Effects of Unsteadiness Due to Wake Passing on Rotor Blade Heat Transfer

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Abstract

In a gas turbine engine, the turbine rotor blades are buffeted by the wakes of the vanes located upstream. There is a transient effect from the passing of wakes on the blade heat transfer. This transient effect has been computed for a representative rotor by introducing a wake upstream via an unsteady inlet flow boundary condition, or “gust” condition. Two cases of turbulent flow and laminar flow with Reynolds numbers of 385,000 and 385 respectively were considered. For the turbulent flow case a quasi-steady calculation was also performed. The variation in the unsteady heat transfer coefficient was found to be as high as 120 percent of the mean. For the turbulent flow case a quasi-steady calculation was also performed. The time mean of the unsteady heat transfer, the mean of the quasi-steady variations and the steady results agree reasonably well on all blade locations except for the turbulent results which differ near the leading edge. The quasi-steady heat transfer results do not agree with the instantaneous unsteady results, although the time-mean values are similar.

Nomenclature

\begin{align*}
C & \quad \text{axial chord length} \\
h & \quad \text{wall heat flux (Tw-Tt)} \\
k_w & \quad \text{fluid conductivity at the wall} \\
Nu & \quad \text{Nusselt number = } hC/k_w \\
p & \quad \text{static pressure} \\
p_0 & \quad \text{relative total inlet pressure} \\
Re & \quad \text{Reynolds number based on the inlet velocity and axial chord} \\
S & \quad \text{wetted surface distance measure from the geometric stagnation point negative on the pressure side and positive on the suction side} \\
T_t, T_w & \quad \text{inlet total temperature and wall temperature} \\
U & \quad \text{characteristic velocity, inlet axial velocity} \\
X & \quad \text{axial location} \\
\omega_r & \quad \text{reduced frequency = } \omega C/U
\end{align*}
I. Introduction

Turbine blades operate in an environment where the reduced frequency (\(\omega C/U\)) is outside of the small reduced frequency regime. The effect of the unsteadiness on the blade surface heat transfer and its significance is unclear. The effect of unsteady flow on heat transfer in other areas of turbine blades such as the blade tip and downstream of cooling holes are of interest. In the case of cooling holes, the time variation in discharge pressure forced by the passing of wakes causes the cooling stream to vary in time. The effect of this oscillation on the overall film-cooling effectiveness and the rate of heat transfer may be non-negligible and one which could be further investigated using unsteady CFD. The type of studies just described requires a three-dimensional unsteady calculation which our current work is planning to address. The work described herein is, however, limited to the surface heat transfer on a radial section of a blade subjected to wake induced buffeting, and is free from other complicating factors.

The effect of flow unsteadiness on heat transfer has been studied under laminar flow conditions for a cylinder in an oscillating stream. The conclusion is that the effect of periodic unsteadiness, under the conditions of reduced frequencies that are much smaller than unity, can be neglected, and instead replaced by quasi-steady results. Quasi-steady conditions are defined by Lighthill as the state of the boundary layer that is appropriate to steady flow at the instantaneous value of the free stream conditions at the edge of the boundary layer. In effect, if the unsteady acceleration of oscillations is small this method can be utilized for simplification. Under the conditions of quasi-steady flow, described by Lighthill (ref. 1), the boundary conditions imposed on the boundary layer are not time variant. We have interpreted the quasi-steady condition as the condition for which one can specify the locations of the wake at the inlet and then solve the steady problem under those conditions. It should however be noted, that freezing the inlet boundary condition (i.e., keeping the wake from moving) results in the wake approaching the blade at a different relative angle. It will be seen later that this boundary condition still results in an average heat transfer that is almost identical to the time mean heat transfer but with the instantaneous value quite different than the unsteady value.

The desire to obtain a complete unsteady flow and heat transfer solution in turbine blades is tempered by the enormity of the resources required. As the computational capabilities grow, obtaining unsteady solutions using turbulence closure models have become more realistic and indeed Unsteady Reynolds Averaged Navier-Stokes (URANS) solutions are becoming common. Two-dimensional solutions of unsteady rotor-stator interaction have been accomplished and such calculations have been used for clocking the blade rows (ref. 2) aimed at improving the efficiency of turbines. Unsteady RANS calculations including the rotor/stator interaction have also been performed to predict unsteady heat transfer on blades and vanes. Those would include the work of Rao et al. (ref. 3) who used a 2 to 3 vane to stator blade count and a 2–D code and the work of Michelassi et al. (ref. 4) who rescaled the blade to maintain a one to one ratio of the vane-blade count and used a 3–D methodology to calculate the blade heat transfer. Abhari et al. (ref. 5) used the code UNSFLO which uses a transformed Euler equation to accommodate the vane to blade count ratio. The aerodynamics of passing of the wakes and the unsteady effect they have on low pressure turbine blades is dealt with in detail in a review paper by Hodson and Howell (ref. 6). The main emphasis as related to low pressure blades is on the common problem of flow separation at condition of cruise speeds at high altitude. Under those conditions, the flow on the suction side of the rotor blade is laminar and prone to separation. The unsteady flow has the potential to be exploited to help energize the boundary layer and thus lessen the losses that would otherwise be produced by the separation. Heidmann performed an analysis (ref. 7) and Heidmann et al. performed an experiment (ref. 8) using unsteady wakes produced by a row of rotating rods passing over a downstream annular turbine blade cascade with showerhead film cooling. Unsteady cases were studied for a range of reduced frequencies as well as no-wake and quasi-steady wake cases. They found that increasing the frequency of rotation has a deteriorating effect on the effectiveness of film cooling. No heat transfer measurements were performed. In this paper we mainly address the issue of unsteady heat transfer on high pressure turbine blades. We will explore the suitability of quasi-steady calculations to replace the unsteady calculations as is at times done to reduce computational time.
II. Calculations

Three-dimensional, URANS calculations were performed to predict heat transfer rate on a rotor blade. The flow was solved in an annular section assuming a slip boundary condition on boundaries possessing normals in the radial direction. Our simulation included a one to one and a two to one vane blade ratio with a gust type boundary condition at the inlet. The guide vane flow was calculated using the same code but in steady mode. The total pressure in the wake thus produced was fitted with a trigonometric function and placed as the boundary condition at the inlet of the rotor. The blade was rotating at 8400 rpm. There were 46 vanes and 76 blades (0.6 ratio). For the calculations presented here a one to one ratio was used. A one to two vane to blade ratio would be more accurate, but would double the computational cost and was not attempted. To study the effect of the one to one assumption, we doubled the frequency while holding the wake size the same to investigate the effect of frequency. The frequency of the wake thus produced is even higher than the actual configuration but was done to provide insight into the effect of frequency.

The computer code used for this study was the Glenn-HT2000 (Steinthorsson (ref. 7)). This computer code was written using object oriented programming principles and the Fortran90 programming language. The numerical procedure uses a finite-volume discretization scheme that is second order accurate in time and space. The computer program uses the MPI (Message Passing Interface) parallel processing. The cases were run on 20 processors of a 98 processor Xeon Linux Cluster. The turbulence model used for the calculations was the Low Reynolds number k-ω model of Wilcox integrating to the walls. The grid used was quite fine adjacent to the blade (y+=1), in the boundary layer and in the free stream. The turbulence model is able to produce an effect similar to the transition from laminar to turbulent flow. In practice however, the transition is not guaranteed to be in the appropriate location. In fact, it is often triggered very near the leading edge which is what occurred in our computations making them fully turbulent except near the leading edge. The following was investigated:

1. Unsteady effect of the passing wake on the rotor blade row downstream for a laminar and two turbulent cases at 0.44 and 0.88 reduced frequency. Unsteady and time average.
2. Steady calculation particular to the average inlet condition of the unsteady case.
3. Quasi-steady flow calculations and determination of the ensemble average of the blade heat transfer.
4. Laminar flow calculation of heat transfer over the blade.

The quasi-steady case was performed as a series of 32 steady calculations with the wake profile specified at equally-spaced intervals across the inlet. This was done to determine if the motion of the wake passing is important relative to the simple presence of the wake. In effect, the quasi-steady case is equivalent to the limiting case of zero reduced frequency.

The unsteady solution process was started from a converged steady initial solution and continued for several cycles until a transient periodic solution to the blade heat transfer was achieved. The final time step was chosen by progressively reducing the time step until there was little change in the unsteady results. The convergence efficiency was also considered and it was then decided to cover each period by 640 time steps.

The particular geometry considered for this case was the blade geometry and flow conditions of the GE-E3 (ref. 10). A simplified case and a full three-dimensional geometry were considered. The three-dimensional calculations are still in progress and will be presented elsewhere. The simplified geometry was a thin ‘sliver’ of the blade for which slip boundary conditions in the upper and lower radial boundaries were specified. There were four grid intervals in the radial direction and the blade-to-blade grid was constructed as shown in figure 1. The grid was refined to resolve the passing of the wake. A coarse grid does not support the wake and the wake dissipates quickly. The simplified case was set to rotate about the rotation axis and was also subjected to a gust type boundary condition upstream. This case was used to investigate the effects described above. The blade row pressure ratio was 0.44 and rotation rate was 8400 rpm. The case was scaled to give a Reynolds number based on the axial chord and inlet velocity of 385,000 for the turbulent flow cases. The Reynolds number for the laminar flow case was 385. The inlet gust boundary condition was specified such that it has a 15 percent total pressure deficit. It has a background turbulence intensity of 2 percent and reaches an intensity of 3.5 percent in the wake. These values were arrived at after the flow through the vane row upstream was calculated independently.
Figure 1.—Blade profile and the grid in a radial plane.

Results

Figure 2, shows the time variation in the local static pressure on the blade surface. This variation in the surface pressure would have repercussions if film cooling were performed on the blade. In fact, it would have resulted in a pulsation of the film-cooling flow. In the figure, in addition to the time average of the pressure we are showing the pressure distribution resulting from a steady calculation. The difference in the steady solution and the time dependent solutions with the wake is obvious. The difference is attributable to the difference in the incidence angle which would be less steep, on the average, due to the presence of the wake. In other words, because we hold the absolute angle as fixed, the reduced velocity in the wake produces a reduced relative angle of attack. This is an important point to consider when running a CFD code for a rotor in steady mode.

Figure 3 shows the unsteady heat transfer under laminar flow conditions. The time averaged values and steady results are also shown in that figure. Those differences are quite small. As the flow is purely laminar, the unsteady variation in heat transfer has to be due to flow acceleration. The correlation coefficient between the unsteady components of shear and Nusselt number was computed and was found to have a value near unity. The correlation was computed taking into account all the points on the blade surface over a complete period. The interpretation is that the heat transfer increase/reduction is due to flow acceleration/deceleration under low Reynolds number conditions. The
good correlation suggests that there is not a large lag between these two effects in laminar flow situations. Figure 4 is a plot of Nusselt number for turbulent flow over the rotor blade, the difference between the average of unsteady calculations over a period and steady calculations does not appear to be large except near the leading edge. This may be due to the differences in the incidence angle or the unsteady transition effect or both. An analysis of the unsteady components of shear and Nusselt number yielded a small correlation coefficient. This assertion can be verified by noting that the mean heat transfer and steady value are matched near the leading edge for the laminar flow case. The effect was explained by Dullenkopf and Mayle (ref. 11) who also proposed a transition model which help predict the time average heat transfer on the blade. This model was used in a calculation of heat transfer over a rotor blade. (Ameri and Arnone (ref. 12)). The real effect is not fully apparent here since the model utilized in this work does not include a physically based bypass transition model. In many instances, such as instances in which there is film cooling near the leading edge, or large enough adverse pressure gradient, transition does occur early. The relative magnitude of the envelope obtained for the laminar and the turbulent flow calculations in figures 3 and 4 is shown in figure 5. The figure shows that the unsteady variation around the mean can be as large as 110 percent of the mean. It is interesting that the unsteady variation experiences a precipitous drop once it gets to the uncovered portion of the blade.

In figure 6 the vector plots correspond to the unsteadiness (instantaneous—time mean) at two different phases of the periodic unsteady wake passing for the turbulent flow computations. The shaded background is the entropy rise. The lighter areas correspond to the wake locations.
Figure 7 shows the unsteady heat transfer for the same flow as in figure 4 except that the wakes occur twice as often. The motivation for this exercise was explained earlier. The figure shows that the size of the unsteady heat transfer envelope has been reduced considerably compared to figure 4. As the case in figure 4 was run with a one to one ratio of vanes to blades (itself too fast by a factor of 1.6), it may therefore be concluded that running with the proper ratio of vanes to blades would likely result in even a larger unsteady heat transfer envelope.

**Quasi-Steady Results**

There have been instances in which workers have used the quasi-steady conditions to simulate unsteady conditions. As Lighthill (ref. 1) points out this condition would be a good substitute for the unsteady case as long as the reduced frequency is small. In order to obtain quasi-steady solutions the wake was moved on a number of locations, of equal spacing, along the inlet boundary and corresponding steady solutions was obtained for those locations. The solution envelopes and the average values are also shown in figure 8. It is observed that the envelope of the unsteady heat transfer (for the lower frequency), in figure 4, is much wider than that of the quasi-steady solution on the suction side. The opposite is observed on the pressure side. The average however, is very close to the average heat transfer obtained for unsteady flow. The difference points to the fact that the quasi-steady solution cannot replace the unsteady solution. But, it is interesting that the cases so far in this work show that either the quasi-steady mean or the steady value can be substituted for the time-mean value. This is especially true on the suction side. On the pressure side, some differences do exist but, the differences may be too small. The one location where the differences appear to exist and could be significant is near the leading edge of the blade. Both the quasi-steady average and steady values are significantly different than average. Figure 9 is the quasi-steady counterpart to figure 6.
Figure 8.—Quasi-Steady flow, Nusselt number versus surface wetted distance.

Figure 9.—View of deviation of the velocity vector from the mean for a quasi-steady frame, $Re = 385,000$. 
Figure 10 shows the phase variation of Nusselt number for the two blade count ratios considered and the quasi-steady solution at those phases for a location one chord length downstream of the leading edge on the suction side of the blade. The figure shows that the quasi-steady values should not be used in place of unsteady values.

Conclusions

In this paper the effect of unsteady wake in a simplified model of the rotor/stator interaction was considered. The wake was modeled after the vane flow was independently simulated. The results are limited to larger reduced frequencies as compared to those that occurred in the real situation because only one blade periodic case was simulated. Two frequencies were considered. It was found that:

1. The steady heat transfer results are good representation of the mean heat transfer for a clean blade (no film cooling and 2-D flow) for all the cases considered.
2. An average computed from a quasi-steady flow is also a good substitute for time average Nusselt number.
3. The quasi-steady value is not a good representation of the heat transfer on the blade for the unsteady values and in fact the envelopes are substantially different.
4. An increase in “reduced frequency” of wake passing from 0.44 to 0.88 (doubling) resulted in a substantial shrinking of the unsteady heat transfer envelope.

References

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