T-matrix method and its applications to electromagnetic scattering by particles: A current perspective

Michael I. Mishchenko a,*, Larry D. Travis a, Daniel W. Mackowski b

a NASA Goddard Institute for Space Studies, 2880 Broadway, New York, NY 10025, USA
b Department of Mechanical Engineering, 201 Ross Hall, Auburn University, AL 36849-5341, USA

A R T I C L E   I N F O

Article history:
Received 25 January 2010
Accepted 26 January 2010

Keywords:
Electromagnetic scattering
T-matrix method
Nonspherical particles
Radiative transfer
Coherent backscattering
Optical particle characterization
Remote sensing

A B S T R A C T

This note serves as a short introduction to the reprint of our article “T-matrix computations of light scattering by nonspherical particles: a review” (JQSRT 1996; 55:535–75). We first discuss the motivation for writing that article and explain its historical context. This is followed by a short overview of more recent developments.

Published by Elsevier Ltd.

Although the T-matrix method was formally introduced by P.C. Waterman in 1965 [1], its widespread use and popularity can be attributed equally to his seminal 1971 article [2] published in Physical Review D (Fig. 1). These papers have been cited 350 and 520 times, respectively, in publication outlets covered by the ISI Web of KnowledgeSM and can both be credited with the subsequent use of the T-matrix approach in more than 1450 peer-reviewed publications on electromagnetic scattering by finite particles alone [3–6] (Fig. 2). An important role in the popularization of the T-matrix method during the 1970s and 1980s belonged to the 1975 paper by Barber and Yeh [7] published in a more traditional optical journal and cited 340 times.

The conceptual scope of a T-matrix has expanded quite dramatically since it was first introduced in Refs. [1,2]. From being a mere bi-product of the extended boundary condition method (otherwise known as the null-field method), the T-matrix has become the centerpiece of a vast domain of science dealing with electromagnetic, acoustic, and elastic wave scattering [8]. In particular, the advent of the superposition T-matrix concept in Refs. [9–11] allows one to give the following general definition.

In the T-matrix method, the incident and scattered electric fields are expanded in series of suitable (vector) spherical wave functions, and the relation between the columns of the respective expansion coefficients is established by means of a transition matrix (or T-matrix). This concept can be applied to the entire scatterer as well as to separate parts of a composite scatterer.

By 1995, the T-matrix method had become the subject of several specialized monographs [12–17] and a sizable body of peer-reviewed journal publications on electromagnetic scattering (Fig. 2). Hence there was a perception that this field was ripe for a review paper, which was, in fact, solicited by the organizer of the first conference on “Light Scattering by Non-Spherical Particles”, Joop Hovenier, for his special issue of JQSRT [18]. Our review [19] was published in 1996 and turned out to be timely indeed. It has been cited more than 300 times and thereby has contributed to the subsequent rapid growth of popularity.
of the $T$-matrix method (Fig. 2). Quite remarkably, two more papers presented at that 1995 conference in Amsterdam and published in Ref. [18] are also among the 17 milestone JQSRT papers featured in this anniversary issue [20,21].

Among the many advances since 1996, perhaps the most significant has been the extension of the analytical orientation-averaging procedure developed in Ref. [22] to the case of an arbitrary multi-sphere cluster in the framework of the superposition $T$-matrix method. Indeed, the resulting paper [23] has been cited 190 times, and its citation rate has been increasing rather than decreasing over time. Another fundamental advance has been the development of the null-field method with discrete sources [24]. From the standpoint of a practical user of the $T$-matrix method, an important tool has been the public-domain package of FORTRAN computer programs available at http://www.giss.nasa.gov/staff/mmishchenko/t_matrix.html. This package is based on developments summarized in Refs. [22,23,25] and has been used in more than 600 peer-reviewed publications. A host of other $T$-matrix programs are available at the web site http://www.scattport.org maintained by Thomas Wriedt.

The range of research areas dealing with the $T$-matrix method and its applications has been quite broad and has included the following:

- Modifications and generalizations of the extended boundary condition method.
- Electromagnetic scattering by anisotropic, bi-isotropic, and chiral objects.
• Modifications and generalizations of the superposition T-matrix method.
• Electromagnetic scattering by periodic arrays of particles and photonic crystals.
• Electromagnetic scattering by discrete random media.
• Symmetry properties of the T-matrix and analytical ensemble-averaging approaches.
• Convergence and efficiency of various implementations of the T-matrix method.
• Calculations for various rotationally symmetric particles.
• Calculations for ellipsoids, polyhedral scatterers, and other particles lacking axial symmetry.
• Calculations for layered and composite particles.
• Calculations for clusters of homogeneous and layered spheres.
• Calculations for clusters of nonspherical monomers.
• Calculations for particles with one or several inclusions.
• Theory and calculations of optical resonances in nonspherical particles and particle clusters.
• Theory and calculations of optical forces and torques on small particles.
• Theory and calculations of internal, surface, and local fields.
• Illumination by focused beams and non-plane waves.
• Theory and calculations of electromagnetic scattering by particles near infinite interfaces.
• Computations of anisotropic and aggregation properties of colloids and other disperse media.
• Use of T-matrix calculations for testing other theoretical techniques, including effective medium approximations.
• Comparisons of T-matrix and controlled laboratory results; analyses of laboratory data.  
• Modeling of scattering properties of mineral aerosols and soil particles.
• Modeling of scattering properties of carbonaceous and soot aerosols and soot-containing aerosol and cloud particles.
• Modeling of scattering properties of cirrus cloud particles and hydrometeors.
• Modeling of scattering properties of terrestrial stratospheric and mesospheric aerosol and cloud particles.
• Modeling of scattering properties of aerosol and cloud particles in planetary atmospheres.
• Modeling of scattering properties of interstellar, interplanetary, and cometary dust, planetary regoliths, and planetary ring particles.
• Modeling of absorption and scattering by particles in combustion systems.
• Modeling of scattering and absorption properties of microorganisms, cells, and tissues.
• Various industrial and military applications.

There are, of course, unsolved problems and challenges in the T-matrix approach. Two obvious new directions that one can think of would be:

• scattering of pulses, e.g., femtosecond laser scattering; and
• inverse problems: given a T-matrix, what information can be gathered regarding the properties of the scatterer?

The volume and extent of new research results are such that now it would be extremely difficult and perhaps impracticable to summarize them in one comprehensive review article or even in a monograph. The specialized monographs [24–30] and topical reviews [31–40] should be a good starting point for a newcomer interested in the theory of the T-matrix method and/or its applications. The multi-part reference database [3–6] should also be helpful by providing a classification of all T-matrix publications on electromagnetic scattering into narrower subject categories similar to those listed above.

Acknowledgments

We thank Joop Hovenier, Michael Kahmert, Nikolai Khlebtsov, M. Pinar Mengiç, Victor Tishkovets, and Gorden Videen for numerous useful discussions. This project was sponsored by the NASA Radiation Sciences Program managed by Hal Maring.

References


