Longitudinal Proximity Effects in Superconducting Transition-Edge Sensors

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We have found experimentally that the critical current of a square thin-film superconducting transition-edge sensor (TES) depends exponentially upon the side length L and the square root of the temperature Tc, a behavior that has a natural theoretical explanation in terms of longitudinal proximity effects if the TES is regarded as a weak link between superconducting leads. As a consequence, the effective transition temperature Tc of the TES is current-dependent and at fixed current scales as 1/L². We also have found that the critical current can show clear Fraunhofer-like oscillations in an applied magnetic field, similar to those found in Josephson junctions. We have observed the longitudinal proximity effect in these devices over extraordinarily long lengths up to 290 μm, 1450 times the mean-free path.

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A superconductor cooled through its transition temperature Tc while carrying a finite dc bias current undergoes an abrupt decrease in electrical resistance from its normal-state value RN to zero. Superconducting transition-edge sensors (TESs) exploit this sharp transition; these devices are highly sensitive resistive thermometers used for precise thermal energy measurements.1 Various models2-6 have been used to explain the noise, Tc, and transition width ΔTc in TESs, all assuming spatially uniform devices. Though some have been shown to be consistent with certain aspects of particular devices, they do not explain measured Tc and ΔTc in TESs generally. In this paper we emphasize the importance of a phenomenon that so far has been neglected in previous theoretical studies of TESs: the longitudinal proximity effect (LoPE). The square superconducting/normal-metal (S/N) bilayers at the heart of the TES have an intrinsic transition temperature Tc0 without leads attached. However, since the bilayers are connected at opposite ends to superconducting leads with transition temperatures well above Tc0, superconductivity is induced longitudinally into the bilayers from the ends via the proximity effect, Fig. 1. As we shall explain later, many of the basic properties of our TES structures are well described by regarding them as SS’S or SN’S weak links.7-9

This observed long-range longitudinal proximity effect also contributes to the basic understanding of S/N heterostructures more broadly. Supercurrents have been measured through S/N/S sandwiches over N thicknesses D as long as 40 μm.10 In these pioneering experiments by Shepherd the clean normal metal (rolled Cu foils) has mean free paths ℓ ≈ 16 μm giving a D/ℓ ≈ 2.5. In contrast we present measurements on SN’S films well described by our proximity effect model with N’ lengths L from 8 to 290 μm with normal-state mean-free paths ℓ ≈ 200 μm giving L/ℓ ratios of 40 to 1450.

Despite poor understanding of the physics governing TESs biased in the superconducting phase transition, significant strides have been made in sensor development.1 TES microcalorimeters have been developed with measured energy resolutions in the x-ray and gamma-ray band of ΔE = 1.8±0.2 eV FWHM at 6 keV,11 and ΔE = 22 eV FWHM at 97 keV,12 respectively—with the latter result at present the largest reported E/ΔE of any non-dispersive photon spectrometer. TESs are successfully used across much of the electromagnetic spectrum, measuring the energy of single-photon absorption events from infrared to gamma-ray energies and photon fluxes out to the microwave range.1 There are active TES research and development programs underway in many physics fields for materials microanalysis,13 mass spectroscopy of biomolecules,14 nuclear nonproliferation,12 synchrotron experiments,15 atomic physics,16 quantum information,17,18 dark-matter searches,10 and astrophysics,1 including future large-scale...
NASA space-based cosmic microwave background and x-ray imaging-spectroscopy observatories.

To achieve high energy resolution it is important to control both the TES's $T_c$ and $\Delta T_c$. Because the energy resolution of calorimeters improves with decreasing temperature, they are typically designed to operate at temperatures around 0.1 K. For a TES, this requires a superconductor with $T_c$ in that range. While there exist a few suitable elemental superconductors, the best results have been achieved using proximity-coupled, S/N bilayers, for which $T_c$ is tuned by selection of the thicknesses of the S and N layers.

We report here the properties of TESs based on square $(L \times L)$ electron-beam-deposited Mo/Au bilayers consisting of a 55 nm Mo layer ($T_c \sim 0.9$ K) to which 210 nm of Au is added. The square side lengths $L$ range from 8 $\mu$m to 290 $\mu$m, and the normal-state resistance per square is $R_N = 17.2 \pm 0.5$ m$\Omega$. The bilayers are connected at opposite ends to Mo/Nb leads having measured superconducting transition temperatures of 3.5 and 7.1 K. Further details on the device fabrication process can be found in Ref. 23.

Our measurements are made in an adiabatic demagnetization refrigerator (ADR) with mu-metal and Nb enclosures providing magnetic shielding for the TES devices and SQUID electronics. The magnetic field normal to the TES device plane is controlled by a superconducting coil with the field value determined from the coil geometry and current. Measurements of the TES resistance $R$ are made by applying a sinusoidal current of frequency 5-10 Hz and amplitude $I_{bias} \sim 50-250$ nA, with zero dc component, to the TES in parallel with a 0.2 m$\Omega$ shunt resistor ($R_{sh}$). The time-dependent TES current is measured with a SQUID feedback circuit with input coil in series with the TES. When $I_{bias}$ is less than the TES critical current $I_c$, $R$ is zero, and all the ac current flows through the TES. However, when $I_{bias} > I_c$ and $R > 0$ during part of the ac cycle, the TES current becomes non-sinusoidal, and its maximum value $I$ becomes less than $I_{bias}$. The TES resistance $R$ at the TES current $I$ is then determined from $R = R_{sh}(I_{bias} - I)/I$.

The critical current $I_c$ is measured, with the ADR held at constant temperature, by ramping the dc bias current from zero and defining $I_c$ as the TES current at the first measured finite resistance ($R \sim 10 \mu\Omega$) across the TES. Record averaging is used at higher temperatures where $I_c$ becomes small.

The solid curves in Fig. 2 show measurements of the critical current $I_c$ over seven decades vs temperature $T$. Note that although we find the intrinsic transition temperature of the Mo/Au bilayer is $T_{ei} = 170.9 \pm 0.1$ mK, at very low currents a zero-resistance state is measured up to much higher temperatures as the TES size is reduced, three times $T_{ei}$ for $L = 8 \mu$m. On the other hand, for the larger TES sizes ($L=130$ and 290 $\mu$m) the critical current $I_c(T)$ decreases rapidly with $T$ near $T_{ei}$. The observed $I_c$ behavior as functions of both $T$ and the length $L$ provides strong evidence that our TESs behave as weak-link devices. The dotted curves in Fig. 2 show calculated values of $I_c$, using the Ginzburg-Landau theory described below. In addition, at appropriately chosen temperatures, the critical currents of these devices exhibit Fraunhofer-like oscillations as a function of an applied magnetic field, behavior characteristic of Josephson weak links. See Fig. 3 for an example. However, the spacing between the minima corresponds to a junction magnetic flux of approximately $BL^2$, similar to the spacing predicted in Ref. 25 for edge-type Josephson junctions in thin-film strips.

Because $I_c$ depends upon $T$ and $L$, the effective tran-
will be described in more detail elsewhere, to explain the simple version of Ginzburg-Landau (GL) theory, which theoretically by numerous authors. However, here we use a the results shown in Figs. 2 and 4. The calculations yield the current.

Also shown in Fig. 4(a) are temperatures $T_{c1} - T_{ci}$ for which the resistances are $R = 0.1 R_N$ and $0.5 R_N$, respectively, from which we define $\Delta T_{c1} = T_{c1} - T_{c0}$ and $\Delta T_{c2} = T_{c2} - T_{c0}$. We also define transition widths from the $I_c$ measurements $\Delta T_{c1} = T_{c1} - T_{c0}$ and $\Delta T_{c2} = T_{c2} - T_{c0}$. In Fig. 4(b) we show that these three measures of the transition width all vary approximately as $1/L^2$, shown by the dotted line. It also follows that $T_c - T_{ci}$ scales linearly with the transition.

Weak links have been studied experimentally and theoretically by numerous authors. However, here we use a simple version of Ginzburg-Landau (GL) theory, which will be described in more detail elsewhere, to explain the results shown in Figs. 2 and 4. The calculations yield the normalized order parameter $f = \vert \psi \vert / \psi_\tau$, where $\psi_\tau$ is the magnitude of the order parameter at the reference points $x = \pm L/2$ adjacent to the leads. At the reference points, the local value of $\psi_\tau^2$ is related to the local penetration depth $\lambda_\tau$ via $\psi_\tau^2 = m_i/\mu_0 \lambda_\tau^2$. There is a second characteristic length in GL theory, the temperature-dependent coherence length $\xi(T) = \xi/|t - 1|^{1/2}$, where $T$ is the absolute temperature, $T_{ci}$ is the intrinsic transition temperature of the weak link in the absence of leads, and $t = T/T_{ci}$ is the reduced temperature.

Near the center of the weak link, the parameter $x = 0$ becomes very small, the local penetration depth $\lambda_\tau = \lambda_\tau/f$ becomes very large. Moreover, in a thin film of thickness $d < \lambda$, magnetic fields and currents spread out over the two-dimensional screening length (or Pearl length$^{25}$) $\Lambda = 2 \pi^2/d = 2 \pi \lambda_\tau/d^2$. For all of our samples there is a range of temperatures $T$ far enough above $T_{ci}$ that at the center of the weak link $L \gg d$ and the current density is $j = \vec{j}_0 \vec{x} = \vec{x} I/W d$, where $I$ is the TES current. When the temperature $T > T_{ci}$ and $L \gg \xi(T)$, numerical calculations show that the current density $j_{x0}$, the order parameter at $x = 0$ in the presence of a current $I_0$, the order parameter at $x = 0$ in the absence of a current $I_0$, and the gauge-invariant phase difference $\phi$ across the weak link are accurately related via $j_{x0}/j_{x0} = \cos(\phi/2)$ and $j_{x0} = j_{x0} \sin \phi = 2j_{x0}/(f_0/f_{00}) \sqrt{1 - (f_0/f_{00})^2}.$

The dependence of $j_{x0}$ upon $\phi$ is similar to that in a Josephson junction.$^{25}$ The critical current density, the maximum supercurrent density that can be carried by the weak link, occurs when $\phi = \pi/2$ and $f_0 = f_{00}/\sqrt{2}$. Figure 5 shows $j_{x0}/j_{c}$ and $\phi/\pi$ as functions of $f_0/f_{00}$.

The GL equations also yield

$$j_{c} = \vec{j}_{c} L d = (F/\xi) e^{-L/\xi},$$

where the factor $F = \phi_0 L d/2(3 \pi \mu_0 \lambda_\tau^2)$ is nearly independent of $T$ for temperatures well below the transition temperature of the leads.

Inferring $T_{ci} = 170.9$ mK from the experimental data in Fig. 2(b) for $L = 290 \mu$m and assuming $\kappa = \lambda_\tau/\xi$, we obtained $\xi = 738$ nm and $\lambda_\tau = 79$ nm by fitting the
transition temperature of the TES should scale very nearly as
\( T_e^{1/2} \). Similar reasoning leads to the conclusion that
the effective transition temperature at which the first voltage appears, we can solve
for \( T_e^2 \) or \( T_e = T_e^1 / T_e^1 \) by setting \( I = I_c \) in Eq. (2), noting that
\( \xi = \sqrt{\xi - 1} / (I \xi) \).

The conclusion is based on our experimental findings that (a) the critical current at the first onset of a voltage along the length depends exponentially upon the length \( L \) and the square root of the temperature difference \( T - T_e^1 \), (b) the current-dependent effective transition temperature \( T_e^1 \), and the transition width scale as \( I / L^2 \), and (c) the TESs show clear Fraunhofer-like oscillations as a function of applied magnetic field, similar to those in Josephson weak links. It follows that the strength of the superconducting order parameter is not uniform over the TES. Our findings have important implications for TES magnetic field sensitivity, which impacts required limits on ambient magnetic field magnitude and fluctuations in TES applications. Proposed uses of the longitudinal proximity effect for TES applications include (1) tuning the effective \( T_e \) of TES arrays by changing \( L \) in mask design, which could compensate for bilayer \( T_e \) variability and increase yield, and (2) making small TESs consisting of superconducting leads separated by normal metal, such as Au with \( T_e = 0 \), avoiding the use of S/N bilayers.

\[ \frac{T_e^1 - T_e^2}{T_e^1} = (\xi / I)^2 \ln^2 \left( F^{1/2} - 1 / (I \xi) \right). \]