TIME-RESOLVED DIFFUSION TOMOGRAPHIC 2D AND 3D IMAGING IN HIGHLY SCATTERING TURBID MEDIA

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ABSTRACT
A method for imaging objects in highly scattering turbid media. According to one embodiment of the invention, the method involves using a plurality of intersecting source/detectors sets and time-resolving equipment to generate a plurality of time-resolved intensity curves for the diffusive component of light emergent from the medium. For each of the curves, the intensities at a plurality of times are then inputted into the following inverse reconstruction algorithm to form an image of the medium:

\[
X^{(k+1)} = (Y^TW + A_k[A_k^TW + A_k^{-1}])^{-1}
\]

wherein W is a matrix relating output at source and detector positions \( r_s \) and \( r_d \), at time t, to position \( r \), A is a regularization matrix, chosen for convenience to be diagonal, but selected in a way related to the ratio of the noise, \( <n> \), to fluctuations in the absorption (or diffusion) \( X \), that we are trying to determine:

\[
A = \lambda_0 \delta_0 \implies \lambda_0 = \langle AX|AX \rangle^{-1}
\]

Y is the data collected at the detectors, and \( X^k \) is the kth iterate toward the desired absorption information. An algorithm, which combines a two dimensional (2D) matrix inversion with a one-dimensional (1D) Fourier transform inversion is used to obtain images of three dimensional hidden objects in turbid scattering media.

25 Claims, 10 Drawing Sheets
Fig. 2
Fig. 5(a)

\[ \lambda = 1000 \]
\[ d\lambda = 0.7 \]

Fig. 5(b)

\[ \lambda = 0.01 \]
\[ d\lambda = 0.7 \]
Fig. 7(a)

Scattering Medium

Absorbing Objects

Input Light

Fig. 7(b)

Input
Fig. 9(a)
1 TIME-RESOLVED DIFFUSION TOMOGRAPHIC 2D AND 3D IMAGING IN HIGHLY SCATTERING TURBID MEDIA

CROSS-REFERENCE TO RELATED APPLICATIONS


STATEMENT AS TO RIGHTS TO INVENTIONS MADE UNDER FEDERALLY-SPONSORED RESEARCH AND DEVELOPMENT

This invention was made, in part, with Government support awarded by NASA and ONR. The Government may have certain rights in this invention.

BACKGROUND OF THE INVENTION

The present invention relates generally to the imaging of objects in highly scattering turbid media and more particularly to a novel technique for imaging objects in highly scattering turbid media.

As can readily be appreciated, there are many situations in which the detection of an object present in a highly scattering turbid medium is highly desirable. For instance, the detection of a tumor embedded within a tissue is one such example. Although X-ray techniques do provide some measure of success in detecting objects in turbid media, they are not well-suited for detecting very small objects, e.g., tumors less than 1 mm in size, or for detecting objects in thick media. In addition, X-ray radiation can present safety hazards to a person exposed thereto.

An alternative technique used to detect objects in turbid media is transillumination. In transillumination, visible or near infrared (NIR) light is incident on one side of a medium and the light emergent from the opposite side of the medium is used to form an image. Objects embedded in the medium typically absorb the incident light and appear in the image as shadows. Unfortunately, the usefulness of transillumination as a detection technique is severely limited in those instances in which the medium is thick or the object is very small. This is because light scattering within the medium contributes to noise and reduces the intensity of the unscattered light used to form the image shadow.

To improve the detectability of small objects located in a turbid medium using transillumination, many investigators have attempted to selectively use only certain components of the transilluminating light signal. This may be done by exploiting the properties of photon migration through a scattering medium. Photons migrating through a turbid medium have traditionally been categorized into three major signal components: (1) the ballistic (coherent) photons which arrive first by traveling over the shortest, most direct path; (2) the snake (quasi-coherent) photons which arrive first by traveling over the shortest, most direct path; (3) the diffusive (incoherent) photons which experience comparatively more scattering than do ballistic and snake photons and, therefore, deviate more considerably from the straight-line propagation path followed by ballistic and snake photons.


Of the above-listed art, Wang et al., "Kerr-Fourier imaging of hidden objects in thick turbid media," Optics Letters, Vol. 18, No. 3, pp. 241-243 (Feb. 1, 1993) is illustrative of transillumination techniques which selectively use the ballistic and/or snake components of light. In this article, there is disclosed a time/space-gating system for use in imaging opaque test bars hidden inside a 5.5 cm-thick 2.5% Intralipid solution. The disclosed system includes three main parts: a laser source, an optical Kerr gate and a detector. The laser source is a picosecond mode-locked laser system, which emits a 1054 nm, 8 ps laser pulse train as the illumination source. The second harmonic of the pulse train, which is generated by transmission through a potassium dihydrate phosphate (KDP) crystal, is used as the gating source. The illumination source is sent through a variable time-delay and is then used to transilluminate, from one side, the turbid medium containing the opaque object. The signal from the turbid medium located at the front focal plane of a lens is collected and transformed to a Kerr cell located at its back focal plane (i.e., the Fourier-transform spectral plane of a 4F system). That portion of the Kerr cell located at the focal point of the 4F system is gated at the appropriate time using the gating source so that only the ballistic and snake components are permitted to pass through. The spatially filtered and temporal-segmented signal is then imaged by a second lens onto a CCD camera.

Although techniques of the type described above, which selectively use ballistic and snake photons to image objects in turbid media, have enjoyed a modicum of success, such techniques have been limited by the fact that detected light signals derived from ballistic and snake photons are typically rather weak, due to the proportionately small number of transilluminated ballistic and snake photons. This problem is further exacerbated in those instances in which the turbid medium is thick and the likelihood of substantial scattering increases.
Accordingly, because diffusive photons constitute the greatest component of the transilluminated light signal, it would be highly desirable to make use of the diffusive component of the light signal in forming an image via transillumination. This objective is made difficult, however, by the fact that diffusive photons tend to traverse a medium along ill-defined paths. One approach to this problem has been to invert the experimental scattering data obtained from various points in the medium using some inverse algorithm and reconstruction approach. This approach is often called diffusion tomography since diffusion or scattering is the dominant factor in the problem. In diffusion tomography, one produces an internal map of the scattering medium using the scattered signals and a mathematical inversion algorithm. The inversion is based upon the physical and mathematical principles governing photon propagation in turbid media. Both time-resolved data and frequency domain data can be used for reconstruction. Examples of diffusion tomography techniques include Arridge, “The Forward and Inverse Problems in Time Resolved Infra-Red Imaging,” Medical Optical Tomography: Functional Imaging and Monitoring SPIE Institutes, Vol. IS11, G. Muller ed., 31–64 (1993); Singer et al., “Image Reconstruction of the Interior of Bodies That Diffuse Radiation,” Science, 248:990–9 (1993); Barbour et al., “A Perturbation Approach for Optical Diffusion Tomography Using Continuous-Wave and Time-Resolved Data,” Medical Optical Tomography: Functional Imaging and Monitoring SPIE Institutes, Vol. IS11, G. Muller ed., 87–120 (1993); M. Patterson et al., SPIE, 1767, 372 (1992); J. Schotland et al., App. Opt., 32, 448 (1993), all of which are incorporated herein by reference.

The foregoing diffusion tomography techniques do not lead to a resolution that is better than about 5–10 mm. Moreover, these techniques are time-consuming and do not readily lend themselves to real-time use.

SUMMARY OF THE INVENTION

It is an object of the present invention to provide a novel technique for imaging objects present in highly scattering turbid media. It is another object of the present invention to provide a technique as described above that overcomes at least some of the disadvantages associated with existing techniques for imaging objects in highly scattering turbid media.

Additional objects, as well as features and advantages, of the present invention will be set forth in part in the description which follows, and in part will be obvious from the description or may be learned by practice of the invention.

The present invention is based on the present inventors’ discovery that objects hidden in highly scattering turbid media can be imaged by a novel, fast and noise-resistant inverse method which involves illuminating a highly scattering turbid medium with a pulse of light, the light emergent from the highly scattering turbid medium consisting of a ballistic component, a snake-like component and a diffusive component; determining the intensity of said diffusive component at a plurality of points in time; and using said intensity determinations to form an image of the object in the highly scattering turbid medium.

The aforementioned illuminating and determining steps preferably include the use of a light source and one or more detectors, said detectors preferably including means, such as a streak camera, for temporally resolving the diffusive component of the emergent light from the highly scattering turbid medium. More preferably, two or more source/detector sets are arranged in an intersecting manner to enable a 2-D or 3-D image to be formed.

Preferably, the following inverse reconstruction algorithm is used to form an image of the turbid medium using the aforementioned intensity determinations:

\[ x^{k+1} = \frac{1}{I^2} \left[ F \left( W + x^k \right) \Lambda \left( W^* W + \Lambda \right)^{-1} \right] \]

wherein \( W \) is a matrix relating output at source and detector positions \( r_s \) and \( r_d \) at time \( t \) to input at a voxel’s position \( r \), \( \Lambda \) is a regularization matrix, chosen for convenience to be diagonal but selected in a way related to the ratio of the noise, \( \eta \), to fluctuations in the absorption (or diffusion) \( \eta \) that we are trying to determine:

\[ \Lambda = \frac{\lambda \omega}{\eta + \omega \eta} \]

\( Y \) is the data collected at the detectors, and \( X_k \) is the \( k \)th iterate toward the desired absorption information.

A distinct advantage of the present method, over existing inverse reconstruction methods for imaging objects located in highly scattering turbid media using diffusive photons, is that the present method can be done with fewer iterations, thereby making possible real-time imaging.

An inverse algorithm, which combines a two dimensional (2D) matrix inversion with a one-dimensional (1D) Fourier transform inversion, is also disclosed herein to obtain images of three-dimensional (3D) objects hidden in turbid scattering media. To obtain such 3D images, the source-detector pairs are arranged in a 2D plane (the x-y plane), which are scanned along the z direction. Data is obtained from S-D pairs at z positions for processing. The reference system is assumed to be uniform and infinite along the z direction. In the above experimental setting, the weight function, \( W \), satisfies translation invariance. In other words, it is a function of \( z \equiv z_0 \), where \( z_0 \) is the z-position of source-detector plane and \( z \) is the coordinate of a voxel.

After making a one-dimensional Fourier transform of \( W \) over \( z \equiv z_0 \), we obtain \( K \) independent matrices, \( W_{y,k}(k) \), parameterized by \( k \), with \( K \) the number of grid-points in the Fourier k-space. We separately calculate the \( K \) inverse matrices \( W_{y,k}(k)^{-1} A(k)^{-1} \), \( k=1,2,3, \ldots, K \), where \( A(k) \) is a matrix for regularization. These inverse matrices are stored as a database for later reconstruction of the image in different hidden object cases. Experimental data in time-resolved (or frequency domain) is \( Y_{x,y,z}(t_0, z_0) \), where \( z_0 \) and \( r_0 \) are \( (x,y) \) coordinates of detector and source; \( t_0 \) is the time slice (or \( \omega \) is frequency). We make a Fourier transform over \( z_0 \) to obtain \( Y_{x,y,z}(t_0, k), k=1,2,3, \ldots, K \). Then we calculate the image in the k space using the following matrix multiplication:

\[ x(k) = Y(k)^* W_{y,k}(k)^* W_{y,k}(k) A(k)^{-1} \]

Then, the inverse 1D Fourier transform of \( X(k) \) over \( k \) generates the 3D distribution of the change of absorption coefficients or scattering coefficients.

The aforementioned method of 3D imaging using matrix inversion and Fourier transform greatly reduces the computational burden compared to standard 3D matrix inversion methods, while maintaining mathematical integrity in the use of Fourier Transform.

To demonstrate the capability of the above-described method, we used said method to obtain a 3D image with 26x26x32 voxels. An image was reconstructed by running about 30 minutes on a Silicon Graphic Indy 4400 computer for 3D. In this manner, the data may be taken and the image calculated while a patient waits for results.

The present invention is also directed to systems constructed in accordance with the foregoing methods.
In the description which follows, reference is made to the accompanying drawings which form a part thereof and in which is shown by way of illustration specific embodiments for practicing the invention. These embodiments will be described in sufficient detail to enable those skilled in the art to practice the invention, and it is to be understood that other embodiments may be utilized and that structural changes may be made without departing from the scope of the invention. The following detailed description is, therefore, not to be taken in a limiting sense, and the scope of the present invention is best defined by the appended claims.

**BRIEF DESCRIPTION OF THE DRAWINGS**

The accompanying drawings, which are hereby incorporated into and constitute a part of this specification, illustrate various embodiments of the invention and, together with the description, serve to explain the principles of the invention. In the drawings wherein like reference numerals represent like parts:

**FIGS. 1(a) and 1(b) are simplified schematic perspective and section views, respectively, of an experimental setup used to test the imaging method of the present invention.**

**FIG. 2 is a graphic representation of various time-resolved curves obtained using the experimental setup of FIGS. 1(a) and 1(b), curves (a) through (c) being obtained by positioning an object in the three locations (a), (b) and (c), respectively, of FIG. 1(b), and the curve labelled "Uniform" being obtained by not positioning the object within the sample medium.**

**FIGS. 3(a) through 3(c) are comparative images of the object of FIG. 1(a) obtained using the method of the present invention with different regularization parameters.**

**FIGS. 4(a) through 4(b) are comparative images of the object of FIG. 1(a) obtained using the method of the present invention with different numbers of iterations.**

**FIGS. 5(a) and 5(b) are comparative images of the object of FIG. 1(a) obtained using the method of the present invention with (a) a comparatively great degree of regularization and no iteration; and (b) a comparatively low degree of regularization and 2000 iterations, respectively.**

**FIG. 6 is an image of the object of FIG. 1(a) obtained using the conventional Simultaneous Algebraic Reconstruction Technique (SART) after 3 hours and 100 iterations.**

**FIGS. 7(a) and 7(b) are schematic views of an experimental setup used to generate a 3D image of two objects hidden in a scattering medium.**

**FIGS. 8(a) and 8(b) are schematic representations of two different arrangements of a pair of 3D objects hidden in a scattering medium.**

**FIG. 9(a) represents a series of images of the objects of FIG. 8(a) shown at different places in the z direction.**

**FIG. 9(b) represents a series of images of the objects of FIG. 8(b) shown at different places in the z direction.**

**DETAILED DESCRIPTION OF PREFERRED EMBODIMENTS**

As indicated above, the present invention is based upon the present inventors’ discovery that objects hidden in highly scattering turbid media can be imaged by a novel, fast and noise-resistant inverse method which comprises, among other things, transillumination of a highly scattering turbid medium using a plurality of intersecting source-detector pairs and using intensity measurements of the diffusive component of the detected light signals taken over a plural-

of time windows (or “time-slices”) in a novel inverse reconstruction algorithm.

The following discussion provides the theoretical basis for the present invention: A scattered signal is, in general, a function of key parameters characterizing the medium. The forward problem is to build a mathematical model that allows computation of signals when a spatial distribution of key parameters is given. This mathematical model is clearly based on the fundamental physical principles governing the interaction. The inverse problem is to find the distribution of these key parameters that best fit the given signal data. For photon propagation in turbid media, the key parameters characterizing the interaction are the absorption length, the transport mean free path, the scattering mean free path, and the index of refraction of media. The parameters are in general functions of position (r) and wavelength (λ). In the case of optical diffusion tomography, the most commonly used key parameters are absorption and transport scattering coefficients, which are the inverse of absorption length and transport scattering mean free path, respectively. The mathematical model governing the photon propagation is the photonic transport theory or its approximations, such as the diffusion theory or the telegrapher’s equation.

To show the basic principle of this technique, diffusion theory is applied here to model light propagation in turbid media. The diffusion equation in turbid media is

\[
\frac{\partial I}{\partial t} + \mu_a(\mathbf{r}) - c(\mathbf{D}(\mathbf{r})) \cdot \nabla I(\mathbf{r}, t) = S(\mathbf{r}, t)
\]

where \( I(\mathbf{r}, t) \) is the field of photon density, \( S(\mathbf{r}, t) \) is the source of laser light, \( \mu_a \) is the absorption coefficient, \( D = 1/3(\mu_a + (1-g)\mu_s) \) is the diffusion coefficient, with \( \mu_s \) the scattering coefficient, \( g \) the scattering anisotropic factor and \( c \) the speed of light in the medium.

We are interested in the following problem: given intensity measurements taken around the media either with objects located therein, \( I(\mathbf{r}, t) \), or without objects located therein, \( I_0(\mathbf{r}, t) \), reconstruct a spatial map of the change in optical parameters (absorption and diffusion coefficients) due to the presence of hidden objects.

The forward problem of scattering can be represented in a matrix form written as

\[
Y = W X + n
\]

where \( Y \) has \( M \times (\text{number of S-D pairs}) \times (\text{number of time slices}) \) elements, which is the change in intensity profile and is a function of the position of source \( \mathbf{r}_s \), the position of detector \( \mathbf{r}_d \), and the time-slice in the profile t. \( X \) has \( N \times (\text{number of voxel elements}) \) wherein a voxel is a space grid element. \( Y = c \mathbf{D} I(\mathbf{r}_s) \) or \( c \mathbf{D} I(\mathbf{r}_d) \) is the time-independent change in the absorption coefficient or the diffusion coefficient in the voxel j due to the presence of hidden objects, and \( n \) is signal detector noise. \( W \) is an \( M \times N \) matrix. Its element is the weight function or "photon measurement density functions." This weight function represents the change in signal at the detector placed at \( \mathbf{r}_d \) at time \( t \) from a source signal originating at \( \mathbf{r}_s \) associated with a unit change in absorption coefficient (or diffusion coefficient) at \( \mathbf{r}_s \) of the reference medium, as implemented by a diffusion process that carries the signal from source at
where $\tau_j$ to the detector at $\tau_j$. Its value is theoretically calculated according to the mathematical model, for example, the diffusion theory in the case shown below.

Using Green’s function formula, for the case of absorption change, $c_\Delta \mu_r$, the element of $W$ is given by

$$w[\vec{r}_j, \vec{r}_i, t] = \frac{\Delta V}{G^0(\vec{r}_j - \vec{r}_i, r, \tau)}$$

where $G^0(\vec{r}_j - \vec{r}_i, r, \tau)$ is the Green’s function of Eq.(1) for a reference system (the system with no hidden object) which gives the normalized photon intensity at $\tau_j$ at time $t$ as migrating photons originate from $\tau_i$ at time $t=0$. In Eq.(3), the second Green’s function in the integral, $G^0(\vec{r}_j, \vec{r}_i, \tau)$, represents the photons that migrate from a source to a given voxel element. The first one, $G^0(\vec{r}_i, \vec{r}_i, \tau)$, represents the photons that migrate from this voxel to a detector. $\Delta V$ is volume of a voxel. Therefore, $W$ in Eq.(3) represents a normalized effect that photons originating from the source migrate through voxel $j$, then further migrate to the detector during a total time of $t$. In the case of diffusion or scattering change, both $G^0$ in the integral of Eq.(3) are replaced by $\nabla G^0$.

$$w[\vec{r}_j, \vec{r}_i, t] = \frac{\Delta V}{G^0(\vec{r}_j - \vec{r}_i, r, \tau)}$$

Thus, $\frac{\Delta V}{\nabla G^0}$ represents the ratio of mean square of noise to the expected mean square deviation in the change of parameters (structural noise).

Since $W$ does not relate to the position and optical parameters of hidden objects, having $W$ for a given reference system (either homogeneous or inhomogeneous), the inverse matrix $[W^T W + A]^{-1}$ can be precalculated and stored as a database, which can be used in clinical cases to find hidden objects. This strategy separates time-consuming work in inversion processes into two parts: Pre-computation is time-consuming and may require the use of a supercomputer. However, it greatly reduces the burden of performing inverse processes in daily clinical cases.

One of the main difficulties in inversion is that most inverse problems are ill-posed. If no noise existed, an inverse image could be reconstructed from Eq.(2) via:

$$X' = Y W W$$

The existence of a small amount of noise should not have much effect on the results obtained. However, the matrix $W W$ is generally ill-posed or near singular. In other words, this matrix has some near-zero eigenvalues. This occurs when the number of measurements is less than the number of unknown parameters $N$ or when the measured signals are not fully independent of each other.

In this case, the effect of small noise will be magnified in the inverse process, and the solution of inversion becomes unstable. One of the methods to overcome the ill-posed problems is regularization, which adds a $\lambda$ to the matrix $W W$. $\lambda$ is relatively small compared to the matrix $W W$; therefore, regularization makes the matrix well-defined, but does not change the characteristics of the image map. The value of $\lambda$ is set according to the experimental noise level and structural noise present in the change of optical parameters. If $\|W W W\| < \lambda$, one may use the following expansion to correct the error introduced by regularization:

$$[W W W + \lambda I]^{-1} = \text{exp}(-\lambda^{-1} W W W) \text{exp}(-\lambda I)$$

The iterations in Eq.(4) are equivalent to the above expansion. If noise $n$ exists, $Y = W X + n$. One wants to find an inverse operator, $\hat{X}$, $\approx X$, which gives the estimated value $\hat{X}$ of $X$, that, in the sense of statistical average, has minimum error. Shaw has derived the following solution:

$$\hat{X} \approx W^{-1} Y = (W W W + \lambda I)^{-1} W W W$$

with $\ldots$ statistical average, $\Delta X = \hat{X} - X$. We see that Eq.(6) is a well-posed expression. This approach is the so-called “well-posed stochastic extension of ill-posed linear processes” or “statistical regularization.” Comparing Eq.(4) and Eq.(6), $\Delta X$ in Eq.(4) is related to $\epsilon = n / \sqrt{AX A X}$. Thus, $\lambda$ represents the ratio of mean square of detector noise to the expected mean square deviation in the change of parameters (structural noise).

The key point is that since $W$ is only reference-related, and does not relate to the position and optical parameters of hidden objects, the inverse matrix $[W^T W + A]^{-1}$ of a given pattern of the reference system, which can be either homogeneous or inhomogeneous, can be pre-calculated and stored as a database for various patients for clinical use.

Our tests show that this novel inverse procedure converges after only 2–4 iterations, which is much faster than the ART or SART procedures currently used. It takes about
one minute to form an image in our reconstruction tests on a Silicon Graphic Instruments (SGI) workstation computer. To demonstrate the present technique, the following experiment was performed. Schematic drawings of the experimental arrangement are shown in FIGS. 1(a) and 1(b). Ultrashort pulses of 100 fs pulse duration at a wavelength of 625 nm were coupled into a rectangular shape random medium by an optical fiber. This geometry was chosen because it is easy to construct an analytical expression of Green’s function $G(y, x)$ in a finite sized 3D volume, which is suitable for testing the physical modeling and the inversion algorithm.

The scattered pulses around the medium were collected by 7 optical fibers and time resolved by a streak camera. The size of the sample was 60x60 mm and the height was 90 mm. The fibers were located at mid-plane. The source fiber was at the center of the boundary wall. Two fibers each were placed on the opposite and the side boundary walls of the sample, and one fiber detector was placed on the incident wall. The scattered pulses collected by the 7 detection fibers and a reference pulse were coupled onto the input slit of the streak camera for multi-channel detection. The medium was Intralipid solution with a transport free path of 2.5 mm and absorption length of about 500 mm. The hidden object was a black painted aluminum rod of diameter of 4.8 mm. Temporal profiles of the scattered pulses around the medium were measured. In this experimental setting, the structure was $z$-independent, so the reconstructed image is presented as a 2-D image. However, the present method could also be used as a 3-D imaging model.

As an example, a typical set of temporal profiles measured for one $S-D$ pair is shown in FIG. 2. In this case, the detector is located slightly across the medium in the line of incidence. Measurements of the uniform medium without the object and with the object placed in three locations 90 degrees apart are also shown. It is clearly shown that the intensity is reduced by introducing the absorbing object, and a larger reduction was observed when the object was placed in the line of the source detector pair. The measurement of 3 object positions is equivalent to 3 measurements by rotating the $S-D$ pairs by 90 degrees while fixing the object location.

In the image reconstruction, an area in the sample was divided into $28x28=784$ voxels, which corresponds to an actual voxel size of $2 \times 2 \times 2$ mm. Measurements of 7 $S-D$ pairs with the above mentioned object locations were used. For each temporal intensity profile, intensity data at 40 time slices uniformly distributed from 602 ps to 2045 ps were used. Thus, the total number of input data points was $21 \times 140 \times 540$. This is one of the important features of our method—the use of hundreds of time slices from the temporal profile of one $S-D$ pair for image reconstruction gives much more information than data obtained in the frequency domain with much higher speed resolution in sub-mm to mm range to detect a defect. The robustness of the method was demonstrated with a small number of fibers. In our programs, $Y$ and $W$ are magnified by a factor of 100. Our regularization parameters are spacing independent:

\[ \lambda_2 = \exp(\lambda_1 \text{ran}) \]  

FIGS. 3(a) through 3(c) show images obtained for $X(1)$ in EQ.(4) with different regularization parameters. Using large $\lambda_2$, the image of the hidden object has already appeared after the first iteration. With a decreasing of $\lambda_2$ down to $10^{-2}$, the image is gradually broken.

FIGS. 4(a) through 4(h) show the results of different numbers of iterations, when the small regularization $\lambda_2$ is used. We see that after $m=50$ iterations, the image of the hidden object begins to appear. After $m=500$, the image becomes stable as no visible change in the shape of the object occurs between $m=500$ to $m=2000$.

FIGS. 5(a) and 5(b) show an image obtained where (a) $\lambda_2=1000$, without iteration, by running 1 minute on a Silicon Graphic Incorp. (SGI) Indy computer where $[W^TW+A]^{-1}$ is stored; and (b) $\lambda_2=10^{-1}$, with 2000 iterations, by running 3 hours on the same computer, respectively. As can be seen, the two images are similar, but the latter has better resolution. Noting that the difference of regularization parameters for these two images is up to 5 orders of magnitude, the stability of the imaging process for the present technique is confirmed.

In both FIGS. 5(a) and 5(b), the presence of an absorber can be clearly seen. The location of the maximum change is about 7 mm away from the center which is about the actual location of the object (10 mm). The full width of half maximum of the absorber is 8 mm which is comparable to the diameter of the object (4.8 mm). The fluctuation at other spatial locations are less than one third of the peak value.

Using different regularization parameters, the same location of the absorber was found, but the maximum peak value and the full width of half maximum were different. One possible reason that the center of the image deviates from that of the experimental set is that the hidden object is not a pure transparent scattering absorber, and the possible effect of reflection on the surface of the rod was not included in our physical model.

For comparison, the result using the SART inversion algorithm, commonly used by others, after 100 iterations (taking $X=0$ as initial input), which runs 3 hours on the same SGI workstation, is shown in FIG. 6. There is no clear image of the absorber, noticing that the maximum absorption coefficient is only 0.0025 which is about 40 times smaller than that obtained by our new algorithm.

We have also tested our technique on simulated temporal data with 15% white noise added. A clear image of a single absorber on the correct position was obtained. These results show that our approach is noise-resistant. This inversion method can include a change of diffusion coefficients, $\Delta D(\text{r}) = \Delta D(\text{r})$, as described before for detecting scattering defects in a highly scattering host medium.

It should be noted that a reconstruction algorithm which is suitable for clinical applications must be computationally rapid in running time while maintaining mathematical integrity. An inverse algorithm mainly based on Fourier transform runs in the fastest way. In order to make a Fourier transform deconvolution available, the condition of "translation invariance" should be satisfied. In other words, the propagator $K(y, x)$ must be the function of $y-x$. This condition is violated in experimental settings in the following three ways: (1) the media is not uniform; (2) there are boundaries on which the light sources and detectors are setting; (3) the propagator here is a function of $(r_x r_y r_z)$; therefore, it is impossible to make a Fourier transform for both $r_x$, $r_y$ and $r_z$. Among above listed violations, (1) is relatively soft, since we can assume a reference with uniform background, and put non-uniform as an image. On the other hand, reconstruction based on the inverse matrix method does not require the condition of translation invariance and can be used for more general cases. For purposes of clinical applications, a three-dimensional (3D) reconstruction algorithm is necessary. Because light diffuses in 3D space, the measurements on a specific layer are affected by the hidden objects on other layers. In extending our approach to the 3D case, we face a new difficulty. The computational complexity to inverse a matrix is about $N^3$, where $N$ is the size of the matrix.
matrix. If one supposes that the size on the third dimension is divided into 30 grids, the computing complexity to inverse a matrix in the 3D case is about 27,000 times that in the 2D case, which makes the pre-computation of an inverse matrix for 3D case unfeasible. To overcome this difficulty, we propose adding a 1D Fourier transform to the 2D matrix inversion.

Therefore, a novel inverse algorithm for obtaining images of 3D objects hidden in scattering media is taught in this invention, the method combining a 2D matrix inversion with a 1D Fourier transform inversion. In our approach the conditions for Fourier transform available are properly treated. This method greatly reduces the computational burden, compared to standard 3D matrix inversion methods. This approach can be used for both time-resolved data and frequency domain data. Using the above mentioned pre-computation and database storage strategy, we tested the present technique. It takes about 30 minutes on a Silicon Graphic Indy 4400 computer to obtain a 3D image of 28x28x32 voxels of mm objects in cm’s imaging media.

The source-detector pairs are arranged on the boundary of scattering media, such as breast and brain, in a 2D plane (the x-y plane), which is scanned along the z direction. Accordingly, z coordinates of sources and detectors are the same, thereby eliminating the violation (3) mentioned above. The reference system is assumed to be uniform and infinite along the z direction. This assumption leads to some deviation in the reconstructed image due to finite z-size in experimental setting. Since there is no source and detector setting on the z-end plane, this end effect becomes less serious. Under the above experimental setting and assumption, W satisfies z-translation invariance. In other words, it is a function of z, (r), where z, is z-position of source-detector plane and z is z-coordinate of a voxel. After making a one-dimensional Fourier transform over z-z, we obtain K independent 2D matrices, W,,(k), parametrized by k, with K the number of grid-points in the Fourier k-space. We separately calculate the K inverse matrices [W,,(k)'W,,(k)+A(k)]-1, k=1,2,3, . . . ,K, where A(k) is a matrix for regularization. These inverse matrices are stored as database for later reconstruction of image in different hidden object cases. The computational complexity now is K times that of inverse of a W,, matrix, which is much less than that of inverse of a W,, matrix.

The experimental data in time-resolved (or frequency domain) are Y(r, t, z), where r t and z are (x,y), coordinates of detector and source, respectively, and t is the slice (or w is frequency). We make a Fourier transform over z to obtain Y(r t, w(k), k=1,2,3, . . . ,K. We then obtain the image in the k-space using the following matrix multiplication:

\[ X(k)=Y(r\cdot t, w(k)) W,,(k)' W,,(k)+A(k)^{-1} \]

Then, the inverse 1D Fourier transform of X(k) over k generates the 3D distribution of the change of absorption coefficients or scattering coefficients.

A simulated experimental setting for a 3D image obtained using a plurality of source-detector (S-D) pairs is shown in FIGS. 7(a) and 7(b). The S-D pairs are arranged around a square of size 60x60 mm². This arrangement of S-D pairs is then rotated 90 degrees and 180 degrees and the plane is scanned 32 steps along z in a range of 120 mm. For each simulated temporal profile, intensities at 40 time slices uniformly distributed from 602 ps to 2045 ps are taken. The number of sampling data are 7x3=40x32. Data both with and without hidden objects are computed to produce Y=1001n(I/I0), adding uniform distributed noise in ±10% range, where I and I₀ are intensity with and without hidden objects, respectively. The volume of sample is divided into 28x28x32 voxels. Two arrangements of hidden absorption objects are separately shown in FIGS. 8(a) and 8(b). The cross-sections of the hidden objects are 4x4 mm² and 6x6 mm². In case (a), both objects are located from the 9th z-layer to the 15th z-layer (about 20 mm in length). In case (b), one is located from the 9th layer to the 13th layer (about 20 mm in length) and another is located from 17th layer to the 20th layer (about 16 mm in length). The W is calculated using Green’s function method based on the diffusion equation. For absorbing coefficients, it is given by the following equation:

\[ W,,(r, t, z) = \frac{4\pi Dc(r, t, z)^{-1/2}}{4\pi Dc(r, t, z)^{-1/2}e^{-\frac{r-r^*}{4Dc(r, t, z)^{-1/2}}} - \frac{r-r^*}{4Dc(r, t, z)^{-1/2}}} \]

Where G,, is 2D Green’s function for reference, D is the diffusion constant and c is the speed of light in the medium. Scattering objects with different l can be also calculated as mentioned above for 2D case. The background transport mean free path is chosen as l,=2.5 mm, and the absorption length l,=500 mm. The absorbing objects have l,=2.5 mm. In making Fourier transform and computing inverse matrix [W,,(k)'W,,(k)+A(k)^{-1}], the regularization matrix is set as A(k)=λ(β(k+1)), with λ and β are parameters for regularization. In this calculation λ=10^-2 and β=0 are taken. The images of the absorption objects are separately shown in FIGS. 9(a) and FIG. 9(b), which correspond to FIGS. 8(a) and FIG. 8(b), respectively. In FIGS. 9(a) and 9(b), index K is the index of layer in z coordinate. The images of hidden objects appear in the right layers where the objects are arranged, with a resolution of about 4 mm. There are some aliased images appearing near the z-end because of discrete sampling.

The following comments, observations, objects, features, uses, applications and/or advantages may be made about the present invention:(1) Temporal intensities extracted at multiple time slices of scattered light profile measured using multiple source detector pairs around turbid media are used as input data for the inversion to obtain the image maps of the media.

(2) An image reconstruction algorithm for imaging highly scattering turbid media is developed. The inversion procedure consists of input scattered light intensity data at different time slices, physical modeling of light propagation in random media, inversion computation algorithm, reconstructed image of spatial distributions of key optical parameters of random media, and image displays.

(3) Using different theoretical models for describing photon migration in random media for imaging. The theory includes transport theory for photon migration, and its approximations, such as the diffusion theory and the telegraph equations.

(4) Key optical parameters, such as the absorption coefficient, the index of refraction, the transport scattering length, the scattering length, and the diffusion constant, are mapped for imaging the internal structure of the turbid media at different light wavelengths. A difference in both absorption and scattering can be imaged to form a map of the internal structure of the turbid media in 3-D.

(5) A fast inversion algorithm is developed based on Shaw’s principle, Eq.(4), in which the weight function

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matrix, W (Eq.(3)), which relates a change in the properties of turbid media to the changes in measured light intensities, can be pre-computed and stored for fast image inversion for each patient.

(6) A cumulant formula is developed to relate the experimentally measured intensities to the prediction from theoretical models based on properties of the turbid media.

(7) 3-D images of spatial distribution of key optical parameters of turbid media can be obtained using this algorithm. 2-D slices of tomographic images can be obtained by taking a section of a 3-D image and displaying it to highlight the location of tumors.

(8) Use the algorithm to image non-invasively tumors and abnormality in human body, such as tumor growths in breasts, tumors in brain, cerebral hemorrhage in brain, hemorrhage in internal organs, prostate.

(9) Using the algorithm with temporal data at various NIR wavelengths from 700 to 1500 nm for image reconstruction for monitoring metabolic states of a given part of human body in vivo.

(10) This novel inverse reconstruction method can be combined with shadowgram type of image techniques to further improve spatial resolution and enhance the presence of the abnormality.

(11) Use single source optical fiber and multiple detector fibers for collecting temporal profiles of the scattered pulses.

(12) Use multiple input source fibers and multiple detector fibers for collecting temporal profiles of the scattered pulses. A time sharing beam deflector will be incorporated to switch the input from one source fiber to another.

(13) Multiple S-D optical fibers are mounted on bra-like or hat-like holders surrounding a breast or a head (brain) to detect temporal intensity profiles of scattered pulses from breast or head (brain) for imaging the internal structure of optical properties.

(14) The lasers used for imaging are Cr\(^{4+}\) Forsterite, Cr\(^{4+}\) YAG, semiconductor lasers, Nd:YAG, and/or Ti:Sapphire lasers. The laser pulses at different wavelengths will be coupled to optical fiber by a time sharing scheme to deliver to the scattering media for spectral imaging.

(15) Temporal intensity profiles of scattered pulses around scattering media are measured using time resolved detection methods, including streak camera, ultrafast pin diodes, fast photomultipliers.

(16) Reconstructed images are to be displayed in 3-D or in 2-D tomography slices.

(17) Manipulating images obtained from claim 9 at different wavelengths to construct difference, sum, ratio and/or hat-like holders surrounding a breast or a head (brain) for imaging the internal structure of optical properties.

(b) determining the intensity of said diffusive component at a plurality of points in time; and

(c) using said intensity determinations to form an image of the object in the highly scattering turbid medium, said using step comprising using a mathematical inversion algorithm to generate an image of the highly scattering turbid medium, said mathematical algorithm being

\[x^{i+1} = (W^T W + \Lambda)^{-1} Y\]

wherein W is a matrix relating output at source and detector positions \(r_s\) and \(r_d\) respectively, at time \(t\) to position \(r\), \(\Lambda\) is a regulation matrix, chosen for convenience to be diagonal but selected in a way related to the ratio of the noise, \(<n^2>\) to fluctuations in the absorption (or diffusion) \(X_f\) that we are trying to determine:

\[\lambda_n = \lambda_{n-1} + \lambda_{n-1}\frac{<n^2>-<n>^2}{\lambda_{n-1}}\]

where \(\lambda_{n}\) is the data collected at the detectors, and \(X_{f}\) is the \(k\)th iterate toward the desired absorption information.

2. The method as claimed in claim 1 wherein said pulse of light has a wavelength in the visible to near infrared region of the spectrum.

3. The method as claimed in claim 2 wherein said pulse of light has a wavelength of about 700 nm to about 1500 nm.

4. The method as claimed in claim 1 wherein said pulse of light is an ultrashort pulse of light.

5. The method as claimed in claim 1 wherein said pulse of light is a laser pulse emitted from a laser selected from the group consisting of Ti:Sapphire lasers, Cr\(^{4+}\) Forsterite lasers, Cr\(^{4+}\) YAG lasers, semiconductor lasers and Nd:YAG lasers.

6. The method as claimed in claim 1 wherein said biological tissue is selected from the group consisting of human breast tissue, human brain tissue, human neck tissue and human prostate tissue and wherein said object is a tumor.

7. The method as claimed in claim 1 further comprising the step of detecting cancerous tumors in said biological tissue using fluorescence spectroscopy.

8. The method as claimed in claim 1 wherein said determining step comprises measuring the intensity of light at a plurality of points in the time frame spanning from 50 ps to 10 ns after illumination.

9. The method as claimed in claim 8 wherein said determining step comprises measuring the intensity of light at hundreds of points in the time frame spanning from 50 ps to 10 ns after illumination.

10. The method as claimed in claim 9 wherein said hundreds of points are determined by slicing the time frame into equal portions.

11. A method of forming a map of a highly scattering turbid medium, the highly scattering turbid medium being a biological tissue, said method comprising the steps of:

(a) illuminating the highly scattering turbid medium with a first pulse of light along a first axis of incidence, whereby the light emergent from the highly scattering turbid medium due to said first pulse of light consists of a ballistic component, a snake-like component and a diffusive component; and

(b) determining, at a plurality of times, the intensity of said diffusive component of the first pulse of light emergent from the highly scattering turbid medium at a plurality of locations; and

(c) illuminating the highly scattering turbid medium with a second pulse of light along a second axis of incidence,
Y is the data collected at the detectors, and $X_k$ is the $k$th iterate toward the desired absorption information.

13. The method as claimed in claim 11 wherein each of said first and said second pulses of light has a wavelength in the visible to near infrared region of the spectrum.

14. The method as claimed in claim 11 wherein each of said first and said second pulses of light is of a wavelength of about 700 nm to about 1500 nm.

15. The method as claimed in claim 11 wherein each of said first and said second pulses of light is a ultrashort pulse of light.

16. The method as claimed in claim 11 wherein said biological tissue is selected from the group consisting of human breast tissue, human brain tissue, human neck tissue and human prostate tissue and wherein said object is a tumor.

17. The method as claimed in claim 11 wherein said determining steps each comprise time-resolving light emergent from the highly scattering turbid medium.

18. The method as claimed in claim 11 further comprising the steps of:

(f) illuminating the highly scattering turbid medium with a third pulse of light along a third axis of incidence, said third axis of incidence intersecting a plane defined by said first and second axes of incidence, whereby the light emergent from the highly scattering turbid medium due to said third pulse consists of a ballistic component, a snake component and a diffusive component; and

(g) determining, at a plurality of times, the intensity of said diffusive component of the third pulse of light emergent from the highly scattering turbid medium at a plurality of locations;