The invention is a real-time takeoff and landing performance monitoring system for an aircraft which provides a pilot with graphic and metric information to assist in decisions related to achieving rotation speed (VR) within the safe zone of a runway, or stopping the aircraft on the runway after landing or take-off abort.

The system processes information in two segments: a pretakeoff segment and a real-time segment. One-time inputs of ambient conditions and airplane configuration information are used in the pretakeoff segment to generate scheduled performance data. The real-time segment uses the scheduled performance data, runway length data and transducer measured parameters to monitor the performance of the airplane throughout the takeoff roll. Airplane and engine performance deficiencies are detected and annunciated. A novel and important feature of this segment is that it updates the estimated runway rolling friction coefficient. Airplane performance predictions also reflect changes in head wind occurring as the takeoff roll progresses.

The system provides a head-down display and a head-up display. The head-up display is projected onto a partially reflective transparent surface through which the pilot views the runway. By comparing the present performance of the airplane with a predicted nominal performance based upon given conditions, performance deficiencies are detected by the system.
Look up airplane performance for $\mu = 0.005$ and $\mu = 0.040$.

Curvefit acceleration versus true airspeed.
INITIALIZE VARIABLES, CONSTANTS

ATMOSPHERIC CALCULATIONS

GENERATION OF BASIS FOR SCHEDULED PERFORMANCE

TABLE LOOKUP

FILTERING OF SENSED PARAMETERS

THROTTLE COMMAND

ENGINE PRESSURE RATIO PREDICTION

THRUST ESTIMATION

POINT MASS PERFORMANCE ESTIMATION

ESTIMATION OF ROLLING FRICTION COEFFICIENT

GENERATION OF BASIS FOR SCHEDULED PERFORMANCE

PREDICT RUNWAY REQUIRED TO ACHIEVE ROTATE SPEED

PREDICT RUNWAY REQUIRED TO STOP

GENERATE GO/ABORT SIGNAL/COMMAND

FIG. 6
FIG. 8C
FIG. 9A
FIG. 10A
The invention described herein was jointly made by employees of the United States Government and a contract employee in the performance of work under NASA Grant No. 31·79, and is subject to the provisions of Public Law 96-517 (35 USC 202) in which the contractor has elected not to retain title.

This application is a continuation-in-part of U.S. patent application Ser. No. 082,766 filed Aug. 6, 1987 and now U.S. Pat. No. 4,843,554 which issued June 27, 1989.

The invention is an airplane takeoff and landing performance monitoring system which utilizes runway ambient condition, flap setting, and airplane loading characteristic information, input both manually and continuously from transducers to a computer, to generate acceleration history curves for predicting airplane performance during takeoff and landing. The results of the airplane performance predictions are compared with measured performance during the progress of the airplane down the runway, and are depicted on both a head-up and a head-down display driven by the computer. An improved estimate of the runway coefficient of rolling friction may be derived by comparing measured with predicted performance.

The take-off and landing performance monitoring system provides the pilot with graphic and metric information to assist in decisions related to achieving rotation speed (VR) within the safe zone of the runway or stopping the aircraft on the runway after landing or take-off abort.

An object of the present invention is to provide a display warning the pilot that the airplane flap lever is in the wrong position for takeoff.

The head-down display indicates the position of the airplane on the runway, indicating runway used and runway distance remaining in predicting the runway distance needed to achieve rotation speed, and the runway needed to stop the airplane.

A comparison of measured and predicted values is utilized in detecting performance deficiencies. These comparisons and the runway length computations lead to GO/ABORT signals. An important feature of the algorithm is that the estimated runway rolling friction is updated based on measured acceleration performance, resulting in more accurate predictions of future performance. Airplane performance predictions also reflect changes in head wind occurring as the take-off roll progresses.

The head-down display indicates the position of the airplane on the runway, indicating runway used and runway available (to ground roll limit line and to the end of the runway), summarizes the critical information.
into a single situation advisory flag, shows engine failures and off-nominal acceleration performance, and indicates where on the runway particular events such as decision speed (\(V_1\)), rotation speed (\(V_R\)) and expected stop points will occur based on both measured and predicted performance. This display also indicated air speed, wind vector, recommended and measured engine pressure ratios (EPR), second-segment climb speed, and balanced field length (BFL).

The head-up display features a subset of the information available on the head-down display. It presents information such as measured EPR, off-nominal acceleration, air speed, current position, ground roll limit line, expected point where rotation speed will occur, and predicted stop points.

**DESCRIPTION OF THE DRAWINGS**

Other objects, features, and advantages of the invention will become apparent from the following detailed description of some preferred embodiments when read in conjunction with the appended drawings wherein:

FIG. 1 is a block diagram of the invention;

FIG. 2 is a flowchart of the pretakeoff segment;

FIG. 3 is a flowchart of the real-time segment;

FIG. 6 is a flowchart of the pretakeoff segment;

FIG. 7A depicts the head-down display presented to the pilot indicating the balanced field length for a particular set of takeoff conditions;

FIG. 7B depicts the graphic rescaling that occurs on the head-down display after the pilot enters the actual runway length;

FIG. 7C shows a situation advisory flag warning the pilot that the runway length is insufficient for takeoff under present conditions;

FIG. 7D depicts the head-up display indicating a right-engine failure before attainment of decision speed; FIG. 7E depicts the head-up display indicating a similar landing or abort condition.

**DETAILED DESCRIPTION OF THE INVENTION**

A preferred embodiment of a system in accordance with the invention is illustrated in FIG. 1, as generally comprising a plurality of transducers 14 for measuring parameters affecting airplane performance, a computer means 15 for receiving and operating upon input data from said plurality of transducers and for driving a display 16 arranged to graphically depict status information in an easily monitored format.

Conventional transducers 14 may be used to measure throttle position, engine pressure ratio, ground speed, long-track acceleration and calibrated air speed. As is well known, these transducers 14 may be positioned throughout the airplane, their outputs being collected at the cockpit and incorporated in to a conventional instrument panel such as may be found in a Boeing 737 manufactured by the Boeing Company. In the present invention, these transducer outputs are gathered together at a transducer interface panel 13, whence they become inputs to the computer means 15.

The preferred embodiment incorporates the flight control computer of the airplane, especially, a Norden model 11/70, as computer means 15; in this case, the inputs from many of the transducers are interfaced to the computer means 15 by the airplane manufacturer. Alternatively, many commercially available computers, such as a Digital Equipment Corp. PDP 11/70, provide an acceptable substitute.

Ambient temperature and pressure, runway wind, airplane weight, flap and stabilizer settings can be input from transducers 14 or manually, using a device such as the Navigation and Control Display Unit (NCDU) found in the Boeing 737 or equivalent data entry device compatible with the selected computer means. The NCDU 17, which normally is used to enter navigational and other information into the flight control computer of the airplane, also serves as an input device in the preferred embodiment of the takeoff and landing performance monitoring system.

As will be explained, algorithms within the computer 15 operate on the input data to generate a prediction of the airplane's acceleration performance. During the progress of the airplane down the runway, these predictions are compared with measured airplane performance. Performance deficiencies are determined and new predictions are made, taking into account the most recently measured performance data.

After the computer means 15 receives and operates upon the information from the NCDU and the transducers 14, the results are transmitted to the head-down display device 16 and to the head-up display device 18 using computer-to-display interfacing techniques familiar to those skilled in the art. The preferred embodiment can utilize existing Horizontal Situation Indicator (HSI) screen found in many modern transports (e.g., Boeing 737/767) as a head-down display device. However, as is known, a dedicated device such as a Sperry Arinc size D display could also be used. The HSI head-down display device 16 usually accommodates a map display used for navigation; however, while the airplane is on
the ground this device serves as display unit for the takeoff and landing performances monitoring system. Once liftoff occurs, the takeoff and landing performance monitoring system head-down display is replaced by the normal HSI information. The head-up display 18 is accomplished by projecting displayed information onto a partially reflective transparent screen utilizing techniques familiar to those skilled in the art. During flight, projection of takeoff performance monitoring system information ceases. The preferred embodiment of the invention incorporates both a head-up and a head-down display; however, the invention may be practiced using either display independently.

The system in accordance with the invention monitors takeoff and landing performance by continuously comparing the actual performance of the airplane with a nominal performance, including predictions of the runway length needed to attain rotation speed, the distance required to stop the airplane, and the remaining runway length.

At any point during the takeoff roll, the amount of runway required to achieve rotation speed is a function of the instantaneous speed of the airplane and how well it will accelerate until rotation speed is achieved. The instantaneous acceleration of the airplane is given by:

\[ a = \frac{Th - D - \mu(W - L)}{m} \]  

(1)

where

- \( a \) = Acceleration (feet/sec/sec)
- \( Th \) = Thrust (lbs)
- \( D \) = Drag (lbs)
- \( \mu \) = Rolling friction coefficient
- \( W \) = Weight (lbs)
- \( L \) = Lift (lbs)
- \( m \) = Mass = \( W/g \) (slugs)
- \( g \) = Gravitational acceleration (feet/sec/sec)

FIG. 2 shows the forces acting on the airplane. The thrust varies with the air speed and the friction coefficient depends on runway and tire condition.

Airplane acceleration represents a composite measure of the performance of the airplane; therefore, performance deficiencies can be detected by comparing actual instantaneous acceleration with a predicted nominal value.

The takeoff and landing performance monitoring system algorithm consists of two segments: a pretakeoff segment and a real-time segment. For each takeoff, the pretakeoff segment is utilized to generate nominal performance data particular to that takeoff run. The real-time segment keeps track of the runway used, the runway remaining, the runway needed to achieve rotation speed, and the runway needed to bring the airplane to a complete stop. These lengths and a comparison of the actual airplane performance with the nominal value from the pretakeoff segment are used in the GO/A-BORT recommendation.

In the pretakeoff segment, the airplane acceleration performance is predicted for two extreme values of rolling friction coefficients: a low value (\( \mu = 0.005 \)) and a high value (\( \mu = 0.040 \)) using the inputs: pressure altitude, ambient temperature, runway wind, airplane weight, center of gravity location, and selected flap setting.

The algorithm consists of three parts as shown in FIG. 3, and can be run off-line on the on-board computer or on ground support computers (not shown) with the results downloaded to the airplane computers.

The first part performs a flight manual look-up to determine the recommended engine pressure ratio for takeoff, the decision speed, the rotation speed and the second segment climb speed. The throttle setting needed to achieve the engine pressure ratio is also computed.

The second part of this segment computes the schedule acceleration performance of the airplane as follows. First the aerodynamic coefficients are extracted from the aerodynamic data base for the airplane as a function of the motion variables. The aerodynamic forces and moments are computed in the stability axis system of the airplane. These forces and moments are then transformed into the body axis system (as seen in FIG. 4). The components of the engine forces and moments along the body axes are determined using a manufacturer-supplied engine model. A manufacturer-supplied landing gear model is utilized in computing the forces and moments generated by it along the body axis system.

The resultant forces acting through the center of gravity along the body X and Z axes are obtained as:

\[ F_{X_{\text{total}}} = F_{X_B} + THR_{XB} + LG_{XB} \]  

(2)

\[ F_{Z_{\text{total}}} = F_{Z_B} + THR_{ZB} + LG_{ZB} \]  

(3)

The resultant moment about the body Y-axis (the pitching moment) is given by:

\[ M_{\text{total}} = M_B + THR_{MB} + LG_{MB} \]  

(4)

Using these forces, moments and body X and Z components of gravitational acceleration, the airplane acceleration along the body axes as

\[ u_B = (F_{X_{\text{total}}}/m) - g \sin \theta_B + (r_B - g \sin \phi_B v_B) \]  

(5a)

\[ \dot{w}_B = (F_{Z_{\text{total}}}/m) - g \cos \theta_B + (q_B v_B - p_B \dot{v}_B) \]  

(5b)

\[ \dot{H}_{CG} = \dot{u}_B \sin \theta + \dot{w}_B \cos \theta \]  

(5c)

with \( p_B = r_B = 0 \).

The pitching moment and the body Y-axis moment of inertia are used in computing the pitch acceleration using

\[ \ddot{\theta}_B = M_{\text{total}}/I_{YY} \]  

(6)

The rate of change of pitch attitude is written as

\[ \dot{\theta}_B = \dot{q}_B \]  

(7)

The parameters (\( \dot{\theta}_B, \dot{u}_B, \dot{H}_{CG}, \dot{w}_B, \dot{\theta}_B, \dot{v}_B, \dot{C}_G \)) are integrated using a second order Adam-Bashworth numerical integration scheme

\[ x_{n+1} = x_n + (\Delta T/2)(3x_n - x_{n-1}) \]  

(8)

to obtain new values for \( \dot{\theta}_B, \dot{u}_B, H_{CG}, \dot{w}_B, \dot{\theta}_B, \dot{v}_B, D_{\theta}w \). Throttle position serves as the input to a throttle servo with the following dynamics:

\[ \dot{\theta}_B(n\Delta T) = \dot{\theta}_B[(n-1)\Delta T] + (1 - \zeta)\dot{\theta}_B(n\Delta T) \]  

(9)
The last part of this segment deals with curve fitting the along track acceleration, \( a \), as a function of the airplane true air speed, \( V_T \), to generate a set of coefficients for a "nominal performance" data set for the takeoff run. A least-square-error cubic polynomial curve fit method is utilized to generate

\[ a = A_0 + A_1 V_T + A_2 V_T^2 + A_3 V_T^3. \]  
10

This process is carried out twice; once for the low friction coefficient and a second time for the high friction coefficient. FIG. 5 illustrates the results obtained from the pretakeoff segment for one set of typical takeoff conditions.

A block diagram of the real-time segment is shown in FIG. 6. This segment performs the following functions:

1. Initially calculates the required throttle setting for takeoff
2. Monitors the engine in terms of parameters such as engine pressure ratio, fuel flow, exhaust-gas temperatures, and engine rotational speed
3. Monitors the performance of the airplane in terms of its acceleration performance
4. Estimates the runway rolling friction coefficient
5. Predicts the distance required to achieve rotation speed
6. Predicts the distance required to stop the airplane and
7. Generates GO/ABORT signals.

The real-time segment requires several input parameters. Some of these are one-time inputs while others are continuously needed inputs. Ambient temperature, ambient pressure, runway wind, weight, flap setting, stabilizer setting, runway available for rotation (i.e., distance to the ground roll limit line), runway available for stopping, and nominal rolling friction coefficient are one-time inputs, whereas throttle position, engine pressure ratio, ground speed, along track acceleration, and calibrated air speed are needed continuously.

The pressure altitude and ambient temperature inputs are used to compute the air density, and temperature and pressure ratios (atmospheric calculations) once during the real-time segment. The generation of a basis for scheduled performance consists of interpolating between the sets of coefficients generated in the pretakeoff segment (equation 10) to obtain a set of coefficients corresponding to the input value for nominal rolling friction coefficient. This computation gives an initial basis for performance comparisons.

Two table lookups are performed in this segment. The first lookup obtains the flight manual recommended stabilizer setting for the given airplane loading configuration. The nominal lift and drag coefficients for the present takeoff roll, increments in lift and drag coefficients with full deflection of the flight and ground spoilers are also determined. The other lookup function is identical to the one in the pretakeoff segment.

Values for the continuously needed parameters are supplied by sensors on the airplane. Before use by the system these sensor outputs are processed through a filter implementation. The measured acceleration and ground speed are processed through a second order complementary filter to estimate the bias present in the acceleration signal as follows:

\[ \hat{a}_n = \hat{a}_{n-1} + K_n (a_n - \hat{a}_n) \]

where

\[ \hat{a}_n = \left[ \begin{array}{c} x_1(n) \\ x_2(n) \end{array} \right] \]

\[ V_G = \left[ \begin{array}{c} V_G \\ a_M \end{array} \right] \]

\[ v_G = a_1(n) \]

The acceleration output from the complementary filter \( (a_F) \), measured values of engine pressure ratio (left and right), and calibrated air speed are passed through a first order lag filter to remove noise, and the outputs from this filter are the values used by the system.

From the manufacturer supplied engine model corresponding to the specific type of airplane involved, an empirical model of the steady state behavior of the engine pressure ratio and thrust is extracted and used to predict these parameters as follows:

\[ EPR_{left} = R_{left} \cdot Temp_{cond} \]

\[ THR_{right} = T_{right} \cdot EPR_{right} \cdot MACH \]

A point mass formulation of the equations of motion is used to estimate the performance of the airplane. First the wind speed and measured ground speed are combined to obtain true air speed, Mach number and dynamic pressure. The nominal life and drag coefficients yield the lift and drag forces. Combining these with the weight and rolling friction coefficient (input value), and the estimated thrust (based on measured engine pressure ratio) results in an estimated airplane acceleration. The measured ground speed is numerically integrated (rectangular integration) to obtain distance along the runway.

The new estimate of the current air speed (CAS) is derived by summing the previously derived ground speed \( (V_{WRW}) \) and the head wind component of the runway wind speed \( (V_{WRW}) \)

\[ CAS = V_G + V_{WRW} \]

The new estimate of the head wind component of the runway wind speed \( (V_{WRW}) \) is derived by adding the previous estimate of the head wind component of the runway wind speed \( (V_{WRW}) \) to the difference between the measured current air speed (CAS) and the estimate of the calibrated air speed (CAS) derived in equation 14.

\[ V_{WRW} = V_{WRW} + (CAS - CAS) \]

Another salient feature of this algorithm is the update of the runway friction coefficient in real-time. The estimation takes place as follows. First, the thrust is represented as a cubic in air speed

\[ THR = T_0 + T_1 V_T + T_2 V_T^2 + T_3 V_T^3. \]  
65
At any true air speed, the acceleration corresponding to two rolling friction coefficients can be written as

\[
a = \left( g(T_0 - \omega W) + T_{1VT} + (T_2 - \frac{1}{2} p_{SCD} + \frac{1}{2} \mu p_{SCD} \frac{W}{T} \frac{\mu}{T}) \right) \frac{T}{W}
\]

where

- \( \mu_2 \): estimate of the actual runway friction coefficient
- \( \mu_1 \): assumed friction coefficient
- \( \Delta \mu \): difference in the friction coefficients.

Thus the actual rolling friction coefficient is estimated as

\[
\Delta \mu = \mu_2 - \mu_1
\]

\[
= (a - \frac{\mu}{T}) (g(W - \frac{1}{2} p_{SCD} \frac{W}{T} \frac{\mu}{T})) \frac{\mu}{T}
\]

Immediately after this process the basis for scheduled performance is recomputed with \( \mu_2 \) as the present estimate of the friction coefficient. (This process can be repeated during the run as many times as appropriate.)

The runway required to achieve rotation speed is computed by a ten step rectangular integration scheme between the present true air speed and the true air speed for rotation. The acceleration in each interval is assumed to remain constant at a value given by the scheduled performance basis for the true air speed at the midpoint of the interval.

To calculate the estimated stopping distance, the system simulates the effect of a series of commands to deploy the flight and ground spoilers to reduce the throttle to an idle setting. Based on these assumptions, the following situation advisory signals are generated:

1. A "NULL" advisory signal will exist (indicating that the takeoff is proceeding satisfactorily) when no engine or performance flags are set and there is adequate distance left to stop on the runway or to reach rotation speed before reaching the ground roll limit for safe takeoff (viz., the "ground roll-limit line").

2. A "GO" advisory signal will result when zero or one engine-failure flags are set, the airplane can still reach rotation speed before reaching the ground roll-limit line, and the runway remaining is less than that required for stopping the airplane.

3. "ABORT" advisory signals result when:
   - (a) The runway length available for reaching rotation speed is less than required;
   - (b) A performance-failure flag is set;
   - (c) One engine-failure flag is set at a speed less than decision speed;
   - (d) Multiple engine flags are set.

4. An "OPTION" advisory signal will result (indicating that both the GO and ABORT options are available) when one engine-failure flag is set at a speed equal to or greater than decision speed, the airplane can reach rotation speed before reaching the ground roll-limit line, and the runway distance remaining is greater than that required for stopping.

As stated previously, the system algorithm is composed of two segments. The pretakeoff segment is activated prior to the start of the takeoff roll, when the pilot enters ambient condition, loading and configuration information into the system through an appropriate input device such as the NCDU 17. Once the pretakeoff computations are complete, the head-down display (the HSI in the preferred embodiment) presents the format shown in FIG. 7A. The number at the departure end of the runway (shown as 4556 in the figure) represents the balanced field length (BFL) calculated for the given conditions. The balanced field length is the initial ground roll distance plus the greater of the remaining distance needed for the airplane to clear a predeter-
mined height at the departure end of the runway (35' in the preferred embodiment) after experiencing an engine failure at decision speed, or the distance required to brake to a stop after experiencing the same engine failure. (The initial ground roll distance is the distance required for the airplane to attain rotation speed using nominal thrust.) At the lower end of the runway graphic 21 is an airplane symbol 22 whose nose marks current longitudinal position. (Tracking the lateral movement of the airplane on the runway was de-implemented, because it was considered distracting to the pilot.) The calibrated air speed (CAS) symbol 23 consists of boxes connected by a horizontal line located at the same distance down the runway 21 as the nose of the airplane 22. The numbers inside the boxes represent calibrated air speed (CAS) in knots. Note that the nose of the airplane is about 500 ft. from the starting end of the runway; this increment is the "runway offset", representing where the on-ramp being used intersects the runway. The takeoff roll begins here.

Further up the runway, a shaded triangle 29 is shown; the apex indicates the longitudinal position where VR will be achieved, based on current conditions. The line 31 to the right of the runway (opposite the apex of the triangle) further denotes this position, and the number beneath it gives VR in knots. Similarly, the number and line 30 on the left side indicate the V1 speed and where it will be achieved.

In reality, there are two triangles, one lying on top of the other—the shaded one 29 representing the real-time prediction of where VR will be achieved and an open triangle 28 marking the initial prediction of where it should occur. The open triangle 28 is thus stationary, but the solid triangle 29 and the V1 30 and VR 31 lines move to indicate the updated estimates based on deviations away from nominal conditions. Just above the position of the triangles is a line 34 that stretches across the runway. This line 34 represents the ground roll limit for reaching VR.

The arrow 32 at the top left of the display represents the wind direction (relative to the runway) and the number beside it represents the wind speed in knots.

The recommended takeoff Engine Pressure Ratio (EPR) setting 33 and the second segment climb speed (V2) 34 in knots are shown at the top right corner of the display for reference. Prior to takeoff, the pilot enters the actual runway length. The system rescales the runway accordingly and inserts the actual runway length in place of the balanced field length as illustrated in FIG. 7B. In the event that the runway length is too short for a safe takeoff, the situation advisory flag (configured as a "STOP" sign) warns the pilot as illustrated in FIG. 7C. (Note that the solid triangle has moved forward across the ground roll limit line, thus indicating that rotation will be achieved too close to the end of the runway to takeoff and clear a specified height if one engine should fail at or after decision speed is reached.) If the flap lever is not positioned correctly when the takeoff begins (i.e., if it is different from the position used by the algorithm for the pretakeoff calculations, the display will appear as shown in FIG. 7D, where the large "X" 40 across the full display warns against takeoff.

The head-up display presented prior to takeoff is depicted in FIG. 7E. The solid rectangle 51 at the bottom of the runway graphic denotes longitudinal position of the center of gravity of the airplane. The apex of the triangle 52 halfway down the runway shows the predicate position where rotation speed (VR) will be reached. The numeric "13" 53 denotes pretakeoff air speed (in this case, due to a 13-kt headwind). The horizontal line 54 across the runway at this position indicates the limit of the distance available for the airplane to reach rotation speed VR. (Engine-pressure-ratio (EPR) bars 56, 57 emanate upward from this position, but are not yet visible on the display, because the engines are still at idle.) At the far (upper) end of the runway symbol 58 is an off-nominal-acceleration indicator 60 (arrow that translates along a horizontal scale). Leftward displacement of the indicator arrow 60 indicates an acceleration deficiency. The off-nominal acceleration arrow 60 remains stationary for minor fluctuations in acceleration (5% is used in the present embodiment), because minor fluctuations are not important to the pilot and jittering of the arrow would be distracting. Hence, arrow 60 only moves when the information it provides becomes important to the pilot.

FIG. 8A illustrates the head-down display depicting a situation with the airplane well into the takeoff run. From the divergence of the triangles 28, 29, it is apparent that the airplane is performing in excess of the predicted nominal performance, because the most recent prediction indicates that rotation speed will be attained sooner than the original nominal prediction. Excess throttle setting above the recommended value or better acceleration performance than expected for the given throttle setting or both account for this situation. In this situation, EPR bars 56, 57 extend beyond the EPR target line 47.

FIG. 8B represents the head-down display of a situation where the airplane performance is below expectation, that is, it is taking longer than expected to achieve rotation speed. Since there is no indication of an engine failure, under performance is due to a lower than recommended throttle setting or poor acceleration performance or both.

FIG. 8C shows that the head-down display situation advisory flag 65 alerts the pilot whenever the acceleration deficiency reaches a specified value (15% in the preferred embodiment), even if the engine are functioning properly. The predicted stop point 35 also becomes visible.

FIG. 8D depicts the head-up display for an acceptable takeoff underway on a balanced field (i.e., minimum runway length for the existing conditions). The two triangles 52, 62 are superimposed and remain so as long as acceleration performance is nominal. The EPR bars 56, 57 indicate that both engines are operating satisfactorily and at approximately the same level.

FIG. 9A shows the head-down display that appears when an engine becomes inoperative before decision speed is attained. The star 35 indicates where the airplane will stop with the application of maximum braking and spoilers. The EPR bar on the right side 57 changes color to indicate the failure, and the situation advisory flag 65 (STOP sign) appears.

FIG. 9B depicts the head-down display where an engine becomes inoperative after decision speed has been attained. The location of the star 35 beyond the end of the runway indicates that inadequate stopping distance remains. The situation advisory flag 24 recommends continuing with takeoff in spite of the engine inoperative indication 57, because insufficient runway remains for stopping.
FIG. 9C illustrates the head-down display where an engine becomes inoperative after decision speed has been achieved, but where adequate stopping distance is still available. The situation advisory flag 41 is presented as a flashing amber inverted triangle to indicate that both go and stop options are available; (current FAA regulations might require the pilot to proceed with takeoff).

The situation depicted in FIG. 9D is for the head-up display during a right-engine failure at about 85 knots on a runway somewhat longer than a balanced field. The EPR bar on the right side 57 has turned red and is shrinking, and the red situation advisory flag (STOP sign) 65 has appeared. Further, the triangles 52, 62 have separated significantly. Just ahead of the airplane symbol, 51, and “X” stop symbol 63 has appeared indicating the point at which calculations indicate the airplane will stop if maximum braking is initiated immediately.

The initiation of an abort (executed by a rapid pull back of the throttle) causes most of the takeoff information to be removed from the head-down display leaving only information pertinent to the abort. FIG. 10A shows an head-down abort display. The solid and open triangles, the V1 and V2 lines, the ground roll limit line, the V1 and EPR numerics, the wind vector, and the engine flags disappear from the display. However, the calibrated air speed 23 in the box to the left of the airplane symbol is replaced by ground speed in knots. The “X” 35, however, remains (representing the stop point using maximum braking, full spoilers, but no reverse thrust) and a new oval symbol 36 appears on the display. This new symbol 36 indicates the position where the airplane will stop using the present level of deceleration (in this case, less than full braking).

FIG. 10B shows the head-up abort display. As with the head-down display, all takeoff-related information has disappeared and the only symbols left are the airplane 51, its ground speed 53, the predicted stop-point using maximum braking 63 and the predicted stop-point using the current level of measured acceleration 64. This display indicates that less than full braking is being applied.

In the preferred embodiment, specific colors and shapes of the situation advisory flag(s) have specific meanings for different conditions, viz.:

<table>
<thead>
<tr>
<th>COLOR</th>
<th>FLIGHT CONDITION</th>
<th>RECOMMENDATION</th>
</tr>
</thead>
<tbody>
<tr>
<td>No Flag</td>
<td>(1) Takeoff is proceeding normally</td>
<td>Continue takeoff</td>
</tr>
<tr>
<td></td>
<td>(2) Airplane can reach VR before reaching ground-roll limit line, but its predicted stop point is beyond end of runway.</td>
<td>Takeoff</td>
</tr>
<tr>
<td>Green/Rectangle</td>
<td>(3) One engine has failed at a speed greater than V1; the airplane can still reach V2 before reaching ground roll limit line, but its predicted stop point is beyond the end of the runway.</td>
<td>Continue or abort the takeoff (plot option)</td>
</tr>
<tr>
<td>Amber/Triangle</td>
<td>(4) Same as (3) except airplane predicted stop point is on the runway.</td>
<td>Abort</td>
</tr>
<tr>
<td>(Blinking)</td>
<td>(5) Airplane will reach VR after it has passed the ground roll limit line.</td>
<td>Abort</td>
</tr>
<tr>
<td>Red/Stop-sign</td>
<td>(6) Multiple engines fail.</td>
<td>Abort</td>
</tr>
</tbody>
</table>

A failed engine is indicated by change in the size and color of the associated EPR bar—attached to the side of the runway graphic. Specifically, the bar shrinks in length and turns red when the EPR decrease exceeds a specified amount.

A performance arrow in the head-up display indicates deviation of the measured longitudinal acceleration from the nominal acceleration curve of values determined by the algorithm for the throttle setting being used. When the deviation exceeds a specified limit (see advisory flag condition (8) above, the abort flag comes on.

What is claimed as new and desired to be secured by Letter Patent of the United States is:

1. In an airplane takeoff and landing performance monitoring system including a display for graphically and continuously depicting the position of an airplane on a runway from and during takeoff relative to where particular events are predicted to occur, the improvement comprising:
   - transducer means for continuously sensing ambient conditions and airplane loading and acceleration information and generating information signals representative thereof;
   - computer means responsive to said information signals for generating an acceleration history curve and predicting future airplane performance from and during takeoff and landing based on said acceleration history curve and said information signals; and
   - head-up display means responsive to signals from said computer means for depicting the position of said airplane on the runway and for depicting the predicted location on the runway where said airplane will achieve any particular speed.

2. The invention as defined in claim 1 including a first means in said transducer means for sensing runway conditions and generating a runway coefficient of rolling friction output signal included in said information output signals; and
   - means in said computer means for storing and updating an initial the estimated runway coefficient of rolling friction based on said information output signals.

3. The invention as defined in claim 1 including second means in said transducer means for sensing wind conditions and generating a runway wind signal during the travel of the airplane down the runway and included in said information signals; and
   - means in said computer means for storing and updating an initial wind value based on said information output signals.

4. The invention as defined in claim 3, wherein the display includes indicia means for depicting wind direction and magnitude.
5. The invention as defined in claim 1, wherein the display means includes indicia means for depicting where on the runway rotation speed is expected to be attained based on the performance history curve and information input prior to takeoff.

6. The invention as defined in claim 5, wherein the display means includes indicia means for depicting where on the runway rotation speed is expected to be attained based on measured airplane acceleration.

7. The invention as defined in claim 6, wherein the display means includes indicia means for depicting where on the runway the airplane is expected to stop based upon an application of maximum braking and fully deployed spoilers.

8. The invention as defined in claim 7, wherein the display means includes indicia means for depicting the last point on the runway at which the airplane, upon achieving rotation speed, can, with one engine inoperative and using scheduled throttle-settings, clear a predetermined height at the departure end of the runway.

9. The invention as defined in claim 8, wherein the indicia means for depicting where on the runway the airplane is expected to stop based upon application of maximum braking and fully deployed spoilers is blanked out until it passes the indicia means for depicting the last point on the runway at which rotation speed can be attained and result in a safe takeoff.

10. The invention as defined in claim 9, wherein the indicia means for depicting where on the runway the airplane is expected to stop based upon application of maximum braking and fully deployed spoilers indicates the loss of a safe stopping option, when its position passes the end of the runway.

11. The invention as defined in claim 7, wherein the display means includes indicia depicting where on the runway the airplane is expected to stop based upon its measured current deceleration.

12. The invention as defined in claim 1, wherein the display includes indicia means for displaying a situation advisory flag.

13. The invention as defined in claim 1, wherein the display includes indicia means for displaying balanced field length prior to takeoff.

14. The invention as defined in claim 1, wherein the display includes indicia means for displaying air speed.

15. The invention as defined in claim 14, wherein ground speed is substituted for air speed in the event of an abort.

16. An airplane takeoff and landing performance monitoring system as defined in claim 1 including:
(a) sensor means in said transducer means for determining ambient temperature and pressure, runway wind, airplane weight and center of gravity, flap and stabilizer settings, throttle position, engine pressure ratio, ground speed, along track acceleration, and calibrated air speed and providing electrical signals representing these quantities to a computer means;
(b) computer data entry means for manually entering runway length information and an estimate of the runway rolling friction coefficient into the computer means;
(c) means in said computer means for generating and comparing an initial predicted acceleration curve and the measured acceleration of said airplane from and during takeoff; and
(d) means in said display means for displaying the deviation between said predicted acceleration and said measured acceleration responsive to signals from said computer means for graphically depicting information of the present performance of the airplane and predictions of future performance.

17. The invention as defined in claim 16, with the addition of means to update the runway coefficient of rolling friction based on performance data acquired during the travel of the airplane down the runway.

18. The invention as defined in claim 1, wherein the display means graphically depicts:
(i) an outline of the runway;
(ii) the position of the airplane on the runway;
(iii) the air speed of the airplane during takeoff;
(iv) the ground speed of the airplane during landing or takeoff abort;
(v) a situation advisory flag;
(vi) a runway length numeric;
(vii) a balanced field length numeric;
(viii) where on the runway rotation speed is expected to be attained based on information input prior to takeoff;
(ix) an updated prediction of where on the runway rotation speed is expected to be attained based on measured acceleration during the progress of the airplane down the runway;
(x) where rotation speed is expected to be attained;
(xi) where the airplane is expected to stop based upon application of maximum braking and fully deployed spoilers;
(xii) the last point on the runway at which rotation speed can be attained and the airplane with one engine inoperative and using scheduled throttle settings can clear, a predetermined height at the departure end of the runway;
(xiii) where on the runway the airplane is expected to stop based upon its measured deceleration;
(xiv) engine operational status indicia; and
(xv) engine pressure ratio indicia.

19. The invention as defined in claim 18, wherein the head-up display means includes means for displaying indicia on a transparent surface within the line of sight of a pilot, thereby enabling the pilot to observe status information while maintaining eye contact with the runway.

20. The invention as defined in claim 1, wherein the display means includes means for projecting displayed information onto a transparent surface within the line of sight of an airplane pilot as he looks toward the departure end of the runway.

21. The invention as defined in claim 20, wherein the transparent surface is the windshield of the airplane.

22. The invention as defined in claim 20, wherein the display means includes means for projecting displayed information onto a transparent surface within the line of sight of an airplane pilot as he looks toward the departure end of the runway.

23. The invention as defined in claim 1 wherein the head-up display means includes means for displaying information on a transparent surface within the line of sight of a pilot, thereby enabling the pilot to observe status information while maintaining eye contact within the runway.

24. The invention as defined in claim 23, wherein the head-up display includes means for graphically displaying engine pressure ratio by means of parallel bars, each of which varies in height in response to the engine pressure ratio of a particular engine.
25. The invention as defined in claim 1 wherein said display means includes means for warning a pilot that flaps of the airplane are not in proper position for take-off.

26. In an airplane takeoff and landing performance monitoring system including a display for graphically and continuously depicting the position of an airplane on a runway from and during takeoff relative to where particular events are predicted to occur, the improvement comprising:

- transducer means for continuously sensing ambient conditions and airplane loading and acceleration information and generating information signals representative thereof;
- computer means responsive to said information signals for generating an acceleration history curve and predicting future airplane performance from and during takeoff and landing based on said acceleration history curve and said information signals; and
- head-up and head-down display means responsive to signals from said computer means for depicting the position of said airplane on the runway and for depicting the predicted location on the runway where said airplane will achieve any particular speed.

27. The invention as defined in claim 26, wherein the head-up display means includes means capable of displaying a subset of the information displayed on the headdown display.

28. The invention as defined in claim 26 including second means in said transducer means for sensing wind conditions and generating a runway wind signal during the travel of the airplane down the runway and included in said information signals; and
- means in said computer means for storing and updating an initial wind value base on said information output signals.

29. The invention as defined in claim 26, wherein the display means includes indicia means for depicting where on the runway rotation speed is expected to be attained based on the performance history curve and information input prior to takeoff.

30. The invention as defined in claim 26 including analog means for indicating the level of engine performance.

31. The invention as defined in claim 26, wherein engine pressure ratio is a level of engine performance and indicated numerically.

32. The invention as defined in claim 26, wherein the display includes indicia means for displaying balanced field length prior to takeoff.

33. The invention as defined in claim 26, wherein the display includes indicia means for displaying air speed.

34. The invention as defined in claim 26 wherein said display means includes means for warning a pilot that flaps of the airplane are not in proper position for take-off.

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