NONLINEAR AEROELASTIC ANALYSIS USING A TIME-ACCURATE NAVIER-STOKES EQUATIONS SOLVER

Geojoe Kuruvila¹, Robert E. Bartels², Moeljo S. Hong³, and Kumar G. Bhatia⁴

¹Flight Sciences Technology, The Boeing Company
5301 Bolsa Avenue, MC H013-B308, Huntington Beach, CA 92646, USA
e-mail: geojoe.kuruvila@boeing.com

²Aeroelasticity Branch, NASA Langley Research Center
MS 340, Hampton, VA 23681, USA
e-mail: r.e.bartels@larc.nasa.gov

³Enabling Technology and Research, The Boeing Company
PO Box 3707, MC 67-LF, Seattle, WA 98124, USA
e-mail: moeljo.hong@boeing.com

⁴Aeroelasticity and Multidisciplinary Optimization, The Boeing Company
PO Box 3707, MC 03-KR, Seattle, WA 98124, USA
e-mail: kumar.g.bhatia@boeing.com

Keywords: Nonlinear Aeroelasticity, Limit Cycle Oscillation, Control Surface Freeplay, Computational Fluid Dynamics.

Abstract. A method to simulate limit cycle oscillation (LCO) due to control surface freeplay using a modified CFL3D, a time-accurate Navier-Stokes computational fluid dynamics (CFD) analysis code with structural modeling capability, is presented. This approach can be used to analyze aeroelastic response of aircraft with structural behavior characterized by nonlinearity in the force verses displacement curve. A limited validation of the method, using very low Mach number experimental data for a three-degrees-of-freedom (pitch/plunge/flap deflection) airfoil model with flap freeplay, is also presented.

1 INTRODUCTION

Classical aeroelastic analysis methods assume linear aerodynamic and structural behavior. While these methods have been quite successful in predicting aeroelastic phenomenon such as flutter, their limitations are also well known. They fail to predict instabilities caused by nonlinearities in the aeroelastic system. In the past two decades considerable experimental and analytical efforts have been devoted to understand nonlinear aeroelasticity. However, accurate prediction of instabilities such as LCO, transonic flutter, and buzz remains a challenge [1]. It is widely believed that these instabilities are caused by nonlinearities in the fluid, or the structure, or both. LCO, for example, is thought to be caused by nonlinear flow due to large shock motion or flow separation, or structural nonlinearities arising from freeplay in hinges and linkages of control surfaces or material behavior [2]. Aging aircraft and combat aircraft carrying heavy external stores are known to experience LCO, typically due to structural nonlinearities. Aerodynamic nonlinearities can be modeled using Navier-Stokes equations for flow simulation. For complex structures like that of an aircraft, it is virtually impossible to determine the sources of all structural nonlinearities. Generally a particular source of nonlinearity, such as control surface freeplay, is explicitly modeled as part of the fluid-structure interaction problem in order to predict system instabilities.
About a decade ago, a study of LCO due to control surface freeplay was conducted by Conner, Tang, Dowell, and Virgin using a three-degrees-of-freedom aeroelastic wing model with piecewise linear flap stiffness [3, 4]. The study included testing in the Duke University low-speed wind tunnel and numerical simulations. A system of piecewise linear state-space models was used for the numerical simulations. The equations of motion were integrated in time using a Runge-Kutta algorithm in conjunction with Hénon’s method to locate the “switching points” in the flap stiffness as it changed from one state to another. Later, Tang, et al. [5] and Gordon [6] successfully used the describing function approach to model this nonlinear problem. To model the aero-structure interaction, Conner and Gordon used linear potential flow theory based Theodorsen’s method while Tang used Peters’ method. The results of their low Mach number (0.02 < \(M_\infty\) < 0.07) simulations correlated reasonably well with experimental data.

The present study explores the feasibility of using a nonlinear aero-structure interaction code for simulating LCO due to control surface freeplay. Such a capability is necessary to understand this phenomenon particularly in the transonic regime where the aerodynamics is highly nonlinear. This paper describes a method where structural nonlinearity due to control surface freeplay is modeled in a nonlinear aerodynamics analysis code. This method has been implemented in CFL3D [7, 8], a time-marching Reynold’s Averaged Navier-Stokes code with linear structural modeling originally developed by NASA Langley Research Center. As a first step, validation of this method has been done using experimental data, from Conner, et al., for the three-degrees-of-freedom airfoil model with freeplay. Simulations of this model using Navier-Stokes and Euler equations and the comparisons of results with experimental data are also presented in this paper.

2 MODELING CONTROL SURFACE FREEPLAY

The standard CFL3D simulates aeroelastic phenomenon using the Euler or the Navier Stokes equations for modeling aerodynamics and a modal dynamic model for structure [7, 8]. The structural model is limited to simulating linear structural behavior. Modeling of structural nonlinearity characterized by piecewise linear stiffness variations, commonly seen in control surfaces with freeplay, is the focus of this study. An idealized behavior of a control surface with such a freeplay is shown schematically in Figure 1. Within a range of deflection angles \((-\delta_0 \leq \delta \leq \delta_0\)\) the control surface experiences no resistance to its movement. Outside this critical range it experiences a linear restoring torque.

![Figure 1: An idealized depiction of symmetric control surface freeplay](image-url)
The aeroelastic equations of motion for a linear structural model written in vector notation are shown in equation (1), where \( \mathbf{m} \), \( \mathbf{d} \), and \( \mathbf{k} \) are the mass, damping, and stiffness matrices, \( \mathbf{\delta} \) the physical displacements vector and \( \mathbf{f} \) the aerodynamic forces vector.

\[
\mathbf{m}\ddot{\mathbf{\delta}} + \mathbf{d}\dot{\mathbf{\delta}} + \mathbf{k}\mathbf{\delta} = \mathbf{f}
\]  

(1)

When some modes have freeplay like the one shown in Figure 1, equation (1) can be modified as,

\[
\mathbf{m}\ddot{\mathbf{\delta}} + \mathbf{d}\dot{\mathbf{\delta}} + \mathbf{k}\mathbf{\delta} + \mathbf{k}\hat{\mathbf{\delta}} = \mathbf{f}
\]  

(2)

where, for modes with freeplay, \( i \),

\[
\hat{\delta}_i = \begin{cases} 
-\delta_{0i}, & \delta_i > +\delta_{0i} \\
-\delta_j, & |\delta_j| \leq +\delta_{0i} \\
+\delta_{0i}, & \delta_i < -\delta_{0i} 
\end{cases}
\]  

(3)

and, for modes without freeplay, \( j \), \( \hat{\delta}_j = 0 \). Note that equation 3 can be easily modified to model asymmetric freeplay behavior.

In equation (2), the restoring torque due to freeplay is modeled as the sum of a linear term \( (k\delta) \) and a nonlinear residual term \( (k\hat{\delta}) \). This decomposition is shown graphically in Figure 2. After moving the residual term to the right hand side and performing modal transformation, equation (2) in generalized form is,

\[
\mathbf{M}\ddot{\mathbf{q}} + \mathbf{D}\dot{\mathbf{q}} + \mathbf{K}\mathbf{q} = \mathbf{F} - \mathbf{\phi}^T\mathbf{k}\hat{\mathbf{\delta}}
\]  

(4)

where, \( \mathbf{M} \), \( \mathbf{D} \), \( \mathbf{K} \), \( \mathbf{q} \), and \( \mathbf{F} \) are the generalized mass, damping, stiffness, displacements, and aerodynamic forces, respectively. They can be expressed as follows.

\[
\begin{align*}
\mathbf{M} &= \mathbf{\phi}^T\mathbf{m}\mathbf{\phi} \\
\mathbf{D} &= \mathbf{\phi}^T\mathbf{d}\mathbf{\phi} \\
\mathbf{K} &= \mathbf{\phi}^T\mathbf{k}\mathbf{\phi} \\
\mathbf{\delta} &= \mathbf{\phi}\mathbf{q} \\
\mathbf{F} &= \mathbf{\phi}^T\mathbf{f}
\end{align*}
\]  

(5)
where \( \phi \) are the eigenvectors of the system \( m\ddot{\delta} + k\delta = 0 \). \( \phi^T k \hat{\delta} \) are the generalized residual forces. In the absence of freeplay, these terms would be zero.

In CFL3D the modal equations of motion are cast in the state-space form and integrated in time. For simplicity, the off-diagonal terms in the damping matrix are assumed to be zero. It results in a 2x2 block diagonal system matrix that is easily integrated using the Laplace transform technique. For modeling freeplay, the residual terms due to nonlinearity in stiffness are added to the right-hand-side of the state-space equations. The left-hand-side remains the same and therefore the technique for integrating the state space equations remains unchanged.

### 3 METHOD VALIDATION MODEL

Data from experiments conducted by Conner are used to validate the formulation described above. A schematic of the model used is shown in Figure 3. It is a two-dimensional rectangular wing with a full-span trailing-edge flap. The wing airfoil cross-sections are NACA 0012 with the aft quarter of the airfoil forming the flap with the hinge at \( \frac{3}{4} \) chord location. The model has three-degrees-of-freedom, namely, pitch, plunge, and flap deflection. The pitch axis is at \( \frac{1}{4} \) chord location. The setup allowed the freeplay band to be an adjustable parameter. For completeness the parameters of the experimental model are given in Table 1.

![Figure 3: NACA 0012 three degrees-of-freedom freeplay simulation model](image)

The displacement vector for this model can be written as,

\[
\delta = \begin{bmatrix} h \\ \alpha \\ \beta \end{bmatrix}^T
\tag{6}
\]

where \( h \), \( \alpha \), and \( \beta \) are plunge, pitch, and flap deflection, respectively. The flap can be preset to have a desired freeplay zone of \( \pm \beta_0 \), i.e., between \( -\beta_0 \leq \beta \leq \beta_0 \) its stiffness is zero. The generalized residual term on the right hand side of equation (4) becomes

\[
\phi^T k \hat{\delta} = \phi^T k \begin{bmatrix} 0 \\ 0 \\ \hat{\beta} \end{bmatrix}^T
\tag{7}
\]

where \( \hat{\beta} \) is given by equation (3).
4 RESULTS

4.1 Characteristics of the linear system

From the mass, inertial, stiffness, and damping parameters of the experimental setup, given in Table 1, the coupled natural frequency of each degree-of-freedom is determined. Comparison of these results with those of Conner’s is shown in Table 2. The numerical results agree with one another. The plunge and pitch frequencies agree reasonably well with experiment. The flap frequency shows a 4% discrepancy with the experiment. Table 3 shows a similar comparison of linear flutter speed and frequency. Here the discrepancies with experiment are larger. CFL3D result shows the least difference. Reference 3 mentions degradation of the stiffness of the springs, especially the pitch-spring, due to fatigue. This could be a reason for the discrepancies.

Table 1: Parameters of the experimental model [3, 4, 5]

<table>
<thead>
<tr>
<th>Geometric parameters</th>
<th></th>
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<tbody>
<tr>
<td>Chord</td>
<td>0.254 m</td>
</tr>
<tr>
<td>Span</td>
<td>0.52 m</td>
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<tr>
<td>Semi-chord, b</td>
<td>0.127 m</td>
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<td>Elastic axis, a w/t/t b</td>
<td>-0.5</td>
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<tr>
<td>Hinge line, c w/t/t b</td>
<td>0.5</td>
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</table>

<table>
<thead>
<tr>
<th>Mass (inertial) parameters</th>
<th></th>
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</thead>
<tbody>
<tr>
<td>Mass of wing</td>
<td>0.62868 kg</td>
</tr>
<tr>
<td>Mass of aileron</td>
<td>0.18597 kg</td>
</tr>
<tr>
<td>Mass/length of wing-aileron</td>
<td>1.558 kg/m</td>
</tr>
<tr>
<td>Mass of support blocks</td>
<td>0.47485 x 2 kg</td>
</tr>
<tr>
<td>$S_a$ (per span)</td>
<td>0.08587 kg m</td>
</tr>
<tr>
<td>$S_\beta$ (per span)</td>
<td>0.00395 kg m</td>
</tr>
<tr>
<td>$I_a$ (per span)</td>
<td>0.01347 kg m²</td>
</tr>
<tr>
<td>$I_\beta$ (per span)</td>
<td>0.0003264 kg m²</td>
</tr>
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</table>

<table>
<thead>
<tr>
<th>Stiffness parameters</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$K_a$ (per span)</td>
<td>37.3 kg m²/s²</td>
</tr>
<tr>
<td>$K_\beta$ (per span)</td>
<td>3.9 kg m²/s²</td>
</tr>
<tr>
<td>$K_h$ (per span)</td>
<td>2818.4 kg/m²/s²</td>
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</table>

<table>
<thead>
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<th></th>
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</thead>
<tbody>
<tr>
<td>$\zeta_a$ (log-dec)</td>
<td>0.01626</td>
</tr>
<tr>
<td>$\zeta_\beta$ (log-dec)</td>
<td>0.0115</td>
</tr>
<tr>
<td>$\zeta_h$ (log-dec)</td>
<td>0.0113</td>
</tr>
</tbody>
</table>

$S_a, S_\beta$: Static moments of wing per unit length of wing-aileron (relative to $a$) and aileron (relative to $c$), respectively.

$I_a, I_\beta$: Moment of inertia per unit length of wing-aileron and aileron about $a$ and $c$, respectively.
4.2 Navier-Stokes solutions with freeplay using measured stiffness

Results of Navier-Stokes analyses with measured stiffness, for freeplay of ±2.12°, are shown here. A three-dimensional grid, but with only one cell across the span, is used for these simulations. The grid has 353x97 points in the streamwise and normal directions, respectively, with 255 points on the airfoil. The freestream velocity for these analyses varies between 7 and 23 meters per second. Sea-level conditions are assumed to determine the other flow parameters. The Reynolds number based on chord is 520,000. Note that at this Reynolds number, only about 60% of the airfoil is likely to have turbulent flow. However, fully-turbulent Navier-Stokes simulations using the Spalart-Allmaras turbulence model are conducted. Each analysis is run for 200,000 time steps with 10 sub-iterations. One time-step is equal to 0.1 millisecond, making each simulation 20 seconds long.

The overall comparisons of Navier-Stokes simulations with experimental results are shown in Figure 4. The scale, $U/U_f$ referred to as the speed-ratio, is the ratio of the flow speed to the linear flutter speed. During the experiment, as the speed was increased, five types of system behavior were observed. At first the initial perturbations damped out. Then, between speed-ratio of 0.23 and 0.37, the system displayed a simple low frequency behavior. From 0.37 to 0.48, the system lost periodicity. Between 0.48 and 0.55 the system became periodic again and the flap oscillated in a “complex” low frequency limit cycle. Beyond speed-ratio of 0.55, the system was abruptly attracted to a high frequency limit cycle. The speed ranges of these five types of behavior are indicated by the lower color bars in Figure 4.

The upper color bars indicate the system behavior simulated by CFL3D. Overall the stages described by the experiment are also seen in the CFD simulation. However, there is considerable discrepancy in speed ranges at which they occur. In these simulations the simple oscillations do not appear until the speed-ratio reaches 0.39. When it reaches 0.42, the

<table>
<thead>
<tr>
<th>Coupled Natural Frequency (Hz)</th>
<th>Experiment</th>
<th>Current Numerical</th>
<th>Conner’s Numerical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plunge</td>
<td>4.375</td>
<td>4.448 (1.7)</td>
<td>4.455 (1.8)</td>
</tr>
<tr>
<td>Pitch</td>
<td>9.125</td>
<td>9.197 (0.8)</td>
<td>9.218 (1.0)</td>
</tr>
<tr>
<td>Flap Deflection</td>
<td>18.625</td>
<td>19.387 (4.1)</td>
<td>19.442 (4.4)</td>
</tr>
</tbody>
</table>

Table 2: Natural frequencies of the linear system (% error relative to experiment in parenthesis)

<table>
<thead>
<tr>
<th>Linear Flutter</th>
<th>Experiment</th>
<th>CFL3D Navier-Stokes</th>
<th>Conner’s Numerical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Speed (m/s)</td>
<td>20.6</td>
<td>22.6 (9.9)</td>
<td>23.9 (16.0)</td>
</tr>
<tr>
<td>Frequency (Hz)</td>
<td>5.47</td>
<td>5.87 (7.3)</td>
<td>6.112 (11.7)</td>
</tr>
</tbody>
</table>

Table 3: Flutter speed and frequency of the linear system (% error relative to experiment in parenthesis)
Oscillations lose periodicity and remains in this state until it becomes 0.53 when the oscillations become periodic again and the flap moves in a “complex” low frequency limit cycle. At a speed-ratio of about 0.58 the system becomes non-periodic again until it reaches 0.63 when it begins to exhibit high frequency LCO. The non-periodic behavior, indicated by the orange bar, is not specifically mentioned in the description of the system behavior during the experiment.

The relative power spectral density for flap frequencies up to 20 Hz at different speed-ratios, shown in Figure 5, presents another view of the system behavior. At first the initial perturbations damp out (purple). Then, as the speed increases (0.39-42), frequencies between 4 and 5 Hz begin to dominate (blue). This results in the “simple periodic low frequency LCO.” At higher speeds (0.42-0.53), in addition to the 5 Hz, 10 Hz oscillations also begin to appear (green). It is weaker than the 5 Hz one, but gains strength as the speed increases. Together they produce a mildly non-periodic behavior. Between speed-ratios of 0.53 and 0.58 (yellow), the strengths of these frequencies stabilize and the oscillations become periodic again. The flap motion has the “complex” structure due to the presence of two dominant frequencies. Beyond 0.58 (orange), the 5 Hz mode loses strength rapidly while the 10 Hz mode gains strength. When the speed-ratio reaches 0.63 (red), the 5 Hz mode dies completely and only the 10 Hz mode remains resulting in the high frequency limit cycle. Beyond this, only one dominant mode exists and its frequency increases with speed. It reaches about 12 Hz near the linear-flutter speed. The power spectral density of plunge and pitch modes are relatively small compared to that of the flap oscillation mode.
For quantitative comparison of the CFL3D results with Conner’s results, time histories of displacements of the three modes are normalized as follows

\[ H(t) = \frac{h(t)}{h_b}, \]
\[ A(t) = \frac{\alpha(t)}{\beta_b}, \]
\[ B(t) = \frac{\beta(t)}{\beta_b} \]  

(8)

where \( h, \alpha, \) and \( \beta \) are the time histories of plunge, pitch, and flap displacements, respectively. \( H, A, \) and \( B \) are the corresponding non-dimensional displacements and \( b \) is the semi-chord. From the non-dimensional amplitudes and using the time step \( \Delta t \), the r.m.s. values are calculated as,

\[ \text{Amp}_{r.m.s} = \sqrt{\frac{1}{N\Delta t} \sum_{n=1}^{N} (\text{Amp}_n)^2 \Delta t} \]  

(9)

Comparisons of CFL3D Navier-Stokes solutions with Conner’s results are shown in Figures 6 and 7. His results include experimental data as well as results from numerical simulation. The aeroelastic model used in his numerical simulations is the linear potential equation based Theodorsen’s method. Two linear models based on this method are combined to capture the nonlinear (piecewise linear) nature of the freeplay. The numerical model appears to scale with the size of freeplay. Experimental data for three freeplay bands (\( \beta_0 = \pm2.12^\circ, \pm1.83^\circ, \) and \( \pm1.15^\circ \)) are presented. Note that there is significant scatter in the experimental data, especially at low speed-ratios where the LCO has multiple dominant frequencies.
Figures 6 and 7 show that, Conner’s results and CFD simulations have similar trends. However, their magnitudes have considerable discrepancies. Normalized r.m.s. amplitude of plunge at lower speed-ratios are closer to Conner’s numerical results than the experimental data. At higher speeds, there is generally better agreement with Conner’s results. For the pitch mode, CFL3D predicts the general trend but the discrepancy at higher speeds is large. Normalized r.m.s amplitude of the flap mode shows reasonable agreement, but at higher speeds the difference is large. The overall agreement of the flap LCO frequencies is reasonable. As mentioned before, at very low speed-ratios the CFL3D results do not show any LCO, while Connor’s experimental and numerical results show simple periodic LCO. The reasons for the discrepancies are not entirely clear. Unknown inconsistencies between experimental and CFD parameters could be one. Based on other simulations (presented below), there is indication that dissipation in flow modeling may also have a role in causing the deviation.

4.3 Euler solutions with freeplay using measured and adjusted stiffness

Results of simulation conducted to evaluate the sensitivity to fluid viscosity and structural stiffness are presented. In one set of numerical experiments the cases presented in section 4.2 are repeated using Euler analysis. In the next set, the cases are repeated with Euler analysis and adjusted stiffnesses. The stiffnesses are adjusted to match the measured coupled natural frequencies of the experimental setup. The presumption here is that the frequencies, in general, can be measured more accurately than stiffnesses. The values of measured and
adjusted reduced stiffnesses are shown in Table 4. Figures 8, 9 and 10 show the results of these analyses.

<table>
<thead>
<tr>
<th>Stiffness</th>
<th>Measured</th>
<th>Adjusted</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plunge (kg/m/s²)</td>
<td>2818.4</td>
<td>2252.9</td>
</tr>
<tr>
<td>Pitch (kg m/s²)</td>
<td>37.3</td>
<td>37.1</td>
</tr>
<tr>
<td>Flap (kg m/s²)</td>
<td>3.9</td>
<td>3.5</td>
</tr>
</tbody>
</table>

Table 4: Measured and adjusted stiffness

Figure 8: Comparison of normalized r.m.s. amplitudes of plunge and pitch modes

Figure 9: Comparison of normalized r.m.s. amplitude of flap deflection and dominant flap frequency

Figure 8 show that Euler analysis moves the results closer to the inviscid results of Connor’s. For the plunge mode, this shift further increases the discrepancy between experimental and CFD results. For the pitch mode, at higher speeds, the Euler results falls within the scatter of experimental data. For the flap mode (Figure 9), there are no major changes at the lower speeds. At higher speeds, the r.m.s. of the amplitudes are slightly lower than Navier-Stokes solutions. For plunge and pitch mode, the changes in results when using adjusted verses measured stiffness are less than the changes from Navier-Stokes to Euler solutions. For the flap mode, at the higher speeds, the changes in amplitude are relatively larger. The differences
in solutions (not shown) between Navier-Stokes solutions with measured and adjusted stiffness values are analogous to the difference between similar Euler solutions.

A summary of results of Navier-Stokes and Euler analyses, using measured and adjusted stiffnesses and their comparison with experiment are shown as histograms in Figure 10. A noticeable change when using Euler analysis is that LCO appears at lower speeds than in the case of Navier-Stokes solutions. Lower dissipation in the Euler formulation may be helping to capture LCO at the lower speeds. The regions with “simple periodic low frequency” LCO and “high frequency” LCO are wider than Navier Stokes results and the other regions are narrower. Adjusting stiffnesses to match the measured frequencies appear to marginally move the numerical results closer to the experimental data. Overall, it is not clear if switching to Euler solutions and/or using adjusted stiffness improved the correlation with experimental data.

![Oscillations lose periodicity](image)
![Complex periodic low frequency LCO](image)
![High frequency LCO](image)
![Simple periodic low frequency LCO](image)
![Transitioning to high frequency LCO](image)

Figure 10: Comparison between experiment, Navier-Stokes and Euler results

### 4.4 Sensitivity to width of freeplay band

Simulations with a freeplay band of $\pm 1.15^\circ$ are compared to those with freeplay of $\pm 2.12^\circ$ in Figures 11 and 12. Euler analyses with stiffness adjusted to match experimentally measured...
frequencies are used here. While Conner’s numerical results scale with the freeplay band, as defined by equation (8), CFL3D results do not. Also note that the experimental data do not scale well either.

4.5 Sensitivity to time-step size

Results of a time-step sensitivity study are shown in Figures 13 and 14. All the solutions presented earlier use a constant time-step of 0.1 millisecond. The flap deflection mode of the experimental setup has the highest coupled natural frequency and it is about 20Hz. In the CFD simulation, one cycle of the highest frequency is discretized into about 500 time intervals. In
this time-step study, selected cases are repeated with time-steps of 0.2, 0.5 and 1.0 millisecond, i.e., each cycle of the highest frequency is modeled with 250, 100, and 50 points. Figure 13 shows the responses of the flap mode undergoing “complex” periodic low frequency LCO. It can be seen that the amplitude and the phase are sensitive to time-step size. Figure 14 shows the changes in amplitudes of the three modes and that of the flap frequency. It also shows the percent change with respect to the solution with the smallest time-step size. As the time-step size increases, the plunge and pitch modes show large difference in amplitudes. The change in flap amplitude and frequency are relatively small. Similar sensitivities are observed at other flow speeds. A reason for this could be the accumulation of error in numerical integration caused by missing the “switching point” of the piecewise linear freeplay behavior. This is identified as a key issue by Conner who uses an adaptive time-stepping algorithm to accurately integrate to the corner of the two linear regions. However, from a CFD time-accuracy point of view, it is often necessary to use a time-step smaller than 0.1 millisecond, especially for complex configurations. So, special treatment to capture the switching-point may not be worthwhile.

5 CONCLUSIONS

A method to simulate LCO due to control surface freeplay has been formulated and implemented in CFL3D, a time-accurate Navier-Stokes code. This method can be used for simulation of LCO of complete aircraft that has freeplay in one or more control surfaces. A reasonable validation of the method has been accomplished using very low Mach number experimental data for a simple three-degrees-of freedom system. There is indication that excessive dissipation in the CFD method may be inhibiting LCO at the low end of the experimental speed range. Uncertainties in the measured stiffnesses and possibly the damping coefficients (not investigated here) may also be contributors to the discrepancies between simulation and experiment.

An adaptive time-stepping scheme to integrate accurately to the “switching point” is not helpful here as very small time-steps are needed for time-accuracy of the aerodynamic solution. While the small time-step requirement is not a major constraint for this 2-dimensional problem, it can be an impediment to analyzing complete aircraft configurations. Finally, the grid perturbation scheme in CFL3D worked flawlessly for this geometrically simple problem. However for complex 3-dimensional configurations, robust grid perturbation remains a challenge. Further analyses using aircraft configuration at transonic Mach numbers need to be performed to fully evaluate this approach for use in industrial applications.
6 ACKNOWLEDGMENT
The first author would like to thank James T. Gordon of Boeing Commercial Airplanes for the discussions on this topic.

7 REFERENCES


