The Global Land-Ocean Temperature Index in Relation to Sunspot Number, the Atlantic Multidecadal Oscillation Index, the Mauna Loa Atmospheric Concentration of CO₂, and Anthropogenic Carbon Emissions

Robert M. Wilson
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<th>Abbreviation</th>
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<tbody>
<tr>
<td>10-yma</td>
<td>10-year moving average</td>
</tr>
<tr>
<td>AMO</td>
<td>Atlantic Multidecadal Oscillation</td>
</tr>
<tr>
<td>BV</td>
<td>bivariate</td>
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<tr>
<td>CO₂</td>
<td>carbon dioxide</td>
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<td>GLOTI</td>
<td>Global Land-Ocean Temperature Index</td>
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<tr>
<td>MLCO2</td>
<td>Mauna Loa CO₂</td>
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<tr>
<td>SSN</td>
<td>sunspot number</td>
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<tr>
<td>SST</td>
<td>sea-surface temperature</td>
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<td>TCE</td>
<td>total carbon emissions</td>
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<td>THC</td>
<td>thermohaline circulation</td>
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<td>TP</td>
<td>Technical Publication</td>
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<td>TV</td>
<td>trivariate</td>
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NOMENCLATURE

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<tr>
<th>Symbol</th>
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<tr>
<td>cl</td>
<td>confidence level</td>
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<tr>
<td>na</td>
<td>number above median</td>
</tr>
<tr>
<td>nb</td>
<td>number below median</td>
</tr>
<tr>
<td>nra</td>
<td>number of runs above median</td>
</tr>
<tr>
<td>$R_{y12}$</td>
<td>sample coefficient of multiple determination</td>
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<tr>
<td>r</td>
<td>coefficient of correlation</td>
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<tr>
<td>$r^2$</td>
<td>coefficient of determination</td>
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<tr>
<td>$S_{y12}$</td>
<td>sample standard error of estimate for multiple determination</td>
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<td>sd</td>
<td>standard deviation</td>
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<td>se</td>
<td>standard error of estimate</td>
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<tr>
<td>t</td>
<td>time</td>
</tr>
<tr>
<td>x</td>
<td>independent variable in regression equation</td>
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<tr>
<td>y</td>
<td>dependent variable in regression equation</td>
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<tr>
<td>z</td>
<td>normal deviate of the sample</td>
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Global warming/climate change has been a subject of scientific interest since the early 19th century. In particular, increases in the atmospheric concentration of carbon dioxide (CO$_2$) have long been thought to account for Earth’s increased warming, although the lack of a dependable set of observational data was apparent as late as the mid 1950s. However, beginning in the late 1950s, being associated with the International Geophysical Year, the opportunity arose to begin accurate continuous monitoring of the Earth’s atmospheric concentration of CO$_2$. Consequently, it is now well established that the atmospheric concentration of CO$_2$, while varying seasonally within any particular year, has steadily increased over time. Associated with this rising trend in the atmospheric concentration of CO$_2$ is a rising trend in the surface-air and sea-surface temperatures (SSTs).

This Technical Publication (TP) examines the statistical relationships between 10-year moving averages (10-yma) of the Global Land-Ocean Temperature Index (GLOTI), sunspot number (SSN), the Atlantic Multidecadal Oscillation (AMO) index, and the Mauna Loa CO$_2$ (MLCO2) index for the common interval 1964–2006, where the 10-yma values are used to indicate trends in the data. Scatter plots using the 10-yma values between GLOTI and each of the other parameters are determined, both as single-variate and multivariate fits. Scatter plots are also determined for MLCO2 using single-variate and bivariate (BV) fits, based on the GLOTI alone and the GLOTI in combination with the AMO index. On the basis of the inferred preferential fits for MLCO2, estimates for MLCO2 are determined for the interval 1885–1964, thereby yielding an estimate of the preindustrial level of atmospheric concentration of CO$_2$. Lastly, 10-yma values of MLCO2 are compared against 10-yma estimates of the total carbon emissions (TCE) to determine the likelihood that manmade sources of carbon emissions are indeed responsible for the recent warming now being experienced. (Parametric values used in this TP are those available prior to the end of 2012.)
2. RESULTS

Figure 1 displays the variation of the annual (thin line) and 10-yma (thick line) values of (a) GLOTI, (b) SSN, (c) AMO, and (d) MLCO2 for the common interval 1959–2011. Individual sunspot cycles are identified in subpanel (b). Inspection of figure 1 suggests that during the common interval 1959–2011, the GLOTI, AMO, and MLCO2 are all trending upwards, while SSN is trending downwards. Furthermore, because the 10-yma value of MLCO2 remains above its annual (same year) average during this common interval, it is apparent that the atmospheric concentration of CO₂ as measured at Mauna Loa, Hawaii, is presently increasing at an accelerated rate, as placement of a straight-edge along the curve clearly shows.

The GLOTI is a measure of the global land-ocean temperature relative to the base period of 1951–1980, where the data are taken from the Global Historical Climate Network, version 3, using elimination of outliers and homogeneity adjustment. The data, as used in figure 1(a), are the January–December averages, available online at <http://data.giss.nasa.gov/gistemp>.33,38

The SSN provides a measure of the strength of solar activity associated with the variation of solar irradiance over the solar cycle.39–42 Annual values of SSN are available online at <ftp://ftp.ngdc.noaa.gov/STP/SOLAR_DATA/SUNSPOT_NUMBERS/INTERNATIONAL>.

The AMO is a temperature oscillation in the detrended SST of the North Atlantic Ocean (0–70° N.) having a period of about 65–70 years that fluctuates between warm (positive) and cool (negative) phases.43,44 The SST pattern has been suggested to be linked to variations in the strength of the Atlantic thermohaline circulation (THC), a density-driven, global circulation pattern that involves the movement of warm equatorial surface waters to higher latitudes and the subsequent cooling and sinking of these waters in the deep ocean.45 In particular, the warm phase of the AMO represents intervals of faster THC, while the cold phase represents intervals of slower THC. From figure 1(c), one surmises that the AMO was reflective of the cool phase between about 1964 and 1994, but now is in the midst of a warm phase (since 1995) that began its rise to more positive values about 1975 (based on 10-yma values). The warm phase is expected to continue for at least another decade or more. Monthly values of the AMO index are available online at <http://www.esrl.noaa.gov/psd/data/correlation/amon.us.long.data>.

The MLCO2 is a measure of the atmospheric concentration of CO₂ as measured at the Mauna Loa Observatory on the Big Island of Hawaii, located on the northern slope of the volcano Mauna Loa at an elevation of 3,400 m above sea level and 800 m below its summit at 19.5° N. and 155.6° W.24,46 Annual averages of the MLCO2 measurements, expressed in ppm, are available online for the interval 1959–2011 at <ftp://ftp.cmdl.noaa.gov/ccg/co2/trends/co2_annmean_mlo.txt>. 
Figure 1. Variation of annual (thin line) and 10-yma (thick line) values of (a) GLOTI, (b) SSN, (c) AMO, and (d) MLCO2 for the common interval 1959–2011.
Figure 2 depicts the scatter plots of the 10-yma values of GLOTI versus (a) SSN, (b) AMO, and (c) MLCO2 for the interval 1964–2006. The diagonal lines in the subpanels represent the inferred preferential linear regressions. The small arrows in each subpanel (and in succeeding figures) indicate the last available 10-yma values for the parameters (i.e., for the year 2006). The 10-yma values in each subpanel generally track smoothly from lower to higher GLOTI values over the interval 1964–2006. Given in each subpanel are the inferred regression equation (y), the coefficient of correlation (r), the coefficient of determination ($r^2$) (a measure of the amount of variance explained by the inferred regression), the standard error of estimate (se), and the confidence level (cl) of the inferred regression, where cl > 90% indicates a marginally statistically important result, cl > 95% indicates a statistically important result, and cl > 99% indicates a highly statistically important result.

Figure 2. Scatter plots of the 10-yma values of GLOTI versus (a) SSN, (b) AMO, and (c) MLCO2 for the interval 1964–2006.
For GLOTI versus SSN, the inferred regression based on the limited time interval 1964–2006 is one found to be only of marginal statistical importance, having $cl > 90\%$, $se = 0.2 \degree C$, and $r^2 = 0.072$, meaning that the inferred regression explains only about 7% of the variance in the 10-yma values of GLOTI during the interval 1964–2006. Also, the inferred regression is found to be one that varies inversely ($r = −0.27$) rather than directly, in contrast to that found when using the much longer interval 1885–2006, one that clearly shows an upward-trending SSN.\(^4\)

For GLOTI versus AMO, the inferred regression ($r = 0.87$) is one that is highly statistically important, having $cl > 99.9\%$, $se = 0.09 \degree C$, and $r^2 = 0.762$, meaning that the inferred regression explains about 76% of the variance in the 10-yma values of GLOTI. Current values of AMO and GLOTI are positive, indicative of the warm phase and the occurrence of a warm anomaly, respectively. The implication then is that the continuing warm phase as indicated by the AMO suggests a continuing positive (warm) global land-ocean temperature anomaly for the near term foreseeable future.

For GLOTI versus MLCO2, the inferred regression ($r = 0.99$) is the strongest of all the inferred regressions, having $cl > 99.9\%$, $se = 0.06 \degree C$, and $r^2 = 0.988$, meaning that the inferred regression explains nearly 99% of the variance in the 10-yma values of GLOTI for the interval 1964–2006. The implication then is that the continuing unabated increase in the atmospheric concentration of CO$_2$ as measured at Mauna Loa strongly suggests a continuing increase in the positive (warm) global land-ocean temperature for the long term foreseeable future.
Figure 3 shows the scatter plots of the 10-yma values of GLOTI versus selected BV fits for GLOTI, including (a) BV1, based on SSN and AMO, (b) BV2, based on SSN and MLCO2, and (c) BV3, based on AMO and MLCO2. The BV fit BV1, having $R_{y12} = 0.895$ and $S_{y12} = 0.086$ °C, represents a slight improvement over using AMO alone, while the BV fit BV2, having $R_{y12} = 0.994$ and $S_{y12} = 0.021$ °C, and especially BV fit BV3, having $R_{y12} = 0.999$ and $S_{y12} = 0.01$ °C, represent significant improvements over using MLCO2 alone (by virtue of their inferred reduced standard error of estimates). (In figure 3, subscripts 1 and 2 refer to parameters 1 and 2, where 1 is SSN and 2 is AMO in BV1; SSN and MLCO2 in BV2; and AMO and MLCO2 in BV3.)

Figure 3. Scatter plots of the 10-yma values of GLOTI versus selected BV fits for GLOTI, including (a) BV1, based on SSN and AMO, (b) BV2, based on SSN and MLCO2, and (c) BV3, based on AMO and MLCO2.
Figure 4 displays the scatter plot of the 10-yma values of GLOTI versus a trivariate (TV) fit for GLOTI (TV1), based on SSN, AMO, and MLCO2. Essentially, the TV1 fit is insignificantly different from that of the BV3 fit (i.e., the $r$ and $se$ are essentially the same for both fits).

![Figure 4. Scatter plot of the 10-yma values of GLOTI versus a TV fit for GLOTI (TV1), based on SSN, AMO, and MLCO2.](image)

$TV1 = -0.032296 + 0.000441SSN + 1.00606BV3$

$R_{y12} = 0.998689$, $Sy_{12} = 0.009859$

Figure 4. Scatter plot of the 10-yma values of GLOTI versus a TV fit for GLOTI (TV1), based on SSN, AMO, and MLCO2.
Figure 5 depicts the scatter plots of the 10-yma values of MLCO2 versus (a) GLOTI and (b) BV4, the BV fit based on both GLOTI and AMO. Of the two fits, the one between MLCO2 and GLOTI alone is the stronger, having $r = 0.994$ and $se = 2$ ppm, as compared to $R_{y12} = 0.992$ and $S_{y12} = 2.4$ ppm for BV4. The diagonal line in figure 5(a) is the inferred preferential linear regression line for MLCO2 versus GLOTI. The regression equations and other statistical parameters are identified in the subpanels.

Figure 5. Scatter plots of the 10-yma values of MLCO2 versus (a) GLOTI and (b) BV4, the BV fit based on GLOTI and AMO.
Figure 6 shows the estimated and observed 10-yma values of MLCO2 for the interval 1885–2006 based on the inferred regressions shown in figure 5. Thus, presuming the validity of the inferred regressions, one finds that, while both fits essentially mimic the observed 10-yma values of MLCO2 (the filled circles) for the interval 1970–2006, slight differences are apparent in the values prior to 1970. In particular, BV4 (the thick line) suggests slightly lower estimated values (by about 10 ppm) for the 10-yma values of MLCO2 during the interval 1885–1964, as compared to using the linear fit based on GLOTI alone. Both extrapolations suggest temporary slight increases in atmospheric concentration of CO₂ near 1900 and the early 1940s, each increase lasting about 20 years in length. Values since about 1975 have been the highest on record and continue to increase with the passage of time.

Figure 6. Estimated and observed 10-yma values of MLCO2 for the interval 1885–2006, based on the inferred regressions shown in figure 5.
Figure 7 compares the estimated (based on BV4) and observed 10-yma values of MLCO2 for the interval 1885–2006 with exponentials based on year \( t \). Fit \( y_1 \) is based on the exponential determined using the 10-yma values from BV4 for \( t = 1890 \) and \( t = 1964 \), and fit \( y_2 \) is based on the exponential determined using 10-yma values from BV4 for \( t = 1964 \) and \( t = 2006 \). For 1890, 1964, and 2006, the 10-yma values from BV4 equal 285.25, 320.08, and 380.39 ppm, respectively. The fits \( y_1 \) and \( y_2 \) are provided merely to demonstrate the approximate fitting to the observed and estimated MLCO2 based on using the BV4 fit and the apparent change that seems to take place in the trending of MLCO2 values relative to the exponential fits sometime around 1970, when the observed and estimated MLCO2 values appear to have transitioned from one following more closely the \( y_1 \) fit to one following more closely the \( y_2 \) fit. (Actual 10-yma values of MLCO2 are now found to be above the estimated values given by the \( y_2 \) exponential fit, indicating that higher values of MLCO2 should be expected sooner rather than later, as given by the \( y_2 \) exponential fit.)

Figure 7. Comparison of the estimated (based on BV4) and observed 10-yma values of MLCO2 for the interval 1885–2006 with exponentials based on year \( t \).
The expected 10-yma value of MLCO2 about 1880 is of interest because it is representative of the preindustrial level of the atmospheric concentration of CO₂. Now, the record of GLOTI yearly values begins in 1880, having a value of –0.32 °C. Consequently, the first available 10-yma value of GLOTI occurs in 1885. However, the record of AMO yearly values begins in 1856, so that the 10-yma value of AMO is known for 1880 (=0.075 °C). For the interval 1885–2006, the residual (i.e., the difference between the yearly value and the corresponding 10-yma value) for GLOTI is about ±0.1 °C, a range that captures about 80% of the residuals. Hence, one can estimate the 10-yma value for GLOTI for the year 1880 to be about –0.32 ± 0.1 °C. Using this value in conjunction with the 10-yma AMO value for 1880 in BV4 allows one to estimate the 10-yma value of MLCO2 for 1880, a value computed to be about 283.6 ± 2.4 ppm, very close to that determined from polar ice cores for the preindustrial level (i.e., about 280 ± 5 ppmv; see Neftel et al.48).

As previously noted, the atmospheric concentration of CO₂ as measured at Mauna Loa appears to be not only increasing over time, but also to be increasing at an accelerated rate. Figure 8 plots the (a) first and (b) second differences of the 10-yma values of MLCO2 for the interval 1964–2006. From figure 8(a), one finds that the average 10-yma value of MLCO2 is growing at the rate of about 1.47 ± 0.31 ppm per year (i.e., the mean ± 1 standard deviation (sd) interval). However, as can be seen from figure 8(a), the average rate inadequately describes the actual year-to-year first difference values. The rate of growth in the 10-yma value of MLCO2 was always below 1.5 ppm prior to 1980 and, except for the brief intervals 1987–1989 and 1991–1992, it always has been equal to 1.5 ppm or greater after 1980, measuring 2.03 ppm in 2005 (the last available first difference value and the largest rate of growth ever measured). Overall, the first difference values are better described using the linear fit given by \( y = -46.207 + 0.024t \), where \( y \) is the expected first difference and \( t \) is the year, rather than using the mean and sd. The linear fit is found to explain about 88% of the variance in the first difference values. For 2006, one expects the first difference to be about 1.99 ± 0.3 ppm (the ±1 se prediction interval), thereby inferring that the expected 10-yma of MLCO2 for 2007 should be about 381.6 ± 1.99 ± 0.3 ppm or about 383.59 ± 0.3 ppm. Presuming the validity of the fit, one estimates the 10-yma value of MLCO2 for 2015 and 2026 to be ≥400 ppm and ≥425 ppm, respectively. If these values prove true, then, from figure 2(c), one expects the 10-yma value of GLOTI to measure about 0.72 ± 0.06 °C in 2015 and about 0.97 ± 0.06 °C in 2026. (It should be noted that the 10-yma of MLCO2 for 2007 is now known to measure 383.67 ppm, thus confirming the prediction above that it would measure about 383.59 ± 0.3 ppm.)
Figure 8. The (a) first and (b) second differences of the 10-yma values of MLCO2 for the interval 1964–2006.

Figure 8(b) displays the variation of the second difference of the 10-yma values of MLCO2 (i.e., the first difference of the first difference). It has a mean of $0.027 \pm 0.047$ ppm per year. Runstesting$^{49}$ of the second difference values strongly suggests that they are distributed randomly, having a normal deviate for the sample ($z = -0.467$), based on the observed number of values above the median ($na = 21$), the number of values below the median ($nb = 20$), and the number of runs above the median ($nra = 10$), where the median second difference value is 0.03.
Recently, Boden et al. reported on the yearly variation of global fossil fuel CO$_2$ emissions. They noted that approximately 356 billion metric tons of carbon have been released into the atmosphere through the combustion of fossil fuels and cement production since 1751, with half of the fossil fuel CO$_2$ emissions having occurred since the mid 1980s. Furthermore, they noted that liquid and solid fuels accounted for about 76.6% of the emissions in 2009, while gas fuels (e.g., natural gas) and cement production accounted for 17.9% and 4.7% of the emissions, respectively.

Figure 9 plots the annual and 10-yma values of the TCE estimates for the interval 1959–2009. For the overall interval 1964–2004, the trend in TCE has grown at the average rate of about 118 million metric tons per year, although the intervals prior to 1975 and after about 1997 have had considerably higher average rates of growth, measuring about 157 and 169 million metric tons per year, respectively. Extrapolation of the 10-yma trend line beyond 2004 using the higher rate of growth in TCE suggests that TCE will measure about 10,000 million metric tons around the year 2017 ± 2 years, and it will measure about 12,000 million metric tons around 2029 ± 2 years. (The rightmost vertical axis gives the total CO$_2$ emission in units of million metric tons.)
Figure 10 plots the 10-yma values of MLCO2 versus TCE, assuming a zero time lag. Clearly, as TCE increases, MLCO2 increases, strongly suggesting that the two parameters are highly statistically correlated, which they appear to be \((r = 0.985 \text{ and } cl > 99.9\% )\). The lower-leftmost filled circle corresponds to the year 1964, and the upper-rightmost filled circle corresponds to the year 2004, with the intervening filled circles corresponding to the intervening sequential years. From the inferred regression \((y)\), one finds that a 10-yma value of TCE = 10,000 million metric tons corresponds to a 10-yma value of about MLCO2 = 408.75 ± 3.79 ppm (the ±1 se prediction interval), while a 10-yma value of TCE = 12,000 million metric tons corresponds to about MLCO2 = 436.31 ± 3.79 ppm. Similarly, from the inferred regression \((x)\), one finds that a 10-yma value of MLCO2 of 400 ppm corresponds to a 10-yma value of about TCE = 9,246 ± 218 million metric tons, while 10-yma values of MLCO2 = 425 ppm and 440 ppm correspond to about TCE = 11,006 ± 218 and 12,062 ± 218 million metric tons, respectively.

As previously noted from figure 9, extrapolation of the 10-yma trend line beyond 2004 using the higher rate of growth in TCE suggests that TCE will measure about 10,000 million metric tons around the year 2017 ± 2 years, and it will measure about 12,000 million metric tons around 2029 ± 2 years, presuming the validity of the extrapolation. Furthermore, from figure 2(c), given the inferred 10-yma values of MLCO2 corresponding to 10-yma values of TCE equal to 10,000 metric tons and 12,000 million metric tons, being equal to about 409 ppm and 440 ppm, respectively, one estimates 10-yma values of GLOTI equal to about 0.82 ± 0.06 °C around 2017 ± 2 years and about 1.13 ± 0.06 °C around 2029 ± 2 years, respectively. A faster (slower) rate of growth in the 10-yma values of TCE implies higher (lower) 10-yma values of MLCO2 and, consequently, higher (lower) 10-yma values GLOTI.
3. DISCUSSION AND CONCLUSION

This TP of the common interval 1964–2006 has revealed a close statistical coupling between the global land-ocean temperature anomaly as described by GLOTI and both the phase of the AMO and the increasing atmospheric concentration of CO\textsubscript{2} as measured at Mauna Loa. On the basis of 10-yma values, the GLOTI is found to be well described using the BV fit \( BV3 = -2.77 + 0.224552 \text{AMO} + 0.008615 \text{MLCO2}, \) having \( R_{y12} = 0.9986 \) and \( S_{y12} = 0.01 \, ^\circ \text{C}, \) where \( BV3 \) represents the 10-yma value of the GLOTI, and the subscripts 1 and 2 refer to the 10-yma parametric values of the AMO and MLCO2 indices, respectively. Likewise, the BV fit \( BV4 = (322.309 + 115.027 \text{GLOTI} - 25.038 \text{AMO}) \) is found to provide a very close fit for the observed 10-yma values of MLCO2, having \( R_{y12} = 0.992 \) and \( S_{y12} = 2.42 \, \text{ppm}. \)

From an extrapolation of the BV4 fit backwards in time, prior to 1964, one finds evidence for two temporary slight increases in the atmospheric concentration of CO\textsubscript{2}, each of about 20 years duration—the first about 1900, having a local peak of about 296±2.4 ppm, and the second in the early 1940s, having a local peak of about 322±2.4 ppm. While the interval prior to about 1970 appears to be better approximated using the exponential \( y_1 = 1.856 + 0.002t, \) where \( y_1 \) is the 10-yma value of MLCO2 and \( t \) is the year, the interval after 1970 appears to be better described using the exponential \( y_2 = -2.085 + 0.004t. \) However, current 10-yma values of MLCO2 now appear to be rising faster than described by the post-1970 exponential. Using the BV4 fit, one estimates the preindustrial value for the atmospheric concentration of CO\textsubscript{2} to be about 283.6±2.4 ppm, very close to that determined from polar ice cores (i.e., about 280±5 ppmv).

The 10-yma value of MLCO2 measured about 382 ppm in 2006. On average, the 10-yma value of MLCO2 is found to be increasing at the approximate rate of about 1.47±0.31 ppm per year. While true, the average rate of growth in the 10-yma values of MLCO2 does not appear to adequately describe the actual year-to-year increases in the 10-yma values. Instead, the rate of yearly increase is better described using the linear fit \( y = -46.207 + 0.024t, \) where \( y \) is the first difference in consecutive year-to-year 10-yma values of MLCO2 and \( t \) is the year. Hence, the 10-yma values of MLCO2 appear to be increasing at an accelerated rate, such that the 10-yma value of MLCO2 is expected to measure ≥400 ppm about the middle-to-latter half of the present decade and ≥425 ppm about the middle-to-latter half of the following decade. Likewise, because of the inferred close association between the 10-yma values of GLOTI and MLCO2, one expects 10-yma values of GLOTI to continue to increase over time, measuring about 0.72±0.06 °C and 0.97±0.06 °C, respectively, when 10-yma values of MLCO2 measure ≥400 ppm and ≥425 ppm.

The rise in 10-yma values of MLCO2 appears to be directly linked to the increase in the 10-yma values of the TCE as deduced from the yearly values of global fossil fuel CO\textsubscript{2} emissions determined by Boden et al.\textsuperscript{37} In particular, the 10-yma values of MLCO2 are found to increase in step with increases in the 10-yma values of TCE, with the inferred correlation having \( r = 0.985 \) and \( cl \gg 99.9\%. \) From the inferred regression between the 10-yma values of MLCO2 and TCE, one finds
that a 10-yma value of TCE equal to about 10,000 million metric tons suggests a 10-yma value of MLCO2 ≥400 ppm and GLOTI ≥0.76 °C, while a 10-yma value of TCE equal to about 12,000 million metric tons suggests a 10-yma value of MLCO2 ≥440 ppm and GLOTI ≥1.07 °C.
REFERENCES


Examined are 10-year moving averages (10-yma) of the Global Land-Ocean Temperature Index (GLOTI) in relation to those of sunspot number, the Atlantic Multidecadal Oscillation (AMO) index, and the Mauna Loa carbon dioxide (CO₂) (MLCO₂) index and 10-yma of MLCO₂ in relation to that of the total carbon emissions (TCE). Using inferred fits between 10-yma values of MLCO₂ and GLOTI and between MLCO₂ and GLOTI and AMO, estimates are determined for the atmospheric concentration of CO₂ during the interval 1885–1964. The atmospheric concentration of CO₂ is inferred to have risen by about 32 ± 2% between 1890 and 2006. Comparison of 10-yma values of MLCO₂ and TCE strongly suggests that manmade sources of carbon emissions are indeed responsible for the recent warming now being experienced. Based on the expected 10-yma values of MLCO₂ for the years 2015 and 2026, 10-yma values of GLOTI are anticipated to measure about 0.72 ± 0.06 °C and 0.97 ± 0.06 °C, respectively, indicating continued warming for the foreseeable future.
The Global Land-Ocean Temperature Index in Relation to Sunspot Number, the Atlantic Multidecadal Oscillation Index, the Mauna Loa Atmospheric Concentration of CO₂, and Anthropogenic Carbon Emissions

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