties: $\theta = 33.0$ degrees, $R_A = 15.4$ inches, $R_C = 7.7$ inches, and $R_O = 184.8$ inches, with a base width of 154.0 inches. This capsule was used as the baseline configuration for optimization.

The baseline configuration lift, drag, and pitching moment coefficient characteristics were obtained for Mach 3.27 using the unstructured Euler code, AIRPLANE, in figures 8, 9, and 10. An angle of attack of zero degrees represents the apex-forward position, and thus 180 degrees angle of attack will position the vehicle with the base (or heat shield) forward. The ability of the Euler computational methods to predict the flow characteristics of this vehicle is very good for these flight conditions. These computational tools were not developed during the Apollo Program, hence wind tunnels were used extensively to obtain aerodynamic data bases for the Apollo configurations. The pitching moment coefficient data shows the design flaw of the Apollo configuration (figure 10). The multiple trim points are shown in both the experimental and computational data. The trim points that occur at pitch angles between about 50 and 85 degrees are undesirable because the apex is still forward and the vehicle is not protected by the blunt base that acts as a heat shield. In addition, the negative slope of the moment curve indicates that the vehicle can achieve stable trim, that is, the capsule will return to the trim point if perturbed from this position. This was a well-known problem of the isolated capsule during the Apollo Program. The remedy to ensure that the capsule heat shield would be in a forward attitude was to include deployable canard surfaces near the rocket nose of the launch escape vehicle (LEV) (ref. 6) and to allow the entire LEV to remain attached during an abort scenario. The LEV consists of the command module, tower assembly, and rocket body. The deployed canard surfaces cause the complete LEV to rotate so that the heat shield is forward. The canard surfaces also help to dampen the aerodynamic forces after the rotation maneuver.

OPTIMIZATION DISCUSSION AND RESULTS

The objective function and range of design variables were chosen to address the performance and (static stability) pitching moment characteristics of the capsule. Other system requirements are not addressed, such as the dynamic stability of the isolated capsule or the aerodynamic heat loads of the capsule. This optimization problem was set up to demonstrate the applicability of unstructured optimization to space capsule design, primarily as proof of concept to show that it is quite capable of achieving improved capsule designs for the currently mandated crew exploration vehicle. The objective function for optimization was described in detail in the parametric study section of this report. The optimization was a three-point design problem with each of the three design points at Mach 3.26. The three points were for three angles of attack, where the first term of the objective function was designed to modify the pitching moment at alpha of 75 degrees to a value of 0.002 to remove the trim point at this condition. The second term was to improve L/D (minimize D/L) at 130 degrees, and the third term was to maintain the trim point at alpha 143 degrees. These three terms are added together with weighting factors of 0.5, 0.25, and 0.25 for the three design points, respectively, to form a single objective function value that is to be minimized during optimization. The
angle of attack of 130 degrees was chosen because \((L/D)_{\text{max}}\) is obtained at this angle in the experimental data (ref. 7). The angle of attack of 143 degrees is the angle where trim occurred for the computational results from AIRPLANE.

The ranges of the design variables were chosen to be the same as those used for the parametric study, namely: \(25 \leq \theta \leq 45\) degrees, \(5 \leq R_A \leq 25\) inches, \(0 \leq R_C \leq 30\) inches, and \(125 \leq R_O \leq 400\) inches. NPSOL will not allow violation of these design variable constraints. In a true multidisciplinary design, each of the many disciplines would have inputs into the range of feasible values that these design variables could take on. Starting from the baseline C01 shape \((\theta, R_A, R_C, R_O) = (33, 15.4, 7.7, 184.8)\), an optimized solution was found at approximately \((35.6, 14.17, 0.0, 297.8)\) with an objective function value of about 0.04954, which is within about 0.1% of the value found parametrically. The four defining parameters for the baseline C01 and subsequently designed Apollo Command Modules are listed together in table 3 for easy reference. Symmetry plane profiles of all members of the four-parameter family considered in this report are plotted in figure 11. The nominal center of gravity at \(x = 105.49, y = -9.086\), which was used to compute the pitching moment, is shown in each of the 14 profiles.

This first optimization required only 43 objective function evaluations (129 flow solutions), which is 7% of what was spent on the parametric study. NPSOL finds an acceptably small objective function by repeated application of gradient approximation and line search steps. Typically only two or three points are needed to approximate each partial derivative numerically, with the central point shared for each dimension. In the present case, it takes five function evaluations to get the first gradient. A suggested difference interval size to use for the first gradient, the expected function precision, a line search tolerance, and an optimality tolerance are parameters set by the operator, among many others. For this case, the values chosen were 1e-1, 1e-5, 1e-3, and 1e-4, respectively. Definitions of these control parameters are provided in the NPSOL documentation and are beyond the present scope to describe.

Surface pressure coefficient plots for the baseline C01 are shown in figures 12, 13, and 14 at the three design-point angles of attack, 75, 130, and 143 degrees, respectively, and at the base-forward trim angle, 143 degrees, in figure 15. The first three figures are flat shaded, while the fourth figure is shaded with two lights in order to cue the viewer’s depth perception. Compare these with surface pressure coefficient plots in figures 16, 17, 18, and 19, for the best parametric shape. Here, the cone appears flatter and the corner is sharp, while the maximum diameter is preserved, and the base-forward trim angle is 139 degrees. Similar plots for the first parametric design are shown in figures 20, 21, 22, and 23. This shape is not as flat, but the corner is still sharp and the trim angle is also 139 degrees.

To evaluate the efficacy of an optimization run, consider the values of the objective function, the three terms that compose its sum (figure 24), and the values of the four design parameters at each evaluation (figures 25, 26, 27, and 28). In these five plots, the numbering starts at function evaluation number 0, which corresponds to the baseline C01 Apollo Command Module shape. The final evaluation is number 42, for a total of 43 evaluations. The optimal solution reported by NPSOL usually is not the last one evaluated, nor is it necessarily the smallest one ever found. The optimal solution should have an objective function that is within the set tolerance. In the present case, NPSOL reported that it could not meet the requested accuracy, but it selected as optimal the point at
evaluation number 33, which also happened to have the smallest objective. The initial objective function was 0.066202, the last value was 0.050072, and the optimal value reported by NPSOL was 0.049537 at evaluation number 33. The objective function is the sum of three terms. The performance term, involving the minimization of CD/CL at the second design point, \( \alpha = 130 \) degrees, dominated the objective function during the whole optimization run, even though the three sigma values were designed to weigh the terms in proportions 50:25:25. The reason for this is that the sigma values were determined by considering 625 points across the whole parametric space, but the optimizer did not have to go to every extreme. Given another opportunity, one might weigh the terms differently, but the present weights still validate the approach.

In this optimization run, the cone half angle, \( \theta \), and the apex radius, \( R_A \), stayed well within their bounds (figures 25 and 26, respectively). On the other hand, the corner radius, \( R_C \), dropped to zero right away and stayed there, for the most part (figure 27). The fourth design parameter, the base radius, \( R_B \), hit the upper limit at 400 only one time during a search (figure 28) at evaluation number 27—the objective function spiked there, too, but NPSOL recovered, as expected.

Both the best parametric and NPSOL optimization approaches resulted in a sharp corner, \( R_C = 0 \), which was permitted by the limits imposed. Pitching moment curves for the baseline C01, best parametric shape, and this first optimized shape are shown in figure 29. A stable trim point is predicted near \( \alpha = 65 \) degrees for C01. The value of CM for the latter two shapes remains positive near the original apex-forward stable trim point, as desired. The CM curve for the best parametric case at \((40, 25, 0, 331.25)\) plots above the optimized case CM in this region, indicating that NPSOL found a shape with a smaller pitching moment penalty at the first design point. Trim at the third design point was not achieved at \( \alpha = 143 \) degrees, but it is an acceptable trade-off. Both the best parametric shape and the optimized shape have stable base-forward trim points at about \( \alpha = 139 \) degrees.

Figure 29 also shows Navier–Stokes predictions for the optimized shape (refs. 8–9) that are in good agreement with the pitching moments predicted by the Euler flow solver, at \( \alpha = 60, 90, 120, \) and 150 degrees. Three more Navier–Stokes comparisons, at \( \alpha = 0, 30, \) and 180 degrees, are shown in figure 30.

Lift-to-drag performance curves are plotted in figure 31 for baseline C01 and the two designs over pitch angles 60 to 150 degrees. The objective function is designed to maximize L/D at the second design point, \( \alpha = 130 \) degrees. Both of the new designs have higher L/D at the second design point, and the angle for which maximum L/D occurs is lower in each case. L/D for the optimized shape is lower at \( \alpha = 130 \) degrees than the value for the best parametric shape, which is another acceptable trade-off. To complete the comparison, figure 32 shows performance curves between pitch angles 0 to 180 degrees.

A second optimization was run subsequently, starting from the same initial baseline and with the same scaling, but changing the objective function so that CM larger than 0.002 added nothing to the objective function at the first design point, where \( \alpha = 75 \) degrees. The extra freedom resulted in an optimized shape at parameter values of approximately \((44.99, 14.18, 0.0, 385.4)\) with an objective function of about 0.04197, which is 15% lower than what was found parametrically. In this case, the cone half angle \( \theta \) bounced against the specified upper limit of 45 degrees, and the corner \( R_C = 0 \) turned out sharp again. The pitching moment near \( \alpha = 75 \) degrees turned out more positive than be-
fore because there was no penalty for going over the target CM. Compare surface pressure coefficient plots in figures 33, 34, 35, and 36, for the second optimized design, with earlier pressure coefficient figures. This optimization required 58 objective function evaluations. The objective function history is plotted for the second optimization in figure 37. The initial objective function was 0.066202, the last value was 0.042130, and the optimal value reported by NPSOL was 0.041970 at evaluation number 23. The lowest objective function was number 40 with a value of 0.041684. Observe that in the fourth gradient NPSOL used three-point numerical approximations to the partial derivatives. The pitching moment penalty at the first design point went to zero right away because of the way it was designed. The histories of design parameters are plotted in figures 38, 39, 40, and 41.

A third optimization was run that combined the objective function just described with a lower limit on the corner radius, $R_c = 5$ inches. In this case the optimized solution shape was (45, 16, 5, 400) with an objective function value of 0.04463. Compare the shapes and surface pressures in figures 42–45 with figures 20–23 and 33–36. Only the apex radius, $R_a = 16$, did not hit a range limit. The goal of eliminating the apex-forward stable trim condition was again achieved, and the optimization finished in 57 evaluations. The objective function history is plotted for the third optimization in figure 46, and the histories of design parameters are plotted in figures 47, 48, 49, and 50. The initial objective function was 0.066202, the last value was 0.044671, and the optimal value reported by NPSOL was 0.044634 at evaluation number 55, which was also the lowest objective function. For gradients, NPSOL used only two-point numerical approximations to the partial derivatives. The moment penalty at the first design point (term 1) went to zero right away because of the way it was designed. The performance term at the second design point dominated the objective function. The trim term at the third design point stayed under control, near zero, the whole time.

Pitching moment curves for the baseline C01 and the three NPSOL optimized shapes are shown in figure 51. The first optimization penalized shapes for which CM exceeded 0.002, but the other two optimizations penalized only shapes with CM lower than 0.002, so CM at $\alpha = 75$ for the first case is the lowest of the three optimized shapes. The CM curve generally shifts up, in the order of optimizations 1, 2, and 3, and the third optimization turns out with base-forward stable trim closer to the baseline than the other two. It may be coincidence that only the baseline and the third optimizations have round corners.

Lift-to-drag performance curves are plotted in figure 52 for the baseline C01 and the three NPSOL optimized shapes. All three optimized shapes perform better at design point 2 than the baseline (where $\alpha = 130$ degrees).

**COMPUTATIONAL DATA CORROBORATION OF OPTIMIZED CAPSULE EULER / EXPERIMENTAL DATA CORROBORATION**

Euler computations were performed on 10 capsules with the parameters shown in table 1. These 10 full-scale test models were wind tunnel tested in a large number of test facilities. All of the wind tunnel data presented were taken from reference 7 and are for static tests that were conducted using
sting mounted models attached to strain-gauge balances to measure the force and moment coefficient data. The reader is referred to reference 7 for further detail on the test and accuracy of the data.

AIRPLANE computations were performed for the 10 configurations at Mach numbers of 1.65, 3.26, 3.27, and 5.0. Additional computations were obtained at Mach 0.4, 0.7, and 1.2 for the C01 configuration. The computational angles of attack ranged from 0 to 180 degrees with 5-degree increments. The pitching moment coefficients of the wind tunnel data and computational predictions are compared for all configurations at Mach 1.65, 3.26 (3.27 for C01), and 5.0. The wind tunnel data were obtained by hand digitizing the data from an electronically scanned version of reference 7. The data at Mach 1.65 are shown in figure 53. Most of the experimental data were taken only for $120 \leq \alpha \leq 180$, whereas the AIRPLANE computations were from 0 to 180 degrees. The data and computations over the entire range of angles of attack are shown in figure 54. The data and computation comparisons for angles of attack of 120 to 180 degrees are shown in figure 55. Here, in figure 55, lies the evidence that the Euler methods are capable of predicting the differences in moment coefficient data between geometrically similar objects. Referring back to table 1, we see that C08, C02, C09, and C10 have cone angles $\theta = 30, 33, 36,$ and 40 degrees, respectively. Considering respective pairs, they differ in cone angle by 3, 3, and 4 degrees. The increments between the experimental data compare well with the increments between the computational predictions. The actual values of the pitching moment also compare fairly well. Configurations C01 and C02 differ in the apex radius, $R_A = 15.4$ and 9.152, respectively. Reducing the apex radius by approximately 6 inches has little effect on the pitching moment characteristics. The computational data show the same result. However, the actual values of the CM predictions differ slightly more than for the C08-C02-C09-C10 data. C03, C02, C04, and C05 differ by corner radius, $R_C = 0, 7.7, 15.4,$ and 23.1 inches, respectively (equal steps), and the increments between the test data are well predicted by the computations. Here again the actual value is shifted slightly, but the increments are well predicted. C06, C02, and C07 represent base radius changes, $R_O = 154, 184.8,$ and 215.6, respectively (equal steps). The increments are also very well predicted by the Euler computations.

Data and computation comparisons for Mach 3.26 for C02–C10 and Mach 3.27 for C01 are shown in figures 56, 57, and 58. The increments are well captured overall by the Euler computational predictions. Inviscid solutions almost invariably predict more negative (nose down) pitching moments than viscous (real world) results, though the differences are small. The overall characteristics of the moment curves are quite similar for Mach 1.65 and 3.26; compare figures 55 and 58.

Data and computation comparisons for Mach 5.0 are shown in figures 59, 60, and 61. The computational predictions compare with experiment in absolute value better for configurations C04, C05, and C08 than was seen for the lower Mach number results, but poorer correlations are seen for C09 and C10 configurations. Compare figures 55, 58, and 61 (Mach 1.65, 3.26, and 5, respectively). Looking solely at the incremental differences between the models, the computational predictions continue to be able to “see” the differences in the configurations at Mach 5.0. Mach 5.0 is about the upper Mach number limit of the Euler computational method. The strong shocks from larger hypersonic Mach numbers would require increased dissipation in the flow solver to achieve convergence, and this would invalidate higher Mach number solutions.

The C01 configuration computations are also compared to the experimental data at lower Mach numbers. The lift and drag comparisons are shown for Mach 1.65 and 5.0 in figures 62, 63, 64, and
65. Mach 3.27 lift and drag results were shown previously in figures 8 and 9. The experimental data for the C01 includes the lower angles of attack and comparisons are over the full 180-degree range. The lift coefficient correlations are very good at Mach 1.65 (figure 62). There is some uncertainty in the lower angle-of-attack data in the experimental data, shown by the multivalued data points. The drag coefficient correlations are poorer than the lift comparisons (figure 63). The Mach 5.0 lift and drag coefficient correlations between experiment and the Euler computations are quite good (figures 64 and 65). The correlations improve with increasing Mach number.

The subsonic, transonic, and low supersonic Mach number pitching moment coefficient data for the C01 configuration are shown in figures 66, 67, and 68. The moment coefficient data from experiment was digitized and compared with the Euler computations. Figure 66 compares the Mach 0.4 results. Very poor correlation is obtained. The computations are unable to predict zero lift and hence zero moment for the symmetrical configurations at angles of attack of 0, 90, and 180 degrees. Flow around a blunt-boded object is likely to be unsteady. The steady-state solutions obtained with the computations are clearly unable to accurately predict the flow characteristics.

**CONCLUDING REMARKS**

A new automated surface mesh generation method was developed for application to parametrically defined capsule shapes. This method proved to be robust and produced high-quality surface meshes. This method extends the existing set of design variables, which are capable of nearly complete configuration design changes to include those applicable to capsule design.

Multipoint optimization was performed on the Apollo Command Module to modify the exterior shape by altering the four vehicle-defining design variables. The goal was to remove a potentially dangerous apex-forward stable trim point while maintaining the apex-aft trim point and improving the performance of the vehicle. The optimization effort resulted in removing the apex-forward trim point while maintaining robust apex-aft stability, resulting in a vehicle with a single trim point with improved cross-range performance. The optimized CM has a larger base radius, a larger included cone angle, and a smaller corner radius than the baseline Apollo CM.

Prior to the optimization effort, a parametric study that varied each of the four vehicle-defining design variables over a range of 5 values was used to assess the design space and provide a method to corroborate the optimization results. It is rarely feasible to explore the design space, but with only four design variables it was possible. The optimization effort required only 7% of the CPU time that was needed for the parametric study to arrive at an optimum that was within 0.1% of the optimum found using the parametric study approach.

The optimization results were validated via independent Navier–Stokes computations for several design conditions, and these results confirmed that the optimized vehicle achieved the single apex-aft trim point. Navier–Stokes data corroborated the inviscid Euler computational data.

Euler computations were performed on 10 capsules that varied the four capsule-defining parameters to produce 10 geometrically similar configurations. These computations were compared with wind
tunnel test data from numerous test facilities where full-scale test models were used. The Euler CFD comparisons were performed for a wide range of Mach numbers: 0.4, 0.7, 1.2, 1.65, 3.26, 3.27, and 5.0. The computational angles of attack ranged from 0 to 180 degrees with 5-degree increments. The comparisons showed the Euler methods are capable of predicting the differences in moment coefficient data between geometrically similar objects; thus the increments between the experimental data of pairs of very similar models compare well with the increments computed by the Euler predictions. The actual values of the pitching moment also compare well at the supersonic and hypersonic Mach numbers, but the agreement lessened as the Mach number decreased for the subsonic Mach number comparisons.
REFERENCES


Table 1. Geometry description of CMs with experimental data for comparison with computational data.

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<td>9.152</td>
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Table 2. Four-dimensional matrix of objective function value multiplied by 1000 and rounded to the nearest integer.

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<td>54 65 83 102 121</td>
<td>53 71 103 136 164</td>
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<tr>
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<td>75 89 113 154 220</td>
<td>54 59 69 85 109</td>
<td>55 63 80 100 119</td>
<td>54 69 99 133 163</td>
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R_A = 5

299 379 502 671 905 | 90 107 138 188 263 | 88 90 98 112 137 | 115 119 127 137 149 | 141 152 168 184 199 |
| 254 329 444 606 823 | 72 89 117 163 233 | 53 60 72 88 112 | 56 68 86 104 123 | 56 77 108 140 166 |
| 257 330 441 595 810 | 71 88 115 159 227 | 52 60 72 88 112 | 56 68 86 104 123 | 56 77 108 140 166 |
| 262 333 441 595 807 | 74 89 115 159 224 | 52 59 70 86 110 | 53 64 81 101 119 | 53 71 101 134 163 |
| 265 338 445 596 805 | 76 91 115 158 223 | 54 59 69 84 108 | 54 62 79 98 118 | 53 68 98 131 161 |

R_A = 10

311 395 521 695 924 | 92 109 142 192 269 | 87 89 97 112 137 | 114 118 125 134 147 | 139 149 166 183 198 |
| 270 349 462 624 846 | 74 92 120 168 238 | 57 65 77 92 117 | 66 77 94 111 127 | 71 92 121 149 172 |
| 271 349 460 618 834 | 73 91 119 164 233 | 51 59 71 87 112 | 54 66 84 102 121 | 55 76 107 138 165 |
| 275 352 462 618 829 | 76 93 119 162 230 | 51 58 69 85 109 | 52 62 80 99 117 | 52 70 100 132 161 |
| 280 357 465 615 826 | 79 95 120 163 229 | 54 58 68 84 108 | 53 61 78 97 116 | 52 67 97 130 159 |

R_A = 15

331 416 543 715 949 | 95 113 146 198 276 | 85 87 96 110 138 | 111 115 123 132 145 | 139 147 163 180 195 |
| 290 368 487 649 871 | 78 96 126 173 246 | 56 64 76 92 117 | 64 76 94 111 128 | 69 91 119 147 169 |
| 291 370 480 643 862 | 77 96 124 171 241 | 51 59 71 87 112 | 53 64 82 100 121 | 54 74 105 135 161 |
| 295 374 485 642 857 | 81 98 125 170 239 | 51 58 69 85 110 | 51 61 78 96 115 | 51 68 98 130 158 |
| 300 378 488 643 853 | 84 100 126 169 238 | 53 58 68 84 108 | 52 59 75 94 114 | 51 65 95 127 156 |

R_A = 20

354 439 569 747 982 | 99 118 152 205 284 | 83 86 95 110 136 | 109 112 119 130 142 | 136 146 161 177 192 |
| 311 393 512 679 905 | 82 102 132 182 256 | 56 63 75 92 117 | 62 73 89 105 122 | 68 88 116 144 166 |
| 318 398 516 672 889 | 85 104 131 178 247 | 51 58 68 85 110 | 49 59 75 94 113 | 50 66 95 127 155 |
| 323 403 517 675 888 | 90 107 133 178 247 | 53 58 68 83 109 | 51 58 73 92 111 | 50 64 92 125 154 |

Table 3. Defining parameters for baseline and designed Apollo Command Modules.

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<td>Second Optimized</td>
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<td>385.4</td>
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<tr>
<td>Third Optimized</td>
<td>45.0</td>
<td>16.0</td>
<td>5.0</td>
<td>400.0</td>
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</table>
Figure 1. Variables used to change the shape of the capsule.
Figure 2. Parametric results of the objective function in the four-dimensional matrix in table 2. Color determined by the value of objective function.
Figure 3. Baseline C01 Apollo Command Module unstructured surface mesh, showing apex, cone, and corner to waist in black, then corner aft of waist and base in red. This and the next four pictures are made with orthographic projection.
Figure 4. Baseline C01 Apollo Command Module unstructured surface mesh near the nose point of the apex. A mirror image is shown in blue.
Figure 5. Baseline C01 Apollo Command Module unstructured surface mesh showing the apex and forward cone. A mirror image is shown in blue.
Figure 6. Baseline C01 Apollo Command Module unstructured surface mesh showing the aft cone and a portion of the corner to the waist in black, then the rest of the corner and the base in red. A mirror image is shown in blue.
Figure 7. Baseline C01 Apollo Command Module unstructured surface mesh showing the forward corner in black, then aft of the waist the corner and base is red, with a mirror image in blue.
Figure 8. Lift coefficient data of the Apollo Command Module (C01) configuration. AIRPLANE computations and experiment.
Figure 9. Drag coefficient data of the Apollo Command Module (C01) configuration. AIRPLANE computations and experiment.
Figure 10. Pitching moment coefficient data of the Apollo Command Module (C01) configuration. AIRPLANE computations and experiment.
Figure 11. Apollo Command Module profiles, showing nominal center of gravity.
Figures 12, 13, 14, and 15. AIRPLANE predictions of $C_p$ on the baseline C01 Apollo Command Module, Mach 3.26, at the three design-point angles of attack (75, 130, 143 degrees) and at base-forward trim (143 degrees, shown shaded with two lights). The 4-tuple $(\theta, R_A, R_C, R_O) = (33, 15.4, 7.7, 184.8)$ defines the baseline C01 Apollo Command Module.
Figures 16, 17, 18, and 19. AIRPLANE predictions of $C_p$ on the Best Parametric Apollo Command Module, Mach 3.26, at the three design-point angles of attack (75, 130, 143 degrees) and at base-forward trim (139 degrees, shown shaded with two lights). The 4-tuple $(\theta, R_A, R_C, R_O) = (40, 25, 0, 331.25)$ defines the best parametric shape using the first objective function.
Figures 20, 21, 22, and 23. AIRPLANE predictions of $C_p$ on the First Optimized Apollo Command Module, Mach 3.26, at the three design-point angles of attack (75, 130, 143 degrees) and at base-forward trim (139 degrees, shown shaded with two lights). The 4-tuple $(\theta, R_A, R_C, R_O) = (35.6, 14.2, 0, 297.8)$ defines the first optimized shape using the first objective function.
Figure 24. NPSOL objective function history for the first optimization of the Apollo Command Module, Mach 3.26. Black dots indicate numerical approximations of partial derivatives. Numbering starts at 0.
Figures 25, 26, 27, and 28. Design parameter values at each objective function evaluation for the first NPSOL optimization, Mach 3.26. The initial 4-tuple \((\theta, R_A, R_C, R_O) = (33, 15.4, 7.7, 184.8)\) defines the baseline C01 Apollo Command Module, and the optimized shape was approximately \((35.6, 14.17, 0.0, 297.8)\).
Figure 29. Pitching moment coefficient for baseline C01, best parametric and first optimized shapes, with Navier–Stokes predictions for the optimized shape (OVERFLOW2) at $\alpha = 60, 90, 120,$ and 150 degrees. See also figure 30.
Figure 30. Alpha 0 to 180 pitching moment coefficient for baseline C01, best parametric and first optimized shapes, with Navier–Stokes predictions for the optimized shape (OVERFLOW2). Compare with figure 51.
Figure 31. Lift-to-drag performance computed by AIRPLANE for baseline C01, best parametric and first optimized shapes. See also figure 32.
Figure 32. Alpha 0 to 180 lift-to-drag performance computed by AIRPLANE for baseline C01, best parametric and first optimized shapes. Compare with figure 52.
Figures 33, 34, 35, and 36. AIRPLANE predictions of $C_p$ on the Second Optimized Apollo Command Module, Mach 3.26, at the three design-point angles of attack (75, 130, 143 degrees) and at base-forward trim (138 degrees, shown shaded with two lights). The 4-tuple $(\theta, R_A, R_C, R_O) = (45, 14.2, 0, 385.4)$ defines the second optimized shape using the second objective function.
Figure 37. NPSOL objective function history for the second optimization of the Apollo Command Module, Mach 3.26. Black dots indicate numerical approximations of partial derivatives. Numbering starts at 0.
Figures 38, 39, 40, and 41. Design parameter values at each objective function evaluation for the second NPSOL Optimization, Mach 3.26. The initial 4-tuple \( (\theta, R_A, R_C, R_O) = (33, 15.4, 7.7, 184.8) \) defines the baseline C01 Apollo Command Module, and the optimized shape was approximately \( (44.99, 14.18, 0.0, 385.4) \).
Figures 42, 43, 44, and 45. AIRPLANE predictions of $C_p$ on the Third Optimized Apollo Command Module, Mach 3.26, at the three design-point angles of attack (75, 130, 143 degrees) and at base-forward trim (142 degrees, shown shaded with two lights). The 4-tuple $(\theta, R_A, R_C, R_O) = (45, 16, 5, 400)$ defines the second optimized shape using the second objective function.
Figure 46. NPSOL objective function history for the third optimization of the Apollo Command Module, Mach 3.26. Black dots indicate numerical approximations of partial derivatives. Numbering starts at 0.
Figures 47, 48, 49, and 50. Design parameter values at each objective function evaluation for the third NPSOL optimization, Mach 3.26. The initial 4-tuple \((\theta, R_A, R_C, R_O) = (33, 15.4, 7.7, 184.8)\) defines the baseline C01 Apollo Command Module, and the optimized shape was approximately \((45, 16, 5, 400)\). In this case, the lower limit for corner radius, \(R_C\), was raised from 0 to 5 inches.
Figure 51. Alpha 0 to 180 pitching moment coefficient computed by AIRPLANE for baseline C01 and the three NPSOL optimized cases. Compare with figure 30.
Figure 52. Alpha 0 to 180 lift-to-drag performance computed by AIRPLANE for baseline C01 and the three NPSOL optimized cases. Compare with figure 32.
Figure 53. Wind tunnel derived pitching moment coefficient data for C01–C10 Configurations at Mach 1.65.
Figure 54. Computational/experimental data corroboration of pitching moment coefficient data for C01–C10 configurations at Mach 1.65, 0 ≤ α ≤ 180.
Figure 55. Computational/experimental data corroboration of pitching moment coefficient data for C01–C10 configurations at Mach 1.65, $120 \leq \alpha \leq 180$. 
Figure 56. Wind tunnel derived pitching moment coefficient data for C01–C10 configurations at Mach 3.26 and 3.27.
Figure 57. Computational/experimental data corroboration of pitching moment coefficient data for C01–C10 configurations at Mach 3.26 and 3.27, 0 ≤ α ≤ 180.
Figure 58. Computational/experimental data corroboration of pitching moment coefficient data for C01–C10 configurations at Mach 3.26 and 3.27, $120 \leq \alpha \leq 180$. 
Figure 59. Wind tunnel derived pitching moment coefficient data for C01–C10 Configurations at Mach 5.0.
Figure 60. Computational/experimental data corroboration of pitching moment coefficient data for C01–C10 configurations at Mach 5.0, $0 \leq \alpha \leq 180$. 
Figure 61. Computational/experimental data corroboration of pitching moment coefficient data for C01–C10 configurations at Mach 5.0, $120 \leq \alpha \leq 180$. 
Figure 62. Lift coefficient comparison for the C01 configuration at Mach 1.65.
Figure 63. Drag coefficient comparisons for the C01 configuration at Mach 1.65.
Figure 64. Lift coefficient comparisons for the C01 configuration at Mach 5.0.
Figure 65. Drag coefficient comparisons for the C01 configuration at Mach 5.0.
Figure 66. Pitching moment coefficient data for Mach 0.4.
Figure 67. Pitching moment coefficient data for Mach 0.7.
Figure 68. Pitching moment coefficient data for Mach 1.2.
The Apollo Capsule Optimization for Improved Stability and Computational/Experimental Data Comparisons

Numerical optimization was employed on the Apollo Command Module to modify its external shape. The Apollo Command Module (CM) that was used on all NASA human space flights during the Apollo Space Program is stable and trimmed in an apex forward (alpha of approximately 40 to 80 degrees) position. This poses a safety risk if the CM separates from the launch tower during abort. Optimization was employed on the Apollo CM to remedy the undesirable stability characteristics of the configuration. Geometric shape changes were limited to axisymmetric modifications that altered the radius of the apex (R_a), base radius (R_b), corner radius (R_c), and the cone half angle (θ), while the maximum diameter of the CM was held constant. The results of multipoint optimization on the CM indicated that the cross-range performance can be improved while maintaining robust apex-aft stability with a single trim point. Navier-Stokes computations were performed on the baseline and optimized configurations and confirmed the Euler-based optimization results. Euler Analysis of ten alternative CM vehicles with different values of the above four parameters are compared with the published experimental results of numerous wind tunnel tests during the late 1960’s. These comparisons cover a wide Mach number range and a full 180-degree pitch range and show that the Euler methods are capable of fairly accurate force and moment computations and can separate the vehicle characteristics of these ten alternative configurations.

Optimization, Space capsules, Stability, Aerodynamic shape optimization, Euler, Experiment, Computational fluid dynamics (CFD)