In-Flight Subsonic Lift and Drag Characteristics Unique to Blunt-Based Lifting Reentry Vehicles

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Lift and drag measurements have been analyzed for subsonic flight conditions for seven blunt-based reentry-type vehicles. Five of the vehicles are lifting bodies (M2-F1, M2-F2, HL-10, X-24A, and X-24B) and two are wing-body configurations (the X-15 and the Space Shuttle Enterprise). Base pressure measurements indicate that the base drag for full-scale vehicles is approximately three times greater than predicted by Hoerner’s equation for three-dimensional bodies. Base drag and forebody drag combine to provide an optimal overall minimum drag (a drag “bucket”) for a given configuration. The magnitude of this optimal drag, as well as the associated forebody drag, is dependent on the ratio of base area to vehicle wetted area. Counterintuitively, the flight-determined optimal minimum drag does not occur at the point of minimum forebody drag, but at a higher forebody drag value. It was also found that the chosen definition for reference area for lift parameters should include the projection of planform area ahead of the wing trailing edge (i.e., forebody plus wing). Results are assembled collectively to provide a greater understanding of this class of vehicles than would occur by considering them individually.

Introduction

Controlled reentry from low Earth orbit and the upper atmosphere of the Earth continues to be of interest. Motivations include the need for a crew return and rescue vehicle from the International Space Station, a fledgling space tourism industry and its desire for low-cost reusable space access, the potential for future military space operations, and recent plans for human spaceflight and exploration as the space shuttle approaches retirement. In addition, precision entry, descent, and landing (EDL) in support of future planetary missions has become an area of active investigation. Fundamental studies by the NASA and NASA in the late 1950s and early 1960s described three basic methods of atmospheric reentry: ballistic reentry, winged reentry, and wingless lifting-body (semiballistic) reentry. The purely ballistic reentry approach necessitates the use of parachutes or parafloors to land, whereas the lifting-body and wing-body approaches allow the possibility of horizontal runway-type landings, given a sufficiently dense atmosphere such as for Earth. Flight examples of these latter two approaches include the M2-F1, M2-F2, HL-10, X-24A, X-24B, and X-15 vehicles and the Space Shuttle Enterprise, which comprise a unique class of aircraft sharing several features in common. These vehicles had lifting reentry shapes and a truncated afterbody forming a blunt base, which resulted in base drag being a significant component of the total drag. In addition, each of these flight vehicles performed routine, unpowa, horizontal landings on either paved or natural surfaces under the control of an onboard human pilot. Furthermore, these vehicles carried high-quality, sensor-recorder systems designed for measuring the parameters needed to define lift and drag. Vehicles without these shared features are not addressed herein. The lift and drag data of the vehicles presented herein were obtained during subsonic, unpowa, coasting flights.

The purpose of this study is to assemble flight-measured lift and drag data from these vehicles under common aerodynamic performance parameters or metrics (that is, the data from all seven vehicles are plotted together) in an attempt to unify the results for this class of vehicles. This array of data is intended to collectively yield information that might otherwise escape notice if the vehicles were individually studied. When it is meaningful, selected performance parameters of the subject vehicles are compared with data formats and standards that are based on classical aerodynamic theory and concepts that range from several decades to a century ago (for example, the concepts of Jones, Allen and Perkins, Helmbold, Krienes, Oswald, and, ultimately, Prandtl and Lanchester). Works explicitly used are referenced.

The innovative and intuitive concepts cited earlier were intended for vehicle configurations that are quite different from the subject

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vehicles. For example, the relevant Jones work applied to sharp-edged, low-aspect-ratio wings; Allen’s and Perkins’ related work addressed high-fineness-ratio bodies of revolution; and the concepts of the others applied to moderate-, high-, and even infinite-aspect-ratio wings. Despite their original purpose or application, several such theoretical relationships and standards have been used herein as a means of organizing and assessing the flight results considered.

This summary of performance metrics is necessarily somewhat limited to comply with journal format requirements. A considerably more comprehensive analysis is available [1], which includes additional metrics, supporting tables, footnotes, six appendices, and more references. Reference [1] and the present summary are intended to provide a useful database and analytical framework with which to compare and evaluate the subsonic aerodynamic performance of new vehicle configurations of the same generic family: low-aspect-ratio lifting reentry shapes with truncated bases. The results can also be used as a first-order design tool to help airframe designers define the outer moldlines of future related configurations as well as assess the predictive techniques used in their design. In addition, this reexamination of lifting reentry vehicles has been prepared and supporting references are cited, so that readers may access the source material and perform independent analyses of these full-scale flight results.

**Historical Background**

At a conference held in March of 1958, manned satellites and methods of reentering the Earth’s atmosphere were comprehensively studied [2–5]. Three different methods of reentry from Earth orbit were considered and discussed within the first four papers. The three methods were ballistic reentry [2], the wingless lifting body [3], and winged configurations [4]. Reference [3] advocates the lifting body mainly on the basis that its expected hypersonic lift-to-drag ratio of approximately 0.5 would provide a maximum tangential reentry deceleration of approximately 2 g, low enough to allow a pilot to intervene in the control of the vehicle during this portion of the reentry. (For a pure ballistic, nonlifting reentry, the peak tangential deceleration was expected to be approximately 8 g.) The first lifting-body concepts included, but were not limited to, very blunt half-cone shapes [3-5]. Those concepts later evolved into configurations that had higher fineness ratios [6–8], and the capability of achieving conventional (although unpowered) horizontal landings was discussed. Numerous wind-tunnel tests were performed on models of candidate versions of the half-cone shape with surfaces that were truncated at the edges. In 1962, unpowered horizontal landings and controllable flight were performed with a miniature, lightweight, radio-controlled model of an M2 half-cone configuration [9]. This demonstration was followed by the construction of a lightweight M2 craft large enough to carry a pilot. This unpowered M2-F1 vehicle demonstrated controllable flight and horizontal landings for a maximum lift-to-drag ratio of 2.8 for subsonic flight. The M2-F1 lift, drag, and stability control characteristics were published in 1965 [10,11].

A heavier and modified version of the M2 shape was built and began flying in 1966. The resulting lift and drag data from subsonic flight were published in 1967 [12]. Other lifting-body configurations (all capable of unpowered horizontal landings) were developed and flight-tested as well. The lift and drag characteristics from subsonic flights have previously been reported for the HL-10 [13], X-24A [14], and X-24B [15]. More information on the evolution and flight testing of the lifting bodies and the evolution of reentry concepts is available [9, 16–19].

The M2-F1 and subsequent lifting bodies were not the pioneer vehicles for performing unpowered (“dead-stick”) landings, but they were the first vehicles with very low aspect ratios (less than 1.5) to routinely land without power. The early rocket-powered research vehicles (the X-1, X-2, and D-558-II aircraft) were also designed for unpowered landings, but they had higher aspect ratios (between 6.0 and 3.6). Later, the X-15 hypersonic research aircraft, which had a published aspect ratio of 2.5 (between those of the early rocket-powered vehicles and the lifting bodies), made routine dead-stick landings. Confidence in the X-15 aircraft being able to land unpowered [20] was based on the successful experience of the earlier rocket-powered aircraft that had the higher aspect ratios and on a series of special landing investigations using low-aspect-ratio fighter-type airplanes [21]. This study investigated subsonic approach and landings at lift-to-drag ratios of 2 to 4 and used extended gear and speed brakes to increase the drag. Lift and drag data for the X-15 aircraft have previously been published [20,22].

Despite the success of the X-15 unpowered landing experience, the early planning for the space shuttle considered “pop-out” auxiliary engines to ensure safe horizontal landings. However, further consideration of the X-15 and lifting-body experience rendered landing engines for the space shuttle as an unnecessary weight and payload penalty [23]. The space shuttle ultimately was designed to make unpowered landings, and thus became the heaviest of the reentry-type vehicles to use routine dead-stick landings. (The Enterprise was 120 times the weight of the M2-F1 vehicle.) The low-speed lift and drag characteristics of the Enterprise have previously been published [24]. Results have been reported for the Enterprise with and without a tailcone [24]. Only the truncated configuration (that is, without a tailcone) is considered here. The lift and drag data that are used on the other six vehicles. Slight use is made of results from the Enterprise (with the tailcone attached) when they reveal a finding that merits documentation.

In recent years, lifting reentry vehicles have been proposed for rescue missions from space (X-38) and to serve as reusable launch vehicles (X-33, X-34, X-37). These vehicles have much in common with the lifting bodies described herein and, if aspect ratio is somewhat increased, with the X-15 aircraft and the Enterprise. This paper presents the subsonic lift and drag characteristics of the M2-F1, M2-F2, HL-10, X-24A, X-24B, and X-15 vehicles and the Space Shuttle Enterprise under uniform performance parameters and formats, with the intent of aiding the definition of exterior moldlines of future candidate reentry vehicles that perform horizontal landings.

As was mentioned in the Introduction section, some of the unifying metrics depend on borrowed concepts and standards that are several decades old and were originally intended for application on winged vehicles of high or moderate aspect ratio. The authors acknowledge that some readers may disagree with how the borrowed concepts and standards are applied herein. The formats, concepts, and standards that have been used, and the information that may be derived therefrom, are offered as a beginning in the quest for understanding the general nature of the subsonic lift and drag for this unique class of vehicles.

**Methods of Analysis and Nomenclature**

This section assembles methods and metrics (performance parameters) used in the analysis of the subject lift and drag data. The primary metrics of aerodynamic performance used herein include lift-curve slope; a modified Oswald lifting-efficiency factor; maximum lift-to-drag ratio; and for minimum drag analysis, equivalent parasite drag area, equivalent skin-friction coefficient, base pressure coefficient, base drag coefficient, and forebody drag coefficient. This list of metrics is not considered all-inclusive; however, it represents those parameters that most directly define lift capability (lift-curve slope and Oswald lifting-efficiency factor). Likewise, lift-to-drag ratio and the other drag factors reliably define subsonic downrange and lateral range capability. Additional lift-drag factors applied to these same vehicles are presented in [1], which is a publishing venue that is less confined in length. This section also defines the nomenclature as the various metrics are introduced.

**Lift-Curve Slope**

Trimmed lift-curve slope data for the subject vehicles are compared with potential flow standards for finite-span wings. The most exact theoretical solution for unswept, rectangular wings at incompressible conditions is considered to be that derived by Krienes [25]. Krienes’s relationship for lift-curve slope $C_l$ and aspect ratio $A$ is well represented by the following relationship from Helmbold

\[ C_l = \frac{1}{A} \left( \frac{2}{3} \frac{C_{L_{max}}}{\alpha} \right)^{0.5} \]
[26], as expressed by Polhamus [27], where \( C_{L_{w}} \) is represented in rad\(^{-1}\):

\[
C_{L_{w}} = \frac{2\pi A}{\sqrt{A^2 + 4 + 2}} \quad (1)
\]

As \( A \) approaches infinity, \( C_{L_{w}} \) approaches 2\( \pi \). At the lowest aspect ratios, Eq. (1) merges with the linear relationship of Jones [28]:

\[
C_{L_{w}} = \frac{\pi A}{2} \quad (2)
\]

Equations (1) and (2) represent lift caused by circulation. Neither of these relationships account for leading-edge vortex lift, such as is developed by high-wet delta wings [29], nor lift generated by vortices resulting from crossflow over the forebody [30–32]. The relationships expressed by Eqs. (1) and (2) are each oblivious to the effects of trim. Although all seven vehicles violate the limitations of Eqs. (1) and (2), as any aircraft during trimmed conditions generally does, these equations are considered to be rational standards for evaluating the relative lifting capability of the subject configurations. The slopes for the lift curves of the present study were obtained over the lift coefficient range extending from the lowest lift coefficient achieved for a given maneuver to a lift coefficient somewhat greater than that required to obtain maximum lift-to-drag ratio.

**Maximum Lift-to-Drag Ratio**

The maximum lift-to-drag ratio \((L/D)_{\text{max}}\) achieved by each of the subject vehicles at subsonic speeds is presented as a function of \( b^2/A_w \) (i.e., span-squared, divided by wetted area). This form of aspect ratio is referred to as the “wetted aspect ratio” [33]. This presentation includes a reference framework consisting of a family of curves representing constant values of equivalent skin-friction coefficient or equivalent viscous-drag coefficient \( C_{f_{w}} \), which is a form of minimum drag coefficient \( C_{D_{\text{min}}} \) (which includes both forebody and base drag). Thus, if

\[
C_{D_{\text{min}}} = \frac{D_{\text{min}}}{\bar{q}S} \quad (3)
\]

where \( \bar{q} \) is dynamic pressure and \( S \) is the reference area, then

\[
C_{f_{w}} = C_{D_{\text{min}}} S \quad A_w \quad (4)
\]

Although \( C_{f_{w}} \) is called the “equivalent skin-friction coefficient,” the important word is “equivalent,” because \( C_{f_{w}} \) is composed of base drag, separation losses, interference drag, protuberance drag, and other losses, in addition to skin friction. The family of reference curves is analogous to that employed in [34], and the curves are defined by the following often-used expression from [35]:

\[
(L/D)_{\text{max}} = \frac{1}{2} \sqrt{\frac{\pi A}{C_{D_{\text{min}}}}} \quad (5)
\]

where the Oswald lifting-efficiency factor \( \varepsilon \) [36] is modified as demonstrated in [37], as follows:

\[
\varepsilon = \frac{(C_L - C_{L_{\text{min}}})^2}{\pi A(C_D - C_{D_{\text{min}}})} \quad (6)
\]

**Minimum Drag of the Vehicle**

Minimum drag is considered in several formats. If the lift coefficient and drag coefficient are based on vehicle planform reference area, the minimum drag coefficient can be defined as in Eq. (3). The discussion on maximum lift-to-drag ratio also revealed that another metric for minimum drag coefficient is the equivalent skin-friction coefficient [Eq. (4)], which is obtained by basing the minimum drag coefficient on the wetted area \( A_w \). The wetted area for each vehicle is considered to be the wetted area of the respective forebody, which includes the body and wings or fins, and thus is the sum of all outer moldline surfaces ahead of an associated base or trailing edge.

Another format for comparing minimum drag for various configurations is the equivalent parasite drag area \( f \). This metric is related to Eq. (3) but eliminates controversy regarding the choice of reference area by being defined as follows:

\[
f = C_{D_{\text{min}}} S = D_{\text{min}} \frac{A_b}{\bar{q}} \quad (7)
\]

Thus, \( f \) is the minimum drag divided by the freestream dynamic pressure. Use of equivalent skin-friction coefficient \( C_{f_{w}} \) [Eq. (4)] and equivalent parasite drag area \( f \) [Eq. (7)] is common among aircraft designers. An early example of their use is given in [38].

Minimum drag has previously been represented as three metrics: \( C_{D_{\text{min}}} \), in which the reference area is the vehicle planform area \( S \), which is sometimes defined subjectively; \( C_{f_{w}} \), in which the reference area is the forebody wetted area \( A_w \), which can be defined objectively and accurately; or as \( f \), in which the reference area is eliminated as a factor. Despite any confusion that might result from such names as “equivalent skin-friction coefficient” and “equivalent parasite drag area” (which have been commonly used for many years), each of the metrics presented earlier for minimum drag should be understood to include all losses caused by the forebody (that is, body plus fins, protuberances, control surfaces, and, if applicable, wings) as well as the drag caused by all base surfaces. Mathematically speaking, the following exists:

\[
C_{D_{\text{min}}} = C_{D_{\text{min}},f} + C_{D_{b}} \quad \frac{A_b}{A_w} \quad (8)
\]

and

\[
C_{f_{w}} = C_{f_{w},f} + C_{D_{b}} \quad \frac{A_b}{A_w} \quad (9)
\]

where \( C_{D_{\text{min}},f} \) is the forebody drag coefficient referenced to \( S \), \( C_{f_{w},f} \) is the equivalent skin-friction coefficient caused by the forebody only, \( C_{D_{b}} \) is the coefficient of base drag (here based on reference area \( A_b \), which is the base area).

**Minimum Forebody Drag**

Significant excess forebody drag exists, in addition to the drag caused by skin friction. One method to quantify the excess forebody drag is to compare the measured minimum drag of a vehicle with the sum of the measured base drag and the calculated skin-friction drag for completely attached, turbulent, boundary-layer flow. The difference that results from this comparison represents losses from multiple sources, which are designated as “excess forebody drag.” The calculated, idealized sum of the base drag and skin-friction drag for each vehicle is obtained from the following:

\[
C_{f_{w}} = C_F + \frac{C_{D_{b}}}{A_b} \quad \frac{A_b}{A_w} \quad c \quad (10)
\]

where \( C_F \) is the turbulent boundary-layer skin-friction coefficient (calculated) of the forebody and \( c \) is a base pressure profile factor.

The values of \( C_F \), representing idealized forebody losses, have been calculated for each of the vehicles at the various flight conditions; adjusted for compressibility effects by the reference temperature method as applied by Peterson [39]; and adjusted for form factor (three-dimensionality) by the coefficient 1.02, as recommended for conical flow [40]. The value of \( C_F \) used to calculate the reference curves presented herein is 0.0023, which is the average value of \( C_F \) for the various vehicles at the flight conditions reported herein. The constant \( c = 0.92 \) is a base pressure profile factor and its origin is explained in [1].

**Base Pressure Coefficients**

Flight-measured base pressure coefficients, base pressure coefficients derived from published incremental drag attributed to
the base, and estimated base pressure coefficients derived from those of a closely related, afterbody-base configuration are compared with two analytical equations developed by Hoerner [32]. These equations were derived from wind-tunnel experiments of small-scale models. Hoerner’s equation for three-dimensional axisymmetric bodies of revolution is as follows:

\[-C_p = \frac{K}{\sqrt{C_{D_{max}}}}\]  \hspace{1cm} (11)

where \( K = 0.029 \) and \( C_{D_{max}} \) is referenced to base area \( A_p \). Hoerner’s equation for quasi-two-dimensional base flow conditions that generate the well-known Kármán vortex street is

\[-C_p = \frac{0.135}{\sqrt{C_{D_{max}}}}\]  \hspace{1cm} (12)

**Lift and Drag Coefficients**

The flight-measured lift and drag coefficients \( C_L \) and \( C_D \) for all seven vehicles were obtained by the accelerometer method \([41,42]\). The relationships for unpowered, gliding flight are

\[C_L = (a_n \cos \alpha + a_l \sin \alpha) \frac{W}{\bar{q}S}\]  \hspace{1cm} (13)

\[C_D = (a_n \sin \alpha - a_l \cos \alpha) \frac{W}{\bar{q}S}\]  \hspace{1cm} (14)

where \( a_n \) and \( a_l \) are the normal and longitudinal accelerations, \( \alpha \) is the angle of attack, \( W \) is the vehicle weight, \( \bar{q} \) is the freestream dynamic pressure, and \( S \) is the reference area.

**Data Uncertainty**

The accurate determination of lift and drag characteristics from flight data requires high-quality sensors and careful attention to detail in sensor calibration and use. In general, lift and drag determination is most sensitive to error in the measurement of thrust, longitudinal and normal acceleration, angle of attack, static pressure, Mach number, vehicle weight, and an accounting of control deflections. For the seven vehicles considered herein, thrust is not a factor, because the data were obtained during coasting flight; thus, a major source of uncertainty is avoided. Some of the problems associated with the measurement of these quantities, and their relative importance, are discussed in \([42]\).

Uncertainty information has been published for four of the subject aircraft: M2-F1, M2-F2, HL-10, and X-15 vehicles. A summary of the available uncertainty data is shown in Table \( 1 \). Background information pertaining to the origins of the data in this table is given in \([1]\). The right-hand column shows the uncertainty in base pressure coefficients \( C_{p_b} \).

These uncertainties represent the square root of the sum of the squares for each of these coefficients when plotted as individual data points. Because these coefficients (as used herein) are obtained from curves faired through numerous data points, the uncertainty of the coefficients resulting from faired data and other metrics should be significantly smaller than those shown in Table \( 1 \).

Corresponding uncertainties are not available for the X-24A and X-24B lifting bodies and the Space Shuttle Enterprise; however, air data system calibration procedures similar to those used on the other four vehicles are known to have been used on these three. In addition, lift and drag were obtained by the accelerometer method for all seven vehicles. Although Table \( 1 \) cannot be established as representing the uncertainties for the latter three vehicles, expecting their uncertainties to be relatively close to those listed is not unreasonable.

**Results and Discussion**

The primary results of this summary study are presented and discussed under three subheadings: “Lift-Curve Slope,” “Maximum Lift-to-Drag Ratio,” and several metrics of “Minimum Drag.” These and other aerodynamic performance metrics, as applied to the subject vehicles, have been reported in \([1]\) in significantly greater detail. Formats for collectively presenting the data were chosen in the hope that one or more formats will yield a greater understanding of the data than would likely occur by individually studying the subject vehicles.

**Lift-Curve Slope**

This section attempts to unify the lift capabilities of the seven flight vehicles previously discussed. The lift-curve slope data for subsonic flight of these vehicles have been assembled from \([10,12,15,22,24]\). Data were obtained during gradual pushover/pullup maneuvers (consequently trimmed for the respective maneuvers) over a range of lift coefficients extending to somewhat greater than that required to achieve the maximum lift-to-drag ratio. These data are compared with generic wind-tunnel model data and to theory for very low and moderately low aspect ratios. Figure \( 1 \) shows three-view drawings of each of the seven vehicles and the M2-F3 lifting body. Major dimensions for each vehicle are presented in Table \( 2 \).

Figure \( 2 \) shows lift-curve slope results for the seven subject vehicles, plotted as a function of aspect-ratio. The often-used Prandtl–Glauert factor (1-\(M^2\)) \(^{0.5} \) has been applied to both the ordinate and abscissa functions, because data for the various vehicles were obtained at different subsonic Mach numbers. Wind-tunnel model data for simple generic lifting-body shapes are also included \([43,44]\). Figure \( 2 \) also shows the relationships of \( C_{L_{\text{th}}} \) to aspect ratio as defined by Helmbold (Eq. \( 1 \)) and, for the lowest aspect ratios, the linear relationship of Jones (Eq. \( 2 \)). Neither of these relationships accounts for lift from crossflow over the bodies or from vortices generated by sharp, highly swept leading edges. Stated another way, Eqs. \( (1) \) and \( (2) \) apply when the flow does not separate from leading or swept lateral edges (that is, these equations represent lift generated by circulation).

The lift-curve slopes for each of the flight vehicles were expected to occur below the Jones and Helmbold relationships, which represent maximum efficiency for medium- or low-aspect-ratio configurations that obtain their lift from circulation. However, the slope value for the M2-F2 is above the theoretical curves, and the slope for the X-15 is relatively high (i.e., between the Jones and Helmbold curves).

The data from the generic model shapes (solid symbols) \([43,44]\) suggest that the M2-F2 slope occurring above the theoretical curves should not be considered to be an anomaly. The reason that the M2-F2 vehicle and the slender model shapes (that is, those having aspect ratios less than 1.0) have relatively high lift-curve slopes may be related to well-developed forebody vortices caused by crossflow, as reported in \([30-32]\). The half-cone shapes, having lateral edges with a small radius, were expected to produce vortex lift. However, the elliptical cone shape with the most slender planform (the lowest aspect ratio) also had a high slope compared with potential theory. Thus, the conjecture that well-developed vortices (resulting from body crossflow) may provide an extra component of lift is afforded credence, even if sharp lateral edges are absent.

Because of this evidence that crossflow (counter-rotating vortex pair) effects may significantly contribute to the lift of the slender forebody portions of lifting bodies, considering that the forebodies of the X-15 aircraft and the Enterprise may likewise generate significant amounts of crossflow lift is appropriate. For these winged

<table>
<thead>
<tr>
<th>Vehicle</th>
<th>( \Delta C_L/C_{L_{\text{th}}} % )</th>
<th>( \Delta C_D/C_{D_{th}} % )</th>
<th>( \Delta C_{p_b}/C_{p_{\text{th}}} % )</th>
</tr>
</thead>
<tbody>
<tr>
<td>M2-F1</td>
<td>( \pm 3.0 )</td>
<td>( \pm 5.5 )</td>
<td>( \pm 7.0 )</td>
</tr>
<tr>
<td>M2-F2</td>
<td>( \pm 1.7 )</td>
<td>( \pm 3.2 )</td>
<td>Not available</td>
</tr>
<tr>
<td>HL-10</td>
<td>( \pm 3.2 )</td>
<td>( \pm 3.9 )</td>
<td>Not available</td>
</tr>
<tr>
<td>X-15</td>
<td>( \pm 4.3 )</td>
<td>( \pm 3.9 )</td>
<td>( \pm 6.4 )</td>
</tr>
</tbody>
</table>
vehicles, therefore, the forebody planform area and the wing area projected to the vehicle centerline are considered to be the reference area. Because the revisions of reference area for the X-15 and space shuttle vehicles are a departure from convention, and because two separate concepts are involved, additional discussion and supporting data are justified. First, inclusion of the forebody planform area with the wing-panel area is justified in part, on the basis of the crossflow lift experienced by lifting bodies \[30-32,43,44\]. In addition, Appendix D of [1] cites fuselage normal force data obtained in-flight from two aircraft (the X-1 and the X-15) that establish that fuselage lift is significant. The second concept, which rejects fuselage planform area aft of the wing trailing edge for inclusion as reference area, conforms to [28] (pgs. 59 and 63), which postulates that for pointed shapes, “sections behind the section of maximum width develop no lift.” This theory, and flight data from the X-1 airplane [45], also shown in Appendix D of [1], taken together, constitute the rationale for this second concept.

As noted earlier, the lift-curve slope data from the half-cone [43] and elliptical cone [44] models tend to confirm the M2-F2 flight results, which exceed the Jones relationship. The values for the elliptical cone models at aspect ratios greater than 1, however, have lift-curve slopes that are significantly lower than both the Helmbold and Jones relationships [Eqs. (1) and (2), respectively]. For the elliptical cone shapes having the highest aspect ratios (that is, clearly nonslender), a lift component caused by circulation dominates and some degree of crossflow additionally exists; whereas at the lowest aspect ratios, the crossflow component of lift is more dominant [31,32].

The model data of [43,44] represent untrimmed conditions; consequently, their lift-curve slopes are expected to be optimistic. It is not surprising, then, that the lift-curve slopes for the five lifting bodies obtained at full scale during trimmed flight form a crude band arrayed approximately 12 to 15% below the small-scale, untrimmed, elliptical cone model results. On the other hand, it is clear that the X-15 and shuttle vehicles (which had wings and lifting-body-like forebodies) benefited significantly from the combination of both lifting components.

The degree of order, or coalescence, of the lift-curve slope data from the several vehicles was achieved only after revising some of the reference areas and span dimensions from those previously published with the original lift-curve data. For the lifting bodies, the physically meaningful reference area should include all planform area projected onto the longitudinal-lateral plane, including the projected area of canted tip or side fins. Improved order was also provided by adjusting the data for compressibility effects. Dimensions given in [46,47] were used to revise those published with the original lift-curve data for the M2-F2 and X-24A vehicles, respectively.

Maximum Lift-to-Drag Ratio

Figure 3 shows maximum lift-to-drag ratio as a function of the ratio of span-squared to wetted area for each of the vehicles in subsonic flight. This format is commonly used by designers of conventional subsonic aircraft, because at subsonic speeds, air vehicle efficiency is most directly influenced by span and wetted area. Reference [33] refers to this abscissa function as the “wetted aspect ratio.”

For the lifting bodies, the X-15 vehicle, and the Enterprise, all of which have significant amounts of base drag, recognizing the “base” effects by assigning base drag to the equivalent skin-friction coefficient parameter \(C_{\delta f}\) is necessary. Consequently, Fig. 3 also shows a reference framework consisting of a family of constant values of \(C_{\delta f}\), as employed by [34]. This family of curves is derived from the often-used expression that relates maximum lift-to-drag ratio to the minimum drag coefficient (here, expressed as \(C_{\delta f}\), aspect ratio, and the lifting-efficiency factor \(\varepsilon\) [Eq. (5)]. The range of the family of \(C_{\delta f}\) curves shown in Fig. 3 covers the range of values experienced by the subject vehicles. Thus, the format used will accommodate this class of vehicles for which minimum drag consists of a large component of base drag as well as friction drag. A lifting-efficiency factor \(\varepsilon\) of 0.6 was assigned to these curves, because this value is approximately the average for the subject vehicles as a group. The dashed curve for the equivalent skin-friction coefficient is included, because it represents a nominally clean modern aircraft that does not have a truncated body and is constrained to an \(\varepsilon\) factor of 0.6. Note in Fig. 3 that when the Enterprise had its blunt base covered with a tailcone, the maximum lift-to-drag ratio increased to 7.5,
relatively close to the dashed curve. The tailcone partially qualifies this configuration as approximating “nominally clean.” However, the intentionally roughened surface of the Enterprise simulating a thermal protection system obviously violates nominally clean requirements. As noted in [1], the tailcone did not contribute to lift; hence, the increase in maximum lift-to-drag ratio can only be attributed to a significant reduction in minimum drag.

The highest values of maximum lift-to-drag ratio at subsonic conditions for five of the blunt-based vehicles and their collective relationship to the reference framework of curves form an array \( \L/D_{\text{max}} \) that should be a useful reference source with which to relate future reentry-type vehicles. A fairing through this data band (as related to the dashed curve) would indicate that this class of vehicles has maximum lift-to-drag ratios that are approximately 55% of those for nominally clean vehicles, having an \( \epsilon \) value of 0.6, without truncated bodies (that is, the dashed curve) for a given aspect ratio. The M2-F1 and HL-10 lifting bodies, which are less efficient, should be no less useful to the degree their apparent lesser efficiency is more fully understood.

Minimum Drag

Minimum drag is presented in several formats to better understand which components are dominant and to reveal the relationship of forebody and base drag. The metrics used, as defined earlier, include equivalent skin-friction coefficient \( C_{Fe} \) and equivalent parasite drag area \( f_{e} \), as shown in Eq. (7).

Although the revised reference areas are believed to be a rational improvement over the areas that they replace (as noted in the “Lift-Curve Slope” section), the format chosen here for graphically presenting the minimum drag eliminates the often arbitrary conventional reference area as a factor. Reference [38] and subsequent others have avoided the concern about reference area definition by multiplying the minimum drag coefficient by the reference area to define an equivalent parasite drag area \( f \), as shown in Eq. (7).

Table 2 Physical characteristics of the vehicles

<table>
<thead>
<tr>
<th>Vehicle</th>
<th>( l ), length, ft</th>
<th>( b ), span, ft</th>
<th>( A ), aspect ratio</th>
<th>( S ), reference area, ( \text{ft}^2 )</th>
<th>( A_w ), wetted area, ( \text{ft}^2 )</th>
<th>( A_b ), base area, ( \text{ft}^2 )</th>
<th>( W ), weight, lb</th>
<th>( M ), Mach range</th>
<th>Fineness ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>M2-F1</td>
<td>20.00</td>
<td>14.17</td>
<td>1.318</td>
<td>152.4</td>
<td>431.0</td>
<td>30.84</td>
<td>1250</td>
<td>0.15</td>
<td>2.50</td>
</tr>
<tr>
<td>M2-F2</td>
<td>22.20</td>
<td>9.95</td>
<td>0.619</td>
<td>160.0</td>
<td>459.0</td>
<td>22.51</td>
<td>6000</td>
<td>0.45 to 0.62</td>
<td>2.94</td>
</tr>
<tr>
<td>HL-10</td>
<td>21.17</td>
<td>13.60</td>
<td>1.156</td>
<td>160.0</td>
<td>460.5</td>
<td>14.83 to 29.13</td>
<td>6000</td>
<td>0.60</td>
<td>2.67</td>
</tr>
<tr>
<td>X-24A</td>
<td>24.50</td>
<td>13.63</td>
<td>0.953</td>
<td>195.0</td>
<td>590.0</td>
<td>11.78 to 25.36</td>
<td>6360</td>
<td>0.50</td>
<td>2.73</td>
</tr>
<tr>
<td>X-24B</td>
<td>37.50</td>
<td>19.14</td>
<td>1.108</td>
<td>330.5</td>
<td>948.4</td>
<td>18.79 to 38.05</td>
<td>8500</td>
<td>0.50 to 0.80</td>
<td>3.93</td>
</tr>
<tr>
<td>X-15</td>
<td>49.50</td>
<td>22.36</td>
<td>1.629</td>
<td>307.0</td>
<td>1186.0</td>
<td>33.0</td>
<td>15,000</td>
<td>0.65 to 0.72</td>
<td>7.18</td>
</tr>
</tbody>
</table>

*Fineness ratio is the vehicle length divided by the diameter of a circle having the same area as the maximum projected cross-sectional area of the vehicle.

Fig. 2 The relationship of lift-curve slope with aspect ratio as obtained in-flight from generic models and from the theories of Jones and Helmbold (Krien).
pressure coefficients over the base or aft sloping surfaces each represent drag increments in excess of the viscous drag generated by the actual wetted surfaces. Hence, this drag metric defines the sum of the drag sources (excluding lift) that include friction drag for turbulent flow conditions as well as drag components in excess of friction. Because even an ideal body will have friction drag, this metric is labeled as a “parasite” factor because the metric includes such parasitic losses.

The equivalent parasite drag area can also be interpreted in terms of an equivalent skin-friction coefficient $C_{F_e}$ by noting the location of a datum point for a given vehicle relative to the family of constant equivalent skin-friction lines (Fig. 4). The equivalent skin-friction coefficient is, of course, another metric that reveals the degree to which measured minimum drag of a vehicle exceeds the ideal minimum drag (that is, the skin-friction drag over the wetted area). The average subsonic skin-friction coefficient over wetted areas for all seven vehicles, assuming flat-plate, turbulent boundary-layer flow (adjusted by a form factor of 1.02) at flight Reynolds numbers, is $C_F = 0.0023$, which can also be considered as a reference value of $C_{F_e}$ (see the dashed line in Fig. 4).

A cursory summary of the data shown in Fig. 4 can be stated as follows:

1) The early generations of lifting bodies, the M2 and the HL-10 vehicles, have equivalent skin-friction coefficients between 0.0170 and 0.0200 (in contrast to the average value of skin friction for all seven vehicles for turbulent flow, 0.0023).

2) For the X-24A and X-15 vehicles, the corresponding equivalent skin-friction coefficients are approximately 0.011.

3) The X-24B vehicle, the last of the lifting bodies, has an equivalent skin-friction coefficient slightly less than 0.009.

4) The wetted surfaces of the Enterprise were purposely roughened to simulate the thermal protection tiles of operational bodies formed by the upper and lower flaps that are used for control in pitch. The upper flap was deflected upward approximately 40 deg, and the lower flap was deflected downward approximately 28 deg. This geometry is known to produce more negative base pressure coefficients [51]. The only measured base pressure data from the X-24B vehicle [48], unfortunately, were obtained with a significantly larger wedge angle than existed for the subsonic control configuration for the X-24B data of this study.

The M2-F1 datum is somewhat unrepresentative of the subject class of vehicles, in that the base region was pressurized to some extent by turning vanes (one on each side, below the rudders). Based on the available flight data, the vehicles considered herein (excepting the data for the M2-F1 vehicle and the X-24B transonic configuration) are best represented by the three-dimensional equation where $K = 0.09$ to 0.10, which means that the base drag of each of the seven vehicles, from approximately 0.009 to 0.020, is from four to slightly more than eight times the skin-friction drag that would occur from an attached turbulent boundary layer alone (see the tabular values for each vehicle, listed in Fig. 4).

### Base Pressure Coefficients

Hoerner [32] compiled base pressure data from projectiles, fuselage shapes, and other small-scale three-dimensional shapes and derived therefrom an equation that related the base drag and base pressure coefficients to the forebody drag of the respective bodies [Eq. (11)]. Reference [32] also includes an equation that describes the analogous relationship for quasi-two-dimensional shapes that shed vortices in a periodic manner, the well-known Kármán vortex street [Eq. (12)]. Base pressure data from some of the subject vehicles will be compared on the basis of the Hoerner relationships and modifications to his equations (using different $K$ values). The search for flight-measured base pressure data for the seven subject vehicles is somewhat disappointing, considering that each of these vehicles has a significant component of base drag. Table 2 shows the results of the literature search.

Note from Figs. 1b and 1c that the M2-F3 vehicle is virtually the same as the M2-F2 vehicle. All configurational dimensions are the same except that a centerline upper vertical fin was added to the M2-F3 vehicle. For this reason, the unpublished base pressure data from the M2-F3 lifting body are accepted as representative of those of the M2-F2 lifting body. Consequently, the M2-F2 and the M2-F3 lifting bodies will be treated as if they were the same vehicle in the analysis to follow.

Because of Hoerner’s convincing demonstration that base pressure is related to forebody drag, comparing the available base pressure coefficients from the subject vehicles to his equations is possible. Figure 5 shows these comparisons. Figure 5 also includes a shaded band for Hoerner’s three-dimensional equation that is bounded by numerator coefficients $K$ of 0.09 and 0.10. By modifying Hoerner’s original equation with these $K$ coefficients, the base pressure coefficients from the X-15, the M2-F3, and the space shuttle vehicles (which are obviously three-dimensional) are observed to fall within, or relatively close to, this band.

Figure 5 also shows that the flight data are relatively close to Hoerner’s quasi-two-dimensional relationship [Eq. (12)]. The relatively higher (more negative) pressure coefficient from the X-24B vehicle (dark triangle) is caused by the large wedge angle, ahead of the base, formed by the upper and lower flaps that are used for control in pitch. The upper flap was deflected upward approximately 40 deg, and the lower flap was deflected downward approximately 28 deg. This geometry is known to produce more negative base pressure coefficients [51]. The only measured base pressure data from the X-24B vehicle [48], unfortunately, were obtained with a significantly larger wedge angle than existed for the subsonic control configuration for the X-24B data of this study.

The M2-F1 datum is somewhat unrepresentative of the subject class of vehicles, in that the base region was pressurized to some extent by turning vanes (one on each side, below the rudders). Based on the available flight data, the vehicles considered herein (excepting the data for the M2-F1 vehicle and the X-24B transonic configuration) are best represented by the three-dimensional equation where $K = 0.09$ to 0.10, which means that the base drag of

### Table 3 Base pressure sources

<table>
<thead>
<tr>
<th>Vehicle</th>
<th>$C_{p_b}$ data</th>
<th>Reference number</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>M2-F1</td>
<td>Yes</td>
<td>[10]</td>
<td>The M2-F3 base pressure data were applied to the M2- F2 vehicle drag data.</td>
</tr>
<tr>
<td>M2-F3</td>
<td>Yes</td>
<td>Unpublished</td>
<td>Base drag data have been published, but no explicit base pressure data were found.</td>
</tr>
<tr>
<td>HL-10</td>
<td>No</td>
<td></td>
<td>Base pressure coefficients were estimated using X-24B results (Appendix F of [1]).</td>
</tr>
<tr>
<td>X-24A</td>
<td>No</td>
<td></td>
<td>Base pressure coefficients were estimated using Mach 0.8 results (Appendix F of [12]).</td>
</tr>
<tr>
<td>X-24B</td>
<td>Yes</td>
<td>[48]</td>
<td>Base pressure data from the orbiting Space Shuttle Columbia have been applied to the drag data from the nonorbiting Enterprise.</td>
</tr>
<tr>
<td>X-15</td>
<td>Yes</td>
<td>[50]</td>
<td></td>
</tr>
<tr>
<td>Space shuttle</td>
<td>Yes</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
blunt-based large-scale vehicles is much higher than predicted by the original three-dimensional equation. Based on evidence from [49,52] and Fig. 5, subsonic flow separating from a relatively large, sharp-edged, three-dimensional base can be argued to exhibit quasi-two-dimensional characteristics. In either case, the data indicate much more negative base pressure coefficients than the unmodified three-dimensional equation $K = 0.029$ would predict.

Optimal Minimal Drag

Excluding the base pressure data from the M2-F1 and the X-24B vehicles for the reasons already given, the flight data from three other vehicles (M2-F3, X-15, and space shuttle vehicles) are believed to represent the generic blunt-based class of vehicles. More large-scale base pressure and overall minimum drag (and hence forebody drag) data must be obtained in-flight to convincingly demonstrate their relationship. Defining this relationship for three or four values of forebody drag for the same outer moldline shape would be most helpful. Until more flight data are obtained or a superior relationship to the curves, note that the data from the vehicles designated by the open symbols (except the M2-F1 and HL-10 vehicles) are in qualitative accord with the semi-empirical curves. As was stated earlier with regard to Fig. 5, the overall $C_{Fb}$ for the M2-F1 vehicle is believed to be lower than the semi-empirical curves suggest, because turning vanes pressurized the base. For the X-24B vehicle in Fig. 6 (the dark triangle), the value of $C_{Fb}$ is believed to be high because of the aforementioned large flared angle that produces high windward surface drag and lowers the leeside pressures on the longitudinal control body flaps. This belief is not only supported by data from [51] but also by speed-brake data from the X-15 aircraft (the dark symbol) that represent a comparable flared, or wedge, angle [53].

With reference to the curves in Fig. 6, analytically determining the minimum, or bucket, value of the equivalent skin-friction coefficient $C_{Fb}$, and the associated forebody equivalent skin-friction coefficient $C_{Fb,low}$ for a given base-area-to-wetted-area ratio $A_b/A_w$ is possible. The curves of Fig. 6 are defined by a revision of Eq. (10), repeated here:

$$C_{Fb} = C_F + C_{Fb} \frac{A_b}{A_w} c$$

Equation (10) was used to calculate $C_{Fb}$ for a case in which no forebody losses existed, except for that of a fully attached, turbulent boundary over a smooth surface (hence, the term $C_F$ on the right side of the equation). For the curves shown in Fig. 6, the abscissa values of $C_{Fb,low}$ are substituted for $C_{Fb}$ in Eq. (10), as follows:

$$C_{Fb} = C_{Fb,low} + C_{Fb} \frac{A_b}{A_w} c$$

where $c = 0.92$, as derived from X-15 experience as a base pressure
profile factor, is explained in [1], and \(C_{p_0}\) is the expression from [32], Eq. (11):

\[-C_{p_0} = \frac{K}{\sqrt{C_{D_{tot,3}}}}\]

where \(K = 0.10\), based on current analysis. Also,

\[C_{D_{tot,3}} = C_{F_{tan}} A_w A_b\]  \(\text{(16)}\)

Substituting Eq. (16) into Eq. (11) and, in turn, Eq. (11) into Eq. (15), gives the following:

\[C_{F_e} = C_{F_{tan}} + \frac{0.10}{\sqrt{C_{F_{tan}}(A_w/A_b) A_w}}\]

\(\text{To determine the coordinates for the bucket value of } C_{F_e}, \text{ the preceding expression is differentiated with respect to } C_{F_{tan}}. \text{ Setting the derivative to zero, the minimum } C_{F_e} \text{ value occurs at}

\[C_{F_{tan}} = 0.1284 \frac{A_b}{A_w}\]  \(\text{(18)}\)

Substituting back into Eq. (17), the minimum of \(C_{F_e}\) for a given base-area-to-wetted-area ratio is

\[C_{F_e} = 0.3852 \frac{A_b}{A_w}\]  \(\text{(19)}\)

These expressions for optimal values of forebody drag and overall minimum drag coefficient are offered as tools for approximation until more definitive relationships are obtained. The present expressions define the coordinates for minima that are consistent with values obtained graphically from working plots; however, they and the families of curves of Fig. 6 are dependent on multiple assumptions. These assumptions include the validity of the Hoerner equation (11) for three-dimensional flow, the assigned value of \(K\) for Eq. (11), and the validity of the base pressure profile factor of 0.92. Generally, improved values for such curves and the expressions for minima [Eqs. (18) and (19)] can be generated as assumptions become based on a more comprehensive database or as a new superior relationship of the variables is formulated.

**Fig. 6** The relationship of equivalent skin-friction coefficients for the complete vehicle and the forebody.

Conclusions

Flight-determined lift and drag characteristics from seven blunt-based lifting-body and wing-body reentry configurations have been compared and related to several standards of aerodynamic efficiency. For lift-curve slope, limited comparisons have been made with wind-tunnel results for generic models and the theoretical relationships of Jones and Helmbold. A summary of major results is as follows:

1) Base pressure coefficient data from the X-15, the M2-F3, and the space shuttle vehicles indicate that to represent large-scale flight vehicles, Hoerner’s equation relating base pressure to three-dimensional forebody drag requires a larger numerator coefficient than Hoerner used. A tentative range of values for the numerator coefficient is from 0.090 to 0.100, rather than Hoerner’s value of 0.029, which is based on small-scale model data.

2) Evidence exists that subsonic flow separating from a relatively large, sharp-edged three-dimensional base can exhibit quasi-two-dimensional characteristics and base pressure coefficients.

3) The nature of the Hoerner base-pressure-to-forebody-drag relationship (regardless of whether the three-dimensional or two-dimensional equation is used, or the numerator coefficient value) causes base drag and forebody drag to combine in a counterintuitive way to form an optimal minimum drag (a drag bucket) over a small range of forebody drag. The magnitude of forebody drag coefficient that defines the bucket depends primarily on the ratio of base area to wetted area of the respective vehicle. This means that a vehicle having a large base-area-to-wetted-area ratio and attached upper surface flow may benefit from surface roughness drag (such as that associated with a thermal protection system) at low lifting conditions; this combination of features may provide some favorable compensation for low-fineness-ratio vehicles having a relatively large base.

4) Minimum equivalent parasite drag area values for the vehicles range from 6.5 to 164.0 \(\text{ft}^2\). Division of equivalent drag area by the associated wetted area provided equivalent parasite skin-friction coefficients, ranging from approximately 0.009 to 0.020 (these coefficients include base drag). These minimum equivalent skin-friction values (for retracted landing gear) range from four to slightly more than eight times the skin-friction drag for the attached, turbulent boundary layer alone.

5) Little order existed to the lift-curve slope data when lift coefficient was based on the reference areas used in the reports from which the data were obtained. Application of more representative reference areas (for five of the seven vehicles) and adjustment of the lift-curve slopes for compressibility provided improved order to the data. These data demonstrate that the choice of a physically meaningful (representative) reference area is of major importance.

6) The lift-curve slopes of the five lifting bodies obtained at full scale during trimmed flight form a crude band arrayed approximately 12 to 15% below untrimmed generic elliptical cone small-scale model results.

7) The chosen definition for a physically meaningful reference area for lift parameters of a lifting body should include all of the planform area projected onto the longitudinal–lateral plane, including the projected area of cantilever tip or side fins. For wing-body combinations, the fuselage forebody is considered to perform as a lifting body. Therefore, the chosen reference area for these configurations includes the projection of all planform area ahead of the wing trailing edge (that is, forebody plus wing). This concept, which rejects projected body planform area aft of the wing trailing edge, is supported by fuselage pressure distribution measurements from the X-1 research airplane.

8) The M2-F2 data demonstrate that the lift-curve slope of very low-aspect-ratio lifting bodies can exceed the lift-curve slope values represented by the relationships of Jones or Helmbold for aspect ratios less than approximately one. The M2-F2 results are not believed to be an anomaly, because they are afforded credence by generic model results, generic leading-edge vortex lift data from highly swept wings, and crossflow (drag) lift data from bodies of revolution.
9) Excepting the M2-F1 and the HL-10 vehicles, the remaining five vehicles form an array (a band of the maximum lift-to-drag ratio over a range of the wetted aspect ratio) that should be a useful reference source with which to relate future reentry-type vehicles or reusable launch vehicles. A fairing through this band of data indicates that the maximum lift-to-drag ratio for this class of vehicles, in which the lifting-efficiency factor is limited to 0.6, is approximately 55% of those for nominally clean vehicles without truncated bodies for a given wetted aspect ratio.

References


P. Huseman
Associate Editor