Hybrid Wing-Body Pressurized Fuselage and Bulkhead, Design and Optimization

Vivek Mukhopadhyay

NASA Langley Research Center, Hampton, Virginia 23681-2199

The structural weight reduction of a pressurized Hybrid Wing-Body (HWB) fuselage is a serious challenge. Hence, research and development are presently being continued at NASA under the Environmentally Responsible Aviation (ERA) and Subsonic Fixed Wing (SFW) projects in collaboration with the Boeing Company, Huntington Beach and Air Force Research Laboratory (AFRL). In this paper, a structural analysis of the HWB fuselage and bulkhead panels is presented, with the objectives of design improvement and structural weight reduction. First, orthotropic plate theories for sizing, and equivalent plate analysis with appropriate simplification are considered. Then parametric finite-element analysis of a fuselage section and bulkhead are conducted using advanced stitched composite structural concepts, which are presently being developed at Boeing for pressurized HWB flight vehicles. With this advanced stiffened-shell design, structural weights are computed and compared to the thick sandwich, vaulted-ribbed-shell, and multi-bubble stiffened-shell structural concepts that had been studied previously. The analytical and numerical results are discussed to assess the overall weight/strength advantages.

Nomenclature

\[ a = \text{spacing between } y\text{-directional stringer or frame.} \]
\[ A = \text{beam column cross section area.} \]
\[ A_{sx} = \text{section area of single } x\text{-directional frame or stringer.} \]
\[ A_{sy} = \text{area of single } y\text{-directional stringer or frame.} \]
\[ b = \text{spacing between } x\text{-directional frame or stringer.} \]
\[ B = \text{total breadth of stiffened panel between end supports.} \]
\[ D = \text{bending rigidity of plate } E t^4/12(1 - \nu^2). \]
\[ D_x = \text{bending rigidity of stiffened orthotropic plate about the } x \text{ axis.} \]
\[ D_y = \text{bending rigidity of stiffened orthotropic plate about the } y \text{ axis.} \]
\[ E_x, E_y = \text{Young’s modulus of orthotropic plate in } x \text{ and } y \text{ directions.} \]
\[ F_{cx}, F_{cy} = \text{yield stress in compression along } x \text{ and } y \text{ directions.} \]
\[ F_{tx}, F_{ty} = \text{yield stress in tension along } x \text{ and } y \text{ directions.} \]
\[ G = \text{shear modulus.} \]
\[ H = \sqrt{D_x D_y} \]
\[ l = \text{area moment of inertia for beam bending about neutral axis.} \]
\[ I_x, I_y = \text{area moment of inertia of } x\text{- and } y\text{-stiffeners about neutral axis.} \]
\[ L = \text{total length of stiffened panel between end supports.} \]
\[ v_x, v_y = \text{Poisson’s ratio along } x \text{ and } y \text{ axis.} \]
\[ M_x, M_y = \text{running bending moments about } x \text{ and } y \text{ axis, respectively (lb-inch/inch).} \]
\[ N_x, N_y = \text{running in-plane load along } x \text{ and } y \text{ directions, respectively (lb/inch).} \]
\[ P_c = \text{compression load on beam-column.} \]
\[ P_{cr} = \text{compression buckling load on beam-column.} \]
\[ P = \text{cabin pressure of 9.2 psi (2P = 18.4 psi).} \]
\[ q = \text{running normal load on beam or pressure on plate.} \]
\[ t = \text{shell or skin thickness.} \]
\[ w = \text{beam or plate deflection at mid-point.} \]
\[ x, y = \text{ } x \text{ and } y \text{ reference axes of the plate, respectively.} \]
\[ z = \text{normal distance from beam or plate neutral plane.} \]
\[ Z_{ox}, Z_{oy} = \text{neutral axis location of } x\text{- and } y\text{-stiffeners from skin mid plane.} \]

1 Senior Aerospace Engineer, Aeronautical Systems Analysis Branch, MS 442, AIAA Associate Fellow. (AIAA-Paper 2013-xxxx, 54th AIAA/ASME/ASCE/AHS/ASC SDM Conference, Boston, MA, April 2013)
I. Introduction

Design of efficient pressurized fuselage configurations for the Hybrid-Wing-Body (HWP) and Advanced Mobility Concept (AMC-X) flight vehicles are challenging opportunities for the efficient structures technology development. The stiffened cylindrical cross-section fuselage of Boeing 777 and 787, shown in figure 1, are quite efficient, since, when pressurized, the skin is mostly under tensile membrane stress. The Airbus A380 has an elliptic egg shaped cross-section which is strengthened by the twin deck floor beams. However, in a HWB fuselage with rectangular cross-section, the internal cabin pressure combined with flight loads primarily result in highly non-linear bending stress and large deformation. It can be shown that these bending stresses are theoretically one order of magnitude higher than the membrane-hoop stress in a conventional cylindrical fuselage of similar size and skin thickness. Moreover, resulting deformation of the outer aerodynamic surface could significantly affect performance advantages provided by the large lifting body. Thus, it is necessary to design an efficient fuselage structure in order to reduce the overall structural deflection and weight penalty, while satisfying the design stress, strain, and buckling safety factors, under the critical design loads. Many structural concepts such as the conventional skin-stringer-frame, ribbed-double-shell, multi-bubble stiffened shell, thick sandwich, J-Frame, Beaded-Hat, and stitched sandwich frame composite construction have been studied under AFRL and NASA research projects. These concepts are schematically shown in Figure 1.

Figure 1. Fuselage section concept analysis models of B777, A380 and HWB class of vehicles.

A highly innovative advanced technology acronymed PRSEUS (Pultruded Rod Stitched Efficient Unitized Structure) is being developed at Boeing Phantom Works, with application to the pressurized HWB vehicles. This involved analysis, design, fabrication and testing of PRSEUS coupons, panels and fuselage components, under the NASA Environmentally Responsible Aviation (ERA) Program’s Airframe Technology subtask for structural weight and risk reduction. This development process for the PRSEUS concept is schematically shown in Figure 2. Some initial results at the coupon, panel and fuselage section under one critical overpressure load condition were presented in Ref. 18. This paper will discuss additional analytical and numerical results of parametric design studies of conceptual fuselage section and bulkhead for comparative weight analysis and optimization. Alternate concepts are also considered for systems study in an attempt to improve the present design further. Only local idealized fuselage section is considered in this paper, with a limited set of critical design loads. The objective is to minimize the local structural weight by 10-20% with stitched composite construction combined with novel structural configuration, compared to the sandwich and multi-bubble concepts that were studied previously. At the vehicle level, aerodynamic and structural systems study for the 100, 200, 300, and 400-pasenger versions were considered.
in Refs. 19-23, in order to estimate the full vehicle structural weight at all critical load conditions. For a recent multi-bubble HWB configuration study, see Ref. 24.

Figure 2. PRSEUS concept development cycle for analysis, design and testing.

II. Classical Stiffened Plate Analysis

Since the Finite Element (FE) model development of the PRSEUS concept requires many levels of simplification and idealization for extension from the coupon level to the fuselage level\(^{18}\), an analytical model is developed at the panel level for rapid parametric study and sizing. This would also enable one to evaluate the effects of skin thickness, frame and rod-stringer spacing and section geometry on the panel deflection due to a pressure load and for buckling analysis due to in-plane compression load. Classical plate theory\(^{25-26}\) and equivalent orthotropic stiffened plate equations\(^{27-29}\) were applied to simplify the PRSEUS model analysis for a rectangular plate. These simple spread-sheet based analytical results are also used for sanity check of the high fidelity FE analysis of panels, fuselage section and bulkhead. SolidWorks\(^{30}\) was used for rapidly building detailed FE models of the vehicle fuselage sections for structural analysis and design. A large number of design options were considered such as the orthotropic skin thickness, frame and rod-stringer spacing, for obtaining stress and strain distributions, deformation pattern and for identifying critical areas. For each configuration, structural weight was computed and compared.

Figure 3. Frame and pultruded rod-stringer stiffened orthotropic plate configuration.

**Stiffened Plate Bending Analysis:** Consider the biaxially stiffened plate shown in Fig. 3. For an isotropic thin rectangular plate of uniform thickness \(t\), length \(L\) and width \(B\), the maximum deflection can be expressed as in Eq. 1 which is a function of the pressure load \(q\), plate bending stiffness \(D\) and the factor \(k\) that is calculated from analytical
solution for this boundary condition. The factor $k$ is presented in tabular form \(^{25}\), as a function of the ratio $B/L$ ($B>L$). For example, for a square plate with built-in edges, $k=0.00126$ for $B/L=1$ (Table 1). For a simply supported isotropic square plate, $k = 0.00406$.

\[ w_{\text{max}} = k \cdot q_L^2 / D \quad \text{where} \quad D = E t^4 / 12(1-\nu^2) \]

Let us assume that the uniform plate-theory assumptions are also applicable to this equivalent stiffened plate. From ideal orthotropic plate theory \(^{25}\), for a simply supported stiffened rectangular plate, the closed form solution for deflection $w$ given by Eq. (2).

\[
(2) \quad w(x, y) = \frac{16q_o}{\pi^6} \sum_{m=1,3,5} \sum_{n=1,3,5} \frac{\sin(m\pi x / L) \sin(n\pi y / B)}{mn} \left( \frac{m^4}{L^4} D_x + \frac{2m^2n^2}{L^2B^2} H + \frac{n^4}{B^4} D_y \right)
\]

The running stiinesses $D_x$, $D_y$ and $H$ can be approximately defined \(^{25,29}\) by Eqs. (3-5).

\[
(3) \quad D_x = \frac{E_x t^3}{12(1-\nu_x \nu_y)} + \frac{E_y I_{xx}}{12(1-\nu_x \nu_y)} + \frac{E' I_x}{b}
\]

\[
(4) \quad D_y = \frac{E_y t^3}{12(1-\nu_x \nu_y)} + \frac{E_x I_{yy}}{12(1-\nu_x \nu_y)} + \frac{E' I_y}{a}
\]

\[
(5) \quad H = \sqrt{D_x D_y}
\]

The terms in Eq.(3-4) are explained in Figure 3. The equivalent plate bending stiinesses $D_x$, $D_y$ resists bending moment $M_x$, $M_y$ about the x- and y- axes, respectively. The attached longitudinal stiffening frames, each with area $A_{xx}$ and individual bending stiiness $E' I_x$ move up the cross-sectional-area-center by $Z_{xx}$ from the plate neutral (mid) plane, thereby increasing the total area and the bending stiffness. The symbol $E'_x$ is used to differentiate the stiiness modulus from the plate modulus $E_x$. Similarly, the transverse stringers or rod-stiffeners, each with area $A_{yy}$ and bending stiffness $E'_y$, increase the bending stiffness $D_y$ by moving up the transverse-section-area center by $Z_{yy}$ from the plate neutral plane.

For the stitched composite orthotropic skin, the following material properties were used \(^{8,9}\), namely $E_x = 9.75 \times 10^6$ psi, $E_y = 4.86 \times 10^6$ psi, $\nu_x = 0.39$, and $\nu_y = 0.2$. A stitched composite frame with a 0.1 inch skin wrapped around a 6 inch high, 0.5 inch thick foam core and a 4-in. wide flange and a 0.1 inch thick base cover strap provide a cross-sectional area of approximately 2 in.$^2$, without considering the foam core, that is mostly for shape stabilization. The frame dimensions are schematically shown in Figure 4(a). The frame flange is stitched to the base skin and are spaced at b=20 in. interval, and with a 0.1 in. skin thickness, the skin area between the frames is approximately 2 in.$^2$. Together, the frame and the skin segment between adjacent frames have running bending stiffness $D_s$ of approximately $5.8 \times 10^6$ lb-in. By using a 0.2 inch thick frame cap (Fig. 4b), $D_s$ increases to $6.3 \times 10^6$ lb-in. This would reduce the stresses, which are highest in the frame cap. For the first rod-stringer shown in Fig.4c, with base to rod-center height of 1.4 in., $D_s = 0.75 \times 10^6$ lb-in. including a 2 in. cover-strap and base skin between the rod-stringers spaced at 6 inch apart. For the rod-stringer in Fig.4d, with base to rod-center height of 1.65 in., $D_s = 1.08 \times 10^6$ lb-in. The rod-stringer in Fig.4e, with 0.208 in. flange thickness, and

![Figure 4. Frame and rod-stringer configurations.](image)
base to rod-center height of 1.65 in., \( D_s = 1.45 \times 10^6 \) lb-in. Next, these frame-stiffened plate stiffness estimates were applied to the classical isotropic plate bending equations. The \( D_s \), \( D_y \) and \( H \) that were computed for this frame-stiffened panel are now applied to a classical plate bending equation subject to a normal, uniform distributed pressure load of \( q \) psi with simple-supported and clamped edge conditions.25-26.

**Simply Supported Plate:** Using Eq. (2) to an anisotropic rectangular plate with \( q_s = 18.4 \) psi, \( L = 120 \) in., \( B = 90 \) in., \( D_s = 5.77 \times 10^6 \) lb-in and \( D_y = 0.75 \times 10^6 \) lb-in, the maximum deflection is 4.5 in. Here, stiffer frames (\( D_s \)) running along the shorter side \( L \), as shown in Fig. 3. If the frames are running along the shorter side \( B \), and the rod-stringers are running along the longer side \( L \), then the deflection can be obtained by simply interchange \( D_s \) with \( D_y \) in Eq. (2). The deflection at mid-point is now reduced to 2.1 inches.

If we apply Eq. (2) to a simply supported isotropic square plate \((L=B, D_s=D_y=D)\) the maximum deflection is can be simply written as in Eq. (1), \( w_{\text{max}} = kqL^4/D \) with \( k = 0.00406 \). If one takes just the first term \((m=1, n=1)\) in Eq. (2), i.e. \( w_{\text{max}} = (4L^2)/(D_x/L^4 + 2H/(L^2B^2) + D_y/B^2) \), then for a square plate \( k = 4/\pi^2 = 0.00416 \). With \( q = 18.4 \) psi, \( D_s = 5.8 \times 10^6 \) lb-in and \( D_y = 0.75 \times 10^6 \) lb-in, application of the exact Eq. (2) gives \( w_{\text{max}} = 3.23 \) inches, for a 104-in. square panel.

For an orthotropic plate, one may modify Eq. (1) to \( w_{\text{max}} = kqL^4/(D_xD_y) \) by replacing \( D \) with \( \sqrt{(D_sD_y)} \), with applicable \( k \) value. For example, with this approximation, for the same 104-in. square panel, the maximum deflection \( w_{\text{max}}=3.52 \) in., about 9% higher than that from Eq. (2). This simple approximation, \( w = kqL^4/(D_sD_y) \) may provide reasonable results for maximum, for appropriate \( k \) value from Table 1.25, 26

### Table 1: Clamped Isotropic Plate max deflection with uniform pressure \( q \):

<table>
<thead>
<tr>
<th>CASE NO</th>
<th>max deflection equation</th>
<th>length ( L ) ( (&lt;B) )</th>
<th>width ( B )</th>
<th>stiffness ( D_x, D_y ) or sq. ( H )</th>
<th>load ( (\text{psi}) )</th>
<th>( k )</th>
<th>max deflection ( w_{\text{max}}=kqL^4/D )</th>
<th>shell skin t</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>( w_{\text{max}}=kqL^4/(D_xL) ), ( L=B )</td>
<td>120</td>
<td>120</td>
<td>5,805,106</td>
<td>18.4</td>
<td>0.00126</td>
<td>0.83</td>
<td>0.104</td>
</tr>
<tr>
<td>2</td>
<td>( w_{\text{max}}=kqL^4/(D_yL) ), ( L=B )</td>
<td>90</td>
<td>90</td>
<td>1,087,872</td>
<td>18.4</td>
<td>0.00126</td>
<td>1.40</td>
<td>0.104</td>
</tr>
<tr>
<td>3</td>
<td>( w_{\text{max}}=k.q/(L^4/\sqrt{D_xD_y}) ), ( L=B )</td>
<td>104</td>
<td>104</td>
<td>2,513,008</td>
<td>18.4</td>
<td>0.00126</td>
<td>1.08</td>
<td>0.104</td>
</tr>
<tr>
<td>4</td>
<td>( w_{\text{max}}=k.q/(L^4/\sqrt{D_xD_y}) ), ( B=1.33 )</td>
<td>90</td>
<td>117</td>
<td>2,513,008</td>
<td>18.4</td>
<td>0.00191</td>
<td>0.92</td>
<td>0.104</td>
</tr>
<tr>
<td>5</td>
<td>( w_{\text{max}}=k.q/(L^4/\sqrt{D_xD_y}) ), ( B=1.33 )</td>
<td>90</td>
<td>120</td>
<td>2,513,008</td>
<td>18.4</td>
<td>0.00196</td>
<td>0.94</td>
<td>0.104</td>
</tr>
<tr>
<td>6</td>
<td>( w_{\text{max}}=k.q/(L^4/\sqrt{D_xD_y}) ), ( B=1.5 )</td>
<td>80</td>
<td>120</td>
<td>2,513,008</td>
<td>18.4</td>
<td>0.00220</td>
<td>0.66</td>
<td>0.104</td>
</tr>
<tr>
<td>7</td>
<td>( w_{\text{max}}=kqL^4/(D_xB) ), ( B=2L )</td>
<td>80</td>
<td>120</td>
<td>5,805,106</td>
<td>18.4</td>
<td>0.00254</td>
<td>1.00</td>
<td>0.104</td>
</tr>
<tr>
<td>8</td>
<td>( w_{\text{max}}=kqL^4/(D_yB) ), ( B=2L )</td>
<td>80</td>
<td>120</td>
<td>5,805,106</td>
<td>18.4</td>
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<tr>
<td>9</td>
<td>( w_{\text{max}}=k.q/(L^4/\sqrt{D_xD_y}) ), ( B=2L )</td>
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<td>180</td>
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<td>10</td>
<td>( w_{\text{max}}=k.q/(L^4/\sqrt{D_xD_y}) ), ( B = 1.55 ) ( L )</td>
<td>90</td>
<td>180</td>
<td>2,513,008</td>
<td>18.4</td>
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<td>120</td>
<td>5,805,106</td>
<td>18.4</td>
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<td>0.104</td>
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<tr>
<td>12</td>
<td>( w_{\text{max}}=k.q/(L^4/\sqrt{D_xD_y}) ), ( B = 1.55 ) ( L )</td>
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<td>120</td>
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<td>18.4</td>
<td>0.00220</td>
<td>1.48</td>
<td>0.104</td>
</tr>
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</table>

### Table 2. Parametric maximum deflections for the 12 cases in Table 1 for a combinatorial set of frame spacing (\( \text{fsp}=20 \) or 24 in.), rod-stiffener spacing (\( \text{rsp}=6 \) or 8 in.) and skin thickness (\( t=0.052 \) or 0.104 in.).

**Clamped Edge Plate:** One can apply this approximation to the Eq. (1) for a clamped edge plates (Ref. 25, Figure 91, pp.197, and Table 35, pp. 202). Table 1 shows the maximum deflection of typical rectangular clamped panels with \( D_s=5.8 \times 10^6 \) lb-in., \( D_y=1.08 \times 10^6 \) lb-in. (Frame in Fig.4a, rod-stringer in Fig. 4d, respectively), and 18.4 psi pressure.
load. The equivalent plate bending stiffness $D_o$ or $D_r$ were computed from Eqs. (3-4) from classical plate theory with 20 inch frame spacing, 6 inch rod-stringer spacing, 0.104 inch skin and frame-wrap thickness.

The column at left shows the equation used for each of the 12 cases. Case 1 is for a frame stiffened ($D_o$) square plate in both directions x and y. Case 2 is for rod-stringer stiffened ($D_r$) square plate in both directions x and y. In the cases 3 to 6, 9, 10, stiffness $D$ is replaced by $\sqrt{D_oD_r}$ as an equivalent orthotropic approximation, as discussed before. In case 3, for a 104 in. square plate, the maximum deflection is approximately 1.08 in. with $q=18.4$ psi. In case 10, a 90x140 stiffened plate (lower bay side-cargo panels) this approximation yields a maximum deflection of 1.08 inches. These approximations yield a median deflection value that cannot distinguish between running direction of frames and rod-stringers in rectangular panels. Hence, in case 11, $D/L^2$ in Eq. (1) is replaced by $0.25[D_o/L^2+2H/(L^2B^2)+D_r/B^2]$ with k factors for the specific B/L ratio (L<B) from Ref. 26, for a better orthotropic approximation. This equation represents stiffer frames ($D_o$) running along shorter direction L and the maximum deflection is 0.8 inches for an 80x120 panel. In case 12, $D/L^2$ is replaced by $0.25[D_o/L^2+2H/(L^2B^2)+D_r/B^2]$, (Interchange $D_o$ with $D_r$) which represents stiffer frames ($D_r$) running along the longer direction B. In this case the maximum deflection is 1.48 inches. This characteristic is similar to that observed from the exact Eq. (2) for the simply supported orthotropic rectangular plate case. Of course, for square orthotropic plate, both equations yield same deflection.

Table 2 (continuation of Table 1) shows maximum deflections for each of the 12 cases, which are computed for eight combinatorial design scenario of frame spacing of 20 and 24 inches, rod-stringer spacing of 6 and 8 inches and skin thicknesses of 0.052 and 0.104 inches. These spread sheet based calculations can be used for panel sizing, weight and configuration optimization as well as for sanity check of numerical finite element results.

**Ideal Beam-Column Buckling analysis:** Consider an ideal straight beam-column to represent a flat cabin roof panel segment, with axial in-plane compression load $P$, and distributed running load $q$ due to the normal cabin pressure. Let $EI$ be the beam bending stiffness over the span-length L. From the beam-column theory, the maximum deflection, bending moment, and bending stresses at mid-span are given by Eqs. (6-8).

(6) \[ w_{max} = \left(\frac{qL^4}{384EI}\right)\eta(\mu), \]  \[ \text{where } \eta(\mu) = 12(2\sec(\mu) - 2 - \mu^2)/(5\mu^2) \]

(7) \[ M_{max} = \left(\frac{qL^2}{8}\right) + P_c w_{max}, \text{ where } \mu = \frac{1}{2} \sqrt{\frac{P}{EI}} \]

(8) \[ \sigma = M_{max}/I + P_c/A \]

The critical buckling load $P_{cr}$ for a simply supported straight beam without initial deformation or eccentric loading is given by $P_{cr} = \frac{\pi^2EI}{L^2}$. Then $\mu = (\pi/2)(P/P_{cr})$, and thus these equations are valid for $P_c < P_{cr}$, or $\mu < \pi/2$. Based on the beam-column equations, the stiffener frame dimensions can be sized to provide adequate section area and bending stiffnesses to prevent buckling. In these beam bending calculations, in order to represent a stiffened panel, the total bending stiffness $EI$ in beam-column equation is replaced with $D_ob$, and the total spanwise running load $q$ is multiplied by $b$, where $b$ is the frame spacing. Applying the simply supported beam-column Eqs. (6-8) with $L=120$ in., $b=20$ in. $D_o=5.8x10^6$ lb-in. (Frame in Fig. 4a), and a 9.2 lb/in. normal running load, the maximum linear deflection is 4.28 in. and the maximum bending stress on the frame top is 6,000 psi without compression load. The critical beam-buckling compression load is 3960 lb/in., assuming that the frame and the plate segment bend like a beam. With a compression load $P_c=1000$ lb/in., $P_c/P_{cr}=0.25$ and the maximum nonlinear deflection is 5.72 in. The maximum bending plus axial stress is 49,000 psi including non-linear bending effect due to the 1000-lb compression load. Hence, for a simply supported ideal frame-stiffened beam-column, the buckling strength needs to be increased significantly.

In the real situation, the PRSEUS panel will be cross- stiffened and all edges will be close to the clamped condition. The beam deflection for the clamped case can be computed by applying equal end-moments $M_o$, which would reduce the end-slopes to zero. This moment and the corresponding maximum deflections are given by Eqs. (9-10).

(9) \[ M_o = -(qL^2/12), \mu \chi(\mu)/\tan(\mu), \text{ where } \chi(\mu) = 3(\tan(\mu) - \mu)/\mu^3 \]

(10) \[ w_{max} = (MoL^2/8EI)(1-\cos(\mu))/\mu^2 \cos(\mu) \]

For the clamped end condition, the linear buckling load $P_{cr}=4.72EI/L^2$ or 15,000 lb/in. in-plane compression running load. The end moment $M_o$ is calculated to be 230,000 lb-in, and the corresponding maximum bending stress at the
frame-top is approximately 78,000 psi at beam ends. The maximum non-linear deflection at mid-span is then 4.8 inches. In order to reduce the deflection and alleviate this high local stress, the panel skin and frame ends need to be reinforced significantly.

**Panel Buckling Analysis:** Consider the simply supported stiffened plate in Fig.3 under normal loading g and in-plane compressive running load N_x, then the solution for deformation can be expressed as a modified form of Eq.(2)

\[
 w(x, y) = \frac{16q_o}{\pi^5} \sum_{m=1,3,5} \sum_{n=1,3,5} \frac{\sin(m\pi x / L) \sin(n\pi y / B)}{m^4 L^4 D_x + \frac{2m^2 n^2}{L^2 B^2} H + \frac{n^4}{B^4} D_y - \frac{N_x m^2}{2 L^2}}
\]

The value of \( N_x \) that renders the denominator of Eq. (11) to zero will provide the in-plane buckling load. Thus for \( m=1, n=1 \), in-plane compressive running load \( N_{scr} = \pi^2 L^2 [D_x/L^2 + 2H/(L^2 B^2) + D_y/B^4] \). For the orthotropic equivalent plate with \( L=120 \) in., \( B=90 \) in., \( D_x = 5.80 \times 10^6 \) lb-in and \( D_y = 1.08 \times 10^6 \) lb-in, the critical in-plane running load \( N_{scr} \) is 12,000 lb/in. For an isotropic square plate, the critical minimum buckling is given by \( N_{scr} = 4\pi^2 D/L^2 \). For a 104x104 in. square simply supported plate with \( D \) replaced by \( v(D D_y) \), \( N_{scr} = 9+100 \) lb/in.

## III. Fuselage Section Analysis.

**Design conditions:** The following critical design load conditions were studied for the fuselage and bulkhead.

1. 18.4-psi internal static over-pressure at ground level (i.e., 2P case).
2. 2.5-g climb condition with an internal cabin pressure of 9.3 psi (i.e., 1P-2.5g case).

The maximum aerodynamic load for the 1P-2.5g case also produces a maximum compression load on the fuselage top panels and a maximum tensile load on the fuselage bottom panels. This bending load is idealized as approximately 5000-lb/in. running compression and tension load along the top and bottom panels, respectively. This in-plane ultimate design load was derived from full-vehicle FEM analysis results and includes all safety margins.

**Material Properties:** For the orthotropic stitched PRSEUS panel, the elastic modulus in the x and y directions are \( E_x = 9.75 \times 10^6 \) psi, \( E_y = 4.86 \times 10^6 \) psi, \( v_{xy} = 0.39 \), \( v_{yx} = 0.2 \), respectively. The average mass density is 0.057 lb/ft^3. For the foam core, \( E = 21000 \) psi, \( G = 7950 \) psi, and the mass density is 0.00361 lb/ft^3. The web and the flange of the pultruded rod-stringer have the same property as the stitched composite material. The pultruded rod has an elastic modulus of \( E' = 1.9 \times 10^7 \) psi and \( v = 0.29 \). This property is used when the built-up rod-stringer is modeled as a beam. In some of the previous panel analysis the web was modeled as shell and the top bulb was modeled as a beam. The stronger x-direction of the orthotropic skin and frame-wrap are always along the frame running direction.

**Failure Criteria:** In the linear analysis, the maximum allowable principal strain is 0.007 for the orthotropic skin and frame wraps. For the orthotropic skin and built-up pultruded rod-stringer average yield stress of \( F_y = 46500 \) psi is used for a conservative safety factor calculation. For solid models of the foam-core, yield stress \( F_y = 440 \) psi. The allowable failure stresses of the orthotropic shell are \( F_{\alpha} = 105100 \) psi, \( F_y = 46500 \) psi, in tension, and \( F_{\gamma} = 79200 \) psi and \( F_{\gamma} = 37900 \) psi in compression, respectively. The maximum allowable
shear stress is 29900 psi. When the rod stringers were modeled as beams, the maximum combined bending and axial stresses were used to check for beam failure. The directional stresses and principal strain distributions along with yield stress based factor of safety were plotted to identify local high stress and strain failure areas.

**Multibay Fuselage Section:** For a detailed description of the Multibay development, fabrication and combined loads test plan and progress, see Refs. 11-16. Figure 5 shows a multi-bay concept model along with the frame and rod-stringer dimensions. This model is substantially simplified, from those described in refs. 11-16, in order to facilitate conceptual study and what-if type analysis. This 3 bay section has a spanwise width of 360 inches, with 90 inch high passenger bay, 72 in. high central cargo bay. This fuselage section has five foam-core frames at 20 in. spacing. Each frame is built-up with 6 in. high, 0.5 in thick foam-core, that are wrapped with 0.104 in. thick (2 stack) composite skin and flanges. The flanges are stitched to the base skin and frame cover straps. The rod-stringers are spaced 8 in. apart on upper and lower surface of each bay, side walls, lower left and right cargo bay and passenger floors. Each rod-stringer is built-up with stitched composite flange, web wrapped around a pultruded carbon rod shown in Fig 4d. The flange is stitched to the base skin and a stringer cover strap16. In this multi-bay concept analysis, the built-up rod-stringers are modeled by beam elements with same cross-section as the built-up rod-stringer and cover strap. The base skin and frame wraps are modeled by shell elements. The foam core is modeled by solid elements. The two mid-cabin sandwich walls are modeled with 2 in. thick foam core and 0.052 in. stitched composite skin without cutouts.

![Figure 6. Multibay displacements (magnified by x10) and principal strain (Five frames at 20 inch spacing, improved rod-stringer at 8 in. spacing, without bulkhead) under internal cabin pressure of 18.4 psi and passenger-floor pressure of 1 psi.](image)

Figure 6 shows the corresponding displacements (magnified by x10) and principal strain under 18.4 internal cabin pressure on all outer walls and 1 psi pressure on passenger floors. Since the bulkhead was not modeled, an all outer-edge-fixed boundary condition was applied. The maximum deflection on the right and left side slanted cargo compartment walls is 1.2 in. Note that the cargo bays are approximated as flat panels, although in actual vehicle these keel panels conform to the aerodynamic shape. The directional stresses and strains on the skin are generally within the allowable limits, except at edge-restraints, cabin-wall-skin junctions, corner junctions and foam-core frame areas. The maximum principal nodal strains are of the order 0.012, at inter-cabin-junctions and unreinforced cabin-corners. In order to reduce large local stresses, these junctions need to be modeled more realistically with doubler and corner braces. These corner junction areas require diagonal braces and additional reinforcements. Additional design refinements are required in these critical areas. The maximum bending and axial stresses on the rod-stiffeners, which were modeled as beam elements are generally within allowable limits, but may exceed locally at the lower cargo bay due to large bending and edge constraints. The stress safety factors are locally 0.5 in this area on the rod-stiffeners but are well above 1 elsewhere. These high stresses can be reduced by adding corner braces, rod-stiffeners with a higher bending stiffness and frames with thicker frame-caps in these areas along with at least 0.1 in. skin due to impact damage concerns. The maximum deflection values from the FE analysis are close to the empirical average values, shown in Tables 1 and 2 (cases 6 and 10) and generally consistent with the analytical deflection values of similar size stiffened plates. However, there are still unresolved issues about the analytical solution of orthotropic clamped plates, including buckling analysis, which will be addressed in future. An isolated test bulkhead analysis is presented next.
IV. Bulkhead Analysis

Fig. 7(a) shows the displacement of an isolated bulkhead configuration with 20 horizontal rods at 8 inches spacing, 19 vertical frames at 20 inches spacing, two stack skin and two stack frame-wrap. Under the 18.4 psi pressure, maximum deflections are of the order 1.13 inches on the upper bulkhead left and right bay segments. The principal strain is generally under 0.007 inch/inch. Local combined maximum axial and bending stresses on the horizontal rod-stringers that were modeled as beam are under 76000 psi. Except for the local stress at the bulkhead-wall joints, due to end-fixity conditions, the majority of resultant stresses are under 70,000 psi. These high stress and deflection can be reduced significantly, by reinforcing the rod-stringers with two-stack wrap as discussed earlier. This is shown in Figure 7(b). The maximum deflection is now reduced to about one inch. The outer bay width for this configuration is reduced by 6 in. on each side. The local maximum beam bending stresses are now under 80,000 psi. The local maximum principal strains are now under 0.007 in/in. These deflections are close to the analytical values presented in Tables 1 and 2 (cases 5 and 11). However the total weight increases slightly to 878 lb. (2.59 lb/sq. feet of surface area), as shown in Table 3.

Figure 7. Bulkhead displacements under an 18.4 psi normal pressure load with fixed end boundary conditions: (a) one stack rod-stringer (Fig. 4d) and (b) two stack rod-stringer (Fig. 4e) with 1.65 inch base to center height.

Table 3. Component weight breakdown of a test bulkhead FE model with vertical frames.

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<tr>
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V. Integrated Multibay and Bulkhead

The Mixed model of integrated multi-bay with bulkhead model, shown in Fig. 8, was studied for two purposes; 1) Simplify the model to determine an equivalent plate to represent the bulkhead and cargo-bay for 2P load; and 2) Capture the critical area behavior for asymmetric bending-torsion loads. The upper crown panels and side 1 bulkheads are modeled with foam-core frames and rod stringers. The bulkhead side 2 is modeled with 1.5 inch thick equivalent flat plate. The bulkhead side 2 is hidden to show the interior details. Bulkhead side 2 upper and lower bays and cargo bays were also modeled with semi-equivalent plate of 1.5 inch thickness. The equivalent thicknesses
were selected to provide same order of deflection on both bulkhead side 1 (stiffened thin shell) and side 2 (uniform shell). Figure 9 shows the corresponding displacements and principal strain with 18.4 psi internal cabin pressure. Although the equivalent plates cannot be used for buckling analysis, they are necessary for scaled system study, comparison with theory, and for building simplified full vehicle model for flight load analysis. This model is presently being developed. Integrated PRSEUS fuselage and bulkhead models will also be developed farther for in-plane load and buckling analysis.

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**Figure 8.** Integrated multi-bay fuselage section and pressure bulkhead configuration.

**Figure 9.** Integrated multi-bay fuselage section displacement and principal strain with 18.4 psi cabin pressure.

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**VI. Summary of FEM Weight Analysis**

The first and second-generation 800 passenger HWB concepts were developed at Boeing Phantom Works through NASA contract and NASA in-house research. In Ref. 5, four structural concepts were studied, namely, Vaulted Ribbed Shell (VLRS), Flat Ribbed Shell (FRS); Vaulted shell with Light Honeycomb Core (VLHC) and Heavy Honeycomb Core (VHHC); and Flat sandwich shell with Light and Heavy Honeycomb Core (FLHC & FHHC). A multi-bubble section concept was analyzed in Ref. 6 and a relative comparison of component non-optimal weight breakdown per unit surface area is shown in the first bar chart in Figure 10. Conventional two floor cylindrical and A380 type elliptic section and stress balanced multi-bubble fuselage sections with frame and longiron stiffened aluminum skin of 3 mm (0.118 inch) shell thickness were also analyzed for comparison.

The weight analysis summary of the Multibay (without pressure bulkhead) is shown in the 3rd bar charts in Figure 10. The weight analysis includes three design scenarios: 1) 2 stack skin and rod-spacing of 8 in.; 2) 2 stack skin and rod-spacing of 6 in.; and 3) 1 stack skin and rod-spacing of 8 inches. Passenger floor has 1 stack skin and rod-spacing of 8 in. The frames are at 20 inch spacing for all 3 cases. The Multibay configuration weight with 2 stack skin and 2 stack frame wrap appears to be a safe-design for this internal pressure load case. The weight can be reduced by using a single stack skin configuration, but the impact damage can be a serious concern. The estimated weight of the multi-bay with 1 stack skin and two stack frame wrap is approximately 1800 lb. (about 1.92 lb/sq. ft of surface...
area) for one stack skin and two stack frame wrap, 8 inch rod-spacing). The maximum deflections are of the order 1.37 inches at outer skin surface of the cargo area (Figure 6). The maximum stresses are of the order 69,000 psi on the skin at the corner junction. The maximum strains are of the order 0.007 in./in., but local strains are higher at corner junctions. In the 4th bar chart, estimated specific weights of three bulkhead configurations are presented from preliminary analysis of three configurations: 1) 2 stack skin, 2 stack rods at 8 in spacing (Fig.7b); 2) 2 stack skin, 1 stack rods at 8 in spacing (Fig.7a); and 3) 1 stack skin, 2 stack rods at 8 in spacing. In all case the vertical frames are at 24 inch spacing. In the first case, the bulkhead weight is 878 lb (2.6 lb/sq. ft. surface area) without considering edge reinforcements and attachment fittings. The maximum deflection is about 1 inch. The stresses and strains are generally within the allowable limits. Although the weights can be reduced in the 2nd and 3rd configuration, the deflection and stresses can be significantly higher.

Figure 10. Summary of relative non-optimal finite element model concept weight per unit surface area.

VII. Conclusions

This finite element analysis and trade studies of a hybrid-wing-body fuselage section indicate that advanced, stitched, composite stiffened plates with rod-stringers and foam-core frames are better than the vaulted double-skin-shell or multi-bubble stiffened-shell concepts. A combination of skin-thicknesses, rod-stringer spacing and frame spacing were considered for the weight reduction trade study. The finite-element-model based specific weights of an ideal three-bay section and bulkhead model are estimated to be 2.0 lb/sq. ft. and 2.6 lb/sq. ft., respectively, depending on the configuration. These specific weight values are comparable to that of the cylindrical fuselage, but are lower than multi-bubble concepts, for the 18.4 psi pressure load condition. Although, 0.052 inch (1 stack) outer skin is preferable from a minimum weight perspective, additional load conditions and buckling studies indicate that 0.104 inch (2 stacks) skin will provide better safety margins and impact damage resistance. Since the sandwich frames take most of the bending load, two stacks of frame-wraps and frame caps are necessary. The combined maximum local bending and axial stresses in the rod-stringers also appear to be high at end-joint areas. With continuing development and testing, this stitched composite technology could make the current hybrid-wing-body concept both structurally feasible and aerodynamically efficient. But, the adverse effect of pillowing on the outer-surface aerodynamic flow should be considered. Systems analysis of the stitched composite bi-axially stiffened shell concept demonstrated that the hybrid-wing-body class of vehicles can be structurally as efficient as
the conventional cylindrical skin-stringer-frame construction. However, alternate concepts should also be considered to improve the present design farther.

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IX. References


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