In-Trail Procedure (ITP) Algorithm Design

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In-Trail Procedure (ITP) Algorithm Design

Cesar A. Munoz and Radu I. Siminiceanu
National Institute of Aerospace (NIA), Hampton, Virginia
IN-TRAIL PROCEDURE (ITP) ALGORITHM DESIGN

César A. Muñoz and Radu I. Siminiceanu †

ABSTRACT

The primary objective of this document is to provide a detailed description of the In-Trail Procedure (ITP) algorithm, which is part of the Airborne Traffic Situational Awareness – In-Trail Procedure (ATSA-ITP) application. To this end, the document presents a high level description of the ITP Algorithm and a prototype implementation of this algorithm in the programming language C.

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1 INTRODUCTION

The In-Trail Procedure (ITP) algorithm is an airborne software module of the Airborne Traffic Situational Awareness – In-Trail Procedure (ATSA-ITP) application in non-radar airspace. This software module is responsible for computing the flight deck information needed by the crew to determine whether the criteria required for an ITP procedure are met or not. This information is processed by a host application that decides how and when it is displayed to the crew.

This document is organized as follows. Section 2 presents a list of definitions that are relevant to the ITP algorithm. Section 3 gives a high level description of the algorithm that includes assumptions, configurable parameters, input and output data, and functional behavior. Finally, a prototype implementation of the algorithm is described in Section 4. Appendix A lists the complete code of the prototype implementation. Appendix B includes auxiliary functions from Williams’ Aviation Formulary [3].

2 DEFINITIONS

The following is a list of definitions, based on the list provided in [2], that are relevant to the description of the ITP algorithm.

• Altitude. “The vertical distance of a level, a point or an object considered as a point, measured from mean sea level (Doc 4444 - PANS-ATM chapter 1).” [2].

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• **Flight Level.** “A surface of constant atmospheric pressure which is related to a specific pressure datum, and is separated from other such surfaces by specific pressure intervals (Doc 4444 - PANS-ATM chapter 1).” [2]. On a day with standard atmospheric pressure (defined in the 1976 US Standard Atmosphere as 29.92 inches of mercury), a flight level of 310 would correspond to an altitude of 31,000 feet mean sea level. Flight levels are always in increments of 1,000 feet.

• **Flight Level Dead Band.** Maximum altitude deviation beyond which an aircraft is not considered to be in a flight level.

• **Ground Speed Differential.** “The speed difference over the ground between the ITP Aircraft and the Potentially Blocking Aircraft along each aircraft’s track. This measurement would use a technique similar to the Doc 4444 - PANS-ATM longitudinal separation procedure using DME (Doc 4444 - PANS-ATM section 5.4.2.3) to determine the Ground Speed Differential. A Positive Ground Speed Differential signifies that the ITP Aircraft and the Reference Aircraft are closing on each other (the separation is being reduced).” [2].

• **Initial Flight Level.** “The flight level of the ITP Aircraft when it determines a climb or descent is desired and before it begins the climb or descent.” [2].

• **In Trail Procedure.** “A procedure employed by an aircraft that desires to change its flight level to a new flight level by climbing or descending in front or behind one, or between two Same Track, Potentially Blocking Aircraft which are at an Intervening Flight Level and which are at less than the standard longitudinal separation minimum.” [2].

• **ITP Aircraft.** “An aircraft that is fully qualified (from an equipment, operator, and flight crew qualification standpoint) to conduct an ITP and whose flight crew is considering a change of flight level.” [2]. For the ITP algorithm, the ITP Aircraft is assumed not to be maneuvering.

• **ITP Maximum Range.** Maximum horizontal range relative to ownship for any aircraft to be included in the traffic list.

• **Maneuvering Aircraft.** Nearby Aircraft whose altitude is between the ITP Aircraft’s initial flight level and the Requested Flight Level, but off the altitude dead bands.

• **Nearby Aircraft.** Aircraft within ITP Maximum Range that are flying in the Same Vicinity, in the Same or Opposite Direction (only aircraft flying in a Cross Direction are excluded).

• **Nearest Aircraft.** At most two Potentially Blocking Aircraft that are closest to the ITP Aircraft. For the ITP algorithm, if the two nearest aircraft are flying in the same direction and at the same flight level, only the closest aircraft is considered to be a nearest aircraft.

• **Opposite Direction.** Aircraft are flying in Opposite Direction if their relative bearing is between 135 degrees and 225 degrees.
• **Positive Mach Difference.** “The difference in Mach between the ITP Aircraft and the Reference Aircraft that would result in the aircraft closing on each other (the separation is being reduced).” [2].

• **Potentially Blocking Aircraft.** “Aircraft flying in the Same Direction at an Intervening Flight Level whose ADS-B report data are available to the ITP Aircraft.” [2]. For the ITP algorithm, aircraft data of a Potentially Blocking Aircraft may not be qualified.

• **Qualified ADS-B.** “Automatic Dependent Surveillance-Broadcast (ADS-B) that meets the accuracy and integrity requirements determined to be required for the ITP.” [2].

• **Reference Aircraft.** “One or two Potentially Blocking Aircraft that meet the ITP criteria and that will be identified to ATC by the ITP Aircraft as part of the ITP clearance request.” [2]. For the ITP algorithm, the data quality of a Reference Aircraft must be qualified for ITP. Furthermore, a Reference Aircraft is not maneuvering and is either the closest ahead or the closest behind Potentially Blocking Aircraft.

• **Requested Flight Level.** “One same direction flight level above (for a climb) or below (for a descent) the Intervening Flight Level, appropriate for the operational region. A requested flight level may be:

  a. 2,000 feet above or below the initial flight level in RVSM airspace with single-direction tracks.

  b. 4,000 feet above or below the initial flight level in non-RVSM airspace with single-direction tracks.

  c. 4,000 feet above or below the initial flight level in RVSM airspace with bi-directional tracks with opposite direction traffic at alternating flight levels.” [2].

• **Same Direction.** Aircraft are flying in the Same Direction if their relative bearing is within ±45 degrees.

• **Same Vicinity.** Aircraft are located in the Same Vicinity, if their lateral offset is less than a Maximum Lateral Offset.

• **Same Track.** “Same direction tracks and intersecting tracks or portions thereof, the angular difference of which is less than 45 degrees or more than 315 degrees, and whose protection areas overlap (i.e., without lateral separation). (Doc 4444 - PANS-ATM section 5.4.2.1.5). These tracks may be a portion of a user preferred route or may be published routes, either fixed or flexible.” [2]. Since the information necessary to compute the same track criterion is not available to the aircraft, the ITP algorithm uses instead the more general concept of Same Direction, Same Vicinity.

• **Track.** “The position on the earth’s surface of the path of an aircraft, the direction of which path at any point is usually expressed as degrees from North (Doc 4444 - PANS-ATM Chapter 1).” [2].
• **Vertical Speed Dead Band.** Maximum vertical speed deviation beyond which an aircraft is considered to be maneuvering.

3 **HIGH LEVEL DESCRIPTION**

The main function of the ITP algorithm is called `itpAlgorithm`. This function is expected to run at a higher frequency than the traffic aircraft information is received. Hence, `itpAlgorithm` assumes that the input data have been coasted and that error-checking has been performed prior to its execution. More precisely, we assume:

• The position of each aircraft is projected to current time from the last state vector and elapsed time. The error between the real position and the projected one is bounded by the maximum cruise speed multiplied by the frequency of the algorithm.

• Traffic input data have an indication of their quality. The value `itpQualified` indicates that the aircraft is equipped with an ADS-B that meets the accuracy and integrity required to perform an ITP. In any other case, including the case of aircraft only equipped with TCAS, this value is set to `itpNonQualified`. Aircraft data that is `itpQualified` may be used for the computation of potentially blocking and reference aircraft. Aircraft data that is `itpNonQualified` may only be used for the computation of potentially blocking aircraft. In any case, for the purpose of the calculations, the data is supposed to be correct.

• The ADS-B reception range is much larger than the separation standards.

3.1 **Run-time Configurable Parameters**

The run-time configurable parameters of `itpAlgorithm` are depicted in Figure 1. A data structure `itpGlobalParameters` includes the following parameters:

![itpGlobalParameters](image)

**Figure 1: Run-time configurable parameters of ITP algorithm**

• **F1Deadband.** Value of *Flight Level Dead Band* in hundreds of feet. The default value is 1.
• **VsDeadband.** Value of *Vertical Speed Dead Band* in feet per minute. The default value is 300.

• **MaxRange.** Value of *ITP Maximum Range* in nautical miles. Currently, the default value of this parameter is set to 160 (see below).

• **MaxLateralOffset.** Maximum lateral offset, in nautical miles, used for the definition of *Same Vicinity*.
Since the official Lateral Separation is defined by the current Flight Information Region (FIR) where the aircraft is located and since this information may not be available to the crew, further analysis is needed to determine an appropriate value.

• **Range1** and **Range2.** The values of the distance parameters used in determining the ITP initiation criteria, in nautical miles.
The default values are set to 15 and 20 nautical miles, respectively.

• **GsDiff1** and **GsDiff2.** The values of the ground speed differential parameters used in determining the ITP initiation criteria, in knots.
The default values are set to 20 and 30 knots, respectively.

The **itpMaxRange** configurable parameter is the maximum range, in nautical miles, beyond which requesting an ITP would not make sense. It is calculated using the Mach number technique chart for a distance to fly between 1 and 600 nautical miles (in most cases the distance between two consecutive way points should not exceed 600 nautical miles) and a Mach difference of 0.03 (as specified for reference aircraft in [2]). In this case, the chart gives an additional 3 minutes separation at common point to ensure at least minimum separation at exit point. Therefore, a 15 minutes required separation at exit point (NATOTS uses 10 minutes but 15 minutes may be used in some airspaces [1]) amounts to a 18 minutes separation at common point. Assuming a maximum cruising speed of Mach 0.87 (based on NATOTS data – see [2]) and a 29000 feet altitude (which is the lowest NATOTS altitude [1]), the maximum cruising speed is 514.93 knots (no wind is assumed). This yields a maximum separation for an ITP of $514.93 \times \frac{18}{60} \approx 154.48$ nautical miles, which is rounded up to 160 nautical miles.

There are also two **non**-run-time configurable parameters:

• **ITP_MAX_TRAFFIC.** Maximum size of traffic aircraft list. This limit is imposed by the design of the avionics system. Currently, this parameter is set to 159, as actual systems allow storage of data for up to 128 traffic aircraft equipped with ADS-B and up to 31 traffic aircraft equipped with TCAS only (aircraft that have both ADS-B and TCAS count only as ADS-B.)

• **ITP_MAX_REFERENCE.** Maximum number of aircraft that may meet the definition of *Reference Aircraft*. Currently, this parameter is set to 2, corresponding to the nearest potentially blocking aircraft in front and behind ownship, if either of those exist. This setting corresponds to the case of a single Intervening Flight Level. The subsequent use of this algorithm for multiple Intervening Flight Levels would require the adjustment of this parameter according to the corresponding concept of operations.
3.2 Data Flow

Figure 2 presents a data flow chart of \texttt{itpAlgorithm}.

3.2.1 Inputs

The function \texttt{itpAlgorithm} gets as inputs a structure \texttt{itpInputs} consisting of:

- \texttt{ownership}. Data of ownership aircraft, of type \texttt{itpAircraft}. This aircraft should meet the definition of \textit{ITP Aircraft}.

- \texttt{traffic}. A list of coasted and error-checked traffic aircraft data. The maximum length of this list is given by the non-configurable parameter \texttt{ITP\_MAX\_TRAFFIC}. The elements of this list are also of type \texttt{itpAircraft}.

- \texttt{requested\_fl}. The requested cruise flight level (in hundreds of feet).

The \texttt{itpAircraft} data structure consists of

- a unique \textit{flight identifier} (\texttt{id}), of type \texttt{itpIdentifier} (strings of up to 255 characters),
- \textit{latitude} (\texttt{lat}), in degrees, in the interval \([-90^\circ, 90^\circ]\),
- \textit{longitude} (\texttt{lon}), in degrees, in the interval \([-180^\circ, 180^\circ]\) – excluding \(180^\circ\); by convention East longitudes are positive,
• **altitude** *(alt)* at standard barometric pressure, in hundreds of feet,
• **ground speed** *(gs)*, in knots,
• **vertical speed** *(vs)*, in feet per minute,
• **ground track** *(trk)*, in degrees from true north, in the interval \([0, 360)\) – excluding 360°, and
• **data quality flag** *(qlty)*, which is either itpQualified or itpNonQualified.

### 3.2.2 Outputs

The function **itpAlgorithm** outputs a data structure **itpOutput** that consists of a number of lists of **itpTraffic** elements:

- **traffic**: a list of all aircraft that are within the **itpMaxRange**.
- **nearby**: a list of indices to **traffic** of all aircraft that meet the definition of *Nearby Aircraft*.
- **pblocking**: a list of indices to **traffic** of all aircraft that meet the definition of *Potentially Blocking Aircraft*. The maximum length of this list is given by the non-configurable parameter **ITP_MAX_TRAFFIC**.
- **nearest**: a list of indices to **traffic** of all aircraft that meet the definition of *Nearest Aircraft*.
- **reference**: a list of indices to **traffic** of aircraft that meet the definition of *Reference Aircraft*. The maximum length of this list is also **ITP_MAX_REFERENCE**.
- **maneuver**: the type of In-Trail Procedure that is available, one of: {**itpNone**, **itpFollowingClimb**, **itpFollowingDescent**, **itpLeadingClimb**, **itpLeadingDescent**, **itpCombinedLeadingFollowingClimb**, **itpCombinedLeadingFollowingDescent**}.

The data structure **itpTraffic** consists of the following fields, which are computed by **itpAlgorithm**:

- **ITP range** *(range)*, in nautical miles: the relative distance to ITP aircraft with respect to a common point. A negative value means that the aircraft is behind the ITP aircraft. Conversely, a positive value means that the aircraft is ahead of the ITP aircraft.
- **ground speed differential** *(gsdiff)*, in knots: the relative ground speed differential to ITP aircraft. A negative value means that the aircraft is slower than the ITP aircraft. Conversely, a positive value means that the aircraft is faster than the ITP aircraft.
- **lateral offset** *(offset)*: traffic relative lateral offset to ownship, in nautical miles.
• **relative position** (*relpos*): traffic relative position to ownship, from the enumerated type `itpRelPos`: `{itpOwnBehindTraffic, itpOwnAheadTraffic, itpNoRelPos}`, where `itpOwnBehindTraffic` is assigned to traffic leading ownship, `itpOwnAheadTraffic` to traffic following ownship, and `itpNoRelPos` to traffic that is flying in a cross direction, i.e., traffic that is neither same direction nor opposite direction.

• **direction of flight** (*dir*), from the enumerated type `itpDirection`: `{itpSameDirection, itpOppositeDirection, itpCrossDirection}

• **traffic type** (*actype*), a numeric value that encodes the role of the traffic aircraft in the ITP and, when necessary, an ITP error code corresponding to this aircraft. This numerical code is computed by binary addition on the following constants (in hexadecimal):

  - `ITP_TRAFFIC` 0x0
  - `ITP_NEARBY` 0x1
  - `ITP_POTENTIALLY_BLOCKING` 0x2
  - `ITP_NEAREST` 0x4
  - `ITP_REFERENCE` 0x8
  - `ITP_BLOCKING` 0x10
  - `ITP_MANEUVERING` 0x20
  - `ITP_TOO_FAST` 0x40
  - `ITP_TOO_CLOSE` 0x80
  - `ITP_UNQUALIFIED_DATA` 0x100

For example, a nearby aircraft that is maneuvering has the associated *actype* value of 0x1 + 0x20 = 0x21 hexadecimal (that is 33 decimal value).

### 3.3 Control Flow

As illustrated in Figure 3, the function `itpAlgorithm` calls, in sequence, the following functions.

- **itpGetNearby**. This function computes the list *nearby*. If the list is empty the execution of `itpAlgorithm` ends.

- **itpGetPotentiallyBlocking**. This function computes the list *potentially_blocking*. If the list is empty, the execution of `itpAlgorithm` ends.

- **itpGetReference**. This function computes the list *reference*.

- **itpGetManeuver**. Given the list *reference*, this function computes the ITP maneuver that is available to the ITP aircraft (or `itpNone`).
Figure 3: Control flow chart of ITP algorithm

4 PROTOTYPE IMPLEMENTATION

A prototype implementation of the ITP Algorithm, written in the programming language C, is electronically available at http://research.nianet.org/~munoz/ITP_Module. The implementation consists of the following files:

- **ITP_Defs.h**, included in Appendix A.1, contains constant and type declarations.
- **ITP_Parameters.c**, included in Appendix A.2, contains the definition of configurable parameters and utility functions to read and modify their values.
- **ITP_Algorithm.h**, included in Appendix A.3, contains the program interface.
- **ITP_Algorithm.c**, included in Appendix A.4, contains the definition of the main functions.
- **ITP_Aviation.h** and **ITP_Aviation.c**, included in Appendix B, contain the implementation of auxiliary functions from Williams’ Aviation Formulary [3].

In the implementation, we use the following naming convention:

- Constants are written in uppercase letters and start with the prefix **ITP**.
- Global variables, types, and function names start with the prefix **itp**.

The actual In-Trail Procedure is implemented by the function **itpAlgorithm**, which has the following interface:
void itpAlgorithm(itpInputs, itpOutputs*);

The function `itpAlgorithm` has two parameters: an input parameter of type `itpInputs`, which is passed by value, and an output parameter of type `itpOutputs`, which is passed by reference. The exact definition of these types is found in the file `ITP_Defs.h`.

The configurable parameters of the algorithm are defined as global variables in the file `ITP_Parameters.c`. These variables are not intended to be directly read or modified by the user. For that reason, the following functions are provided in the interface:

```c
itpAltitude itpGetGlobalFlDeadband();
double   itpGetGlobalVsDeadband();
double   itpGetGlobalMaxRange();
double   itpGetGlobalMaxLateralOffset();
double   itpGetGlobalRange1();
double   itpGetGlobalGsDiff1();
double   itpGetGlobalRange2();
double   itpGetGlobalGsDiff2();
#endif
void itpSetGlobalFlDeadband(itpAltitude);
void itpSetGlobalVsDeadband(double);
void itpSetGlobalMaxRange(double);
void itpSetGlobalMaxLateralOffset(double);
void itpSetGlobalRange1(double);
void itpSetGlobalGsDiff1(double);
void itpSetGlobalRange2(double);
void itpSetGlobalGsDiff2(double);
void itpResetGlobalParameters();
```

As expected, functions with the prefix `itpGetGlobal` read the variables and functions with the prefix `itpSetGlobal` write them. The function `itpResetGlobalParameters` resets all the configurable global parameters to their default value.

Finally, the following functions are provided to check and decode the information returned by the ITP algorithm:

```c
itpBool itpIsClosing(itpTraffic trf);
itpBool itpIsNearby(itpTraffic trf);
itpBool itpIsPotentiallyBlocking(itpTraffic trf);
itpBool itpIsNearest(itpTraffic trf);
itpBool itpIsReference(itpTraffic trf);
itpBool itpIsBlocking(itpTraffic trf);
itpBool itpIsManeuvering(itpTraffic trf);
itpBool itpIsUnqualifiedData(itpTraffic trf);
itpBool itpIsTooClose(itpTraffic trf);
itpBool itpIsTooFast(itpTraffic trf);
```

10
void itpBlckCode2String(itpIdentifier s, itpTraffic trf);

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REFERENCES


A IMPLEMENTATION OF THE ITP ALGORITHM

A.1 Constant and Type Declaration

```c
/*======================================================
 * ITP algorithm constants and types
 * Author: Cesar A. Munoz (NIA)
 *        Radu I. Siminiceanu (NIA)
 *
 * File : ITP_Defs.h
 * Release: ITP_Module-6.d (10/11/06)
 * =======================================================*/

#ifndef ITP_DEFS
#define ITP_DEFS

/* General constants */
#define ITP_STR_LEN 255
#define ITP_VER "ITP_Module-6.d (10/11/06)"
#define ITP_INVALID_VALUE -999999
#define ITP_MAX_TRAFFIC 159
#define ITP_MAX_REFERENCE 2

/* Default parameter values */
#define ITP_FL_DEADBAND 1  /* 100ft */
#define ITP_VS_DEADBAND   300.0 /* ft/min */
```
#define ITP_MAX_RANGE 160.0 /* nmi */
#define ITP_MAX_LATERAL_OFFSET 15.0 /* nmi */

/* ITP initiation criteria constants */
#define ITP_RANGE_1 15.0 /* nmi */
#define ITP_GS_DIFF_1 20.0 /* knots */
#define ITP_RANGE_2 20.0 /* nmi */
#define ITP_GS_DIFF_2 30.0 /* knots */

/*-------------------------------------
Enumerated types
-------------------------------------*/
typedef enum {itpQualified, itpNonQualified} itpDataQuality;

typedef enum {itpNone,
             itpFollowingClimb, itpFollowingDescent,
             itpLeadingClimb, itpLeadingDescent,
             itpCombinedLeadingFollowingClimb,
             itpCombinedLeadingFollowingDescent
} itpDataQuality;

typedef enum {itpOwnBehindTraffic, itpOwnAheadTraffic,
             itpNoRelPos} itpRelPos;

typedef enum {itpSameDirection, itpOppositeDirection,
             itpCrossDirection} itpDirection;

/*-------------------------------------
Type of traffic aircraft
-------------------------------------*/
typedef unsigned int itpAcType;

/*-------------------------------------
Substitute types
-------------------------------------*/
typedef char itpIdentifier[ITP_STR_LEN];
typedef int itpAltitude; /* hundreds of feet */
typedef int itpBool;

#define ITP_FALSE 0
#define ITP_TRUE 1

/*-------------------------------------
Traffic/aircraft record
-------------------------------------*/
/**-------------------------------------*/
typedef struct {
    itpIdentifier id; /* flight identifier */
    double lat; /* latitude, in degrees: -90 ≤ lat ≤ 90 */
    double lon; /* longitude, in degrees: -180 ≤ lon < 180 */
        /* (west is negative) */
    itpAltitude alt; /* altitude, in 100s ft: alt > 0 */
    double gs; /* ground speed, in knots: gs > 0 */
    double vs; /* vertical speed, in ft/min */
    double trk; /* ground true track, in degrees 0 ≤ trk < 360 */
    itpDataQuality qlty; /* data quality */
} itpAircraft;

/*----------------------------------------
   Input lists
   ----------------------------------------*/
typedef struct {
    itpAircraft ac[ITP_MAX_TRAFFIC];
    int len;
} itpAircraftList;

/*---------------------------------------
   Record-type to bundle inputs together
   ---------------------------------------*/
typedef struct {
    itpAircraft ownship;
    itpAircraftList traffic;
    itpAltitude requested_fl;
} itpInputs;

/*----------------------------------------
   Output lists
   ----------------------------------------*/
typedef struct {
    itpIdentifier id;
    double range; /* ITP range to ownship */
    double gsdiff; /* Ground speed differential */
    double offset; /* Lateral offset */
    itpRelPos relpos; /* Traffic relative position to ownship */
    itpDirection dir; /* Direction: same, opposite, cross */
    itpAcType actype; /* Type of aircraft. This is a bitmask that */
        /* must be decoded through the functions: */
        /* itpIsNearby, itpIsPotentiallyBlocking, */
        /* itpIsNearest, itpIsReference */
} itpOutput;
typedef struct {
    itpTraffic trf[ITP_MAX_TRAFFIC];
    int len;
} itpTrafficList;

typedef int itpTrafficIdx; /* Index of aircraft */

typedef struct {
    itpTrafficIdx nrbyx[ITP_MAX_TRAFFIC];
    int len;
} itpNearbyList;

typedef struct {
    itpTrafficIdx blckx[ITP_MAX_TRAFFIC];
    int len;
} itpBlockingList;

typedef struct {
    itpTrafficIdx nrstx[ITP_MAX_REFERENCE];
    int len;
} itpNearestList;

typedef struct {
    itpTrafficIdx refx[ITP_MAX_REFERENCE];
    int len;
} itpReferenceList;

/*--------------------------------------------------------
 Record-type to bundle outputs together
 --------------------------------------------------------*/
typedef struct {
    itpTrafficList traffic;
    itpNearbyList nearby;
    itpBlockingList pblocking;
    itpNearestList nearest;
    itpReferenceList reference;
    itpManeuver maneuver;
} itpOutputs;
void itpEmptyOutputs(itpOutputs *outputs);

/*----------------------------------------------
 Function to reset the global parameters
----------------------------------------------*/
void itpResetGlobalParameters();

/*-------------------------------
 Get current parameter values
-------------------------------*/

itpAltitude itpGetGlobalFlDeadband();
double   itpGetGlobalVsDeadband();
double   itpGetGlobalMaxRange();
double   itpGetGlobalMaxLateralOffset();
double   itpGetGlobalRange1();
double   itpGetGlobalGsDiff1();
double   itpGetGlobalRange2();
double   itpGetGlobalGsDiff2();

/*----------------------------------------------
 Functions to set parameters to custom values
----------------------------------------------*/
void itpSetGlobalFlDeadband(itpAltitude);
void itpSetGlobalVsDeadband(double);
void itpSetGlobalMaxRange(double);
void itpSetGlobalMaxLateralOffset(double);
void itpSetGlobalRange1(double);
void itpSetGlobalGsDiff1(double);
void itpSetGlobalRange2(double);
void itpSetGlobalGsDiff2(double);

#endif

A.2  Global Parameters

/*======================================================
 ITP algorithm global parameters
 Author: Cesar A. Munoz (NIA)
        Radu I. Siminiceanu (NIA)
=======================================================*/
#include "ITP_Defs.h"

struct {
    itpAltitude FlDeadband; /* flight level deadband (100s ft) */
    double VsDeadband; /* vertical speed deadband (ft/min) */
    double MaxRange; /* maximum range (nmi) */
    double MaxLateralOffset; /* maximum lateral offset for same vicinity (nmi) */
    /* ITP initiation criteria */
    double Range1;
    double GsDiff1;
    double Range2;
    double GsDiff2;
} itpGlobalParameters = {
    ITP_FL_DEADBAND,
    ITP_VS_DEADBAND,
    ITP_MAX_RANGE,
    ITP_MAX_LATERAL_OFFSET,
    ITP_RANGE_1,
    ITP_GS_DIFF_1,
    ITP_RANGE_2,
    ITP_GS_DIFF_2
};

/*----------------------------------------------
function to reset the global parameters
----------------------------------------------*/

void itpResetGlobalParameters() {
    itpGlobalParameters.FlDeadband = ITP_FL_DEADBAND;
    itpGlobalParameters.VsDeadband = ITP_VS_DEADBAND;
    itpGlobalParameters.MaxRange = ITP_MAX_RANGE;
    itpGlobalParameters.MaxLateralOffset = ITP_MAX_LATERAL_OFFSET;
    itpGlobalParameters.Range1 = ITP_RANGE_1;
    itpGlobalParameters.GsDiff1 = ITP_GS_DIFF_1;
    itpGlobalParameters.Range2 = ITP_RANGE_2;
    itpGlobalParameters.GsDiff2 = ITP_GS_DIFF_2;
}

/*------------------------------------------------
Functions to set global parameters
--------------------------------------------------*/
void itpSetGlobalFlDeadband(itpAltitude fdb) {
    itpGlobalParameters.FlDeadband = fdb;
}

void itpSetGlobalVsDeadband(double vdb) {
    itpGlobalParameters.VsDeadband = vdb;
}

void itpSetGlobalMaxRange(double maxr) {
    itpGlobalParameters.MaxRange = maxr;
}

void itpSetGlobalMaxLateralOffset(double latoff) {
    itpGlobalParameters.MaxLateralOffset = latoff;
}

void itpSetGlobalRange1(double range1) {
    itpGlobalParameters.Range1 = range1;
}

void itpSetGlobalGsDiff1(double gs1) {
    itpGlobalParameters.GsDiff1 = gs1;
}

void itpSetGlobalRange2(double range2) {
    itpGlobalParameters.Range2 = range2;
}

void itpSetGlobalGsDiff2(double gs2) {
    itpGlobalParameters.GsDiff2 = gs2;
}

/*------------------------------
Get current parameter values
------------------------------*/

itpAltitude itpGetGlobalFlDeadband() {
    return itpGlobalParameters.FlDeadband;
}

double itpGetGlobalVsDeadband() {
    return itpGlobalParameters.VsDeadband;
double itpGetGlobalMaxRange() {
    return itpGlobalParameters.MaxRange;
}

double itpGetGlobalMaxLateralOffset() {
    return itpGlobalParameters.MaxLateralOffset;
}

double itpGetGlobalRange1() {
    return itpGlobalParameters.Range1;
}

double itpGetGlobalGsDiff1() {
    return itpGlobalParameters.GsDiff1;
}

double itpGetGlobalRange2() {
    return itpGlobalParameters.Range2;
}

double itpGetGlobalGsDiff2() {
    return itpGlobalParameters.GsDiff2;
}

A.3 Program Interface

/*======================================================
 ITP algorithm main file
 Author: Cesar A. Munoz (NIA)
      Radu I. Siminiceanu (NIA)

 File : ITP_Algorithm.h
 Release: ITP_Module-6.d (10/11/06)
======================================================*/

#ifndef ITP_ALG
#define ITP_ALG

#include "ITP_Defs.h"

/* Is traffic closing with respect to ownship ?*/
itpBool itpIsClosing(itpTraffic trf);
/* Blocking type recognizers */
itpBool itpIsNearby(itpTraffic trf);
itpBool itpIsPotentiallyBlocking(itpTraffic trf);
itpBool itpIsNearest(itpTraffic trf);
itpBool itpIsReference(itpTraffic trf);
itpBool itpIsBlocking(itpTraffic trf);
itpBool itpIsManeuvering(itpTraffic trf);
itpBool itpIsUnqualifiedData(itpTraffic trf);
itpBool itpIsTooClose(itpTraffic trf);
itpBool itpIsTooFast(itpTraffic trf);

/* Decodes actype */
void itpBlckCode2String(itpIdentifier s, itpTraffic trf);

/* ITP main function */
void itpAlgorithm(itpInputs, itpOutputs*);

#endif

A.4 Code

/*====================================================================
 ITP algorithm main file
 Author: Cesar A. Munoz (NIA)
     Radu I. Siminiceanu (NIA)

 File : ITP_Algorithm.c
 Release: ITP_Module-6.d (10/11/06)
====================================================================*/

#include "ITP_Aviation.h"
#include "ITP_Algorithm.h"
#include <string.h>

/*====================================================================
 Internal constants: Type of traffic aircraft
====================================================================*/

#define ITP_TRAFFIC 0x0
#define ITP_NEARBY 0x1
#define ITP_POTENTIALLY_BLOCKING 0x2
#define ITP_NEAREST 0x4
#define ITP_REFERENCE 0x8
#define ITP_BLOCKING 0x10
#define ITP_MANEUERVERING 0x20
#define ITP_TOO_FAST 0x40
#define ITP_TOO_CLOSE 0x80
#define ITP_UNQUALIFIED_DATA 0x100

/*============================================================================
 Auxiliary functions
============================================================================*/

double itpGeoRange(itpAircraft ac1, itpAircraft ac2) {
    double lt1, ln1, lt2, ln2;
    lt1 = ac1.lat * ITP_RAD_PER_DEG;
    ln1 = ac1.lon * ITP_RAD_PER_DEG;
    lt2 = ac2.lat * ITP_RAD_PER_DEG;
    ln2 = ac2.lon * ITP_RAD_PER_DEG;
    return ITP_ABS(itpDistance(lt1, ln1, lt2, ln2)) * ITP_NMI_PER_RAD;
}

itpDirection itpGetDirection(double trk1, double trk2, double upto) {
    double delta;
    trk1 = itpTo360(trk1);
    trk2 = itpTo360(trk2);
    delta = ITP_MAX(trk1, trk2) - ITP_MIN(trk1, trk2);
    if (delta <= upto || delta >= 360 - upto)
        return itpSameDirection;
    if (180 - upto <= delta && delta <= 180 + upto)
        return itpOppositeDirection;
    return itpCrossDirection;
}

void itpGetTrafficData(itpInputs inputs, itpOutputs *outputs, int i) {
    itpAircraft own, ac;
    double lta, lna, lto, lno, crsa, crso, lti, lni, trko;
    double dai, doi;
    int eps;
    int inter;

    own = inputs.ownship;
    ac = inputs.traffic.ac[i];
    lto = own.lat * ITP_RAD_PER_DEG;
    lno = own.lon * ITP_RAD_PER_DEG;
    crso = own.trk * ITP_RAD_PER_DEG;
    lta = ac.lat * ITP_RAD_PER_DEG;
lna = ac.lon*ITP_RAD_PER_DEG;
crsa = ac.trk*ITP_RAD_PER_DEG;
inter = itpIntersection(lta,lna,crsa,lto,lno,crso,&lti,&lni);
/* printf("inter: %d (%6.2f,%6.2f)\n",inter,
   lti*ITP_DEG_PER_RAD,lni*ITP_DEG_PER_RAD); */
if (inter < 0) {
   /* No intersection */
   trkoa = itpCourse(lto,lno,lta,lna)*ITP_DEG_PER_RAD;
   eps = (itpGetDirection(own.trk,trkoa,90) == itpSameDirection? 1: -1);
   outputs->traffic.trf[i].range =
      eps*ITP_ABS(itpDistance(lta,lna,lto,lno))*ITP_NMI_PER_RAD;
   outputs->traffic.trf[i].offset = 0;
} else {
   doi = itpDistance(lto,lno,lti,lni);
   dai = itpDistance(lta,lna,lti,lni);
   outputs->traffic.trf[i].offset =
      itpCrossTrackError(lto,lno,lta,lna,lti,lni)*ITP_NMI_PER_RAD;
   /* Intersection behind of traffic */
   if (inter == 1 || inter == 3)
      dai *= -1;
   /* Intersection behind of ownship */
   if (inter == 2 || inter == 3)
      doi *= -1;
   if (outputs->traffic.trf[i].dir == itpSameDirection)
      outputs->traffic.trf[i].range = (doi - dai)*ITP_NMI_PER_RAD;
   else
      outputs->traffic.trf[i].range = (doi + dai)*ITP_NMI_PER_RAD;
}
outputs->traffic.trf[i].relpos = outputs->traffic.trf[i].range < 0?
   itpOwnAheadTraffic : itpOwnBehindTraffic;
if (outputs->traffic.trf[i].dir == itpSameDirection)
   outputs->traffic.trf[i].gsdiff = ITP_SIGN(outputs->traffic.trf[i].range)*
      (inputs.ownship.gs - inputs.traffic.ac[i].gs);
else
   outputs->traffic.trf[i].gsdiff = ITP_SIGN(outputs->traffic.trf[i].range)*
      (inputs.ownship.gs + inputs.traffic.ac[i].gs);
}

itpAltitude itpGetFlightLevel(itpAircraft ac) {
   int err = ac.alt % 10;
   int f1 = ac.alt / 10;
   if (err <= itpGetGlobalFlDeadband())
      return 10*f1;
   if (err >= 10-itpGetGlobalFlDeadband())
      return 10-err10;
}
return 10*(fl+1);
return ITP_INVALID_VALUE;
}

itpBool itpIsManeuveringAircraft(itpAircraft ac) {
    return
        itpGetFlightLevel(ac) == ITP_INVALID_VALUE ||
        ITP_ABS(ac.vs) > itpGetGlobalVsDeadband();
}

itpBool itpIsAtInterveningFlightLevels(itpInputs inputs, itpAircraft ac) {
    int eps;
    itpAltitude flown;
    flown = itpGetFlightLevel(inputs.ownship);
    eps = ITP_SIGN(inputs.requested_fl - flown);
    return
        flown != ITP_INVALID_VALUE &&
        eps*flown < eps*ac.alt &&
        eps*ac.alt < eps*inputs.requested_fl;
}

void itpGetNearby(itpInputs inputs, itpOutputs *outputs) {
    int i;
    outputs->traffic.len = 0;
    outputs->nearby.len = 0;
    for (i=0; i < inputs.traffic.len; i++) {
        outputs->traffic.trf[i].actype = ITP_TRAFFIC;
        strcpy(outputs->traffic.trf[i].id,inputs.traffic.ac[i].id);
        outputs->traffic.trf[i].dir = itpGetDirection(inputs.traffic.ac[i].trk,
            inputs.ownship.trk,45);
        if (outputs->traffic.trf[i].dir == itpSameDirection ||
            outputs->traffic.trf[i].dir == itpOppositeDirection) {
            itpGetTrafficData(inputs,outputs,i);
            /* if same vicinity */
            if (itpGeoRange(inputs.traffic.ac[i],inputs.ownship) <=
                itpGetGlobalMaxRange() &&
                outputs->traffic.trf[i].offset <= itpGetGlobalMaxLateralOffset()) {
                outputs->traffic.trf[i].actype |= ITP_NEARBY;
                outputs->nearby.nrbyx[outputs->nearby.len] = i;
                outputs->nearby.len++;
            }
        }
    }
}
} else {
    outputs->traffic.trf[i].offset = ITP_INVALID_VALUE;
    outputs->traffic.trf[i].range = ITP_INVALID_VALUE;
    outputs->traffic.trf[i].gsdiff = ITP_INVALID_VALUE;
    outputs->traffic.trf[i].relpos = itpNoRelPos;
}
outputs->traffic.len++;
}

itpBool itpIsClosing(itpTraffic trf) {
    return trf.gsdiff > 0;
}

itpAcType itpGetBlockingType(itpInputs inputs,
    itpTrafficList traffic,
    itpTrafficIdx idx) {
    itpAircraft ac;
    itpTraffic trf;
    itpAcType actype;

    actype = 0x0;
    ac = inputs.traffic.ac[idx];
    trf = traffic.trf[idx];

    if (itpIsManeuveringAircraft(ac))
        actype |= ITP_MANEUVERING;
    if (ac.qlty != itpQualified)
        actype |= ITP_UNQUALIFIED_DATA;
    if (ITP_ABS(trf.range) < itpGetGlobalRange1())
        actype |= ITP_TOO_CLOSE;
    if (itpIsClosing(trf)) {
        if (trf.gsdiff > itpGetGlobalGsDiff2() ||
            ITP_ABS(trf.range) ≥ itpGetGlobalRange1() &&
            ITP_ABS(trf.range) < itpGetGlobalRange2() &&
            trf.gsdiff > itpGetGlobalGsDiff1())
            actype |= ITP_TOO_FAST;
        if (trf.gsdiff > itpGetGlobalGsDiff1() &&
            trf.gsdiff ≤ itpGetGlobalGsDiff2() &&
            ITP_ABS(trf.range) < itpGetGlobalRange2())
            actype |= ITP_TOO_CLOSE;
    }
    if (!actype)
        actype = ITP_BLOCKING;
}
void itpBlckCode2String(itpIdentifier s, itpTraffic trf) {
    strcpy(s,"");
    if (itpIsBlocking(trf))
        strcat(s,"B");
    if (itpIsManeuvering(trf))
        strcat(s,"M");
    if (itpIsUnqualifiedData(trf))
        strcat(s,"U");
    if (itpIsTooClose(trf))
        strcat(s,"C");
    if (itpIsTooFast(trf))
        strcat(s,"F");
}

itpBool itpIsNearby(itpTraffic trf) {
    return trf.actype & ITP_NEARBY;
}

itpBool itpIsPotentiallyBlocking(itpTraffic trf) {
    return trf.actype & ITP_POTENTIALLY_BLOCKING;
}

itpBool itpIsNearest(itpTraffic trf) {
    return trf.actype & ITP_NEAREST;
}

itpBool itpIsReference(itpTraffic trf) {
    return trf.actype & ITP_REFERENCE;
}

itpBool itpIsBlocking(itpTraffic trf) {
    return trf.actype & ITP_BLOCKING;
}

itpBool itpIsManeuvering(itpTraffic trf) {
    return trf.actype & ITP_MANEUVERING;
}

itpBool itpIsTooClose(itpTraffic trf) {
    return trf.actype & ITP_TOO_CLOSE;
}
itpBool itpIsTooFast(itpTraffic trf) {
    return trf.actype & ITP_TOO_FAST;
}

itpBool itpIsUnqualifiedData(itpTraffic trf) {
    return trf.actype & ITP_UNQUALIFIED_DATA;
}

void itpGetPotentiallyBlocking(itpInputs inputs, 
                                itpOutputs *outputs) {

    int i,idx;

    outputs->pblocking.len = 0;
    for (i=0; i < outputs->nearby.len; i++) {
        idx = outputs->nearby.nrbyx[i];
        if (outputs->traffic.trf[idx].dir == itpSameDirection &&
                itpIsAtInterveningFlightLevels(inputs,inputs.traffic.ac[idx])) {
            outputs->traffic.trf[idx].actype |=
                itpGetBlockingType(inputs,outputs->traffic,idx);
            outputs->pblocking.blckx[outputs->pblocking.len] = idx;
            outputs->pblocking.len++;
        }
    }
}

void itpGetNearest(itpInputs inputs, 
                    itpOutputs *outputs) {

    int i,j,k,idx,jdx;
    outputs->nearest.len = 0;
    /* Find nearest ITP_MAX_REFERENCE aircraft */
    for (i=0; i < outputs->pblocking.len; i++) {
        idx = outputs->pblocking.blckx[i];
        for (j=0; j < outputs->nearest.len; j++) {
            jdx = outputs->nearest.nrstx[j];
            if (ITP_ABS(outputs->traffic.trf[idx].range) <
                ITP_ABS(outputs->traffic.trf[jdx].range))
                break;
        }
        if (j < ITP_MAX_REFERENCE) {
            for(k=ITP_MIN(outputs->nearest.len,ITP_MAX_REFERENCE-1); k > j; k--)
                outputs->nearest.nrstx[k] = outputs->nearest.nrstx[k-1];
            outputs->nearest.nrstx[j]=idx;
        }
    }
}
if (outputs->nearest.len < ITP_MAX_REFERENCE)
    outputs->nearest.len++;
}

/* Remove nearest at the same flight level same direction */
 idx=outputs->nearest.nrstx[0];
 for (i=0,j=1,idx=outputs->nearest.nrstx[0]; j < outputs->nearest.len; j++) {
    jdx = outputs->nearest.nrstx[j];
    if (itpGetFlightLevel(inputs.traffic.ac[idx]) !=
        itpGetFlightLevel(inputs.traffic.ac[jdx]) ||
        ITP_SIGN(outputs->traffic.trf[idx].range) !=
        ITP_SIGN(outputs->traffic.trf[jdx].range)) {
        outputs->traffic.trf[idx].actype |= ITP_NEAREST;
        idx = jdx;
        i++;
    }
}
if (i < outputs->nearest.len) {
    outputs->traffic.trf[idx].actype |= ITP_NEAREST;
    i++;
}
outputs->nearest.len = i;

void itpGetReference(itpInputs inputs,
                      itpOutputs *outputs) {

    int i,idx;
    itpGetNearest(inputs,outputs);
    outputs->reference.len = 0;
    for (i=0; i < outputs->nearest.len; i++) {
        idx = outputs->nearest.nrstx[i];
        if (!itpIsBlocking(outputs->traffic.trf[idx])) {
            outputs->reference.len = 0;
            break;
        } else {
            outputs->traffic.trf[idx].actype |= ITP_REFERENCE;
            outputs->reference.refx[outputs->reference.len] = idx;
            outputs->reference.len++;
        }
    }
}

void itpGetManeuver(itpInputs inputs,
itpOutputs *outputs) {
    itpBool climb, lead, follow;
    int i;

    outputs->maneuver = itpNone;
    lead = 0;
    follow = 0;
    climb = (inputs.requested_fl > inputs.ownship.alt);
    for (i=0; i<outputs->reference.len; i++) {
        if (outputs->traffic.trf[outputs->reference.refx[i]].relpos ==
            itpOwnAheadTraffic)
            lead = 1;
        else
            follow = 1;
    }
    if (lead && follow)
        outputs->maneuver = (climb? itpCombinedLeadingFollowingClimb :
            itpCombinedLeadingFollowingDescent);
    else if (lead)
        outputs->maneuver = (climb? itpLeadingClimb : itpLeadingDescent);
    else
        outputs->maneuver = (climb? itpFollowingClimb : itpFollowingDescent);
}

/*-----------------------------------------------
   ITP main function.
   CAVEAT: itpGlobalParameters should be set before
   calling itpAlgorithm
   -----------------------------------------------*/

void itpSetOutputs(itpOutputs *outputs) {
    outputs->traffic.len = 0;
    outputs->nearby.len = 0;
    outputs->pblocking.len = 0;
    outputs->nearest.len = 0;
    outputs->reference.len = 0;
    outputs->maneuver = itpNone;
}

void itpAlgorithm(itpInputs inputs, itpOutputs *outputs) {
    itpSetOutputs(outputs);
    itpGetNearby(inputs, outputs);
    if (!itpIsManeuveringAircraft(inputs.ownship) &&
        outputs->nearby.len > 0) {
itpGetPotentiallyBlocking(inputs,outputs);
if (outputs->pblocking.len > 0) {
    itpGetReference(inputs,outputs);
    if (outputs->reference.len > 0)
        itpGetManeuver(inputs,outputs);
}

B AVIATION FORMULARY

Except for the function ITP_intersection, which was developed by R. Siminiceanu, all the other functions were taken from William’s Aviation Formulary [3].

B.1 Program Interface

```
/*======================================================================
 Aviation Formulary
 Author: Cesar A. Munoz (NIA)
        Radu I. Siminiceanu (NIA)

 File : ITP_Aviation.h
 Release: ITP_Module-6.d (10/11/06)
 =========================================================================*/

#ifndef ITP_AVI
#define ITP_AVI

#include <math.h>

#define ITP_MAX(a,b) ((a) > (b) ? (a) : (b))
#define ITP_MIN(a,b) ((a) < (b) ? (a) : (b))
#define ITP_ABS(x) ((x) < 0 ? - (x) : x)
#define ITP_SQ(x) (x*x)
#define ITP_SIGN(x) ((x) < 0 ? - 1 : 1)
#define ITP_PI 3.14159265358979323846
#define ITP_RAD_PER_DEG (ITP_PI/180.0)
#define ITP_DEG_PER_RAD (180.0/ITP_PI)
#define ITP_FT_PER_NMI 6076.11548556431
#define ITP_NMI_PER_RAD (ITP_EARTH_RADIUS_FT/ITP_FT_PER_NMI)
#define ITP_ALMOST_ZERO 0.00001

int itpIsAlmostZero(double x);
double itpSqrtSafe(double x);
```
double itpAsinSafe(double x);
double itpAcosSafe(double x);
double itpAtanyxSafe(double y, double x);
double itpTo2pi(double x);
double itpTo360(double x);
double itpDistance(double lat1, double lon1, double lat2, double lon2);
double itpCourse(double lat1, double lon1, double lat2, double lon2);
int itpIntersection(double lat1, double lon1, double crs13,
    double lat2, double lon2, double crs23,
    double *lati, double *loni);
double itpCrossTrackError(double lat1, double lon1,
    double lat2, double lon2,
    double lat3, double lon3);
#endif

B.2 Code

/****************************************************************************
 These formulas are taken from Aviation Formulary v1.42:
 http://williams.best.vwh.net
 - all units are in radians
 - modified to convention "east is positive"

 Author: Cesar A. Munoz (NIA)
        Radu I. Siminiceanu (NIA)

 File : ITP_Aviation.c
 Release: ITP_Module-6.d (10/11/06)
 ****************************************************************************/

#include <stdio.h>
#include <stdlib.h>
#include "ITP_Aviation.h"

int itpIsAlmostZero(double x) {
    return ITP_ABS(x) < ITP_ALMOST_ZERO;
}

double itpSqrtSafe(double x) {
    return sqrt(ITP_MAX(x,0.0));
}

double itpAsinSafe(double x) {

return asin(ITP_MAX(-1.0,ITP_MIN(x,1.0)));
}

double itpAsinSafe(double x) {
    return asin(ITP_MAX(-1.0,ITP_MIN(x,1.0)));
}

double itpAtanyxSafe(double y, double x) {
    if (itpIsAlmostZero(x) && itpIsAlmostZero(y))
        return 0.0;
    return atan2(y,x);
}

double itpTo2pi(double x) {
    double mod = x - 2*ITP_PI*((int) (x/(2*ITP_PI)));
    if (mod < 0) mod += 2*ITP_PI;
    return mod;
}

double itpTo360(double x) {
    double mod = x - 360.0*((int) (x/360.0));
    if (mod < 0) mod += 360.0;
    return mod;
}

double itpDistance(double lat1, double lon1, double lat2, double lon2) {
    return 2*itpAsinSafe(itpSqrtSafe(ITP_SQ(sin((lat1-lat2)/2)) +
            cos(lat1)*cos(lat2)*sin((lon2-lon1)/2)*
            sin((lon2-lon1)/2)));
}

double itpCourse(double lat1, double lon1, double lat2, double lon2) {
    if (itpIsAlmostZero(cos(lat1)))
        return (lat1>0 ? ITP_PI : 0.0);
    return itpTo2pi(itpAtanyxSafe(sin(lon2-lon1)*cos(lat2),
            cos(lat1)*sin(lat2)-
            sin(lat1)*cos(lat2)*cos(lon2-lon1)));
}

/* This function returns:
   -1 : no intersection,
   0 : ahead of both,
   1 : behind of 1, ahead of 2
   2 : behind of 2, ahead of 1
   */
3: behind of both

If positive (*ilat,*ilon) is the intersection point */

```c
int itpIntersection(double lat1, double lon1, double crs13,
                    double lat2, double lon2, double crs23,
                    double *ilat, double *ilon) {

double crs12, crs21, ang1, ang2, ang3, dst12, dst13, lat3, lon3;
double modcrs13, modcrs23, delta;
int flipped1, flipped2;

crs13 = itpTo2pi(crs13);
crs23 = itpTo2pi(crs23);
dst12 = itpDistance(lat1, lon1, lat2, lon2);
crs12 = itpCourse(lat1, lon1, lat2, lon2);
crs21 = itpCourse(lat2, lon2, lat1, lon1);

ang1=crs13-crs12;
ang2=crs21-crs23;

if (ITP_ABS(sin(ang1)) < 0.1 &&
    ITP_ABS(sin(ang2)) < 0.1)
    /* if (itpIsAlmostZero(sin(ang1)) && itpIsAlmostZero(sin(ang2))) */
    return -1;

flipped1 = 0;
flipped2 = 0;
modcrs13 = crs13;
modcrs23 = crs23;

if (0<=crs13 && crs13<=ITP_PI) { /* ownship going east */
    if (crs13 <= crs21 && crs21 <= crs13+ITP_PI) { /* target on left side */
        if (crs23 > crs13+ITP_PI || crs23 < crs13) {
            modcrs23 = itpTo2pi(crs23 + ITP_PI);
            flipped2 = 1;
        }
        flipped1 = (crs21 < modcrs23 && modcrs23 < crs13+ITP_PI);
    }
    else { /* target on the right side */
        if (crs23 > crs13 && crs23 < crs13+ITP_PI) {
            modcrs23 = itpTo2pi(crs23 + ITP_PI);
            flipped2 = 1;
        }
        if (itpIsAlmostZero(ITP_ABS(crs21))) crs21 = crs21 + 2*ITP_PI;
        flipped1 = ((crs21 > crs13+ITP_PI &&
                     crs13+ITP_PI < modcrs23 && modcrs23 < crs21) ||
```
(crs21 < crs13 && (modcrs23 > crs13+ITP_PI || modcrs23 < crs21));
}
else { /* ownship going west */
    if (crs21 ≥ crs13 || crs21 ≤ crs13-ITP_PI) {/* target on the left side */
        if (crs13-ITP_PI < crs23 && crs23 < crs13) {
            modcrs23 = itpTo2pi(crs23 + ITP_PI);
            flipped2 = 1;
        }
        flipped1 = ((crs21 > crs13 && (modcrs23 > crs21 || modcrs23 < crs13-ITP_PI)) ||
                     (crs21 < crs13-ITP_PI && modcrs23 > crs21 &&
                      modcrs23 < crs13-ITP_PI));
    }
    else { /* target on the right side */
        if (crs23 > crs13 || crs23 < crs13-ITP_PI) {
            modcrs23 = itpTo2pi(crs23 + ITP_PI);
            flipped2 = 1;
        }
        if (itpIsAlmostZero(ITP_ABS(crs21))) crs21 = crs21 + 2*ITP_PI;
        flipped1 = (modcrs23 > crs13-ITP_PI && modcrs23 < crs21);
    }
}

ang1 = itpTo2pi(crs13-crs12+ITP_PI) - ITP_PI;
ang2 = itpTo2pi(crs21-modcrs23+ITP_PI) - ITP_PI;
ang1 = ITP_ABS(ang1);
ang2 = ITP_ABS(ang2);

if (flipped1) {
    ang1 = itpTo2pi(ITP_PI - ang1);
    modcrs13 = itpTo2pi(crs13 + ITP_PI);
}

ang3 = itpACosSafe(-cos(ang1)*cos(ang2) + sin(ang1)*sin(ang2)*cos(dst12));
if (itpIsAlmostZero(sin(ang3))) {
    *ilat = 0.0;
    *ilon = 0.0;
    return -1;
}

dst13 = itpASinSafe(sin(ITP_ABS(ang2))*sin(dst12)/sin(ang3)));
lat3 = itpASinSafe(sin(lat1)*cos(dst13)+cos(lat1)*sin(dst13)*cos(modcrs13));
delta = itpAsinSafe(sin(crs13)*sin(dst13)/cos(lat3));

if (flipped1==0)
  lon3 = itpTo2pi(lon1 + delta + ITP.PI) - ITP.PI;
else
  lon3 = itpTo2pi(lon1 - delta + ITP.PI) - ITP.PI;

*ilat = lat3;
*ilon = lon3;
return 2*flipped2 + flipped1;
}

/* Track error to common point (lat3,lon3), wrt (lat2,lon2) */
double itpCrossTrackError(double lat1, double lon1,
                        double lat2, double lon2,
                        double lat3, double lon3) {
  double crs31, crs32,dst32;
  dst32 = itpDistance(lat3, lon3, lat2, lon2);
  if (itpIsAlmostZero(cos(lat3))) {
    /* (lat3,lon3) is a Pole */
    crs31 = lon1;
    crs32 = lon2;
  } else {
    crs31 = itpCourse(lat3, lon3, lat1, lon1);
    crs32 = itpCourse(lat3, lon3, lat2, lon2);
  }
  return ITP_ABS(itpAsinSafe(sin(dst32)*sin(crs32-crs31)));
# In-Trail Procedure (ITP) Algorithm Design

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## Abstract
The primary objective of this document is to provide a detailed description of the In-Trail Procedure (ITP) algorithm, which is part of the Airborne Traffic Situational Awareness – In-Trail Procedure (ATSA-ITP) application. To this end, the document presents a high level description of the ITP Algorithm and a prototype implementation of this algorithm in the programming language C.