Mars Ascent Vehicle Gross Lift-off Mass Sensitivities for Robotic Mars Sample Return

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April 2011
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Abstract

The Mars ascent vehicle is a critical element of the robotic Mars Sample Return (MSR) mission. The Mars ascent vehicle must be developed to survive a variety of conditions including the trans-Mars journey, descent through the Martian atmosphere and the harsh Martian surface environments while maintaining the ability to deliver its payload to a low Mars orbit. The primary technology challenge of developing the Mars ascent vehicle system is designing for all conditions while ensuring the mass limitations of the entry descent and landing system are not exceeded.

The NASA In-Space Propulsion technology project has initiated the development of Mars ascent vehicle technologies with propulsion system performance and launch environments yet to be defined. To support the project’s evaluation and development of various technology options the sensitivity of the Mars ascent vehicle gross lift-off mass to engine performance, inert mass, target orbits, and launch conditions has been completed with the results presented herein.

1.0 Introduction

For decades NASA and the science community have been working towards a robotic Mars Sample Return (MSR) mission. There have been numerous studies to evaluate MSR mission architectures, technology needs and development plans, and top-level mission requirements (Refs. 1 to 4). The Mars program has divided the MSR mission into three phases, each requiring a separate launch from Earth. The first launch consists of a lander and rover to perform sample collection and caching. This is followed by the launch of the Mars orbiter, which acts as the Earth return vehicle. The final phase of the mission is the launch of the second lander containing the Mars ascent vehicle (MAV). A notional depiction of the MSR architecture is included in Figure 1 and shows the potential for the order of the last two launches to change as mission planning continues. The first of these missions, the sample collection and caching, is scheduled as a joint NASA/ESA 2018 mission. Currently, the orbiter and lander missions are tentatively planned for 2022 and 2024, respectively. The MSR mission is one of the most challenging robotic missions ever attempted due to large number of system elements and technology development risks. One of the largest technology development risks for the MSR mission is the MAV.

NASA’s In-Space Propulsion Technology (ISPT) project has recently been assigned the development of the MAV technologies with a requirement to perform multiple terrestrial flight demonstrations prior to the MSR preliminary design review (PDR). The MAV and its associated landing platform element PDR is expected to occur in 2018. To meet this technology readiness date, the ISPT project released a MAV
Request for Information in December of 2008, and released a solicitation for the MAV propulsion system development in February of 2009. These awards will begin with system studies for various MAV propulsion concepts followed by a down select for the propulsion system development and demonstration.

The critical metric for the MAV is the landed mass required to complete its mission. The landed mass is limited due to the use of the Mars Science Laboratory (MSL) Skycrane, in the baseline entry descent and landing (EDL) system, to provide the final propulsive descent (Ref. 5). As a result of the landed mass restrictions, the objective is to minimize the Gross Lift-Off Mass (GLOM) of the MAV system.

MAV propulsion concepts being considered include solid, liquid, hybrid systems with state-of-the-art propellants and numerous subsystem architectures. These various concepts all have GLOM implications on the MAV system. The MSR science team is also still evaluating potential landing sites and evaluating landing accuracy of the EDL system. The landing site latitude, surface gradient, MAV launch platform orientation, MAV angle of elevation at launch, and other parameters all impact the MAV GLOM. To understand the primary MAV GLOM sensitivities to the MAV performance characteristics and landing site requirements, an extensive parametric trade has been completed and the results are presented herein.

2.0 MAV Baseline Description

2.1 Top Level MAV Requirements

The fundamental requirement for a successful MAV mission is the delivery of 5 kg of payload, which includes samples of the Martian surface as well as the sample containment system, to orbit. This requirement can be accomplished using a wide variety of engine and vehicle assumptions that fall into two major categories. First is a family of in-line two-stage vehicle designs to reach orbit known as two stage to orbit (TSTO) solutions. TSTO concepts use two separate propulsion systems with the first stage jettisoned before the second stage is used. The other major category of vehicle designs uses only a single stage with a restartable propulsion system and is referred to as a single stage to orbit (SSTO) solution. SSTO vehicle concepts do not jettison any part of the stage during ascent with considerations given to both restartable liquid and hybrid engines as well as timed solid rocket motor designs.
To allow for a stable orbit at Mars, the MAV must be able to place the sample into a 500 km circular orbit, with dispersions no greater than ±100 km (Ref. 6). The inclination of the rendezvous orbit has yet to be established and will ultimately depend on the largest landing latitude that the EDL system can guarantee for the MAV. This is due to the assumption that the target orbit inclination of the MAV will be greater than the launch site latitude. The vehicle must be capable of achieving its target inclination within ±0.2° (Ref. 6).

The MAV must be designed to accommodate a wide variety of launch conditions due to the inability of the EDL system to precisely land at a predetermined location with desired launch orientation. At the time of this analysis, the MAV was targeted to land at Martian latitudes within 45° of the equator, resulting in the assumption of a 45° baseline launch latitude. Additional analysis of the EDL system indicates that launch latitudes of no greater than 30° could be provided to the MAV, however this information could not be included in this assessment. The current GLOM results, although baselined for a 45° latitude launch, encompass launches from any latitude less than or equal to 45°.

Uncertainty in landing location also necessitates that the MAV be capable of launching from a wide range of launch orientations. The results presented show the performance impact of a requirement to land on slopes of up to 20° from horizontal and guarantee a launch within 30° of the targeted launch elevation (Ref. 6). In addition to the launch elevation of the MAV, the azimuth of the launch platform on the Mars surface may also be uncontrolled. This could result in a launch into a nonoptimal launch azimuth orientation resulting in an associated reduction in performance. Currently the precision with which the optimal launch azimuth could be maintained during EDL is unknown. Options exist to mitigate the performance impact due to launch azimuth variation, including tighter controls on the final portions of EDL to orient the lander along the optimal launch azimuth or the use of a turntable to rotate the MAV into an optimal launch orientation. The elevation and azimuth assumptions made are intended guide decisions on the necessary lander capabilities. Eventually, these launch requirements will be traded at a system level against the MAV GLOM growth necessary to accommodate off-nominal launch conditions.

### 2.2 MAV TSTO Ascent Trajectory Profile

The MAV TSTO ascent profile is relatively simple and differs from most terrestrial launch vehicle profiles given that it does not use a continuous burn from surface to orbit. Instead two separate burns are used. The first burn starts at engine ignition (time = 0) and begins a 0.2 sec fixed attitude burn necessary to clear the launch platform. The first burn continues with an optimal pitch over maneuver. Depending on the controls being used, this maneuver could include optimal roll and yaw maneuvers in conjunction with pitch. Following the optimal control section of the burn, the aerodynamic angles (angle of attack, side slip and bank angle) are manipulated to put the vehicle in a zero aerodynamic angle orientation by the end of the first burn. After first stage burnout, the vehicle coasts to apoapsis, jettisoning the first stage and payload fairing before the start of the second stage burn. The current baseline assumption is that jettison occurs at an altitude of 200 km, but realistically it can occur any time after leaving the Martian atmosphere (approximately 100 km above the Martian surface) and before second stage ignition with no penalty to performance. Just prior to reaching apoapsis, a significantly shorter second burn, using an optimized control profile, is performed to raise the periapsis altitude and circularize the orbit. A theoretical operational concept, with baseline times and Martian altitudes, can be found in Figure 2.

### 2.3 TSTO Baseline Vehicle Design

The TSTO vehicle concept used for this analysis is a based on a vehicle previously developed by the NASA MAV team in 2001 (Ref. 7). The system masses, as sized for this vehicle, are shown in Table 1 with the baseline thrust and Isp assumptions in Table 2. These assumptions result in a total vehicle GLOM of 267.5 kg. The MAV solid rocket motor performance assumptions are consistent with the use of a stretched STAR 17A solid motor first stage and a stretched STAR 13A second stage. It is assumed for all studies, except for those involving stage masses, that propellant mass can be adjusted while holding dry mass static.
Figure 2.—MAV TSTO ascent operational concept.

TABLE 1.—TSTO MAV BASELINE MASSES

<table>
<thead>
<tr>
<th>MAV element</th>
<th>Mass, kg</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stage 1 dry</td>
<td>27.7</td>
<td>Motor casing, nozzle and interstage</td>
</tr>
<tr>
<td>Stage 1 propellant</td>
<td>158.6</td>
<td>Solid propellant stretched Star 17A derivative</td>
</tr>
<tr>
<td>Stage 2 dry</td>
<td>38.4</td>
<td>Motor casing, avionics, payload attach structure</td>
</tr>
<tr>
<td>Stage 2 propellant</td>
<td>34.7</td>
<td>Solid propellant Star 13A derivative</td>
</tr>
<tr>
<td>Payload fairing</td>
<td>3.1</td>
<td>PLF jettisoned with first stage at 200 km</td>
</tr>
<tr>
<td>Payload</td>
<td>5.0</td>
<td>Sample and Container</td>
</tr>
</tbody>
</table>

TABLE 2.—TSTO MAV BASELINE THRUST AND ISP

<table>
<thead>
<tr>
<th>Engine parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stage 1 thrust (N)</td>
<td>21576.8</td>
</tr>
<tr>
<td>Stage 1 Isp (s)</td>
<td>285.7</td>
</tr>
<tr>
<td>Stage 1 exit area (m²)</td>
<td>0.032</td>
</tr>
<tr>
<td>Stage 2 thrust (N)</td>
<td>6318.9</td>
</tr>
<tr>
<td>Stage 2 Isp (s)</td>
<td>285.5</td>
</tr>
<tr>
<td>Stage 2 exit area (m²)</td>
<td>0.0093</td>
</tr>
</tbody>
</table>

The Martian atmosphere and winds were modeled using a tabular representation of a mean Mars Global Reference Atmospheric Model (GRAM). Mars shape and gravity were specified using an oblate model with the constants listed in Table 3.

As the analysis to follow will show, mission and launch site assumptions have a large effect on the resulting vehicle GLOM. Therefore, it is necessary to identify the specific mission and launch site assumptions used in TSTO baseline such that the effects of the vehicle sensitivities presented can be better understood. The baseline launch site location and launch site orientation assumptions are specified in Table 4 along with the target orbital parameters.
TABLE 3.—MARS OBLATE GRAVITY MODEL

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>J2</td>
<td>1.96e-03</td>
</tr>
<tr>
<td>J3</td>
<td>0.0</td>
</tr>
<tr>
<td>J4</td>
<td>0.0</td>
</tr>
<tr>
<td>Mars gravitational constant (km³/s²)</td>
<td>42828.3</td>
</tr>
<tr>
<td>Mars rotation rate (rad/s)</td>
<td>0.71e-04</td>
</tr>
<tr>
<td>Mars equatorial radius (km)</td>
<td>3393.9</td>
</tr>
<tr>
<td>Mars polar radius (km)</td>
<td>3376.8</td>
</tr>
</tbody>
</table>

TABLE 4.—TSTO MAV BASELINE LAUNCH SITE AND MISSION ASSUMPTIONS

<table>
<thead>
<tr>
<th>Trajectory assumption</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Latitude (degrees)</td>
<td>45.0</td>
</tr>
<tr>
<td>Longitude (degrees)</td>
<td>0.0</td>
</tr>
<tr>
<td>Launch elevation angle (degrees)</td>
<td>90.0 (Vertical)</td>
</tr>
<tr>
<td>Launch azimuth (degrees)</td>
<td>88.8 (Optimal)</td>
</tr>
<tr>
<td>Target circular orbit altitude (km)</td>
<td>500</td>
</tr>
<tr>
<td>Target orbit inclination (degrees)</td>
<td>45</td>
</tr>
</tbody>
</table>

It is important to note that the 2001 TSTO vehicle assumes use of only pitch control with-in the plane of the launch azimuth, which is varied at the start of the problem to target a 45° inclination. Additionally, there is no control rate limit imposed, which results in control rates of approximately 20° per second. During this study, a concern was immediately raised that control rates of this magnitude were too large for a reasonable flight profile. A decision was made to limit all body control rates to 5° per second, since previous experience has shown that body control rates larger than this may result in the vehicle exceeding structural limits or requiring additional vehicle structure (James McDuffie, personal communication, December 16, 2009). Figure 3 shows the effect on the baseline GLOM, 267.5 kg, as the body pitch rate is constrained to various levels. The performance deltas in Figure 3 assume only pitch control, with launch azimuth optimized. Since the goal is to produce the lightest possible MAV to meet mission requirements, the 5 kg (2 percent) growth that results from a control rate change is not insignificant. The performance delta for control rate restrictions placed on out-of-pitch-plane control rates at a nonoptimal launch azimuth are larger and are addressed in Section 6.0.

![GLOM Growth at Varying Control Rate Restrictions](image)

Figure 3.—GLOM growth compared 2001 TSTO baseline for restricted control rates.
2.4 MAV SSTO Ascent Trajectory Profile

The SSTO MAV mission profile is similar to the TSTO trajectory in that it also uses two separate burns to reach orbit. The primary difference for the SSTO trajectory is that these burns are completed by the same stage. The first burn starts at engine ignition (time = 0) and begins the 0.2 sec vertical rise necessary to clear the launch platform. After vertical rise, the first burn continues with an optimal pitch over maneuver. Depending on the controls being used, this maneuver could include optimal roll and yaw maneuvers in conjunction with pitch over. Following the optimal control section of the burn, the aerodynamic angles (angle of attack, side slip, and bank angle) are varied to put the vehicle in a zero aerodynamic angle orientation by the end of the first burn. After burnout, the vehicle coasts to apoapsis, jettisoning the payload fairing before the start of the second stage burn. The current baseline assumption is that payload fairing jettison occurs at an altitude of 200 km, but can realistically occur any time after leaving the Martian atmosphere (approximately 100 km above the Martian surface) and before the start of the second burn with no effect on performance. Just prior to reaching apoapsis, a significantly shorter second burn, with an optimized pitch profile, is performed by the same stage to raise periapsis altitude and circularize the orbit. A theoretical operation concept, with baseline times and altitudes, can be found in Figure 4.

Figure 4.—MAV SSTO ascent operational concept.
2.5 SSTO Baseline Vehicle

Differing from the TSTO vehicle concept, the SSTO concept was not based on an existing vehicle design. The SSTO baseline inert mass was assumed to be similar to the sum of the TSTO baseline inert stage masses with some mass savings due to the removal of systems duplicated on both TSTO stages. An Isp equal to the stretched Star 17A motor was assumed, with an optimized thrust level. The much lower thrust level allowed the SSTO vehicle to complete the MAV mission with much less propellant than would have been necessary at higher thrust levels. The SSTO baseline vehicle configuration, including the optimized engine thrust, is detailed in Table 5 and Table 6. The SSTO mission and launch site assumptions were identical to those used for the TSTO vehicle and are repeated in Table 7 with the vehicle launching from a vertical orientation.

The SSTO baseline used only pitch steering, with control rates limited to $5^\circ$ per second, while varying launch azimuth to target inclination. Models for the MAV aerodynamics, Mars Gravity and Mars atmosphere are identical to the TSTO vehicle baseline. Further discussion of the SSTO baseline trajectory assumptions is included in the Section 5.0.

<table>
<thead>
<tr>
<th>MAV element</th>
<th>Mass, kg</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stage dry</td>
<td>61.9</td>
<td>Motor casing, avionics, payload attach structure</td>
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<tr>
<td>Payload fairing</td>
<td>3.1</td>
<td>PLF jettisoned with first stage at 200 km</td>
</tr>
<tr>
<td>Payload</td>
<td>5.0</td>
<td>Sample and container</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Engine parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thrust (N)</td>
<td>4425.7</td>
</tr>
<tr>
<td>Isp (s)</td>
<td>285.7</td>
</tr>
<tr>
<td>Exit area (m$^2$)</td>
<td>0.032</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Trajectory assumption</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Latitude (degrees)</td>
<td>45.0</td>
</tr>
<tr>
<td>Longitude (degrees)</td>
<td>0.0</td>
</tr>
<tr>
<td>Launch elevation angle (degrees)</td>
<td>90.0 (Vertical)</td>
</tr>
<tr>
<td>Launch azimuth (degrees)</td>
<td>87.3 (Optimal)</td>
</tr>
<tr>
<td>Target circular orbit altitude (km)</td>
<td>500</td>
</tr>
<tr>
<td>Target orbit inclination (degrees)</td>
<td>45</td>
</tr>
</tbody>
</table>
3.0 Trade Space Description

The mission and launch assumptions of the MAV have a direct effect on the vehicle GLOM, primarily through the amount of propellant necessary to successfully reach orbit for each set of assumptions. Vehicle mass and engine performance assumptions also have an effect on MAV GLOM, through the mass of the components used as well as their effect on the amount of propellant needed to reach orbit.

To better understand the sensitivities to be discussed, Figure 5 depicts the assumed relationship between launch latitude and launch inclination with targeted inclination always assumed to be greater than or equal to the launch latitude. The orientation of the launch platform on the surface of Mars is also important to understand and is illustrated in Figure 6. The platform orientation is defined using two angles, the launch elevation angle, 90° as shown, and the launch azimuth, measured clockwise from north. For each combination of launch latitude, targeted orbit inclination and launch elevation angle the optimal launch azimuth is calculated during analysis. The optimal launch azimuth corresponds to the minimum GLOM solution for each latitude and inclination combination. For the sensitivities presented here, it is more useful to express the simulated vehicle launch azimuth as the angle from the optimal launch azimuth, as defined in Figure 6. Further description and discussions of these values is found in Section 6.0, along with the sensitivity results.

Figure 5.—Target orbit inclination in relation to launch latitude.
TABLE 8.—RANGE OF MAV PARAMETERS ANALYZED

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Minimum</th>
<th>Maximum</th>
</tr>
</thead>
<tbody>
<tr>
<td>Launch latitude (degrees)</td>
<td>0</td>
<td>90</td>
</tr>
<tr>
<td>Launch elevation (degrees)</td>
<td>30</td>
<td>90</td>
</tr>
<tr>
<td>Angle from optimal launch azimuth (degrees)</td>
<td>0</td>
<td>180</td>
</tr>
<tr>
<td>Engine Isp (s)</td>
<td>255</td>
<td>355</td>
</tr>
<tr>
<td>Engine thrust (N)</td>
<td>Optimal</td>
<td>21576.8</td>
</tr>
<tr>
<td>Total inert mass (kg)</td>
<td>30</td>
<td>70</td>
</tr>
<tr>
<td>Target inclination (deg)</td>
<td>0</td>
<td>90</td>
</tr>
<tr>
<td>Target orbit altitude (km)</td>
<td>400</td>
<td>600</td>
</tr>
</tbody>
</table>

The large trade space of mission, launch and vehicle assumptions that were analyzed for MAV GLOM sensitivities are listed, with ranges, in Table 8. It should be noted that this analysis looked only at northern latitudes but it is assumed, due to symmetry, that launches from southern latitudes would remain the same. To break down this vast trade space, the parameters were studied in several different ways.

First, assuming use of an optimal launch azimuth, a large matrix of MAV GLOM sensitivities were completed for all combinations of launch latitude, launch elevation, and targeted orbit inclination. Second, sensitivities for launches at a nonoptimal launch azimuth were run for all launch elevation angles at the baseline launch latitude of 45° targeting a 45° orbital inclination. Although only off-azimuth launches from 0° to 180° were analyzed, it is assumed due to symmetry that launch from 0° to –180° would produce similar results. The remaining vehicle and mission sensitivities were run using the baseline launch and mission assumptions, including the use of an optimal launch azimuth at a vertical launch elevation, as listed in Table 4.

The previously developed TSTO MAV solid rocket concept is assumed to be the primary MAV baseline design for this analysis. Therefore, sensitivities to all parameters listed in Table 8 were run with vehicle assumptions consistent with the TSTO baseline vehicle. This included a range of vehicle sensitivities large enough to show how GLOM would change if using a liquid engine instead of the solid motor design. A subset of vehicle and mission sensitivities were also evaluated for the SSTO concept, such that the viability for further evaluation could be established.
4.0 Analysis Tools and Methodology

4.1 OTIS

Optimal Trajectories by Implicit Simulation program (OTIS) is a general-purpose simulation and optimization program, which can be used to perform trajectory performance studies (otis.grc.nasa.gov) (Ref. 8). A user can simulate and optimize a wide variety of vehicles such as aircraft, missiles, reentry vehicles, ascent vehicles, satellites, and interplanetary vehicles. The vehicle models used in OTIS are defined by user inputs; there are no embedded, vehicle specific aerodynamic or propulsion models. OTIS is primarily a point mass, three-degree of freedom (3DOF) program. It makes available to the user two well known and proven optimizer options: SNOPT and SLSQP. The program name is derived from the implicit methods used to solve differential equations, which were distinctive at the time of OTIS’ origin. Although named after its implicit integration capabilities, OTIS is capable of generating flight paths using implicit, explicit or analytical integration. Trajectory analysis using OTIS can be performed with respect to any of the major bodies in the solar system.

4.2 POST 3D

Program to Optimize Simulated Trajectories (POST) 3D is a generalized point mass, discrete parameter targeting and optimization program (Ref. 9). POST provides the capability to target and optimize point mass trajectories for a powered or unpowered vehicle near an arbitrary rotating, oblate planet. POST has been used successfully to solve a wide variety of atmospheric ascent and reentry problems. The generality of the program is evidenced by its multiple phase simulation capability which features generalized planet and vehicle models. This flexible simulation capability is augmented by an efficient discrete parameter optimization capability that includes equality and inequality constraints.

4.3 Analysis Methodology

Vehicle sensitivities were established for the MAV through the minimization of the GLOM. In all cases, this results in the vehicle propellant load being varied to minimize the total vehicle mass. POST and OTIS used control angles, along with propellant weights, to find the optimal combination of parameters. In selected cases, thrust was also left open for optimization to also characterize the thrust level providing minimal vehicle mass. The majority of cases used static vehicle weights and engine parameters as described in Section 2.0.

The sensitivities presented here were initially run in both POST and OTIS such that both the baseline cases and sensitivity results could be compared. To do so, Python scripts were developed to independently run each desired vehicle sensitivity. The functionality of the scripts necessary to run each analysis program was quite different due to the differing methods in which POST and OTIS operate. Despite differences in operation, these run scripts provided three important functions: run each optimization case while ensuring an optimal result, vary the input parameters necessary to accomplish each parameter sweep and record desired output data for post processing.

To run each case, the scripts contained the ability to correctly read and interpret the optimization output from POST or OTIS. After each case was successfully optimized, the script would automatically increment the parameter, or parameters, of interest and rerun the program. This process was repeated until the entire parameter range was completed. For OTIS, no additional guess generation or guess tweaks were necessary, as the next case was easily converged from a previously converged case. In POST, the operation was a bit more complex as it was necessary to use a combination of a bi-section step algorithm and a genetic algorithm to automatically generate independent variable guesses for each new POST run that would allow successful problem completion. This allowed for less user interaction with each POST run and helped to minimize noise in the POST GLOM results.
Figure 7.—Comparison of POST and OTIS MAV GLOM sensitivity data.

POST and OTIS comparisons show matching results for the baseline cases as well as matching trends for the various GLOM sensitivities completed. A detailed comparison of the POST and OTIS SSTO and TSTO baseline cases can be found in Section 5.0. A close match between these programs is not unexpected, as previous studies have shown a close correspondence between POST and OTIS results (Ref. 10). Although great care was taken to ensure that POST found the most optimal solution, a great deal of noise was observed in the POST GLOM sensitivity results. An in depth comparison between the POST and OTIS sensitivities is not included here, but matching trends were observed for all sensitivities analyzed. Due to the smoother resulting OTIS trends, all GLOM sensitivity data discussed in this document is derived from OTIS results. An example of the noise in the POST GLOM results, compared to OTIS results, is found in Figure 7.

5.0 MAV Baseline Comparison

5.1 TSTO POST and OTIS Trajectory Comparison

Using the payload, dry mass, thrust and Isp assumptions listed in Table 1 and Table 2 an OTIS TSTO model was developed at NASA’s Glenn Research Center (GRC) along with a POST TSTO model by the team at NASA’s Marshall Space Flight Center (MSFC). The existing TSTO baseline mission and launch site assumptions were also used as defined in Table 4. This includes the important assumption of a vertical launch orientation and the use of an optimal launch azimuth. As described above, the propellant loads for both the first and second stages were allowed to vary so that the minimum overall GLOM could be achieved. The orbital targets were defined using orbit radius, inertial velocity, inertial flight path angle and inclination with the values listed in Table 9.
TABLE 9.—TRAJECTORY TARGET PARAMETERS

<table>
<thead>
<tr>
<th>Orbital target parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Orbit radius (km)</td>
<td>3893.9</td>
</tr>
<tr>
<td>Inertial velocity (km/s)</td>
<td>3.316</td>
</tr>
<tr>
<td>Inertial flight path angle (degrees)</td>
<td>0.0</td>
</tr>
<tr>
<td>Orbital inclination (degrees)</td>
<td>45.0</td>
</tr>
</tbody>
</table>

Both programs used launch inertial Euler angles to control the vehicle orientation during the first and second burns. Figure 8 shows the basis for the launch inertial Euler control angles. This coordinate system is centered at the longitude and geodetic latitude of the launch site with a fundamental plane formed by the y and z-axis, parallel to local horizontal. The x-axis, $X_{launch}$, is perpendicular to this plane and points up (i.e., lies along the positive radius vector). The z-axis, $Z_{launch}$, is the reference direction and points downrange along the launch site azimuth, as measured clockwise around $X_{launch}$, with the y-axis, $Y_{launch}$, completing the right-handed system. The launch inertial Euler angles, are then calculated based on the coordinate system in Figure 8 using a 1-3-2 Euler angle rotation as shown in Figure 9. In this diagram, the first rotation is by the inertial Euler roll angle, $\phi$, around the vehicle’s x-axis, $X_{body}$, which in initially concurrent with $X_{launch}$. The second rotation of the inertial Euler yaw angle, $\psi$, is then completed around the vehicle z-axis, $Z_{body}$. The third and final rotation is the inertial Euler pitch angle, $\theta$, around the vehicle y-axis, $Y_{body}$.
Figure 9.—Launch inertial Euler control angle rotation sequence.

### TABLE 10.—COMPARISON OF OTIS AND POST BASELINE TSTO BASELINE TRAJECTORIES

<table>
<thead>
<tr>
<th>Comparison parameter</th>
<th>POST</th>
<th>OTIS</th>
<th>POST - OTIS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gross lift-off mass (kg)</td>
<td>271.75</td>
<td>272.63</td>
<td>–0.88 (0.32%)</td>
</tr>
<tr>
<td>Launch azimuth (deg)</td>
<td>88.77</td>
<td>87.56</td>
<td>1.21 (1.37%)</td>
</tr>
<tr>
<td>First stage propellant load (kg)</td>
<td>149.31</td>
<td>153.85</td>
<td>–4.54 (–3.04%)</td>
</tr>
<tr>
<td>Second stage propellant load (kg)</td>
<td>48.24</td>
<td>44.67</td>
<td>3.58 (7.41%)</td>
</tr>
<tr>
<td>Mission time (s)</td>
<td>656.67</td>
<td>659.09</td>
<td>–2.42 (–0.37%)</td>
</tr>
<tr>
<td>Maximum dynamic pressure (Pa)</td>
<td>11956.65</td>
<td>12290.78</td>
<td>–334.13 (–2.79%)</td>
</tr>
<tr>
<td>Maximum dynamic pressure (psf)</td>
<td>249.72</td>
<td>256.70</td>
<td>–6.98 (–2.79%)</td>
</tr>
</tbody>
</table>

Both the POST and OTIS models use one linear segment to control the inertial Euler pitch angle during pitch over, with inertial roll and yaw angles set to zero. For this analysis, a linear control segment is defined as period of time where the control angle is varied at a constant (linear) rate. To reach a zero angle of attack (AOA) before first stage burnout, aerodynamic control angles (AOA, side slip, and bank angle) are then used with one linear control segment for each angle. After first stage burnout, aerodynamic control angles continue to be used to maintain a zero aerodynamic angle gravity turn. The second stage burn then uses one linear segment to control the inertial Euler pitch angle, with the inertial Euler roll and yaw angles held constant. For the TSTO vehicle model, the vehicle orientation is assumed to remain unchanged throughout the coast period up to the start of the final burn through use of the vehicle’s reaction control system (RCS). The OTIS and POST baseline vehicle models, using the assumptions detailed above, are shown in Table 10. All comparisons in Table 10 are relative to POST, meaning the OTIS result is subtracted from POST and then compared to the POST result to determine the percentage difference.

The comparison results demonstrate a match of the MAV trajectory from each program with a GLOM difference between the POST and OTIS baselines of less than 1 kg or about 0.3 percent. Due to the control rate restriction imposed it can be seen that both the OTIS and POST GLOM are approximately 5 kg greater than the existing TSTO baseline of 267.5 kg, which is consistent with the GLOM trend found in Figure 3. The percentage deltas in the propellant load of each stage appear to be large, but the total propellant burned by each simulation is similar, as evident by the small GLOM differences. The different solutions found by each program cause more propellant to be burned by OTIS in the first stage and less in the second.
evident that these differences in each burn also result in slightly different burn times, again with little change to the overall trajectory. Finally the maximum dynamic pressure difference is a direct result of the slightly longer OTIS burn on the first stage. A dynamic pressure difference of 6.98 psf, out of 249.7 psf, is a small difference compared to loads experienced by many Earth based launch vehicles.

In conjunction with the small deltas in the parameters discussed, similar trends in other key trajectory parameters also demonstrate the close POST/OTIS model match. Important trajectory parameters compared for match purposes include all vehicle control angles, physical states and loading indicators. All parameter comparisons are not shown here for brevity. Figure 10 through Figure 13 show the geodetic altitude, inertial velocity, inertial pitch angle, angle of attack, and dynamic pressure plotted against mission elapsed time (MET). All plots show matching trends with only minor differences. The differences in the length of the first and second burn, as discussed above, can be seen more clearly in the plot of inertial velocity and geodetic altitude versus time, Figure 10. OTIS adds more velocity in the first burn; both programs then lose velocity through the coast to apoapsis and, after the second burn, end at the same inertial velocity target. The effects of the Mars GRAM wind model are evident in the plot of inertial pitch angle, Figure 11, between approximately 20 and 150 sec. The odd shape found from the control history of both programs results from holding zero angle of attack through the wind profile modeled. The assumption made is that the vehicle will always stay oriented with the velocity vector relative to the wind, which may not be the case in the real world. This simplifying assumption has very little impact in overall vehicle performance but does affect the shape of the controls and launch azimuth necessary to target the required inclination. Figure 14 and Figure 15 demonstrate how the control angle histories change when no wind profile is modeled. For the baseline case, when wind was not included, the GLOM increased by approximately 0.2 kg, demonstrating dependence on the wind for additional vehicle performance is insignificant. Further impacts of wind modeling and the assumption of control continuity will be discussed in Section 6.0.

![Geodetic Altitude and Inertial Velocity vs Time](image)

Figure 10.—Comparison geodetic altitude and inertial velocity histories for OTIS and POST TSTO baseline.
Figure 11.—Comparison of inertial Euler control angle history for OTIS and POST TSTO baseline.

Figure 12.—Comparison of AOA history for OTIS and POST TSTO baseline.
Figure 13.—Comparison of dynamic pressure history for OTIS and POST TSTO baseline.

Figure 14.—OTIS inertial Euler pitch history comparison of wind modeling.
5.2 SSTO POST and OTIS Trajectory Comparison

Similar to the TSTO models, a GRC OTIS model and MSFC POST model were completed for the SSTO baseline vehicle. Comparison of the POST and OTIS SSTO models were complicated by the optimization of thrust. As comparisons between the POST and OTIS solutions were completed, using the assumptions in Table 5 through Table 7, two main points became evident: POST was locked onto a suboptimal solution which did not utilize all available pitch control rate and OTIS was leveraging the modeled wind profile to find a slightly lower GLOM solution. To mitigate the effect of wind on the design solution, the wind profile was removed from all SSTO cases to prevent it from driving the design of the vehicle. With POST locked onto a suboptimal solution, a decision was made to compare POST and OTIS with OTIS constrained to use the POST generated values of optimal thrust and control rate.

The SSTO baseline comparison also shows that allowing the vehicle orientation to vary at the start of the second burn results in both a smaller GLOM and smaller optimized thrust value. Similar to the TSTO vehicles, where it is assumed that the MAV RCS system is used to maintain a constant vehicle orientation, the SSTO RCS system would be used to orient the vehicle to a more optimal second stage burn orientation.

A minimum GLOM OTIS solution was established using the baseline assumption of a $5^\circ$ per second control rate with no lower limit on the optimized thrust value. As noted, matching the POST solution required additional constraints in OTIS, as listed in Table 11, to model the values used by POST. The parameters in Table 11 are the optimal values of the independent variables calculated by POST to minimize initial mass for the SSTO baseline. All three solutions for the SSTO vehicle can be found in Table 12, which compares the POST solution to the OTIS case that uses the restricted parameters in Table 11. Importantly, the last column in Table 12 is the minimum GLOM OTIS case that is considered the baseline solution to which all SSTO sensitivities should be compared. All comparisons in Table 12 are relative to POST, meaning the OTIS results is subtracted from POST and then compared to the POST results to determine the percentage difference.

![Figure 15.—OTIS AOA history comparison of wind modeling effects.](image)
TABLE 11.—OTIS CONSTRAINTS NECESSARY TO MATCH POST SSTO BASELINE

<table>
<thead>
<tr>
<th>Additional OTIS constraints</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>POST thrust (N)</td>
<td>6082.0</td>
</tr>
<tr>
<td>POST control rate (degree/sec)</td>
<td>3.1</td>
</tr>
</tbody>
</table>

TABLE 12.—COMPARISON OF OTIS AND POST BASELINE SSTO BASELINE TRAJECTORIES

<table>
<thead>
<tr>
<th>Comparison parameter</th>
<th>POST</th>
<th>OTIS (POST Match assumptions)</th>
<th>POST - OTIS</th>
<th>OTIS (minimum GLOM assumptions)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gross lift-off mass (kg)</td>
<td>288.2</td>
<td>288.6</td>
<td>-0.4 (-0.1%)</td>
<td>285.6</td>
</tr>
<tr>
<td>Launch azimuth (deg)</td>
<td>91.8</td>
<td>87.2</td>
<td>4.6 (5.0%)</td>
<td>87.3</td>
</tr>
<tr>
<td>Propellant load (kg)</td>
<td>218.2</td>
<td>218.8</td>
<td>-0.6 (-0.3%)</td>
<td>215.7</td>
</tr>
<tr>
<td>Mission time (s)</td>
<td>1039.8</td>
<td>1062.0</td>
<td>-22.1 (-2.1%)</td>
<td>1204.2</td>
</tr>
<tr>
<td>Maximum dynamic pressure (Pa)</td>
<td>3363.3</td>
<td>3505.6</td>
<td>-142.3 (4.2%)</td>
<td>2996.0</td>
</tr>
<tr>
<td>Maximum dynamic pressure (psf)</td>
<td>70.2</td>
<td>73.2</td>
<td>-3.0 (-4.2 %)</td>
<td>62.6</td>
</tr>
<tr>
<td>Thrust (N)</td>
<td>6082.0</td>
<td>6082.0</td>
<td>0.0</td>
<td>4425.7</td>
</tr>
<tr>
<td>Max control rate (deg/s)</td>
<td>3.1</td>
<td>3.1</td>
<td>0.0</td>
<td>5.0</td>
</tr>
</tbody>
</table>

Comparisons of POST to the OTIS cases using similar thrust and control rate assumptions, show that the OTIS GLOM matches POST within 0.1 percent or approximately 0.4 kg. However, this close match in GLOM does come with a slight difference to the trajectories flown by both programs. The two major differences show up in total mission time, 22.1 sec, and initial launch azimuth, 4.6°. Differences in launch azimuth are primarily related to the control sets used for both solutions. Similar to the TSTO solution, the OTIS model uses the launch inertial Euler control set, Figure 9, for both vehicle burns. The POST model used the launch inertial Euler control set for the first burn, but due to convergence issues used the inertial aerodynamic control set for the second burn. Differing control sets necessitated the use of different launch azimuths to target the same inclination. The total mission time difference is closely correlated with the remaining large difference observed in dynamic pressure of 2.9 psf. This difference is smaller than that found in the TSTO comparisons, but a larger percentage due to the smaller overall SSTO maximum dynamic pressure. Compared to the TSTO baseline, the SSTO trajectories all fly a much slower, more depressed trajectory, due to the much smaller thrust used on the SSTO vehicle. When comparing the SSTO trajectories, the POST case flies a slightly more lofted trajectory, hence the lower dynamic pressure of 70.2 psf. This causes POST to reach apoapsis slightly before the OTIS trajectory resulting in a smaller overall mission time.

The minimum GLOM OTIS case, by using a lower thrust and body control rates of up to 5° per second, is able to reduce GLOM by an additional 3 kg compared to POST. This comes with a dynamic pressure 7.7 psf lower than the POST case and a significantly longer total mission time. The lower thrust, coupled with a higher control rate, allows OTIS to gain velocity over a longer period of time resulting in longer first burn. This effect results in the lower dynamic pressure observed for this trajectory. The differences and similarities between all three trajectories are more easily observed in plots of geodetic altitude, inertial velocity, inertial Euler pitch angle, inertial Euler yaw angle, and dynamic pressure plotted against mission elapsed time (MET) found in Figure 16 through Figure 19.

In looking at these comparison plots, key characteristics are noted. First is the difference in burn lengths that is evident in Figure 16, which shows inertial velocity and geodetic altitude. The Minimum OTIS GLOM case can be observed to burn substantially longer than the other two cases and adds more velocity during the first burn. However it is interesting to note, that this larger velocity is coupled with a less lofted trajectory, resulting in the much longer burn time. Also of note is the absence of wind effects in the inertial control angles, due to the removal of the wind model for the SSTO vehicle analysis. Finally, both the inertial pitch and yaw plots, Figure 17 and Figure 18, clearly show the discontinuous control angles at the beginning of the second burn in both the POST and OTIS simulations.
Figure 16.—Comparison of geodetic altitude and inertial velocity histories for POST and OTIS SSTO baselines.

Figure 17.—Comparison of inertial Euler pitch control history for POST and OTIS SSTO baselines.
Figure 18.—Comparison of inertial Euler yaw control history for POST and OTIS SSTO baselines.

Figure 19.—Comparison of dynamic pressure history for POST and OTIS SSTO baselines.
The SSTO match results again demonstrate that with consistent assumptions, POST and OTIS produce similar trajectory results. Comparisons between these trajectories show that both programs are modeling the SSTO vehicle in a similar manner indicating matching simulations. This is demonstrated both in the performance match and through comparison of the trajectory parameter trends. In this case, OTIS was able to fully utilize the baseline mission constraints to find a more optimal solution. Additional discussion of the use of a wind model and its effects on the SSTO GLOM sensitivities is included in Section 7.0.

6.0 TSTO GLOM Sensitivities

6.1 GLOM Sensitivity to Target Inclination, Launch Latitude, and Launch Elevation

Before, and to a lesser degree after, a landing site is selected there is the potential for variability in the location and type of terrain on which the MAV launch platform may come to rest. Although the MAV lander is targeted to land with ±30° latitude of the equator, a broader latitude range of 0° to 90° was analyzed to establish complete GLOM growth trends. The launch elevation angle, as shown in Figure 6, is defined as the launch angle of the MAV measured from local horizontal. This results in a 90° elevation angle when the MAV is launched vertically as modeled for the TSTO and SSTO baseline cases. Launch latitudes between 0° and 90° were analyzed at launch elevations from 30° to 90°. Also shown in Figure 6 is the orientation of the MAV launch azimuth relative to the optimal launch azimuth. For all latitude/inclination/elevation sensitivities shown, the vehicle is always launched along the optimal launch azimuth, which corresponds to an off optimal azimuth angle of zero as defined in Figure 6. Section 6.2 will discuss the nonoptimal launch azimuth geometry in further detail and present GLOM sensitivities at varying off optimal launch azimuth and elevation combinations.

For each latitude and elevation combination, a range of target inclinations up to 90° was also analyzed. From spherical geometry, only inclinations greater than or equal to the current latitude can be reached during ascent, as shown in Figure 5. To reach an inclination lower than the current latitude, an additional burn would be necessary after reaching orbit. The GLOM penalty for doing an additional burn is quite high as demonstrated in Figure 20, which shows the total GLOM increase from the OTIS TSTO baseline, 272.6 kg, plotted against on-orbit inclination change capability. The GLOM increase observed consists of the propellant necessary to perform the on-orbit inclination change maneuver as well as the additional MAV GLOM needed to lift that propellant to orbit. If the MAV were to launch from a 30° inclination and needed to end up in an equatorial (0° inclination) orbit, a 30° on-orbit inclination change would be necessary with an associated GLOM increase of approximately 168 kg.

For a launch latitude of 0° (equatorial) the resulting GLOM growth for varying both launch elevation and target orbit inclination are shown in Figure 21. It is noted that for optimal azimuth launches at a launch latitude and target inclination of zero, any elevation angle less than 90° results in a GLOM less that the TSTO baseline of 272.6 kg. The minimum total GLOM was found at a launch elevation angle near 45°. This can be more clearly seen in Figure 22, which shows only the 90°, 45°, and 30° launch elevation angles. A direct relationship between GLOM and inclination was hard to develop due to the nonlinear nature of the results. Figure 23 plots the slope of the curves shown in Figure 22 and demonstrates this nonlinear behavior. It can be observed that as the targeted inclination reaches 90°, the change in GLOM per degree inclination approaches a constant value of 0.33 kg GLOM per degree in inclination. This translates into a maximum GLOM necessary to cover launches to inclinations up to 90° of approximately 286 kg, an increase of about 13 kg over the TSTO baseline. Further, by limiting launches to inclinations less than or equal to 45°, the baseline GLOM can be maintained for any launch elevation angle. For brevity, only the equatorial latitude results are shown here. The remaining elevation and inclination combinations for all launch latitudes are shown in Appendix A.
Figure 20.—GLOM growth for an on-orbit inclination change necessary to reach inclinations lower than the launch latitude.

Figure 21.—GLOM sensitivity for all launch elevations and target orbit inclinations at a launch latitude of 0°.
Figure 22.—GLOM sensitivity for selected elevations and target orbit inclinations at a launch latitude of $0^\circ$.

Figure 23.—Slope of GLOM change per degree of inclination for a launch latitude of $0^\circ$ at selected launch elevations.
Interesting insight results from looking at the same GLOM sensitivities at a constant launch elevation angle for combinations of launch latitude and target inclination, found in Figure 24 for a $90^\circ$ launch elevation and Figure 25 for a $45^\circ$ launch elevation. Both of these figures demonstrate that for any target inclination, GLOM grows by about 0.23 kg per $10^\circ$ of launch latitude. The data run for all other combinations of launch parameters, not shown here, demonstrates that GLOM growth of this magnitude can be expected for all launch elevations. This means that if targeting a $90^\circ$ inclination orbit, the GLOM difference between launching from a pole, instead of the equator, is only about 2 kg. This is a significant finding as this indicates that launch latitude makes very little difference in the size of the MAV, as long as that latitude is less than or equal to the target inclination.

Figure 24.—GLOM sensitivity for all launch latitudes to target orbit inclinations greater than the launch latitude, at a launch elevation of $90^\circ$.

Figure 25.—GLOM sensitivity for all launch latitudes to target orbit inclinations greater than the launch latitude, at a launch elevation of $45^\circ$.
For a launch latitude of 45° and a vertical launch elevation, a number of inclination sweeps were run to estimate the effects of control rate, control continuity and wind modeling on the GLOM sensitivities presented in this section. It is expected that the trends shown here are representative of the remaining launch elevations and launch latitudes. As Figure 26 and Figure 27 show, control continuity and the use of a wind model have less that 0.25 kg effect on the GLOM trends generated. Although not shown here, the effects of these modeling assumptions remain similar when combined. The use of varying pitch body control rates for these sweeps was also analyzed, with the results found in Figure 28. GLOM is predictably lower with the use of higher body control rate limits and matches closely with the GLOM trend presented in Figure 3.

**Figure 26.**—Impact of control continuity on TSTO GLOM sensitivity of a vertical launch elevation to an inclination greater than the launch latitude of 45°.

**Figure 27.**—Impact of wind modeling on TSTO GLOM sensitivity of a vertical launch elevation to an inclination greater than the launch latitude of 45°.
Figure 28.—Impact of control rate limit on TSTO GLOM sensitivity of a vertical launch elevation to an inclination greater than the launch latitude of 45°.

6.2 Sensitivity to Launch Azimuth and Launch Elevation

The GLOM sensitivities discussed for latitude, inclination and launch elevation, all assume that the MAV is able to lift off and pitch over directly into the optimal launch azimuth. This provides the minimal GLOM for each set of launch conditions. The optimal launch azimuth varies greatly as the launch latitude and target inclination change. However, the entry, descent and landing system may not be able to guarantee that the MAV launch platform will land in an orientation that allows a direct launch into the optimal launch azimuth. This necessitates that GLOM sensitivities be established for launches to azimuths not aligned with the optimal launch azimuth. As depicted in Figure 6, the distance from the optimal launch azimuth for each case considered is quantified as the angle from the optimal launch azimuth. An angle from optimal azimuth of zero results in a vehicle launch aligned with optimal, while an angle 180° represents a launch in exactly the opposite direction from the optimal azimuth.

GLOM sensitivities were established from the baseline launch assumptions, with a launch from a latitude of 45° and an inclination target of 45°. Each nonoptimal launch azimuth case was analyzed using the full set of control angles, allowing for the vehicle’s pitch, yaw and roll angles to be varied. This is necessary since it is not possible to launch from varying launch azimuths to the same inclination target without the use of out of pitch plane control. Similar to the TSTO baseline, all out of pitch plane controls are calculated using one linear control segment during the first stage burn with a second linear segment used to ramp aerodynamic angles to zero. Each angle is also controlled using one linear segment during the second stage burn.

Launch elevation angle is a key driver in the sensitivity of GLOM to launch azimuth variation. If the vehicle is assumed to always launch at a 90° launch elevation angle, as shown in Figure 6, the optimal azimuth can be reached with very little effect to GLOM. As launch elevation angle is decreased, the effect on GLOM to launch at varying azimuths increases dramatically. This assessment considers the impact to GLOM if launch elevation can be guaranteed within 30° of the targeted launch elevation. Therefore, GLOM comparisons were made for elevation angles from 60° to 90°, to establish sensitivities for a
mission designed to launch vertically. GLOM comparisons were also made for a mission designed to launch at a 45° elevation, for elevation angles from 30° to 75°. The results for off optimal azimuth angles from 0° to 180° are shown for the vertical launch in Figure 29 with deltas based on the baseline GLOM of 272.6 kg. Figure 30 shows the 45° launch elevation sensitivities, compared to a baseline GLOM of 265.8 kg. It is assumed that GLOM sensitivities to launch azimuth are symmetric, with the GLOM growth for off azimuth angles from 0° to –180° being similar to the results for off azimuth angles from 0° to 180° shown here.

Figure 29.—GLOM delta for off optimal launch azimuths based on vertical launch with GLOM of 272.6 kg.

Figure 30.—GLOM delta for off optimal launch azimuths based on 45° elevation launch with GLOM of 265.8 kg.
The off optimal launch azimuth cases analyzed demonstrate that for a nonvertical launch, maintaining the launch azimuth within approximately 80° of optimal, keeps the total GLOM under the documented TSTO baseline of 272.6 kg. For a targeted 45° launch, if the launch azimuth can be guaranteed with approximately 70° of optimal, the TSTO baseline GLOM can be maintained. Additionally a launch azimuth restriction of approximately 40° from optimal would allow for GLOM to be reduced by about 6 kg from the TSTO baseline vertical launch GLOM. If the launch azimuth cannot be guaranteed within these ranges, it is apparent that launching close to vertical provides the smallest GLOM growth for large off azimuth angles. The performance sensitivities shown are only valid for launch inclinations and latitudes between 0° and 45°. Launches to inclinations greater than 45° will result in higher GLOM increases for off azimuth launches, caused by the larger GLOM necessary for an optimal azimuth launch to high inclinations.

Similar to the previous set of sensitivities, additional GLOM sweeps were completed to identify the effects of varying control rates as well as not enforcing control continuity for the start of the second burn. These cases were run for only a launch elevation of 45° while targeting an orbital inclination of 45°. The angle from optimal azimuth was varied between 0° and 90°, with GLOM comparisons made back to the baseline TSTO GLOM of 272.6 kg. Figure 31 shows the effect on the presented GLOM sensitivities, when the maximum body control rate was varied. In these cases all angles were controlled and therefore limited to this maximum rate. These cases are driven primarily by the speed at which they can roll and yaw into the optimal azimuth so it is not surprising that increasing controls rates reduce the GLOM at 90° off azimuth by 10 kg. The use of control continuity was also examined, while maintaining the baseline body control rate of 5° per second with results shown in Figure 32. It is quickly observed that control continuity has very little effect the GLOM trend observed, with GLOM being reduced by less than 0.25 kg.

![Figure 31.—GLOM delta for off optimal launch azimuths using varying control rate limits, based on a GLOM of 272.6 kg.](image-url)
6.3 Circular Orbit Altitude Sensitivity

With the sensitivity to insertion orbit inclination well characterized, it was also necessary to determine sensitivity to the targeted circular orbit altitude. As Figure 33 shows, the delta in GLOM for variations in targeted altitude are small. A weight change of approximately 5.1 kg of GLOM per 50 km of altitude was observed, with GLOM growing as circular orbit altitude increases. This partial was much lower than expected and results in minimal impact to the vehicle for changes in final orbit altitude.

6.4 Vehicle Mass and Engine Parameter Sensitivities

6.4.1 Stage Mass

All sensitivities presented to this point assumed vehicle mass and engine parameters consistent with the TSTO baseline. To analyze the effect of changes to the inert mass of both TSTO stages, a matrix of different first and second stage mass combinations were run. The range studied represents a total inert mass range of 30 to 70 kg, with the mass shifted between each stage to cover all combinations of first and second stage masses. After running the entire matrix of cases developed, two different plots were generated. The first, Figure 34, shows the GLOM growth along lines of constant first stage mass, for varying second stage masses. The second, Figure 35, show the opposite, with lines of constant second stage mass for varying first stage weights.
From Figure 34 and Figure 35, partials were identified for GLOM growth with respect to mass changes in each stage. These show that for every kilogram of first stage growth, a GLOM increase of 1.9 kg can be expected. For the same 1 kg growth on the second stage, a 4.6 kg growth in GLOM can be expected. A third partial falls out from the first two; in that vehicle GLOM can be decreased by 2.7 kg for every kilogram of mass that can be shifted from second stage to the first. Since the first stage can stay with the vehicle until just before second stage ignition, this could present the opportunity to reduce GLOM by shifting functionality, and mass, to the first stage. These partials demonstrate the well-known benefit of staging, showing that mass added to the first stage comes at a cheaper cost to performance than mass added to the second stage.

For a constant Isp, the partials identified apply to any combination of inert masses, and do not change as total vehicle mass increases. As other vehicle parameters changed, the calculated mass partials also change. This is evident in Figure 36 and Figure 37, which show the change in dry mass partial as Isp is changed for both the first and second stage. Although the partial does not change drastically over the Isp range analyzed, it does show that increases in Isp allow mass to be added to the vehicle at a lower rate. However, the reverse also applies that the GLOM savings are mitigated at higher Isp values for decreases in stage mass. These are important partials for vehicle designers to keep in mind as investments are considered in stage mass reductions and Isp improvement.
Figure 34.—TSTO GLOM sensitivity to second stage mass variation for a fixed first stage mass.

Figure 35.—TSTO GLOM sensitivity to first stage mass variation for a fixed second stage mass.
Figure 36.—Second stage dry mass sensitivity at varying values of Isp.

Figure 37.—First stage mass sensitivity at varying values of Isp.
6.4.2 Engine Isp and Thrust

Engine parameter GLOM sensitivities are also very important to consider for the MAV design. As done for other sensitivities, vehicle masses and mission parameters are held constant to the baseline assumptions. For thrust variations, Isp is held constant to baseline values while the thrust is held constant for the Isp partial. It is recognized the Isp and thrust are typically linked, along with potential mass increases. But as with other sensitivities discussed, this is intended to demonstrate the singular effect of each parameter. The effect to GLOM of varying the Isp is shown in Figure 38. The assumption was made that the Isp of both stages is the same, leading to the Isp listed in Figure 38 being used for both the first and second stages.

It is noted the resulting trend follows what would be expected due to the exponential nature of the rocket equation. An Isp range of 255 to 355 sec was analyzed assuming a representative solid propellant Isp similar to the baseline of 285 sec with a representative liquid system Isp of 310 sec. Due to the nonlinear nature of the Isp GLOM trend, linear relationships around each representative system Isp were established, and are valid for approximately 10 sec of Isp around each design point. For a solid system, every additional second of Isp, a GLOM reduction of approximately 1.3 kg can be expected. A liquid system showed similar results with each additional second of Isp resulting in a GLOM reduction of approximately 1 kg.

Unlike Isp, the thrust of each stage was considered separately. For each stage the sensitivity was analyzed around the baseline thrust value. The GLOM sensitivity for variations in second stage thrust, Figure 39, shows that MAV GLOM is insensitive to second stage thrust, which is not unexpected. The very low vehicle gross mass of the second stage (payload, propellant, and dry mass) results in a very high thrust to weight ratio for the range analyzed, allowing little change in the propellant mass needed for a short circularization burn. The first stage thrust GLOM sensitivity, Figure 40, shows a reduction of GLOM is possible by reducing first stage thrust. The minimum GLOM solution was found at a thrust value of 8930 newtons, which is less than half the baseline first stage thrust value. Reducing thrust to this value results in a GLOM reduction of only 4.4 kg.
Figure 39.—TSTO GLOM sensitivity to second stage thrust, first stage thrust held constant.

Figure 40.—TSTO GLOM sensitivity to first stage thrust, second stage thrust held constant.
Although the effects of using an optimized thrust are small for the baseline launch assumptions used for Figure 40 and Figure 41 shows that the effect of thrust on GLOM begins to increase when incorporated in with other vehicle sensitivities. At angles far from the optimal azimuth, the GLOM savings from the longer burn resulting from a lower, optimal, thrust grow considerably.

Figure 42 demonstrates that the GLOM reduction from Isp improvements is maintained for off azimuth launches at an almost constant reduction in GLOM. Both curves in Figure 42 were run using the same thrust value of 21,577 N further indicating that GLOM savings result from increases in Isp only. These results indicate that further study is necessary of the secondary effects on other vehicle sensitivities caused by engine parameter changes, as large additional GLOM benefits may be possible.
Figure 42.—TSTO delta GLOM difference for off azimuth launches using a representative liquid Isp, based on a GLOM of 272.6 kg.

6.5 Verification of Combined TSTO Sensitivities

The TSTO sensitivities, as presented, all considered changes in only a maximum of three parameters at a time. Additionally sensitivities to off optimal azimuth were run only for nominal mission assumptions. The data presented in this paper is most useful if the multiple sensitivities can be combined to quickly determine GLOM predictions for numerous vehicle and mission configurations. To show the effect of doing this, cases were selected that combined various sensitivities. In some cases this included changing launch site, mission and vehicle parameters concurrently.

To complete these comparisons, the plots of GLOM sensitivity for elevation and inclination as well as those of elevation and off optimal azimuth angle were used in combination with the numerous vehicle partials identified. For each case, a set of parameters was selected to vary from their nominal values. The GLOM increase, or decrease, from TSTO baseline is then estimated using the presented vehicle sensitivities. OTIS cases were then run using the same sets of parameters to verify the GLOM predictions. Cases were not chosen at random but instead use combinations of parameters that are expected to be of some interest for the current MAV design and are intended to show the potential effects of using the sensitivities presented outside the ranges analyzed. The vehicle cases verified are shown in Table 13, with the vehicle parameters, mission parameters, predicted GLOM and the actual GLOM from OTIS. The GLOM comparisons are calculated as the actual GLOM subtracted from the predicted GLOM and then compared back to the actual GLOM as a percentage. All parameters from the baseline TSTO case are also included in Table 13 to allow comparisons of the changes made for each verification case.
<table>
<thead>
<tr>
<th>Verification Case</th>
<th>1st stage</th>
<th>2nd Stage</th>
<th>Mission Assumptions</th>
<th>Results</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Thrust (N)</td>
<td>Isp (s)</td>
<td>Stage Mass (kg)</td>
<td>Launch Latitude (deg)</td>
</tr>
<tr>
<td>TSTO Baseline</td>
<td>21577</td>
<td>285.7</td>
<td>27.66</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 1</td>
<td>21577</td>
<td>285.7</td>
<td>27.66</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 2</td>
<td>21577</td>
<td>285.7</td>
<td>27.66</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 3</td>
<td>21577</td>
<td>285.7</td>
<td>27.66</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 4</td>
<td>21577</td>
<td>285.7</td>
<td>27.66</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 5</td>
<td>21577</td>
<td>310</td>
<td>27.66</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 6</td>
<td>21577</td>
<td>310</td>
<td>40</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 7</td>
<td>21577</td>
<td>310</td>
<td>40</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 8</td>
<td>21577</td>
<td>310</td>
<td>40</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 9</td>
<td>21577</td>
<td>285.7</td>
<td>27.66</td>
<td>6318.9</td>
</tr>
<tr>
<td>Case 10</td>
<td>13000</td>
<td>285.7</td>
<td>27.66</td>
<td>6318.9</td>
</tr>
</tbody>
</table>
When nominal thrust and Isp values are used, the results demonstrate that for launches under a latitude of 45°, off azimuth GLOM predictions using performance sensitivities match within approximately 5 percent of the actual GLOM. When thrust and Isp variations are combined with off optimal azimuth angles, predictions are off by larger amounts, but still match within approximately 10 percent of the actual GLOM. It is clear that additional study of off azimuth results at all possible launch latitudes is necessary to establish more accurate predictions. GLOM savings are observed for using lower Isp and thrust values for all launch conditions. As already discussed, the engine sensitivities established for the baseline TSTO case do not directly apply when baseline mission and launch conditions are changed as shown in Figure 41 and Figure 42. This is due to the changes in burn times that occur with changing engine parameters, which cannot be easily predicted. If engine improvements are considered, additional studies of off nominal launches need to be analyzed in further detail. Overall these results demonstrate that the off azimuth GLOM sensitivities, run at a 45° latitude, provide a good preliminary estimate of off azimuth GLOM growth at lower latitudes. However, caution is advised for application of performance sensitivities at latitudes close to the equator and in cases that use large changes in thrust and Isp.

6.6 Nominal Mission Availability for a MAV Designed for Off Nominal Launch Conditions

To cover off nominal launches, the MAV will be designed with a GLOM large enough to cover a wide variety of launch and mission conditions. The possibility exists that a large GLOM MAV could still land in an optimal launch configuration, making it necessary for it to provide only enough performance for the baseline mission. To verify that a large GLOM MAV can fly a baseline mission, propellant masses from two verification cases, shown in Table 14, were run using the baseline mission and launch site assumptions as described in Table 4. The assumption was maintained that a solid rocket system was used, such that the burn could not be cut off early. Three-angle control was allowed and launch at the optimal launch azimuth was assumed. In all cases, a control scheme could be found in OTIS that allows the vehicle to waste the extra performance and achieve nominal mission targets with a mass equal to the payload and second stage dry mass. Figure 43 through Figure 45 show the selected cases compared to the TSTO baseline in geodetic altitude, inertial velocity, inertial Euler pitch and inertial Euler yaw control angles. All plots show large differences that are a result of OTIS bleeding off extra performance to accomplish a nominal mission. This analysis clearly demonstrates that the MAV can be designed for the worst possible launch conditions while maintaining the ability to launch at more optimal launch orientations.

<table>
<thead>
<tr>
<th>Verification case</th>
<th>Launch latitude, deg</th>
<th>Angle from optimal azimuth, deg</th>
<th>Target inclination, deg</th>
<th>Launch elevation, deg</th>
<th>Gross liftoff mass, kg</th>
<th>Stage 1 propellant, kg</th>
<th>Stage 2 propellant, kg</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case 1</td>
<td>30</td>
<td>180</td>
<td>45</td>
<td>30</td>
<td>343.4</td>
<td>203.0</td>
<td>66.4</td>
</tr>
<tr>
<td>Case 4</td>
<td>30</td>
<td>180</td>
<td>45</td>
<td>80</td>
<td>275.1</td>
<td>152.7</td>
<td>48.3</td>
</tr>
</tbody>
</table>
Figure 43.—Geodetic altitude and inertial velocity of large GLOM MAV, flown on a nominal mission.

Figure 44.—Inertial Euler pitch history of large GLOM MAV, flown on a nominal mission.
7.0 SSTO Performance Sensitivities

7.1 Engine Thrust and Isp

Only a small subset of the TSTO sensitivities were run for the SSTO vehicle. This was done to get a better understanding of the validity of using a SSTO for this mission, without committing resources to a study of the full set of launch site sensitivities analyzed for the current baseline TSTO design. The SSTO baseline description noted that thrust optimization was used to establish the SSTO baseline. In addition to the optimal thrust value of 4425 Newtons, the SSTO GLOM corresponding to thrust values up to the TSTO baseline of 21576 Newtons were calculated. Results are shown for a trajectory without wind modeling as the curve with diamond markers in Figure 46. All points in Figure 46 were run by varying thrust only, with all other vehicle parameters, launch conditions and mission targets set to SSTO baseline values as described in Table 5, Table 6, and Table 7. Additionally, GLOM sensitivities over the same thrust range were completed using the wind profile modeled in the TSTO case with results in Figure 46 plotted with square markers.

Three important conclusions are drawn from this data. First, is that the difference in GLOM with and without wind modeling over the same thrust range is less than 0.5 kg. Using an optimized thrust for the SSTO case a larger GLOM reduction is observed when compared to the TSTO thrust sensitivities. For the TSTO case, shown in Figure 40, a reduction in GLOM of approximately 4.4 kg is observed when using an optimized thrust value. Figure 46 clearly shows that for the SSTO case, the use of an optimal thrust value reduces GLOM by 21.6 kg, almost five times the TSTO results. Although an overall optimal thrust was established, which corresponds to the minimum GLOM SSTO case, the curve is very flat near this optimal thrust with only 0.4 kg of GLOM growth at thrust level up to 5300 N. This allows for a broader array of thrust design solutions, with minimal penalty to GLOM. This has important design ramifications for the SSTO design. If a near optimal thrust vehicle design cannot be used for an SSTO MAV, a significant increase in GLOM would be necessary.
GLOM values for variations in Isp were also calculated; again holding thrust at the optimal values with all other vehicle parameters set to the SSTO baseline values. Figure 47 shows GLOM sensitivities to Isp from 255 to 355 sec. Similar to the TSTO Isp sensitivity two average Isp values were established for solid and liquid systems: 285 for solid motors and 310 sec for liquid rocket systems. Around these Isp values, approximate linear slopes were established with 1.4 kg of GLOM reduction found for every second of solid motor Isp increase and 1.1 kg of GLOM reduction predicted for every second of liquid rocket engine Isp increase. These values are very similar to the TSTO Isp results and are important to note that GLOM reductions possible may allow higher Isp engines to trade very well into the MAV system.
7.2 Stage Mass Sensitivities

The SSTO stage mass, including payload fairing, was varied between an absolute minimum of 25 kg to a maximum of 70 kg. As in other sensitivities, all other parameters were held to SSTO baseline values. A linear trend of approximately 3.9 kg of GLOM growth per kg of additional dry stage mass was calculated and shown in Figure 48.

![SSTO GLOM vs Stage Dry Mass](image1)

**Figure 48.**—SSTO GLOM sensitivity to dry mass.

![SSTO GLOM vs Circular Orbit Altitude](image2)

**Figure 49.**—SSTO GLOM sensitivity to circular orbit altitude.
7.3 Circular Orbit Altitude Sensitivity

The circular orbit altitude trade was run for the SSTO vehicle design, to determine the additional benefit of using a SSTO design in combination with a lower altitude circular orbit. The results, found in Figure 49, show that the sensitivity of the SSTO design to circular orbit altitude is smaller than that of the TSTO design. A slope was calculated of approximately 2.3 kg of GLOM for every 50 km of additional orbital altitude, compared to the 5.1 kg slope for the TSTO vehicle. This difference is largely due to the lower thrust used in the SSTO case, allowing for adjustments in the trajectory to be made without large changes in the SSTO GLOM.

8.0 Conclusions

A large number of vehicle sensitivities were completed for both the TSTO and SSTO MAV designs. When possible simple numerical sensitivities, commonly referred to as vehicle partial derivatives, were established to directly relate GLOM growth with the design parameter of interest. These design relationships have been highlighted throughout this paper and are summarized below for the TSTO and SSTO vehicles in Table 15.

Two areas of the MAV trade space were found to have very little effect on the resulting vehicle GLOM: launch latitude for inclination targets greater than that latitude (when using an optimized launch azimuth) and the second stage engine thrust for the TSTO orbit vehicle. While other vehicle parameters cannot be classified as insensitive, the results show very small GLOM growth over the ranges analyzed. This is the case for GLOM growth due to circular orbit altitude in both the TSTO and SSTO vehicle designs. The TSTO GLOM also shows very little effect over a large range of first stage thrust values. This allows for a wide range of thrust solutions for either stage of the TSTO MAV design.

The greatest impact to GLOM is observed in the launch site orientation sensitivities run for the TSTO vehicle. If azimuth cannot be controlled within a small range around the optimal launch azimuth, large growth in GLOM can be expected for off azimuth cases unless a near vertical launch can be guaranteed. It is also obvious from the relationships presented in Table 15 that the system mass and propulsion performance of the MAV could also have a large effect on GLOM, especially if large changes from the current baseline are made.

**TABLE 15.—MAV QUANTITATIVE VEHICLE SENSITIVITIES**

<table>
<thead>
<tr>
<th>TSTO Vehicle Design Sensitivities:</th>
</tr>
</thead>
<tbody>
<tr>
<td>o Approximately 5.1 kg of GLOM increase per 50 km of circular orbit</td>
</tr>
<tr>
<td>o Approximately 4.6 kg of GLOM increase per kg of second stage dry mass</td>
</tr>
<tr>
<td>o Approximately 1.9 kg of GLOM increase per kg of first dry stage</td>
</tr>
<tr>
<td>o Approximately 2.7 kg of GLOM decrease per kg of second stage dry mass shifted to the first stage</td>
</tr>
<tr>
<td>o Approximately 0.23 kg of GLOM per 10° of launch latitude, for constant launch elevation angle and constant target inclination</td>
</tr>
<tr>
<td>- For a 90° inclination mission, GLOM grows by 2 kg when launching from the pole instead of the equator</td>
</tr>
<tr>
<td>o For a solid system: approximately 1.3 kg of GLOM reduction per second of increased Isp</td>
</tr>
<tr>
<td>o For a liquid system: approximately 1.0 kg of GLOM reduction per second of increased Isp</td>
</tr>
<tr>
<td>o The use of a wind model in TSTO MAV analysis has less than a 0.25 kg impact on GLOM</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>SSTO Vehicle Design Sensitivities:</th>
</tr>
</thead>
<tbody>
<tr>
<td>o Approximately 3.9 kg of GLOM increase per kg increase in stage dry mass</td>
</tr>
<tr>
<td>o Approximately 2.3 kg of GLOM increase per 50 km of circular orbit</td>
</tr>
<tr>
<td>o For a solid system: ~1.4 kg of GLOM reduction per second of increased Isp</td>
</tr>
<tr>
<td>o For a liquid system: ~1.1 kg of GLOM reduction per second of increased Isp</td>
</tr>
<tr>
<td>o The use of a wind model in SSTO MAV analysis has less than a 0.5 kg impact on GLOM</td>
</tr>
</tbody>
</table>
9.0 System Implications

The primary intention of the results presented was to help guide decisions on the investments necessary to produce a MAV capable of launching in a variety of conditions and still remain small enough to fit into the landed mass restrictions. As these sensitivities were completed, the authors have developed a set of recommendations that could allow GLOM savings and still support a variety of launch site locations and conditions.

First, if the landing system can guarantee the launch azimuth within approximately 40° of the optimal launch azimuth, the MAV should be designed to launch at a 45° elevation and incorporate the resulting reduction in GLOM. A change in the baseline launch elevation to 45°, from vertical, could result in additional benefits to the launch platform as a 45° launch angle may be easier to achieve. It should be noted, that if azimuth cannot be guaranteed within 40° but could be guaranteed to within approximately 70° of the optimal launch azimuth, a 45° launch elevation could be used while maintaining the current TSTO baseline mass. If azimuth restrictions are not possible, a launch elevation near 90° is necessary to minimize GLOM growth.

The current analysis demonstrates the impact of launching at elevations of up to 30° from the design point. Due to the large GLOM variations that result from changes in launch elevation, it is recommended that launch elevation accuracy be restricted to approximately 10° from the design point. This would allow additional GLOM savings and provide more flexibility in the launch azimuth constraints necessary to utilize a lower baseline launch elevation.

The final recommendation is related to the physical design of the TSTO MAV. Functionality could be moved from the second stage to the first with a GLOM savings of 2.7 kg per kilogram moved with no impact to performance due to the ability to jettison the first stage just before second stage ignition. Reconfiguring the distribution of important systems between both stages, could allow significant GLOM savings without a major change to the current MAV propulsion and mission assumptions.

10.0 Future Work

Further work is needed in three key areas to refine the current data: MAV body control rate limits, TSTO nonoptimal azimuth launches at low latitudes and SSTO launch orientation sensitivities. The existing 2001 TSTO baseline design, utilized body control rates of 20° per second; a rate believed to be unsuitable for the current vehicle design. For the sensitivities presented in this paper a 5° per second body control rate was assumed, as it is currently well within historically used limits. However, it was shown that off azimuth GLOM sensitivities could be mitigated to some extent with the use of a higher body control rate. Therefore, a more detailed study is necessary to determine what control rates could be used for MAV. It would be necessary to model the MAV using a six-degree of freedom simulation, which would allow the interaction of a gimbaled engine with the relatively small MAV to be studied in greater detail. With a six-degree of freedom model, differing vehicle body rates could be imposed to determine when, and if, the MAV becomes uncontrollable or exceeds structural design limits.

The verification results presented indicate that further study of nonoptimal azimuth launches at lower launch latitudes is required to more accurately predict GLOM trends. This would include further analysis using the models already completed for this study and a more extensive trade matrix of inclination and launch latitudes for the off azimuth angles analyzed. The current data provides an adequate initial GLOM estimate for launches at latitudes lower than 45°, but does not incorporate all necessary effects of launching from those latitudes. This is especially true if a higher Isp or lower thrust MAV design is under consideration, as errors could grow quite high for off optimal azimuth launches due to differences in burn time caused by engine parameters changes.
Finally, if the SSTO vehicle design is to be strongly considered, launch site and launch orientation sensitivities need to be completed similar to those shown here for the TSTO design. These could be completed with the previously developed models using the analysis methodology described for the TSTO sensitivities. It is assumed that trends will be similar to the TSTO design, but the magnitude of SSTO GLOM growth could far exceed the TSTO design for some cases.
Appendix A.—Gross Lift-off Mass Sensitivities for Launch Elevations From 0° to 90° Targeting Inclinations from 0° to 90° for Launch Latitudes From 0° to 90°

TSTO GLOM vs Inclination for All Launch Elevations
Launch Latitude = 5 deg

Figure 50.—TSTO GLOM sensitivities for a launch latitude of 5°.

TSTO GLOM vs Inclination for All Launch Elevations
Launch Latitude = 10 deg

Figure 51.—TSTO GLOM sensitivities for a launch latitude of 10°.
Figure 52.—TSTO GLOM sensitivities for a launch latitude of 15°.

Figure 53.—TSTO GLOM sensitivities for a launch latitude of 20°.
Figure 54.—TSTO GLOM sensitivities for a launch latitude of 25°.

Figure 55.—TSTO GLOM sensitivities for a launch latitude of 30°.
Figure 56.—TSTO GLOM sensitivities for a launch latitude of 35°.

Figure 57.—TSTO GLOM sensitivities for a launch latitude of 40°.
Figure 58.—TSTO GLOM sensitivities for a launch latitude of 45°.

Figure 59.—TSTO GLOM sensitivities for a launch latitude of 50°.
Figure 60.—TSTO GLOM sensitivities for a launch latitude of 55°.

Figure 61.—TSTO GLOM sensitivities for a launch latitude of 60°.
Figure 62.—TSTO GLOM sensitivities for a launch latitude of 65°.

Figure 63.—TSTO GLOM sensitivities for a launch latitude of 70°.
Figure 64.—TSTO GLOM sensitivities for a launch latitude of 75°.
References


The Mars ascent vehicle is a critical element of the robotic Mars Sample Return (MSR) mission. The Mars ascent vehicle must be developed to survive a variety of conditions including the trans-Mars journey, descent through the Martian atmosphere and the harsh Martian surface environments while maintaining the ability to deliver its payload to a low Mars orbit. The primary technology challenge of developing the Mars ascent vehicle system is designing for all conditions while ensuring the mass limitations of the entry descent and landing system are not exceeded. The NASA In-Space Propulsion technology project has initiated the development of Mars ascent vehicle technologies with propulsion system performance and launch environments yet to be defined. To support the project’s evaluation and development of various technology options the sensitivity of the Mars ascent vehicle gross lift-off mass to engine performance, inert mass, target orbits, and launch conditions has been completed with the results presented herein.

14. ABSTRACT
Ascent; Mars Sample Return (MSR) mission; Mars landing; Mars surface; Optimal Trajectories by Implicit Simulation program (OTIS); Mars ascent vehicle; Mars surface samples; Descent

15. SUBJECT TERMS

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