Detection of Ionospheric Alfvén Resonator Signatures in the Equatorial Ionosphere

Authors

Fernando Simões¹, Jeffrey Klenzing¹, Stoyan Ivanov², Robert Pfaff¹, Henry Freudenreich¹, Dieter Bilitza³, Douglas Rowland¹, Kenneth Bromund¹, Maria Carmen Liebrecht¹, Steven Martin¹, Peter Schuck¹, Paulo Uribe¹, Tatsuhiro Yokoyama¹

1 – NASA/GSFC, Heliophysics Science Division, Space Weather Laboratory (code 674), Greenbelt, Maryland, USA
2 – Department of Physics, Georgia Institute of Technology, Atlanta, Georgia, USA
3 – NASA/GSFC, Heliophysics Science Division, Heliospheric Physics Laboratory (code 672), Greenbelt, Maryland, USA
4 – George Mason University, Space Weather laboratory, Fairfax, Virginia, USA

Abstract

The ionosphere response resulting from minimum solar activity during cycle 23/24 was unusual and offered unique opportunities for investigating space weather in the near-Earth environment. We report ultra low frequency electric field signatures related to the ionospheric Alfvén resonator detected by the Communications/Navigation Outage Forecasting System (C/NOFS) satellite in the equatorial region. These signatures are used to constrain ionospheric empirical models and offer a new approach for monitoring ionosphere dynamics and space weather phenomena, namely aeronomy processes, Alfvén wave propagation, and troposphere-ionosphere-magnetosphere coupling mechanisms.
1. Introduction

The period of low solar activity during the recent solar cycle 23/24 minimum was unique during the space age, offering exceptional conditions for investigating space weather in the near-Earth environment, namely ionospheric phenomena. This atypical long-lasting low solar activity is particularly suitable for investigating, from a different perspective, a variety of ionospheric and magnetospheric processes, namely waves in plasma. Here we report in situ ionospheric measurements taken in the equatorial region, namely Alfvén wave signatures related to known, yet unfamiliar, ionospheric resonance phenomena. These findings offer a new approach to assess ionospheric plasma density and dynamics, in particular above the F-peak, contributing to improve empirical models of the ionosphere.

Alfvén waves are low frequency oscillations that occur in an ionized fluid permeated by a magnetic field such as the Earth ionosphere or magnetosphere. Perturbations in plasma homogeneity produce ion motion, a restoring magnetic field tension takes place to balance particles inertia, and an oscillation is created, generating magneto-hydrodynamic (MHD) waves. When the wave vector is parallel to the background magnetic field, Alfvén waves are transverse and termed shear Alfvén modes; when the wave vector is perpendicular to the background magnetic field, Alfvén waves are longitudinal and correspond to magnetosonic modes [e.g., Lysak, 1999]. To a first approximation, these waves are dispersionless. Local and global plasma density heterogeneities in the ionosphere and magnetosphere allow for formation of waveguide and resonator structures where magnetosonic and shear Alfvén waves propagate. For example, the ionospheric magnetosonic waveguide results from magnetosonic wave reflection about the ionospheric F-region, where the Alfvén index of refraction is the highest; magnetosonic waves can be guided thousands of kilometers in the ionosphere between the northern and southern
hemispheres due to ionospheric ducting [Greifinger and Greifinger, 1968]. MHD waves can also be partially trapped in the vertical direction between the lower boundary of the ionosphere and the magnetosphere, a resonance mechanism known as Ionospheric Alfvén Resonator (IAR) [Polyakov and Rapoport, 1981]. So far, IAR signatures have been clearly observed on the ground at mid and high latitudes [Belyaev et al., 1990]; satellite-based observations in the auroral region have been also claimed [Grzesiak, 2000; Chaston et al., 2002]. We present in situ ionospheric electric field measurements related to IAR distinctive signatures detected in the equatorial region. These IAR electric field signatures offer complementary means for ionospheric plasma density diagnostic, and also contribute for the investigation of ionosphere dynamics and space weather monitoring. Besides, these findings corroborate independent measurements claiming that ionospheric models have been significantly overestimating plasma density under solar minimum conditions.

2. Ionospheric Alfvén Resonator

Specific ionospheric plasma density variations with altitude can form a resonant cavity between the lower boundary of the ionosphere (~100 km) and an altitude of about one Earth radius. MHD waves can be partially trapped and amplified in the vertical direction between the two boundaries, producing distinctive resonance signatures in both Ultra and Extremely Low Frequency (ULF-ELF) spectra, in the range 0.01-40 Hz. The IAR excitation source is likely related to lightning or geomagnetic pulsations though irrefutable proof has yet to be established. Particular spectral resonance structures have been considered evidence for IAR phenomena [Belyaev et al., 1990]. Subsequent measurements have expanded our knowledge of IAR dynamics consistently [Grzesiak, 2000; Chaston et al., 2002; Bösinger et al., 2004; Parent et al.,
In addition to intrinsic spectral structures, the main characteristics of IAR shear Alfvén waves include a vertical wave vector and horizontal oscillations of the electric and magnetic fields. When losses are taken into account, coupling between the shear Alfvén and magnetosonic modes is possible and the resonator response is more intricate (see complementary information in the modeling section). Because a background magnetic field radial component, $B_r$, is required, IAR excitation may only occur off the magnetic equator.

The Alfvén index of refraction, defined by

\[ n_A = \frac{c}{V_A}, \]  

where $c$ is the velocity of light in free space and $V_A$ the Alfvén velocity in the medium, is crucial to understand how the IAR functions. Shear Alfvén waves can be reflected in the ionosphere, and consequently trapped, if sharp gradients (with respect to the wavelength) of the refractive index occur. The Alfvén velocity is defined by

\[ V_A = \frac{B}{\sqrt{\mu_0 \rho}}, \]  

where $B$ is the background magnetic field, $\rho$ is the density of charged particles ($e^-$, $H^+$, $He^+$, and $O^+$), and $\mu_0$ is the permeability of vacuum. Since shear Alfvén modes propagate parallel to the background magnetic field and the wave vector is approximately vertical inside the resonator, the resonance effect is more pronounced at high latitudes, where the dip angle is larger and, consequently, the magnetic field vertical component more important. Figure 1 shows typical profiles of electron density, Alfvén velocity, and index of refraction, and also illustrates that the resonator response occurs primarily close to the F-peak. The dashed line represents an
approximate profile often used for obtaining IAR analytical solutions; under such conditions, the
frequency and Q-factor of the resonator are \([Polyakov and Rapoport, 1981; Lysak, 1999]\]

\[ f_n = V_A \frac{n+1/4}{2(L+H)} \]  \hspace{1cm} (3)

and

\[ Q_n = \frac{1+L/H}{\pi \varepsilon} \]  \hspace{1cm} (4)

where \( L \) and \( H \) are the length and scale height of the Alfvén velocity ‘well’, respectively,
\( \varepsilon \equiv V_{A_{\min}}/V_{A_{\max}} \) is related to the depth of the well, and \( n=0,1,2,\ldots \) is the eigenmode number.

Because the lower eigenmodes are often buried in the background noise, it is helpful calculating
the frequency difference between consecutive peaks, which is defined by

\[ \Delta f = \frac{V_A}{2(L+H)} \]  \hspace{1cm} (5)

The Q-factor of the resonator increases, i.e., better wave propagation conditions occur, when
the Alfvén velocity ionospheric well is deep, wide, and sharp. The threshold condition for wave
amplification in the IAR upper boundary, derived from resonator reflection and transmission
coefficients, is given by the inequality

\[ \frac{\pi \varepsilon \omega H}{V_A} < 1 \]  \hspace{1cm} (6)

where \( \omega \) is the angular frequency of the propagating wave.
This condition is normally valid in the lower boundary of the resonator, and reflection happens, because \( \nabla n_A \) is sharp; shear Alfvén waves are nevertheless able to propagate down to the ground not only because the ionospheric barrier is relatively thin and waves can emerge below the D-region but also because good propagation conditions occur when Pedersen conductivity matches the Alfvén wave impedance. Measurement of IAR parameters contributes to ionosphere and magnetosphere characterization by solving the MHD inverse problem, i.e., inferring medium properties from wave dispersion data.

**SUGGESTED LOCATION OF FIGURE 1**

### 3. C/NOFS Measurements

The Communications/Navigation Outage Forecasting System (C/NOFS) satellite was launched in April 2008 into a low inclination (13 degree) orbit of with perigee at 401 km and apogee near 867 km [de la Beaujardière et al., 2004], and has provided invaluable data to investigate the ionospheric equatorial region electrodynamics, namely scintillations, plasma depletions, neutral winds, aeronomy processes, and low frequency electromagnetic waves [de la Beaujardière et al., 2009; Heelis et al., 2009; Klenzing et al., 2011; Simões et al., 2011a]. Among the scientific payload, the Vector Electric Field Instrument (VEFI) is used to investigate electric and magnetic fields; VEFI consists of a three-axis double probe electric field detector that provides continuous DC and AC electric field measurements, a magnetometer, and two optical sensors for lightning detection [Pfaff et al., 2010; Holzworth et al., 2011]. The double probe sensitivity in the ULF-ELF range is \( \sim 10 \text{nVm}^{-1}\text{Hz}^{-1/2} \) for a sampling rate of 512 s\(^{-1}\).
Spectrograms of the electric field meridional (vertical) and zonal (east-west) components measured near the terminator during orbits 666-667 are shown in Figure 2. Sunset and satellite eclipse occur at about 1507 and 1515 UT for orbit 666, and 1644 and 1652 UT for orbit 667. The pattern resembling a fingerprint in the spectrograms is compatible with an IAR signature and is visible in the bottom-left corner of each plot (1500-1512 and 1636-1648 UT), where the satellite moves from 650 to 450 km altitude, approaching perigee. The peak amplitude is larger in the zonal component because the IAR electric field is horizontal, consistent with model predictions. The top right panel also shows lines extending deep in the night sector (1639-1705 UT). The electric field spectral density is about 10 and 15 dB above the background noise in the meridional and zonal components, respectively. The fuzzy, wide horizontal stripes visible close to 8, 14, 20, 26, and 32 Hz in the plots are Schumann resonance modes, ELF signatures of the longitudinal mode of the earth-ionosphere cavity [Simões et al., 2011a].

**SUGGESTED LOCATION OF FIGURE 2**

Figure 3 illustrates a magnification of Figure 2 to emphasize a narrow spectral line detected during orbit 667 and flagged by arrows. A few spectra in the vicinity of the event are showing the background signal. The event starts at about 16:41:24 UT and lasts ~0.5 s. In addition to the distinctive waveform bearing evidence for dispersion and amplitude modulation, the spectral line presents a few more noteworthy characteristics: (i) a dozen peaks overlapping the fingerprint signature, i.e., peak frequencies of the event match the fingerprint spectral features; (ii) the Q-factor is roughly twice that of the fingerprint; (iii) a peak amplitude of ~0.5 µVm⁻¹Hz⁻¹/² that seems almost constant in the frequency range 1-15 Hz and is about 2.5 times larger than in the
fingerprint; (iv) the peak is absent above 14 Hz and only reappears beyond 20 Hz modulated by Schumann resonance modes; (v) like in the fingerprint, the ratio of the electric field zonal to meridional component is ~2. Finally, peak distribution shows $\Delta f\sim1.1$ Hz and $f_{th}\sim14$ Hz, where $f_{th}$ is a threshold frequency. A closer inspection also shows a morphological transition occurring around 14 Hz in the spectrograms, where the resonance grows fainter.

Figure 4 presents the electric field intensity, $E$, and $\Delta f$ variation when the resonator signature is observed in orbit 667, i.e., about the terminator, in the range 0-20 Hz. Both $E$ and $\Delta f$ clearly increase within the time span considered. The solid lines represent modeling results discussed in section 4. Figure 5 shows an even stronger IAR signature with larger frequency detected during orbit 694. Another interesting feature seen both in Figures 2 and 5 is the markedly asymptotic increase of frequency when the satellite is moving toward ellipse.

SUGGESTED LOCATION OF FIGURES 3 AND 4

The IAR signature seen near dusk is also detected at dawn when orbit conditions are reversed, i.e., perigee occurs in the early morning sector, as shown in Figure 6. In addition to IAR frequency decrease near sunrise, the plot shows narrow lines imprinted in the structured hiss visible in the meridional component during nighttime. It is worth mentioning that $\Delta f$ in the structured hiss is only slightly larger than near dawn, and up to 20 lines are apparent. These observations were made during orbit 2898, in 28-29 October 2008.

SUGGESTED LOCATION OF FIGURE 5
4. Modeling

Although the IAR analytical theory is valuable for providing perceptive, approximate solutions, numerical modeling is required when real ionospheric profiles are chosen (cf. Figure 1). An algorithm based in the finite element method has been recurrently used to solve low frequency electromagnetic wave propagation phenomena (transient, eigenmode, harmonic, and parametric analyses) in the surface-ionosphere cavity of the Earth and other planets [Simões et al., 2007, 2008a, 2008b, 2009]; the algorithm has been upgraded with the fluid dynamics formalism for solving MHD equations and computing IAR eigenfunctions. The IAR numerical model is based on the linearized, cold, multi-fluid description for electrons and ions in collisional plasma [Lysak, 1999]. The algorithm separates the longitudinal and transverse components with respect to the geomagnetic field, utilizes altitude as the independent variable, and computes the shear Alfvén and magnetosonic eigenmodes. This model employs four parameterizations of the medium that are dependent of the Pedersen (\(\sigma_P\)) and Hall (\(\sigma_H\)) conductivities, and of the transverse heterogeneity current (\(j_\perp\)): (M1) lossless medium (\(\sigma_P=\sigma_H=j_\perp=0\)); (M2) lossy medium without mode coupling (\(\sigma_P\neq0, \sigma_H=j_\perp=0\)); (M3) lossy medium with coupling (\(\sigma_P\neq0, \sigma_H\neq0, j_\perp=0\)); (M4) lossy medium with coupling and local transverse heterogeneity (\(\sigma_P\neq0, \sigma_H\neq0, j_\perp\neq0\)). Hall conductivity introduces a driving action in the resonator through coupling between the shear Alfvén and magnetosonic modes. Magnetic diffusivity due to parallel conductivity and transverse heterogeneity often generates instabilities in the resonator [Lysak and Song, 2002]. Medium parameterization requires information about the background magnetic field, collision frequency, ion composition, and electron density to derive the Alfvén velocity and conductivity tensor. The amplitude and vertical component of the magnetic field are evaluated from the International Geomagnetic Reference Field (IGRF-11) model [Finlay et al., 2010]. The electron
density and ion composition are computed from the International Reference Ionosphere (IRI-2007) model [Bilitza and Reinisch, 2009]. We also run the numerical model with the most recent release (IRI-2011) to contrast IRI performance improvements. The effective collision frequency is derived either from the International Standard Atmosphere (ISA) or from the Naval Research Laboratory Mass Spectrometer Incoherent Scatter radar (NRLMSIS-E-00) empirical model, which provides composition, temperature, and density distribution of neutrals [Lide et al., 2010; Picone et al., 2002]. To a first approximation, medium parameterization inaccuracy is due to electron density and ion composition uncertainty rather than to that of magnetic field or collision frequency [Simões et al., 2009]. The eigenfrequencies computed with the numerical model (configuration M3) are shown in Figure 4 along with C/NOFS results. Model parameters are evaluated against electron density and ion composition profiles considering various constraints from IRI and the Ion Velocity Meter (IVM) data recorded onboard C/NOFS: (P0) IRI-2007 default parameterization; (P1) IRI density profile normalized against IVM plasma density recorded during fingerprint observation (altitude ~500 km); (P2) IRI density and ion composition profiles normalized against IVM data under conditions defined in P1; (P3) composite electron density profile combining IVM mean density in the altitude range between 400 and 850 km (a full discussion of the monthly and seasonal averages can be found in Klenzing et al. [2011]) and IRI elsewhere; (P4) composite electron density and ion composition profiles under conditions defined in P3; (P5) profile similar to P4 but with the IVM density distribution decreased by one standard deviation; (P6) IRI-2011 default parameterization. Because the density profiles cannot be fully reconstructed from 2008 due to uneven data coverage, the June solstice 2009 values are used for the purpose of this study; this is nevertheless appropriate since measurements during 2008 and 2009 are closer to each other than they are to the IRI predictions for either year.
5. Discussion

The existence of an ionospheric resonator that is able to trap shear Alfvén waves was predicted theoretically and later identified in spectral resonance structures in the ULF range [Polyakov and Rapoport, 1981; Belyaev et al., 1990]. Since then, IAR multiple spectral lines have been reported both on the ground [Bösinger et al., 2004; Parent et al., 2010], at mid and high latitudes, and onboard satellites in the auroral region [Grzesiak, 2000; Chaston et al., 2002].

C/NOFS data extends IAR signature detection to the low-latitude regions, where the shear Alfvén mode is much less effective. VEFI is nevertheless able to detect IAR signatures because plasma density is smaller during low solar activity and C/NOFS coverage extends to mid magnetic latitudes as well.

According to modeling, high $\Delta f$ and $Q$-factor offer better conditions for IAR fingerprint identification because peaks are stronger and better resolved. Ideally, the most favorable conditions to observe the IAR spectral structures onboard C/NOFS occur close to the F-peak, off the magnetic equator, during nighttime, and low solar activity because $\Delta f \propto B_r/\sqrt{\rho}$. Close to the terminator, because the background noise remains limited and strong refraction happens, dusk and dawn offer privileged conditions for observing the IAR signature (Figures 2 and 6). The frequency increasing near the terminator in orbits 666, 667, and 694 is most likely due to a fast, strong variation of plasma density in the ionosphere. A similar, reversed effect is seen in orbit 2898 near dawn. Supplementary material combining audio and video formats of the ELF spectrograms can be found here (LINK TO REPOSITORY SERVER). In addition to familiar, typical ionospheric transient phenomena such as whistlers, tweeks, chorus, and hiss, the low frequency sound with pitch increasing - a sort of reversed whistler effect - is a distinctive characteristic of the IAR signature related to plasma density strong decreasing near the
The sound related to the IAR signature shows better quality when the signal is processed with a low pass filter. Although consistent with source power increasing, the electric field enhancement seen in Figure 4 is likely due to improvements of resonator efficiency, i.e., sharper boundaries. The IAR signature is detected preferentially at low altitude, e.g., below 600 km, when the satellite is clearly inside the resonator and where better propagation conditions happen.

Ground measurements of ULF electric and magnetic fields are usually suitable for deriving not only IAR frequencies but also the Q-factor, from which resonator efficiency is inferred. Computation of IAR spectral peak full width at half maximum provides a reasonable estimate of cavity losses; a Q-factor in the order of 10 has been reported on the ground [Belyaev et al., 1990]. Following a similar approach, we obtain Q-factors in the range 15-20 for most orbits and ~30 for the narrow event reported in orbit 667. Qualitatively, these results seem plausible and consistent with equation (4). However, the Q-factor computed with the numerical model (either M2 or M3) overestimates observations considerably \( Q \equiv \operatorname{Re}(f)/2\operatorname{Im}(f) \approx 50 \). Additionally, neither plasma density and composition variability nor uncertainty in collision frequency is able to bringing measurements and modeling to a reasonable agreement. Configuration M4 does not seem to provide a reasonable agreement either despite some uncertainty in the \( j_{\perp} \) parameter. To assess the collision frequency uncertainty we use both ISA and NRLMSIS-E-00 models of the neutrals but difference between the computed Q-factors is small. However, anomalously low solar extreme-ultraviolet irradiance and thermospheric density during solar activity minimum 23/24 have been reported [Solomon et al., 2010; Emmert et al., 2010], suggesting that such a contracted atmosphere may have modified the shape of the collision frequency profile significantly.
As on the ground, the lowest Schumann resonance peaks are stronger than spectral resonance structures attributed to IAR phenomena. During the day, IAR signatures are not easily detected from orbit; under such conditions, the resonator is ineffective or, less likely, shows dense lines that cannot be resolved by VEFI and then regarded as noise. During nighttime, IAR lines are frequently visible \((E \approx 0.2 \, \mu \text{Vm}^{-1}\text{Hz}^{-1/2})\) unless masked by the wider, stronger Schumann resonance modes \((E \approx 0.5 \, \mu \text{Vm}^{-1}\text{Hz}^{-1/2})\); on the ground, for comparison purposes, magnetic field amplitude of IAR (at high latitude) and Schumann resonance are typically 0.1 and 1 pT, respectively.

According to IAR theory, the electric field of the shear Alfvén mode should be horizontal. Figures 2 and 5 show that the electric field horizontal (zonal) component is indeed dominant but a vertical component is also present. A comprehensive assessment is impracticable because the electric field component along the geomagnetic field and magnetic field data are not available at that time. Nevertheless, vertical and horizontal components are clearly observed, suggesting a coupling between shear Alfvén and magnetosonic modes.

Several natural mechanisms have been proposed regarding IAR excitation, including lightning [Surkov et al., 2006; Shalimov and Bösinger, 2008], transient luminous events, e.g., sprites [Sukhorukov and Stubbe, 1997], and ionospheric-magnetospheric plasma waves, e.g., geomagnetic pulsations [Lekhtinen et al., 1995; Lysak and Song, 2003]. The IAR artificial excitation has also been claimed by means of ULF-ELF transmitters that match the resonator frequency or by changing the macroscopic parameters of the ionosphere with radar pulses [Trakhtengertz et al., 2000]. However, the cause-effect relation between excitation source and wave emission is difficult to establish and the subject remains unsolved. For example, geomagnetic pulsations (e.g., \(\text{Pc1}, \text{Pc2}, \text{and Pi1}\)) may play multiple roles in generation, filtration,
modulation, or propagation phenomena in IAR dynamics [Demekhov et al., 2000; Prikner et al., 2004]. It is unlikely these mechanisms play similar roles at high and low latitudes because particle precipitation is more important in the auroral region and lightning is concentrated close to the equator. Although the narrow event observed during orbit 667 (Figure 3) bears resemblance to Pc1 waves, namely range of frequency and amplitude modulation, we could not establish a direct connection to lightning, particle precipitation, or geomagnetic activity. Nevertheless, the sudden peak amplitude transition at $f_{th} \approx 14$ Hz seems meaningful and is perhaps related to medium transparency conditions in the top-side of the ionosphere defined in equation (6). The significant increase of both the Q-factor and the electric field during the event (Figure 4) is consistent with a narrow band electromagnetic source because the background noise remains unaltered, suggesting that feedback amplification occurs [Pokhotelov et al., 2001; Lysak and Song, 2002]. The threshold condition for wave amplification defined in equation (6) can be used for computing the cutoff frequency and constraining density profile parameterization.

Another interesting structure is seen during nighttime in the vertical/meridional component during orbit 2898 (Figure 6). The presence of multiple narrow lines imprinted in hiss is intriguing because $\Delta f$ is commensurate with the IAR signature and almost 20 peaks are seen, but the structure is noticeable in the vertical rather than horizontal component. Although in depth assessments are necessary, we hypothesize this structure corresponds to the magnetosonic mode since $\Delta f$ is similar to that of IAR and an electric field vertical component prevails. The observation of these resonance lines seems to require generation of strong hiss, possibly associated to plasma turbulence or better propagation conditions in the medium (e.g., ionospheric ducting). This feature could alternatively be related to processes occurring elsewhere and enhanced by an increasing of local ionospheric turbulence. Additionally, the lower cutoff at $\sim 25
Hz is close to the O$^+$ gyrofrequency and its shape somewhat resembles to that of the ion density, suggesting lower hybrid modes may play a role. Either way, investigation of hiss structure characteristics may lead to a better understanding of possible magnetosonic and shear Alfvén mode coupling but is not the main purpose of this work.

SUGGESTED LOCATION OF FIGURE 6

Figure 7 shows a comparison between IAR model predictions considering IRI-2007 default parameterization and VEFI measurements made in 31 May 2008, corresponding to about 15 orbits. The signature is visible and better resolved in VEFI data when $\Delta f$ is larger. Alternation between high and low peaks is related to magnetic field asymmetry with respect to the geographic equator and minima refer to magnetic equator crossings. The IAR frequency measured by VEFI is at least 5 times larger than model predictions (cf. Figure 4), suggesting that IRI is significantly overestimating plasma density under solar minimum conditions, in line with independent assessments [Heelis et al., 2009; Lühr and Xiong, 2010; Vlasov and Kelley, 2010]; IRI predictions of density and composition are worst close to the terminator, too [Klenzing et al., 2011]. Additionally, the increase in $\Delta f$ is also steeper than IRI predictions, suggesting larger density gradients near the terminator, a conclusion also drawn for the D-region from observations onboard balloons for different solar activity [Simões et al., 2009, 2011c]. Although the modifications introduced in IRI profiles - taking into account plasma density and composition as measured by C/NOFS - provide larger $\Delta f$, additional corrections are necessary to IRI for fitting IAR results. Profiles P1-P5 show a better – though insufficient – agreement between IAR features and the ionospheric plasma environment than that of uncorrected IRI.
parameterization (P0). According to P1-P5, all corrections increase $\Delta f$ but the resonator seems more sensitive to composition and top-side profile shape than plasma density uncertainty, because $H^+$ fraction is significantly underestimated and the density profile is sharper than IRI predictions above 500 km. These results show that $\Delta f$ is more sensitive to profile shape than plasma density or composition, a result also corroborated by the analytical approximation ($\Delta f \propto (L + H)^{-1}$ and $\Delta f \propto \rho^{-1/2}$). Since ground measurements are more frequent and reliable than above the F-peak, it is not surprising that IRI is less accurate for the topside ionosphere. Additionally, unlike radar networks and ground-based ionosonde data that usually imply constant latitude and longitude, topside ionosonde [e.g., Benson and Bilitza, 2009] and in situ measurements [e.g., Klenzing et al., 2011] are trajectory dependent. Most likely, corrections to plasma density during the 23/24 solar minimum are also necessary below the F-peak, as suggested by IVM measurements above 400 km [Klenzing et al., 2011]. Although insufficient, IRI-2011 shows an improvement compared to older models (P6 vs. P0). Since modification of the electron density profile by one standard deviation (P4 vs. P5) brings modeling and measurements to a much better agreement, a statistical study of IAR features detected throughout the mission is necessary because IRI usually provides monthly averages.

**SUGGESTED LOCATION OF FIGURE 7**

Modeling also suggests that equatorial ionospheric spread-F should have significant impact in IAR structures due to sharp, large transition in plasma density. Although no clear evidence of IAR sudden frequency variation due to spread-F phenomena has been found in C/NOFS data so far, the numerical model predicts $\Delta f$ increasing by as much as a factor of 5 when plasma density
decreases by 2 orders of magnitude, depending on the size of the bubble. The Q-factor also
increases significantly. Therefore, IAR fingerprint characterization would be also useful for
inferring spread-F vertical extension.

The characterization of IAR signatures contributes to the investigation of ionosphere
dynamics. In some cases, the following parameters can be derived from ELF measurements: $\Delta f$, $Q$, and $f_{th}$. In general, the analytical profile includes four variables: $\varepsilon$, L, H, and $V_A$, where the
Alfvén velocity is a function of plasma density and composition. The system is underdetermined
and additional constraints are necessary, e.g., the plasma density and composition. Moreover, the
analytical profile is unrealistic and intricate plasma distributions must be considered. Although
challenging, the most practical way of inferring the density profiles is by solving the MHD
inverse problem considering fingerprint signatures as modeling constraints – in practice, the
more reasonable approach is solving the direct MHD problem iteratively to determine the best fit
for IAR data [Simões et al., 2011b]. In such a case, $\Delta f_n$ and $Q_n$ variation with the eigenmodes
should be used instead of mean values. For example, the Q-factors measured in orbit 667 show a
small, steady increasing with the eigenmodes, and $\Delta f$ degeneracy is removed when plasma
density above the F-peak deviates from an exponential profile or medium losses are taken into
account. Since plasma density irregularities also produce uneven $\Delta f$ distributions, IAR detailed
characterization eventually provides multiple $\Delta f_n$, $Q_n$ constraints for MHD inverse problem
solutions, which are useful for determining the plasma composition and density profile, as well
as the total electron content. Future studies combining both ULF and high frequency techniques
such as GPS, radar, and radio occultation might provide even better approaches to constrain
plasma density and composition distributions, in particular close to the terminator.
6. Conclusion

Ionospheric in situ measurements onboard C/NOFS satellite show, for the first time, IAR signatures in the equatorial region. We derive frequency peak distribution and Q-factors of the resonator from IAR representative signatures, which contribute to a better characterization of ionospheric plasma dynamics at low latitude. Measurements onboard C/NOFS also show a peculiar, narrow event and structured hiss consisting of multiple lines possibly related to IAR dynamics, but their full significance, possibly related to modes coupling and feedback amplification mechanisms, requires further investigation. The IAR signature identified in ELF spectrograms can be used for inferring both medium properties and dynamics of the ionosphere. A MHD numerical model combining various parameterizations suggests that IAR is a resourceful tool for deriving plasma density profiles and investigating ionospheric irregularities; the model also confirms that during low solar activity IRI is not only overestimating plasma density but responding slowly to density gradients near the terminator, in line with independent assessments. Identification of IAR signatures at low latitude by C/NOFS is unexpected and valuable, offering new means for investigating the top-side equatorial ionosphere, namely plasma dynamics and interaction with the magnetosphere and solar wind. IAR signatures can be used to constrain not only plasma total density and composition of the ionosphere but also the shape of the profile, taking advantage of the valuable C/NOFS electric field dataset. Future developments should include a statistical analysis throughout the mission to identify geographical, seasonal, and solar wind/magnetospheric related characteristics.
7. Acknowledgements

The Communication/Navigation Outage Forecast System (C/NOFS) mission, conceived and
developed by the US Air Force Research Laboratory, is sponsored and executed by the USAF
Space Test Program. We acknowledge support from the Air Force Office of Scientific Research.
FS and JK are supported by an appointment to the NASA Postdoctoral Program at the Goddard
Space Flight Center, administered by Oak Ridge Associated Universities through a contract with
NASA. The work performed by SI at Goddard Space Flight Center was made possible by the
NASA Education Office through the Undergraduate Student Research Program managed by the
Universities Space Research Association.

8. References

Belyaev, P.P., S.V. Polyakov, V.O. Rapoport, and V.Yu. Trakhtengerts (1990), The ionospheric

Benson, R.F., and D. Bilitza (2009), New satellite mission with old data: Rescuing a unique data

Bilitza, D., and B.W. Reinisch (2009), International Reference Ionosphere 2007: Improvements

Bösinger, T., A.G. Demekhov, and V.Y. Trakhtengerts (2004), Fine structure in ionospheric
Alfvén resonator spectra observed at low latitude (L=1.3), *Geophys. Res. Lett.*, 31, L18802,


Figure 1: Low latitude typical ionospheric profiles of (from left to right) electron density ($N_e$), Alfvén velocity ($V_A$), and index of refraction ($n_A$). The dashed line represents an Alfvén velocity theoretical profile often used for obtaining IAR analytical solutions, where $L$, $H$, and $\varepsilon$ refer to the length, scale height, and depth of the Alfvén velocity ‘well’ ($V_A^2(z) = V_A^{2\text{min}}/(\varepsilon^2 + e^{-z/H})$ above $z \sim 400$ km). Commonly, most IAR power is confined in the altitude range 100-500 km and $\varepsilon \sim 0.01$, $L \sim 300$ km, and $H \sim 300$ km.
Figure 2: ELF spectrograms of the (top) meridional/vertical and (bottom) zonal/east-west electric field components measured with VEFI during orbits (left) 666 and (right) 667 on 31 May 2008. The resonator dispersion signature is the pattern resembling to a fingerprint visible in the bottom-left corner of each plot (1500-1512 and 1636-1648 UT). In the top-right panel, narrow lines are ubiquitous in the spectrogram (1639-1705 UT). The arrows indicate time of (1) sunset and (2) satellite eclipse. C/NOFS coordinates during IAR observation: altitude $\Rightarrow$ 650-500 km, 600-450 km; latitude $\Rightarrow$ 9°S-13°S, 11°S-13°S; longitude $\Rightarrow$ 10°E-50°E, 20°W-20°E, for orbits 666 and 667, respectively.
Figure 3: Spectra and waveforms of the (left) meridional and (right) zonal ELF electric fields measured during orbit 667. (Top) The arrows identify an interesting event starting at about 16:41:24 UT. The 3 strongest vertical lines in the spectrograms are satellite-related artifacts. (Middle) Spectral line of the event (red) and contiguous lines (black) for background noise comparison purposes. Note the peak amplitude sudden variation at about 14 Hz. (Bottom) Electric field waveforms of the event after removing the DC component.
Figure 4: (Top) Electric field amplitude, $E$, and (bottom) frequency difference between consecutive peaks, $\Delta f$, of the IAR modes evaluated from the zonal component about the terminator in the range 0-20 Hz. The mean and standard deviation of the zonal component are computed considering 30 s bins. The error bars indicate the standard deviation of each sample, where the sample size varies between 3 and 14, depending on the number of lines resolved in the spectrogram. The solid lines P0-P6 are computed with the MHD numerical model for composite plasma density profiles (see text for details); color code: P0 (black), P1 (red), P2 (cyan), P3 (magenta), P4 (blue), P5 (orange), and P6 (green).
Figure 5: ELF spectrograms of the (top) meridional/vertical and (bottom) zonal/east-west electric field components measured with VEFI during orbit 694 in 2 June 2008. In addition to the IAR structure, the lowest Schumann resonance signatures, identified as fuzzy horizontal lines at about 8, 14, and 20 Hz, are also noticeable in the horizontal component. The arrows indicate time of (1) sunset (1049 UT) and (2) satellite eclipse (1058 UT). The IAR frequencies seem to increase drastically at 1054 UT. C/NOFS coordinates during IAR observation: altitude ⇒ 750-550 km; latitude ⇒ 10°S-13°S; longitude ⇒ 40°E-100°E.
Figure 6: ELF spectrograms of the (top) meridional and (bottom) zonal electric field components measured with VEFI during orbit 2898, in 28-29 October 2008. The white rectangles delimit the detailed views shown in the right-hand-side. C/NOFS coordinates during IAR observation: altitude ⇒ 400-480 km; latitude ⇒ 6°S-10°S; longitude ⇒ 80°E-120°E.
Figure 7: Comparison between IAR model predictions using IRI-2007 default parameterization and VEFI measurements in 31 May 2008. (Top) The solid line indicates the $\Delta f$ of the resonator computed with the IAR model. The green bars show when the fingerprint is identified in C/NOFS data; bar height subjectively assesses fingerprint quality (legibility, intensity, resolvability). The IAR signature is clearly observed in 10 out of 15 consecutive orbits. (Bottom) Average magnetic field radial component, $B_r$, in the altitude range $10^2$-$10^3$ km at the satellite latitude/longitude; the gray and black markers represent nighttime on the ground and along satellite path, respectively.