Self–Consistent Model of Magnetospheric Electric Field, Ring Current, Plasmasphere, and Electromagnetic Ion Cyclotron Waves: Initial Results

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Short title: MAGNETOSPHERE–IONOSPHERE MODEL
Abstract.

Further development of our self-consistent model of interacting ring current (RC) ions and electromagnetic ion cyclotron (EMIC) waves is presented. This model incorporates large scale magnetosphere-ionosphere coupling and treats self-consistently not only EMIC waves and RC ions, but also the magnetospheric electric field, RC, and plasmasphere. Initial simulations indicate that the region beyond geostationary orbit should be included in the simulation of the magnetosphere-ionosphere coupling. Additionally, a self-consistent description, based on first principles, of the ionospheric conductance is required. These initial simulations further show that in order to model the EMIC wave distribution and wave spectral properties accurately, the plasmasphere should also be simulated self-consistently, since its fine structure requires as much care as that of the RC. Finally, an effect of the finite time needed to reestablish a new potential pattern throughout the ionosphere and to communicate between the ionosphere and the equatorial magnetosphere cannot be ignored.
1. Introduction

Electromagnetic ion cyclotron (EMIC) waves are a common and important feature of the Earth’s magnetosphere. The source of free energy for wave excitation is provided by the temperature anisotropy of ring current (RC) ions, which naturally develops during inward convection from the plasmasheet. The EMIC waves have frequencies below the proton gyro–frequency, and they are excited mainly in the vicinity of the magnetic equator with a quasi field–aligned wave normal angle [Cornwall, 1965; Kennel and Petschek, 1966]. These waves were observed in the inner [LaBelle et al., 1988; Erlandson and Ukhorskiy, 2001] and outer [Anderson et al., 1992a, 1992b] magnetosphere, at geostationary orbit [Young et al., 1981; Mauk, 1982], at high latitudes [Erlandson et al., 1990], and at ionospheric altitudes [Iyemori and Hayashi, 1989; Brä�sy et al., 1998].

Feedback from EMIC waves causes nonadiabatic pitch–angle scattering of the RC ions (mainly protons) and their loss to the atmosphere, which leads to the decay of RC [Cornwall et al., 1970]. This is especially important during the main phase of storms, when RC decay is possible with a time scale of around an hour or less [Gonzalez et al., 1989]. During the main phase of major storms RC $O^+$ may dominate [Hamilton et al., 1988; Daglis, 1997]. These ions cause damping of the $He^+$–mode EMIC waves, which may be very important for RC evolution during the main phase of the greatest storms [Thorne and Horne, 1994; 1997]. Obliquely propagating EMIC waves interact well with thermal plasmaspheric electrons due to Landau resonance [Thorne and Horne, 1992; Khazanov et al., 2007b]. Subsequent transport of the dissipating wave energy into the
ionosphere causes an ionospheric temperature enhancement [Gurgiolo et al., 2005]. This
wave dissipation is a mechanism proposed to explain stable auroral red arc emissions
present during the recovery phase of storms [Cornwall et al., 1971; Kozyra et al., 1997].
Measurements taken aboard the Prognoz satellites revealed a so-called “hot zone”
near the plasmapause, where a temperature of plasmaspheric ions can reach tens of
thousands of degrees [Bezrukikh and Gringauz, 1976; Gringauz, 1983; 1985]. Nonlinear
induced scattering of EMIC waves by thermal protons [Galeev, 1975] was used in the
RC-plasmasphere interaction model by Gorbachev et al. [1992] in order to account for
these observations. An extended analysis of thermal/suprathermal ion heating by EMIC
waves in the outer magnetosphere was presented by Anderson and Fuselier [1994],
Fuselier and Anderson [1996] and Horne and Thorne [1997]. Relativistic electrons
(≥ 1 MeV) in the outer radiation belt can also strongly interact with EMIC waves
[Thorne and Kennel, 1971; Lyons and Thorne, 1972]. Data from balloon-borne X-ray
instruments provides indirect but strong evidence that EMIC waves cause precipitation
of outer-zone relativistic electrons [Foat et al., 1998; Lorentzen et al., 2000]. These
observations stimulated theoretical and statistical studies, which demonstrated that
EMIC wave-induced pitch-angle diffusion of MeV electrons can operate in the strong
diffusion limit with a time scale of several hours to a day [Summers and Thorne, 2003;
Albert, 2003; Meredith et al., 2003]. This scattering mechanism is now considered to
be one of the most important means for relativistic electron loss during the initial and
main phases of storm. All of the above clearly demonstrates that EMIC waves strongly
interact with electrons and ions of energies ranging from ∼ 1 eV to ∼ 10 MeV, and that
these waves strongly affect the dynamics of resonant RC ions, thermal electrons and ions, and the outer radiation belt relativistic electrons. The effect of these interactions is nonadiabatic particle heating and/or pitch–angle scattering, and loss to the atmosphere. The rate of ion and electron scattering/heating in the Earth’s magnetosphere is not only controlled by the wave intensity–spatial–temporal distribution but also strongly depends on the spectral distribution of the wave power. Unfortunately, there are still very few satellite–based studies of EMIC waves, especially during the main phase of magnetic storms, and currently available observational information regarding EMIC wave power spectral density (mainly from the AMPTE/CCE and CRRES satellites) is poor [Engebretson et al., 2008]. Ideally, a combination of theoretical models and available–reliable data should be utilized to obtain the power spectral density of EMIC waves on a global magnetospheric scale throughout the different storm phases. To the best of our knowledge, there is only one model that is able to self–consistently simulate a spatial, temporal and spectral distribution of EMIC waves on a global magnetospheric scale during the different storm phases [Khazanov et al., 2006]. This model is based on first principles, and explicitly includes the wave generation/damping, propagation, refraction, reflection and tunneling in a multi–ion magnetospheric plasma. The $He^+$–mode EMIC wave simulations based on this model have showed that the equatorial wave normal angles can be distributed in the source region, i.e. in the region of small wave normal angles, and also in the entire wave region, including those near 90°. The occurrences of the oblique and field–aligned wave normal angle distributions appear to be nearly equal with a slight dominance of oblique events [Khazanov and
This theoretical prediction is supported by a large data set of the observed wave ellipticity [Anderson et al., 1992b; Fraser and Nguyen, 2001; Meredith et al., 2003]. The observation of a significant number of linearly polarized events near the equator suggests that waves are often highly oblique there. Using the more reliable wave step polarization technique, Anderson et al. [1996] and Denton et al. [1996] analyzed data from the AMPTE/CCE spacecraft, presented the first analysis of near linearly polarized waves for which the polarization properties were determined. They found a significant number of wave intervals with a wave normal angle $\theta > 70^\circ$, the highest $\theta$ ever reported. Compared to field–aligned waves, such highly oblique wave normal angle distributions can dramatically change the effectiveness (by an order of magnitude or more) of both the wave–induced RC proton precipitation [Khazanov et al., 2007b] and relativistic electron scattering [Glauert and Horne, 2005; Khazanov and Gamayunov, 2007]. Strong sensitivity of the scattering rates to the wave spectral characteristics, and the wide distribution of EMIC wave normal angles observed in the magnetosphere, suggests that in order to employ EMIC waves for heating and/or scattering of the magnetospheric particles in a model, the wave spectral distribution will require special care, and should be properly established.

The resulting EMIC wave power spectral density depends on the RC and cold plasma characteristics. On the other hand, the convective patterns of both RC ions and the cold plasmaspheric plasma are controlled by the magnetospheric electric field, determining the conditions for the interaction of RC and EMIC waves. Therefore, this electric field is one of the most crucial elements necessary to properly determine the
wave power spectral density. The region 2 field–aligned currents (FACs) couple the
magnetosphere and ionosphere. This large scale coupling determines and maintains a
self–consistent dynamic of the electric field and RC [Vasyliunas, 1970; Jaggi and Wolf,
1973; Garner et al., 2004; Fok et al., 2001; Khazanov et al., 2003b; Liemohn et al.,
2004]. A self–consistent simulation of the magnetosphere–ionosphere system should
provide, at least in principle, the most accurate theoretical electric field. The EMIC
waves resulting in the magnetosphere are not only a passive element in the coupled
RC–ionosphere system but also may influence the electrodynamics of coupling. During
storm times, the wave–induced RC proton precipitation not only changes the FAC
distribution, but can potentially modify the conductance and/or the neutral gas velocity
in the ionosphere–thermosphere system [Galand et al., 2001; Galand and Richmond,
2001; Fang et al., 2007a, 2007b]. Both of these characteristics are crucial elements
in the magnetosphere–ionosphere electrodynamics. Such wave–induced modification
can be especially important equatorward of the low–latitude edges of the electron and
proton auroral ovals where the wave–induced RC ion precipitation may be a dominant
energy source. In addition, electrons and protons do not interact in the same way with
the atmosphere. One should keep in mind that energetic protons ionize more efficiently
than electrons do because their energy loss for each produced electron is smaller than
that of energetic electrons [Galand et al., 1999]. Therefore, even if the proton energy
flux is smaller compared to the electron flux, the response of the atmosphere to protons
can be significant. The above arguments suggest that a self–consistent model of the
magnetospheric electric field, RC, plasmasphere, and EMIC waves is needed to properly
model wave spectral distribution and to improve the modeling of the large scale
magnetosphere–ionosphere electrodynamics.

In this study, we present a new computational model that is a result of coupling
two RC models developed by our group. The first model deals with the large scale
magnetosphere–ionosphere electrodynamic coupling and provides a self–consistent
description of RC ions and the magnetospheric electric field [Liemohn et al., 2001;
Ridley and Liemohn, 2002; Liemohn et al., 2004]. The second model is governed by a
coupled system of the RC kinetic equation and the wave kinetic equation. This model
self–consistently treats a mesoscale electrodynamic coupling of RC and EMIC waves,
and determines the evolution of the EMIC wave power spectral density [Khazanov et
al., 2006; Khazanov et al., 2007a]. The RC–EMIC wave model explicitly includes the
wave growth/damping, propagation, refraction, reflection, and tunneling in a multi–ion
magnetospheric plasma. Although RC ions and EMIC waves in the second model are
treated self–consistently, the electric field is externally specified. So far, the above two
models were used independently. As such, the main purpose of this paper is to present
a new self–consistent model of the magnetospheric electric field, RC, plasmasphere, and
EMIC waves along with initial results from the model simulations. The results presented
in this study were obtained from simulations of the May 2–4, 1998 geomagnetic storm,
that we previously analyzed using an analytical formulation of the Volland–Stern electric
field [Khazanov et al., 2006; Khazanov et al., 2007b].

This article is organized as follows: In section 2 we present a complete set
of the governing equations, and formulate the approaches used in the model
simulations. In the same section, we specify the initial/boundary conditions, and the interplanetary/geomagnetic characteristics, which drive our model. In section 3 the initial results from these simulations and discussion are provided. Finally, in section 4 we summarize.

2. RC–EMIC Wave Model and Magnetosphere–Ionosphere Coupling

2.1. Governing Equations

To simulate the RC dynamics we solve the bounce–averaged kinetic equation for the phase space distribution function of the major RC species \((H^+, O^+, \text{ and } He^+),\) as originally suggested in the models of Fok et al. [1993] and Jordanova et al. [1996].

The distribution function, \(F(r_0, \varphi, E, \mu_0, t),\) depends on the radial distance in the magnetic equatorial plane \(r_0,\) geomagnetic east longitude, kinetic energy \(E,\) cosine of the equatorial pitch angle \(\mu_0,\) and time \(t.\) For the \(He^+–\)mode EMIC waves we also use the bounce–averaged kinetic equation. This equation describes a physical model of EMIC waves bouncing between the off–equatorial magnetic latitudes, which correspond to the bi–ion hybrid frequencies in conjugate hemispheres, along with tunneling across the reflection zones and subsequent strong absorption in the ionosphere (for the observational and theoretical justifications of this model see [Gamayunov and Khazanov, 2008; Khazanov et al., 2007a]). The bounce–averaged wave kinetic equation was derived in our previous paper [Khazanov et al., 2006], and it explicitly includes the EMIC wave
growth/damping, propagation, refraction, reflection, and wave tunneling in a multi–ion magnetospheric plasma. In the present study, following Khazanov et al. [2006], we ignore the azimuthal and radial drifts of the wave packets during propagation, we do not include the wave tunneling across the stop zone, and consequently use a truncated wave kinetic equation. The resulting system of equations to drive RC–EMIC wave coupling takes the form:

\[
\begin{align*}
\frac{\partial F}{\partial t} + \frac{1}{r_0^2} \frac{\partial}{\partial r_0} \left( r_0^2 \left( \frac{dF}{dt} \right) \right) + \frac{\partial}{\partial \varphi} \left( \left( \frac{d\varphi}{dt} \right) F \right) \\
+ \frac{1}{\sqrt{E}} \frac{\partial}{\partial E} \left( \sqrt{E} \left( \frac{dE}{dt} \right) F \right) + \frac{1}{\mu_0 h(\mu_0)} \frac{\partial}{\partial \mu_0} \left( \mu_0 h(\mu_0) \left( \frac{d\mu_0}{dt} \right) F \right) \\
= \langle \left( \frac{\delta F}{\delta t} \right) \rangle_{\text{loss}},
\end{align*}
\]

(1)

\[
\frac{\partial B_w^2(r_0, \varphi, t, \omega, \theta_0)}{\partial t} + \langle \dot{\theta}_0 \rangle \frac{\partial B_w^2}{\partial \theta_0} = 2 \langle \gamma(r_0, \varphi, t, \omega, \theta_0) \rangle B_w^2.
\]

(2)

On the left–hand side of equation (1), all the bounce–averaged drift velocities are denoted as \( \langle \cdots \rangle \) and may be found in many previous studies [e. g., Khazanov et al., 2003a]. The term on the right–hand side of this equation includes losses from charge exchange, Coulomb collisions, RC–EMIC wave scattering, and ion precipitation at low altitudes [e. g., Khazanov et al., 2003a]. Loss through the dayside magnetopause is taken into account, allowing a free outflow of the RC ions from the simulation domain.

In equation (2), \( B_w \) is the EMIC wave spectral magnetic field, \( \omega \) and \( \theta_0 \) are the wave frequency and equatorial wave normal angle, respectively, \( \langle \dot{\theta}_0 \rangle \) is the bounce–averaged drift velocity of the wave normal angle, and \( \langle \gamma \rangle \) is a result of averaging the local growth/damping rate along the ray phase trajectory over the entire wave bounce period. The factor \( \langle \gamma \rangle \) takes into account both the wave energy source due to interaction with
the RC ions and the energy sink due to absorption by thermal and hot plasmas.

To perform bounce averaging in equation (2), the ray phase trajectory should
be known, and we obtain it by solving the set of ray tracing equations. For a plane
group these equations can be written as [e. g., Haselgrove, 1954; Haselgrove and
Haselgrove, 1960; Kimura, 1966; Khazanov et al., 2006]

\[
\frac{dr}{dt} = -(\frac{\partial G}{\partial k})_r,
\]

(3)

\[
\frac{r d\lambda}{dt} = -(\frac{\partial G}{\partial k})_\lambda,
\]

(4)

\[
\frac{dk_r}{dt} = k_\lambda \frac{d\lambda}{dt} + (\frac{\partial G}{\partial r})_r,
\]

(5)

\[
\frac{dk_\lambda}{dt} = -k_\lambda \frac{dr}{dt} + (\frac{\partial G}{\partial r})_\lambda.
\]

(6)

In equations (3)–(6), the Earth–centered polar coordinate system is used to characterize
any point \( P \) on the ray trajectory by length of the radius vector, \( r \), and magnetic
latitude, \( \lambda \). Two components, \( k_r \) and \( k_\lambda \), of the wave vector are given in a local Cartesian
coordinate system centered on the current point \( P \) with its axes oriented along the
radius vector and magnetic latitude direction, respectively. The function \( G(\omega, k, r) \) has
roots for EMIC eigenmodes only, i. e., \( G = 0 \) at any point along the EMIC wave phase
trajectories. Equations (3)–(6) are also used to obtain the off–equatorial power spectral
density distribution for EMIC waves, which is needed to calculate the bounce–averaged
pitch angle diffusion coefficient in the right–hand side of equation (1). (For more details
about the system of equations (1)–(6) and its applicability please see our previous
papers [Khazanov et al., 2003a; Khazanov et al., 2006; Khazanov et al., 2007a].)
The bounce–averaged pitch angle diffusion coefficient on the right–hand side of equation (1) is a functional form of the EMIC wave power spectral density, and \( \langle \gamma (r_0, \varphi, t, \omega, \theta_0) \rangle \) in equation (2) is a functional form of the phase space distribution function. So, there is a system of coupled equations, and the entire set of equations (1)–(6) self–consistently describes the interacting RC and EMIC waves in a quasilinear approximation. Compared to our previous RC–EMIC wave studies, which are based on equations (1)–(6) only [Khazanov et al., 2006; 2007b], we are now going to take into account the magnetosphere–ionosphere coupling by self–consistently treating the current closure between RC and the ionosphere.

Vasyliunas [1970] mathematically formulated a self–consistent model of the magnetosphere–ionosphere coupling by providing the basic equations governing the system. He outlined a logical chain of the model as follows: (1) the magnetospheric electric field determines the distribution of RC ions and electrons and, particularly, the total plasma pressure at any point; (2) from the plasma pressure gradients, the electric current perpendicular to the magnetic field can be calculated; (3) because the total current density should have zero divergence under magnetospheric conditions, the divergence of the perpendicular current density must be canceled by the divergence of FAC density, and so the divergence of the perpendicular current integrated along the entire field line gives the total FAC flowing into/out of the conjugate ionospheres; (4) from the requirement that FAC is closed by the horizontal ohmic currents in the ionosphere, the distribution of the electric potential in the ionosphere can be found; and (5) the ionospheric potential can be mapped back into the magnetosphere along
geomagnetic field lines, and the requirement that this “new” magnetospheric electric
field agrees with the “initial” magnetospheric field closes the magnetosphere–ionosphere
system.

To quantify the above logical chain, Vasyliunas [1970] used the following equations:

\[ \mathbf{J}_\perp (r_0, \varphi, s) = \frac{\mathbf{B}}{B^2} \times \left( \nabla P_\perp + \frac{P_\parallel - P_\perp}{B^2} (\mathbf{B} \cdot \nabla) \mathbf{B} \right), \]  

(7)

\[ J_{||,i} (\lambda(r_0), \varphi) = -B_i (\lambda(r_0), \varphi) \int_{s_S}^{s_N} \nabla J_\perp \frac{d s}{B(r_0, \varphi, s)}, \]  

(8)

\[ \nabla \mathbf{I}_i = j_{||,i} \sin \chi, \quad \mathbf{I}_i = \Sigma \left( -\nabla \Phi_i + \frac{\mathbf{V}_n}{c} \times \mathbf{B}_i \right), \]  

(9)

where \( P_\perp \) and \( P_\parallel \) are the total plasma pressure (we neglect the electron pressure in the
current study) perpendicular and parallel to the external magnetic field \( \mathbf{B} \), respectively,
and \( \mathbf{J}_\perp \) is the perpendicular current density. The FAC density at the ionospheric level
is \( J_{||,i} \) (positive for current flowing into the ionosphere), \( B_i \) is the magnetic field in
the ionosphere, and integration in equation (8) is done along the entire magnetic field
line between foot points \( s_S \) and \( s_N \). The coordinates \( (\lambda(r_0), \varphi) \) are the corresponding
ionospheric latitude and MLT for the magnetic field line crossing the equatorial plane at
\( (r_0, \varphi) \) (assuming that \( \varphi \) is the same at the equator and at the ionospheric altitude). In
equations (9), \( \mathbf{I}_i \) and \( \Sigma \) are the height integrated horizontal ionospheric current density
and conductivity tensor, respectively, and \( \chi \) is an inclination of the magnetic field (dip
angle). The electric potential at the ionosphere level is \( \Phi_i \), and \( \mathbf{V}_n \) is the velocity of the
neutral gas in the ionosphere. Following many previous studies, in the present study we
assume that the neutral gas corotates with the Earth and neglect the potential drop
between the ionosphere and the equatorial magnetosphere [e. g., Ebihara et al., 2004].
Finally, it should be noted that, in general, equation (9) is written for the northern and southern ionospheres with the corresponding FAC \( j_{||,i} \), while equation (8) gives only the total FAC flowing into/out of the conjugate ionospheres but the obvious equation \( J_{||,i} = j_{||,i}(s_S) + j_{||,i}(s_N) \) is held.

The set of equations (1)–(9) drives the RC, the EMIC waves, and the magnetospheric electric field in a self-consistent manner if all the initial and boundary conditions are specified and the ionospheric Hall and Pedersen conductances are known. A block diagram of the self-consistent coupling of the RC, EMIC waves, plasmasphere, and ionosphere is presented in Figure 1. The system characteristics in orange boxes are externally specified, and the dashed lines connect the model elements, which are currently not linked.

2.2. Approaches Used in Simulations

The geomagnetic field used in the present study is taken to be a dipole field. It is a reasonable approximation for the present study because the most important results are obtained from simulations of the May 2–3, 1998 period (\( Dst = -106 \) nT) when the Earth’s magnetic field is only slightly disturbed in the inner magnetosphere [e.g., Tsyganenko et al., 2003]. The convection electric field is calculated self-consistently as described in subsection 2.1, and the total electric field includes both the magnetospheric convection and corotation field. The equatorial cold electron density, \( n_e \), is obtained from the dynamic global core plasma model of Ober et al. [1997]. This model is basically the same as a time-dependent model of Rasmussen et al. [1993], which was used in our
previous studies, except the Ober et al. model is linked with a self–consistent electric field obtained from the system (1)–(9), while the Rasmussen et al. model is driven by the Volland–Stern convection field [Volland, 1973; Stern, 1975] with $Kp$ parameterization. Thus, the cold plasma density dynamics is also electrically self–consistent in our global RC–EMIC wave model. This is extremely important for a correct description of the EMIC wave generation/damping and propagation. In order to model the EMIC wave propagation and interaction with RC, we also need to know the density distribution in the meridional plane. In the present study we use a magnetic field model for the meridional density distribution, i. e., $n_e \sim B$, because a more sophisticated analytical model by Angerami and Thomas [1964] used in our previous studies [e. g., Khazanov et al., 2006] was found to give nearly the same results. The meridional model is then adjusted to the equatorial density model. So the resulting plasmaspheric model provides a 3D spatial distribution of the electron density. Besides electrons, the cold magnetospheric plasma is assumed to consist of 77% $H^+$, 20% $He^+$, and 3% $O^+$, which are in the range of 10 – 30% for $He^+$ and 1 – 5% for $O^+$ following the observations by Young et al. [1977] and Horwitz et al. [1981]. Geocoronal neutral hydrogen number densities, needed to calculate loss due to charge exchange, are obtained from the spherically symmetric model of Chamberlain [1963] with its parameters given by Rairden et al. [1986].

During the main phase of major storms, RC $O^+$ may dominate [e. g., Hamilton et al., 1988; Daglis, 1997] and, as a result, contribute to strong damping of the $He^+$–mode EMIC waves [Thorne and Horne, 1997]. Although there is no doubt that, in principle,
this process is important, let us evaluate the validity of excluding the $\text{He}^+$-mode damping by RC $O^+$ in the May 2-4, 1998 storm simulation. Using the RC kinetic model of Jordanova et al. [1998], Farrugia et al. [2003] found that during the main phase of the May 4, 1998 storm the energy density of RC $H^+$ is greater than twice that of $O^+$ at all MLTs, and the contribution of $\text{He}^+$ to the RC energy content is negligible.

This implies that the RC $O^+$ content does not exceed 30% during the main phase of this storm. This estimate was obtained from a global simulation, which did not include oxygen band waves. On the other hand, Bräysy et al. [1998] observed a very asymmetric $O^+$ RC during the main phase of the April 2–8, 1993 storm, which may suggest that a majority of the RC oxygen ions get lost before they reach the dusk MLT sector. This result is difficult to explain in terms of charge exchange and Coulomb scattering, and suggests that the production of EMIC waves contributes significantly to RC $O^+$ decay during the main and early recovery phases. In other words, due to the generation of the $O^+$-mode EMIC waves, most RC $O^+$ might precipitate before reaching the dusk MLT sector [Bräysy et al., 1998]. Therefore, to estimate the RC $O^+$ content correctly, the $O^+$-mode should be included in the simulation, and it is likely that Farrugia et al. [2003] overestimated the RC $O^+$ content during May 4, 1998. Moreover, the calculations of Thorne and Horne [1997] clearly demonstrated that even the RC $O^+$ percentage noted above cannot significantly suppress the $\text{He}^+$-mode amplification, and only slightly influences the resulting growth; inclusion of 26% $O^+$ in the RC population causes the net wave gain to decrease by only 20%. In addition, the most important results shown in the present study are obtained from simulations of the May 2–3, 1998 period, i. e.,
the first main ($Dst = -106$ nT) and recovery phases of the May 1998 large storm, when
the RC $O^+$ content should be even smaller than the Farrugia et al. estimate for May 4,
1998. It is for these reasons that we chose to exclude RC $O^+$ in the present simulations,
and to assume that the RC is entirely comprised of energetic protons.

Equation (9) must be solved taking into account the contributions from both
the northern and southern ionosphere. Because in the present study we assume the
magnetic field lines to be equipotentials, the northern and southern ionospheres can
just be replaced by an effective single ionosphere with $\Sigma = \Sigma_S + \Sigma_N$, and total FAC $J_{||,i}$ flowing into/out of it. After the resulting equation is solved, and $\Phi_i$ is found, we
can easily calculate the FACs $j_{||,i}(s_S)$ and $j_{||,i}(s_N)$ flowing into/out the southern and
northern ionosphere.

The ionospheric Hall and Pedersen conductances in our model are not calculated
self–consistently but rather specified by empirical models. The resulting conductance
arises from four sources: (1) direct solar extreme ultraviolet (EUV), (2) scattered solar
EUV on both sides of the terminator, (3) starlight, and (4) auroral particle precipitation.
The direct solar conductance is controlled by the solar zenith angle and the solar UV
and EUV radiations, which correlate with the solar radio flux index $F_{10.7}$. In the present
study we use the empirical model of Moen and Brekke [1993] for determining direct
solar conductance. The scattered solar EUV and starlight conductance models are taken
from the study of Rasmussen and Schunk [1987]. In order to specify the conductance
from auroral precipitation, we use either the Hardy et al. [1987] statistical model or an
empirical relationship between the FACs and the local Hall and Pedersen conductance
established by Ridley et al. [2001; 2004]. The Hardy et al. model is compiled from the electron precipitation patterns obtained by the DMSP satellites and gives the Hall and Pedersen conductance as a function of MLT and magnetic latitude for seven levels of activity as measured by $K_p$. The Ridley et al. relationship was derived using the assimilative mapping of ionospheric electrodynamics (AMIE) technique [Richmond and Kamide, 1988]. The AMIE technique was run at a one–minute cadence for the entire month of January 1997, using 154 magnetometers. This resulted in almost 45000 2D maps of the Hall and Pedersen conductances and FAC. The conductance was derived from the Ahn et al. [1998] formulation, which relates ground–based magnetic perturbations to the Hall and Pedersen conductances. The Ridley et al. analysis showed an exponential relationship between the local FAC and the conductance [see Amm, 1996; Goodman, 1995]:

$$\Sigma = \Sigma_0 e^{-A|j||i|},$$  

(10)

where the constants $\Sigma_0$ and $A$ are independent of the magnitude of $j||i|$ but depend on location and whether the current is upward or downward. Although the Ridley et al. relationship is entirely empirical and not based on first principles, by using it we introduce into the model at a degree of self–consistency between the ionospheric conductance and FAC. This is a principle modification because a self–consistent description of the ionospheric conductance makes equation (9) nonlinear compared to the case of statistical conductance model. For previous use of the Ridley et al. relationship in the RC simulation see Liemohn et al. [2005].
To conclude this subsection, we note that the numerical implementations used to solve equations (1)–(6) are described in details in our previous publications [Khazanov et al., 2003a; 2006], and to solve equation (9) a preconditioned gradient reduction resolution (GMRES) solver is used [Ridley et al., 2004]. The GMRES method is robust enough to handle a wide variety of FAC and conductance patterns.

2.3. Initial and Boundary Conditions

The initial RC distribution is constructed from the statistically derived quiet time RC proton energy distribution of Sheldon and Hamilton [1993] and the pitch angle characteristics of Garcia and Spjeldvik [1985]. The night–side boundary condition for equation (1) is imposed at the geostationary distance, and it is obtained using flux measurements from the Magnetospheric Plasma Analyzer [Bame et al., 1993] and the Synchronous Orbit Particle Analyzer [Belian et al., 1992] instruments on the geosynchronous LANL satellites during the modeled event. Then, according to Young et al. [1982] and Liemohn et al. [1999], we divide the total flux measured at geostationary orbit between the RC $H^+$, $O^+$, and $He^+$ depending on geomagnetic and solar activity as measured by $Kp$ and $F_{10.7}$ indices. Only the $H^+$ flux is used as a boundary condition in the simulation.

In the present study, the poleward boundary for equation (9) is taken at magnetic latitude $\lambda = 69^\circ$. On this boundary, we specify the electric potential using either the Weimer [1996] statistical model (hereinafter the W96 model), which is driven by the interplanetary magnetic field (IMF) $B_Y$, $B_Z$ components and solar wind velocity,
or the convection model of Volland and Stern [Volland, 1973; Stern, 1975] with $Kp$ parameterization given by Maynard and Chen [1975] and shielding factor of 2 (hereinafter the VS model). The second boundary condition is specified at $\lambda = 30^\circ$, and we use either the W96 model or the VS model, both of which give the potential close to zero at that latitude. It should be noted that the result of calculation is insensitive to the choice of the lower boundary condition, as demonstrated by Wolf [1970]. So, the magnetospheric electric field is calculated self-consistently in the domain $30^\circ < \lambda < 69^\circ$.

At the same time, we should emphasize that, compared to RC, the cold electron density is modeled in a more extended domain of $L \leq 10$, and in order to specify the electric field in the entire $L \leq 10$ region, we use either the W96 or the VS model for the magnetic latitude above $\lambda = 69^\circ$.

The initial RC, plasmasphere, and EMIC wave distributions are derived independently and, moreover, they have nothing to do with a particular state of the magnetosphere/plasmasphere system during a simulated event. Only the boundary conditions provided by the LANL satellites can be considered as data reflecting a particular geomagnetic situation (and, to a certain extent, the employed ionospheric conductance model and an imposed cross polar cap potential drop). Therefore, before the simulation of a particular geomagnetic event can occur, we first must find an appropriate initial state for the RC, electric field, plasmasphere, and EMIC waves that is self-consistent and reflects the particular geomagnetic situation. To obtain the self-consistent initial distributions for the entire system, we first prepared the plasmasphere by running the Ober model for 20 quiet days. Then, at 0000 UT on
1 May, 1998, a simulation of equations (1)–(10) was started using all the controlling parameters and the initial/boundary conditions along with a background noise level for the $He^+$-mode EMIC waves [e. g., Akhiezer et al., 1975]. We ran the model code for 24 hours to achieve a quasi-self-consistent state for the system. Note that 24 hours has nothing to do with the typical time for wave amplification and instead reflects the minimum time needed to adjust the RC and waves to each other and to the real prehistory of a storm. The self-consistent modeling of the May 1998 storm period was started at 0000 UT on 2 May (24 hours after 1 May 0000 UT) using solutions of equations (1), (2), and the cold plasma distribution at 2400 UT on 1 May as the initial conditions for further simulation.

2.4. Interplanetary and Geomagnetic Drivers for the Model

The ionospheric boundary condition in our simulations is driven either by IMF $B_Y$, $B_Z$ components and solar wind velocity (the W96 model) or the 3-hour $K_p$ index (the VS model). The Hardy et al. [1987] ionospheric conductance model is driven by $K_p$. All of these driving parameters are shown in Figure 2 during the May 2–4, 1998 period. Interplanetary data are obtained from the Magnetic Field Investigation [Lepping et al., 1995] and the Solar Wind Experiment [Ogilvie et al., 1995] instruments aboard the WIND satellite. The interplanetary configuration of May 1–5, 1998 consists of a coronal mass ejection (CME) interacting with a trailing faster stream [Farrugia et al., 2003]. The CME drives an interplanetary shock observed by the instruments aboard the WIND spacecraft at about 2220 UT on May 1. Three episodes of the large negative IMF $B_Z$
component were monitored. The first episode started at $\sim 0330$ UT on May 2 (27.5 hours after May 1, 0000 UT), the second at 0230 UT on May 4 (74.5 hours after May 1, 0000 UT), and the third (not shown) at $\sim 0200$ UT on May 5 (98 hours after May 1, 0000 UT). These caused a “triple–dip” storm with the minimums $Dst = -106$ nT, $Dst = -272$ nT, and $Dst = -153$ nT (not shown). The planetary $Kp$ index reached maximum values of $Kp \approx 7^-$ and $Kp \approx 9^-$ at the times when $Dst$ minimums were recorded.

3. Results and Discussion

3.1. Magnetospheric Electric Field

The cross polar cap potential (CPCP) drop gives a rough quantitative assessment of the strength of convection in the inner magnetosphere. We calculate the CPCP drop as a difference between the maximum and minimum values of the potential at $\lambda = 67.5^\circ$ (at $L \approx 7$). Results of our calculations are shown in Figure 3. The lines in red, green, and blue show results from a self–consistent simulation, while the CPCP drop shown in black is for reference purposes only. Note that the red line lies somewhat higher than the black one. This is because we do not calculate FACs between $\lambda = 69^\circ$ and $\lambda = 67.5^\circ$ in the present simulations, and so there is no shielding taken into account unlike in the analytical formulation of the VS potential (black line in Figure 3). When the W96 model is imposed at $\lambda = 69^\circ$, the CPCP drops are very similar for both conductivity models, and the blue line is just slightly higher than the green one. The CPCP drop
resulting from the VS model is larger during the majority of May 2–4, except for about 13 hours on May 2 and 12 hours on May 4, when the CPCP drop from the W96 model is greater. It is seen that the W96 potential drop spikes to 300 kV during the main phase on May 4, whereas the VS boundary condition results in a maximum CPCP drop of only 150 kV.

Although the CPCP drop may serve as an overall measure of the convective strength, it does not give the morphology and strength of the electric field in the inner magnetosphere. To provide such insight, we selected six snapshots of the equatorial electric field patterns from May 2, and one snapshot at hour 77 (0500 UT on May 4). The corresponding electric potential contours are shown in Figure 4. The view is over the North Pole with local noon to the left. We present results for three runs. The equipotentials from a simulation with the VS model at the high latitude ionospheric boundary and the Hardy et al. conductance are shown in the first row. The other two runs are performed with the W96 model applied at $\lambda = 69^\circ$, and differ only by the conductance model assumed. The second row shows results for the Hardy et al. conductance model, while the third row is for a case when the Ridley et al. empirical relationship between the FAC and conductance is used. The potential configurations in Figure 4 are similar to those from the Rice Convection Model [e.g., Garner et al., 2004]. Overall, there are qualitatively the same large-scale potential distributions in all three models, presented in Figure 4 with a well defined large-scale dawn-to-dusk electric field. Despite this, the potential patterns reveal large differences in both the magnitude of the potential and the shape of the contours. This suggests a difference in
the fine structure of the electric field distribution since this field is proportional to the
gradient of the potential.

One obvious feature observed in Figure 4 is a significantly enhanced electric field
in the region $L \approx 3 - 4$ in the dusk–post–midnight MLT sector at hour 77 (and, not
shown, at hour 76). This radially narrow intensification of the radial electric field
(poleward electric field in the ionosphere) creates a westward flow channel, mainly in
the dusk–to–midnight MLT sector, while a region of westward (antisunward) convection
is also observed in the post–midnight sector equatorward of $L = 3$ (see Figure 4). This
westward flow channel has come to be called the subauroral polarization stream (SAPS)
[Foster and Burke, 2002; Foster and Vo, 2002]. The SAPS effect arises from the region 2
FACs, which flow down into the subauroral ionosphere and close the region 1 FACs
through the poleward Pedersen currents. Because of the low conductance at subauroral
latitudes, the Pedersen current generates an intense poleward electric field between the
region 2 FAC and the low–latitude edge of the auroral particle precipitation [Southwood
and Wolf, 1978; Anderson et al., 1991, 1993; Ridley and Liemohn, 2002; Mishin and
Burke, 2005].

To show the potential structure and electric field inside the SAPS region, we took
two meridional cuts across the entire simulation domain and the corresponding results
are shown in Figure 5. Figures 5a, b show the potential profiles on the dawn–dusk
meridian for hours 33 and 77. Results for three simulations are presented along with a
profile for the analytical VS model. The corresponding equatorial radial electric fields
are shown in Figures 5c, d for MLT=18. Only a slight electric field intensification
(< 2.7 mV/m) is observed in the dusk sector for hour 33 (see Figure 5c), while we see an extremely developed SAPS in Figure 5d (< 13.4 mV/m). The strongest electric field intensification in Figure 5d takes place for cases when the W96 model is used in combination with either the Hardy et al. conductance model or the Ridley et al. relationship. In the latter case, we see a slightly stronger electric field in the dusk MLT sector and a developed dawnside electric field of about 5 mV/m (see Figure 5b).

Although the SAPS localization is correctly predicted by our model, it is likely that the SAPS electric field in Figure 5d is overestimated for the W96 boundary condition. Indeed, from the statistical model based on the electric field data measured by the Akebono/EFD instrument, Nishimura et al. [2007] derived the equatorial $E_Y$ electric field component in the dusk SAPS region to be 6 mV/m during the main phase of storm. It should be noted, however, that the SAPS electric field can sometimes reach more than 10 mV/m during the main phase of geomagnetic storms [Shinbori et al., 2004], and the CPCP drop derived by Nishimura et al. [2007] is 180 kV, whereas in our simulation it is 300 kV. The measurements taken by the double-probe electric field instrument on-board the CRRES spacecraft show a similar electric field magnitude [Wygant et al., 1998]. There are at least two reasons that may lead to an overestimation of the SAPS electric field in our simulations. (1) Because the W96 model was constructed from data with IMF under 10 nT, this model essentially overestimates the CPCP drop during the May 4 event when IMF was around 40 nT [e.g., Burke et al., 1998]. (2) In the present simulations, we did not take into account the FACs beyond geostationary orbit, which may contribute essentially to the shielding of midlatitudes from a high latitude driving
convection field; the effect of FAC is proportional to the volume of the magnetic flux
tube, and from the estimate by Vasyliunas [1972] the effect of FAC at L=6.6 is about
20% of the FAC effect at L=10. Both of these issues will be addressed in future studies.

3.2. Plasmasphere

The plasmapause, and/or dayside plume, and/or detached plasma are the favorable
regions for EMIC wave generation in the inner magnetosphere. This is because
the density gradient there is enhanced and counteracts refraction caused by the
magnetic field gradient and curvature [e.g., Horne and Thorne, 1993; Fraser et al.,
2005; Khazanov et al., 2006]. As a result, the net refraction is suppressed at the
plasmapause/plume edge allowing wave packets to spend more time in the phase region
of amplification. Thus, the cold plasma distribution is extremely crucial for EMIC
wave excitation. Both the convection and the corotation electric fields control the cold
plasma dynamics. As such, we will first present the snapshots of the total electric
potential obtained from our simulations. Figure 6 shows the resulting equipotential
contours, that also coincide with the instantaneous cold plasma flow. The most striking
reconfiguration of the potential is observed in the second and third rows in the 28 and
30 hour snapshots. Referring to Figure 3, we see that starting at hour 28 the CPCP
drop increases by about 100 kV during one hour for the W96 convection model. The
strong convection causes a shrinking of the closed equipotential contours as shown in
Figure 6 (there is stronger shrinking during hour 29). Later, an extremely developed
SAPS is observed at hours 76–77 (see subsection 3.1), and the overshielding electric field
(negative $E_Y$) following a decrease of the CPCP difference in the W96 model is found in the inner magnetosphere at hour 79 (not shown).

Figure 7 shows the selected distributions of the equatorial cold plasma density for three self–consistent simulations. For each run, the plasmasphere was first prepared by running the Ober code for 20 quiet days. Then, starting at 0000 UT on 1 May, 1998, we solved the equations (1)–(10) using the initial and boundary conditions and the time series for all controlling parameters (see subsection 2.3). For the VS model (first row), a broad dayside plume is formed a few hours before hour 28. Subsequently, up to hour 39 gradual intensification of the convection (see Figures 3 and 4) causes nightside plasmaspheric erosion and the plume narrowing in the MLT extent. The latter takes place mostly in the eastward flank of the plume where the convection and corotation fields reinforce each other, while the duskside plume edge remains roughly stationary [Spasojevi´c et al., 2003; Goldstein et al., 2005]. During the following storm progression, the magnetospheric convection field driven by the VS potential drop remains relatively high (see Figure 3), and the convection patterns are relatively steady (3–hour cadence). Compared to the second and third rows in Figure 7, these result in the most eroded and shrunken plasmasphere at hour 77 with a well–defined nightside plasmapause (compare these results with Figure 7 in [Khazanov et al., 2006] where the entire plasmasphere was driven by the analytical formulation of the VS potential).

Cold plasma density distributions in the second and third rows of Figure 7 are qualitatively similar to each other, but exhibit quite a bit of difference compared to distributions in the first row. At hour 28, the plasmasphere is well–populated, and the
plasmapause is well-defined. Starting at hour 28, an increase of the CPCP drop by 100 kV during one hour (see Figure 3) causes formation of the plume by hour 29 (not shown), and the presented snapshots at hour 30 are close to those at hour 29. One of the most distinguishable features observed in the second and third rows is the presence of a cold plasma on the nightside. To emphasize the existence of the recirculated detached plasma material, we show in Figure 8 the detailed plasma density evolution in the extended domain of $L \leq 10$. It is clearly seen in Figure 8 how this recirculated detached plasma is forming and reentering the inner magnetosphere. The radial electric field for MLT=18 and 19 is also shown in Figure 9 for hours 28 and 29. The negative electric field in the outer region in Figure 9b is resulting in plasma recirculation. However, we have to emphasize that a great care is needed to interpret these simulation results. During an extreme condition, the W96 model may predict a two-cell convection pattern with its focuses located at low latitude. The anti-sunward ionospheric plasma flow predicted by the W96 model may correspond to the lobe and the outer part of low-latitude boundary layer (LLBL) in the magnetosphere. In the dayside magnetosphere, when the plasmaspheric cold plasma is transported to LLBL, the cold plasma will flow in the anti-sunward direction [e.g., Ober et al., 1998]. At the same time, reentry of the cold plasma from LLBL back to the magnetosphere may not be simple as predicted by the W96 model.

Although the cold plasma recirculation is seen in both the second and the third rows of Figure 7, the observed similarity is only qualitative and all the quantitative characteristics are quite different. After hour 39, the W96 CPCP drop decreased and
fluctuated around 50 kV except for four hours on May 4 when the CPCP drop spikes to 300 kV during the second main phase of the storm (see Figure 3). In both cases, the resulting plasmaspheres at hour 77 are extremely diffusive with shallow density gradients. This is because the anti-sunward plasma flow is especially strong during the second main phase of the storm. To demonstrate that, we show in Figure 10 the total \[ \text{radial electric field versus MLT for } L=8, 9, \text{ and } 10 \text{ at hour 77}. \] The negative radial electric field in the afternoon–premidnight MLT sector causes a counter clockwise plasma convection. The MLT extent of the negative electric field in the afternoon–premidnight MLT sector grows with L-shell, resulting in the backward plasma flow for MLT $> 15$ at $L=10$. This recirculation supplies the cold plasma in the nightside preventing the plasmasphere to be eroded. At the same time, as we emphasized above, a great care is needed to interpret these results.

To show the equatorial cold plasma density profiles during the periods of a well-defined and a shallow plasmapause we selected hours 33 and 77. Results of our simulations are shown in Figure 11. We see a “classical” profile of the plasmapause for hour 33, when the plasma density decreases about two orders of magnitude over $0.5 - 0.75 \, R_E$. The combination of the W96 model and the Ridley et al. relationship results in a detached plasma with a peak density of $20 \, \text{cm}^{-3}$, which is clearly observed in Figure 11a (see also the third row in Figure 7). During hour 77, the plasmasphere driven by the VS CPCP drop is the most eroded and, although the plasmasphere boundary layer is wider than in Figure 11a and the plasma density drop is smaller, the plasmapause is still well-defined. For simulations with the W96 potential at the
high latitude ionospheric boundary, both density profiles shown in Figure 11b exhibit a shallow density gradient without the plasmapause while there is a clear change of the profile slope for the W96–Hardy et al. result. Note that there are also no steep density gradients outside of geostationary orbit (not shown).

3.3. RC Proton Precipitation

The convection electric field controls the global precipitating patterns of RC. As RC protons approach the Earth via the convection electric field, they precipitate into the loss cone because the equatorial loss cone angle increases with decreasing L–shell somewhat more than the equatorial pitch angle increases [e. g., Jordanova et al., 1996]. Note that precipitation due to Coulomb collisions with thermal plasma takes place mainly inside the plasmapause, and the wave–induced ion precipitation is organized in the radially narrow regions in the plasmasphere boundary layer [e. g., Gurgiolo et al., 2005; Khazanov et al., 2007b]. The RC proton precipitating fluxes integrated over two energy ranges 1 – 50 keV and 50 – 400 keV are calculated as

\[
J_{\Omega lc} = \frac{1}{\Omega_{lc}} \int_{E_1}^{E_2} dE \int_{\mu_{lc}}^{1} d\mu_0 j, \quad \Omega_{lc} = \int_{\mu_{lc}}^{1} d\mu_0,
\]  

(11)

where \( \mu_{lc} \) is the cosine of the equatorial pitch angle at the boundary of the loss cone, and \( j \) is the equatorial differential flux of RC protons. The snapshots of the fluxes for low and high energies are shown in Figure 12 and 13, respectively. The results from three self–consistent runs with a specified combination of the high latitude ionospheric boundary potential and conductance model are shown. For low energy, the most intense
precipitating fluxes near the end of the second main phase (hour 77) are observed in
the second and third rows of Figure 12 when the W96 model is used. This takes place
because the convection field is strongest in these two cases (see Figure 4). The spot–like
spatial structure in the postnoon–midnight MLT sector is due to the wave–induced
precipitation with the strongest fluxes up to $10^7 \text{ cm}^{-2}\text{s}^{-1}\text{sr}^{-1}$.

The penetrating electric field driven by the W96 boundary field causes precipitation
of energetic RC ions well earthward of the low energy ion precipitation. It is clearly
seen in Figure 13 that the W96 boundary potential leads to a strong precipitation of
the high energy ions near the inner edge of RC during the second main phase on May 4.
The high energy precipitating fluxes maximize at about two times stronger magnitude
than the maximal fluxes observed in the range 1 – 50 keV.

3.4. Energy Distribution for He$^+$–Mode EMIC Waves

The coupling of the magnetosphere and ionosphere by the region 2 FACs gives a
self–consistent description of the magnetospheric electric field. This field controls the
convective patterns of both RC ions and the cold plasmaspheric plasma, changing the
conditions for EMIC wave generation/amplification. The equatorial (MLT, L–shell)
distribution of the squared wave magnetic field,

$$B_w^2(r_0, \varphi, t) = \int_{\omega_{\text{min}}}^{\omega_{\text{max}}} d\omega \int_0^\pi d\theta_0 B_w^2(r_0, \varphi, t, \omega, \theta_0),$$

is shown in Figure 14 for the He$^+$–mode EMIC waves. As before, the results from three
self–consistent simulations are presented. Comparing Figure 14 with the cold plasma
density distribution in Figure 7, we see that EMIC waves are distributed in the narrow regions inside the plasmasphere boundary layer where the density gradient is enhanced. Although, during hours 30–39, the spatial wave distributions in the first and second rows look similar, on average, there are much more waves in a simulation with the VS boundary condition than in a simulation with the W96 potential during entire May 2. Moreover, there are practically no waves in the latter simulation after hour 39 (not shown) while in the former case we observe the extended regions of intense waves during the majority of the time up to hour 60 (not shown). This is because the plasmapause is well-defined and the CPCP drop is higher in the case of the VS potential boundary compared to the case of the W96 potential when the plasmasphere is highly diffusive (a shallow density gradient) and RC is less intense (lower the local growth rate).

The density distributions in the second and third rows of Figure 7 demonstrate quite a bit of difference in the after-dusk MLT sector starting at hour 33. The plasmapause in the third row is located closer to the Earth, and the density gradient is shallowed by the detached plasma. At the same time, we observe much less wave activity in the third row of Figure 14 than in the second row. This is likely due to the effect of the density distribution, because the global potential drop is even higher in the third row of Figure 4 (suggesting a more intense RC) compared to the second row.

There are practically no waves during the second main and recovery phases, except for moderate wave activity in the hour 77 snapshots in the first and third rows of Figure 14. In the case of the VS–Hardy et al. combination, the plasmapause is well-defined during hour 77 (see Figures 7 and 11) and waves can grow despite a less
intense RC in this case. On the other hand, the RC is strongly developed for the case of the W96 potential, and wave growth rate is essentially higher than in the first row, causing a wave generation despite the plasmasphere being extremely diffusive and the density gradient being shallow.

### 3.5. Ionosphere Reconfiguration and Communication Time

All of the results presented above were obtained from simulations when only a 30 min time delay between WIND and the high latitude ionospheric boundary was applied. Both the reconfiguration time needed to reestablish a new potential pattern throughout the ionosphere and communication time between the ionosphere and the equatorial magnetosphere were assumed to be zero. These allowed us to update the equatorial electric field for each time step (a minute). However, this is not the case and both the ionospheric reconfiguration time and the Alfvén propagation time are essentially higher than a minute [e. g., Ridley et al., 1998]. This implies that the ionosphere cannot reconfigure instantly in response to change of the interplanetary conditions, and that the magnetospheric electric field requires a finite time to be reestablished.

*Ridley et al.* [1998] studied the ionospheric convection changes associated with changes of the IMF. They found that the total reconfiguration time of the ionosphere is in the range 3–26 min with an average of 13 min. Taking 7 min as a typical communication time between the ionosphere and the equatorial magnetosphere (for example, the magnetopause–ionosphere communication time is $8.4 \pm 8.2$ min as estimated by Ridley
et al. [1998]), on average, the same 13 min are needed to reestablish a new potential pattern in the magnetosphere but a 7 min delay should be applied to the ionospheric pattern. Because a great deal of scatter was reported for both time scales, below we simply adopt 20 (= 13 + 7) min as a time needed to reestablish a new potential pattern in the equatorial magnetosphere.

To assess the importance of the finite ionospheric reconfiguration and communication time effect, we reran the “W96–Hardy et al.” simulation. Starting at hour 24, we averaged the interplanetary parameters and FACs over a 20 min window before passing them to the ionospheric solver, and updated the equatorial electric field only once every 20 min. Figure 15 shows the equatorial potential contours from this simulation along with the contours from the previous simulation, when the equatorial electric field is updated for each time step. The results during seven consecutive hours are shown (hours 35–41). The potential distributions in the first and second rows are quite a bit different suggesting that the finite ionospheric reconfiguration and communication time effect may be important, especially for the fine temporal–spatial structure of the plasmasphere–magnetosphere system. Although the “new” electric field alters the RC, wave, and cold plasma distributions, we show only the results for cold plasma density. Figure 16 demonstrates a difference in the cold plasma density distribution introduced by the effect of a finite time required to reestablish a “new” distribution of the magnetospheric electric field. Although the density distributions in these two simulations are identical at hour 24, the plasmapause/plume shapes get a visible difference in the dawn–noon MLT sector starting at hour 29 (not shown). Later, starting
at hour 35, an essential difference between the density distributions is observed in the night MLT sector (see Figure 16). After hour 56, the cold plasma density distributions in these two simulations are similar. This is expected after a longterm interval of system evolution, while the fine density structure still differs from time to time depending on the differences in the electric field distributions in these two simulations.

Although a more sophisticated methodology is required to treat and separate the effects of the finite ionospheric reconfiguration and communication time, Figures 15 and 16 clearly demonstrate that the finite time effect is important, especially for the fine temporal–spatial structure of the system. This implies that the instant interplanetary parameters cannot be used in order to specify the outer ionospheric boundary condition, but rather some kind of the averaging procedure should be applied to these parameters before passing them to the ionospheric solver.

4. Summary

The scattering rate of magnetospheric RC ions and relativistic electrons by EMIC waves is not only controlled by the wave intensity–spatial–temporal distribution but strongly depends on the spectral distribution of the wave power. There is growing experimental [Anderson et al., 1996; Denton et al., 1996; Anderson et al., 1992b; Fraser and Nguyen, 2001; Meredith et al., 2003] and theoretical [Horne and Thorne, 1993; Khazanov et al., 2006] evidence that EMIC waves can be highly oblique in the Earth’s magnetosphere. Compared to field–aligned waves, the highly oblique wave normal angle distributions can dramatically change the effectiveness (an order of magnitude
or more) of both the RC proton precipitation [Khazanov et al., 2007b] and relativistic electron scattering [Glauert and Horne, 2005; Khazanov and Gamayunov, 2007].

Strong sensitivity of the scattering rates to the wave spectral characteristics suggests that in any effort to model EMIC wave–induced heating and/or scattering of the magnetospheric particles, the wave spectral distribution requires special care and should be properly established. Unfortunately, there are still very few satellite–based studies of EMIC waves, especially during the main phase of magnetic storms, and currently available observational information regarding EMIC wave power spectral density is poor [Engebretson et al., 2008]. So, a combination of comprehensive theoretical models and available data should be utilized to obtain the power spectral density of EMIC waves on the global magnetospheric scale throughout the different storm phases. To the best of our knowledge, there is only one model that is able to simulate a spatial, temporal and spectral distribution of EMIC waves on the global magnetospheric scale during the different storm phases [Khazanov et al., 2006]. This model is based on first principles and is governed by a coupled system of the RC kinetic equation and the wave kinetic equation, explicitly including the wave generation/damping, propagation, refraction, reflection and tunneling in a multi–ion magnetospheric plasma.

The convective patterns of both the RC ions and the cold plasmaspheric plasma are controlled by the magnetospheric electric field, thereby determining the conditions for interaction of RC ions and EMIC waves. Therefore, this electric field is one of the most crucial elements in simulating the wave power spectral density on a global magnetospheric scale. Self–consistent simulation of the magnetosphere–ionosphere
system should provide, at least in principle, the most accurate theoretical electric
field [Vasyliunas, 1970; Jaggi and Wolf, 1973]. The need for a self–consistent model
of the magnetospheric electric field, RC, plasmasphere, and EMIC waves is evident.
In the present study we have incorporated the large scale magnetosphere–ionosphere
electrodynamic coupling in our previous self–consistent model of interacting RC ions
and EMIC waves [Khazanov et al., 2006]. The resulting computational model treats
self–consistently not only EMIC waves and RC ions but also the magnetospheric electric
field, RC, and plasmasphere.
A few runs of this new model were performed to get a qualitative assessment of
the effects of the high latitude ionospheric boundary condition and the ionospheric
conductance. The results presented in this study were obtained from simulations
of the May 2–4, 1998 geomagnetic storm (mostly the May 2–3 period). We have
performed three simulations that differ by the electric potential specified at the high
latitude ionospheric boundary (we used the W96 model and the VS model with $K_p$
parameterization), and/or the ionospheric conductance from auroral precipitation
(utilizing the Hardy et al. conductance model and the Ridley et al. relationship between
the FACs and the conductance). The following three combinations have been used in
the simulations: (1) the VS model and the Hardy et al. model; (2) the W96 model and
the Hardy et al. model; and (3) the W96 model and the Ridley et al. relationship. In
addition, one more simulation has been done: (4) the W96 model and the Hardy et
al. model applying a 20 min window as the time needed to reestablish a new potential
pattern in the magnetosphere. The RC in the present study has been simulated inside...
geostationary orbit only, and the high latitude ionospheric boundary has been placed near the ionospheric projection of this orbit. The findings from our initial consideration can be summarized as follows:

1. Although the poleward boundary for the ionospheric potential is specified at the projection of geostationary orbit in most models (probably except the Rice Convection Model), we are not able to specify well the ionospheric potential there. Indeed, the existing models of ionospheric electric potential (like the AMIE technique [Richmond and Kamide, 1988], the Weimer [1996, 2001] and the Boyle et al., [1997] models) are much more reliable at high latitudes and give a poor representation of the potential and its significant variation in the inner magnetosphere [Foster and Vo, 2002]. In addition, the effect of FACs is proportional to the volume of the magnetic flux tube, and so this effect at L=6.6 is about 20% of the FAC effect at L=10, suggesting that FACs beyond geostationary orbit may produce a major shielding of midlatitudes from a high latitude driving field. So the region beyond geostationary orbit should be included in the magnetosphere-ionosphere coupling. An extension of the simulation domain, at least to $\lambda = 72^\circ$, is vital for a truly self-consistent modeling of the magnetosphere–ionosphere coupling.

2. Compared to the case of the Hardy et al. model, the Ridley et al. empirical relationship between the FAC and conductance produces quite a bit of difference in the potential distribution and, overall, stronger convection at the subauroral latitudes (see Figures 4 and 5). This difference strongly affects the cold plasma distribution, RC precipitation pattern, and EMIC waves (see Figures 7, 11, 12, 13, and 14). More
importantly, a self–consistent description of the ionospheric conductance makes equation (9) nonlinear compared to the case of a statistical conductance model. This is a principle point requiring that a self–consistent model, based on first principles, of the ionospheric conductance should be incorporated into a simulation of the magnetosphere–ionosphere coupling.

3. A fine density structure in the plasmasphere boundary layer, plume, detached plasma etc. controls the wave propagation. This fine structure may be a more crucial factor in controlling the generation of EMIC waves, than just the intensity/distribution of the RC and the local plasma density. There is very large difference between the wave activity in the second and third rows in Figures 14 while the density distributions in the second and third rows in Figures 7 do not differ so dramatically. This suggests that to model the EMIC wave distribution and wave spectral properties accurately, the plasmasphere should be simulated self–consistently because its fine structure requires as much care as that of the RC.

4. It is shown that the effect of a finite time needed to reestablish a new potential pattern throughout the ionosphere and to communicate between the ionosphere and the equatorial magnetosphere is important. This effect was ignored in all previous simulations but it should be taken into account to model a self–consistent electric field properly.

Concluding we would like to emphasize that in order to make significant progress in developing a truly self–consistent model of the electric field, we need to considerably improve our ability to accurately specify the electric field at high latitudes and
ionospheric conductance. Without this ability, we will not be able to accurately specify
EMIC wave spectra in the inner magnetosphere and correctly describe the wave–induced
heating and/or scattering of the magnetospheric particles.

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References


Amm, O. (1996), Comment on “A three–dimensional, iterative mapping procedure for the implementation of an ionosphere–magnetosphere anisotropic Ohm’s law boundary condition in global magnetohydrodynamic simulations”, *Annales Geophysicae*, 14, 773.


Engebretson, M. J., M. R. Lessard, J. Bortnik, J. C. Green, R. B. Horne, D. L. Detrick,


Foat, J. E., R. P. Lin, D. M. Smith, F. Fenrich, R. Millan, I. Roth, K. R. Lorentzen,


Glauert, S. A., and R. B. Horne (2005), Calculation of pitch angle and energy


Khazanov, G. V., K. V. Gamayunov, D. L. Gallagher, J. U. Kozyra, and M. W. Liemohn (2007b), Self–consistent model of magnetospheric ring current and propagating electromagnetic ion cyclotron waves. 2. Wave induced ring current...


Rasmussen, C. E., S. M. Guiter, and S. G. Thomas (1993), Two–dimensional model of


Shinbori, A., T. Ono, M. Iizima, and A. Kumamoto (2004), SC related electric and magnetic field phenomena observed by the Akebono satellite inside the


Tsyganenko, N. A., H. J. Singer, and J. C. Kasper (2003), Storm–time distortion of the


Young D. T., T. J. Geiss, H. Balsiger, P. Eberhardt, A. Ghiedmetti, and H. Rosenbauer
(1977), Discovery of $He^{2+}$ and $O^{2+}$ ions of terrestrial origin in the outer

Young D. T., S. Perraut, A. Roux, C. de Villedary, R. Gendrin, A. Korth, G. Kremser,
and D. Jones (1981), Wave–particle interactions near $\Omega_{He^+}$ observed on GEOS 1
and 2, 1, Propagations of ion cyclotron waves in $He^+$–rich plasma, *J. Geophys.
Res.*, 86, 6755.

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**Figure 1.** The block diagram of the RC, EMIC waves, plasmasphere, and ionosphere coupling in our model. The system characteristics in orange boxes are externally specified and the dashed lines connect the model elements that are currently not linked.

**Figure 2.** The interplanetary and geomagnetic characteristics during May 2–4, 1998. From the top to the bottom panels: the interplanetary magnetic field GSM $B_Y$ and $B_Z$ components, the solar wind velocity, 3–hour $K_p$ index, and the measured $Dst$ index. The hours shown are counted from 0000 UT on 1 May, 1998.

**Figure 3.** The cross polar cap potential drop from differently driven convection models during May 2–4, 1998. The black line, shown for reference, is the potential drop from the shielded Volland–Stern model with $K_p$ parameterization. The red, green, and blue lines represent the self–consistent results obtained with either the VS or W96 model imposed at $\lambda = 69^\circ$, and either the Hardy et al. conductance model or the Ridley et al. empirical relationship between the FAC and conductance (see legend in the figure). In order to drive the W96 model, a 30 min time lag between WIND and the high latitude ionospheric boundary is adopted after *Farrugia et al.* [2003].
Figure 4. The equatorial potential contours in the inner magnetosphere without corotation field. The view is over the North Pole with local noon to the left. All of the indicated hours are counted from 0000 UT on 1 May, 1998. (first row) Results from a simulation with the VS model at the high latitude ionospheric boundary and the Hardy et al. conductance model. (second row) Simulation with the W96 model at $\lambda = 69^\circ$ and the Hardy et al. conductance model. (third row) The same as in the second row except that the Ridley et al. empirical relationship between the FAC and the local Hall/Pedersen conductance is used. Equipotentials are drawn every 8 kV.

Figure 5. (a, b) The potential profiles on the dawn–dusk meridian, and (c, d) the equatorial radial electric field along MLT=18 for hours 33 and 77.

Figure 6. Same as Figure 4, except that the corotation field is included.

Figure 7. The equatorial cold plasma density distributions from three self-consistent simulations. (first row) Results from a simulation with the VS model at the high latitude ionospheric boundary and the Hardy et al. conductance model. (second row) Simulation with the W96 model at $\lambda = 69^\circ$ and the Hardy et al. conductance model. (third row) The same as in the second row except that the Ridley et al. empirical relationship between the FAC and conductance is used.

Figure 8. The equatorial cold plasma density distribution in the extended domain of $L \leq 10$. The electric field is specified by the W96 model above $\lambda = 69^\circ$ but it is calculated self-consistently below this latitude using the Ridley et al. relationship between the FAC and conductance.
**Figure 9.** The total radial electric field (including the corotation field) in the equatorial plane. A combination of the W96 model and the Ridley et al. relationship was used to produce these results. Two profiles for MLT=18 and 19 are shown for hours 28 and 29. The positive (negative) radial electric field is considered to be parallel (antiparallel) to the radius–vector.

**Figure 10.** The total equatorial radial electric field versus MLT. A combination of the W96 model and the Ridley et al. relationship was used to produce these results. Three profiles for L=8, 9, and 10 are shown for hour 77. The positive (negative) radial electric field is considered to be parallel (antiparallel) to the radius–vector.

**Figure 11.** The equatorial cold plasma density versus L-shell for hours 33 and 77. The profiles for hour 33 are plotted along MLT=19, while the profiles for hour 77 are plotted along MLT=18.

**Figure 12.** The RC proton precipitating fluxes averaged over the equatorial pitch–angle loss cone and integrated over the energy range $1 - 50$ keV.

**Figure 13.** Same as Figure 12, except that the precipitating fluxes are integrated over the energy range $50 - 400$ keV.

**Figure 14.** The distributions of squared wave magnetic field for the $He^+$-mode EMIC waves. (first row) Results from a simulation with the VS model at the high latitude ionospheric boundary and the Hardy et al. conductance model. (second row) Simulation with the W96 model at the ionospheric boundary and the Hardy et al. conductance model. (third row) The same as in the second row except that the Ridley et al. empirical relationship between the FAC and conductance is used.
Figure 15. The equatorial potential contours in the inner magnetosphere without a corotation field. The view is over the North Pole with local noon to the left. All of the results are from simulations with the W96 potential at the high latitude ionospheric boundary and use the Hardy et al. conductance model. (first row) The magnetospheric electric field is updated each minute in accordance with the instantaneous interplanetary conditions (a 30 min time delay is applied) and FACs. (second row) The interplanetary parameters and FACs are averaged over a 20 min window prior to sending them to the ionospheric solver and the magnetospheric electric field is updated once every 20 min. Equipotentials are drawn every 8 kV.

Figure 16. The equatorial cold plasma density distributions from simulations with the W96 potential at the high latitude ionospheric boundary and the Hardy et al. conductance model. (first row) The magnetospheric electric field is updated each minute accordingly to the instantaneous interplanetary conditions (with a 30 min time delay) and FACs. (second row) The interplanetary parameters and FACs are averaged over a 20 min window prior to sending them to the ionospheric solver and the magnetospheric electric field is updated once every 20 min.
measured Dst
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- VS at MLat=69° & Hardy et al. Σ-model
- W96 at MLat=69° & Hardy et al. Σ-model
- W96 at MLat=69° & Ridley et al. Σ-model

Hours after 00 UT on May 1, 1998
Dawn/Dusk Potential Profile (kV)

(a) Hour 33
- VS shielded model
- VS & Hardy et al
- W96 & Hardy et al
- W96 & Ridley et al

Equatorial Radial Field (mV/m)

(b) Hour 77

(c) Hour 33 MLT=18

(d) Hour 77 MLT=18
May 2-4, 1998: Thermal Plasma Density for Instant E-field reconfig, and 20 min reconfig time.