Moments of Inertia

Uninhabited Aerial Vehicle (UAV)
Dryden Remotely Operated Integrated Drone (DROID)

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Agenda

- Personal Background
- Research
  - Importance
  - Measure, Weight, CG
  - Design Hardware and Test
  - Machining
  - Hangar
  - Safety Mitigations
  - Critical Design Review (CDR)
  - Tech Brief
  - Test
  - Analyze Data
- Lessons Learned
- Future Plans
- Questions

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Personal Background

- CSUN Applied Mathematics Master Student
- CA Mathematics Council Member
- CSUN Mathematics Club Member
- National Science Foundation Scholarship Recipient
- NASA Intern
The mass properties of an object are simply the proportionality constants between applied force and the resulting acceleration:

\[ f = m \ddot{x} \]
\[ T = j \alpha \]

This is Newton’s 2nd law for 1 Degree of Freedom (DOF) translation and rotation, respectively.

When expanded to 6 DOF:

\[
\begin{bmatrix}
F_x \\
F_y \\
F_z \\
M_x \\
M_y \\
M_z
\end{bmatrix}_{p} = 
\begin{bmatrix}
m & 0 & 0 \\
0 & m & 0 \\
0 & 0 & m \\
m_{Z_{CG}} & m_{Y_{CG}} & 0 \\
m_{X_{CG}} & -m_{X_{CG}} & 0 \\
-m_{Z_{CG}} & m_{Y_{CG}} & m_{X_{CG}}
\end{bmatrix} 
\begin{bmatrix}
\dot{x} \\
\dot{y} \\
\dot{z} \\
\dot{\theta}_x \\
\dot{\theta}_y \\
\dot{\theta}_z
\end{bmatrix}_{p}
\]

CG information
Inertia Tensor
6 DOF acceleration
Importance

The inertial characteristics have direct consequences on:

- Aerodynamics!
- Propulsion!
- Structures!
- Control!
Measure and Weight
Design

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Shuttle Hangar
Safety

- Human Hazard Analysis
- Loss of Asset/Mission Hazard Analysis
Approvals

- Critical Design Review (CDR)
- Tech Brief
Data Analysis

- Time Constraints
- Basic Geometric Shapes
- MATLAB
- Error
Lessons Learned

- Dryden vs. Disneyland
- Learning
- Team Effort
- Double check all work
- Stress Testing
- Use steel instead of aluminum
Future Plans

- GSRP at NASA Headquarters
- Graduate
- Work for NASA
Questions?

Mark, Chris, Aaron, Lesli, Stephanie, Alex, and Helida!
All photos provided by: NASA photographer, Thomas P. Tschida and INSPIRE Team!

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BACK-UP: Inertia Calculations

\[ I_{Pod} = \left( \frac{g}{16\pi^2} \right) \left( \frac{d^2}{l} \right) T^2 \left( W_{Pod} + W_{Rig} \right) - I_{Rig} \]

Where,
- \( I \) = Yaw Mass Moment of Inertia, [lb-in\(^2\)]
- \( g \) = gravity, [in/sec\(^2\)]
- \( d \) = Distance Between Cables, [in]
- \( l \) = Cable Length, [in]
- \( T \) = Period of Oscillation, [sec]
- \( W \) = Weight, [lb]

Reference:
NACA TN No.351