THE SIZE EVOLUTION OF PASSIVE GALAXIES: OBSERVATIONS FROM THE WIDE-FIELD CAMERA 3 EARLY RELEASE SCIENCE PROGRAM


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ABSTRACT

We present the size evolution of passively evolving galaxies at $z \approx 2$ identified in Wide-Field Camera 3 imaging from the Early Release Science program. Our sample was constructed using an analog to the passive BzK galaxy selection criterion, which isolates galaxies with little or no ongoing star formation at $z \gtrsim 1.5$. We identify 30 galaxies in $\sim 40$ arcmin$^2$ to $H < 25$ mag. By fitting the 10-band Hubble Space Telescope photometry from 0.22 $\mu$m $\lesssim \lambda_{\text{obs}} \lesssim 1.6 \mu$m with stellar population synthesis models, we simultaneously determine photometric redshift, stellar mass, and a bevy of other population parameters. Based on the six galaxies with published spectroscopic redshifts, we estimate a typical redshift uncertainty of $\sim 0.033(1+z)$. We determine effective radii from Sérsic profile fits to the $H$-band image using an empirical point-spread function. By supplementing our data with published samples, we propose a mass-dependent size evolution model for passively evolving galaxies, where the most massive galaxies ($M_\star \sim 10^{11} M_\odot$) undergo the strongest evolution from $z \approx 2$ to the present. Parameterizing the size evolution as $(1+z)^{-\alpha}$, we find a tentative scaling of $\alpha \approx (-0.6 \pm 0.7) + (0.9 \pm 0.4) \log(M_\star/10^9 M_\odot)$, where the relatively large uncertainties reflect the poor sampling in stellar mass due to the low numbers of high-redshift systems. We discuss the implications of this result for the redshift evolution of the $M_\star - R_e$ relation for red galaxies.

Key words: galaxies: evolution – galaxies: fundamental parameters – galaxies: structure

Online-only material: color figures

1. INTRODUCTION

Understanding the red, passively evolving galaxies at intermediate redshifts ($z \approx 2$) is one of the outstanding challenges of galaxy evolution studies. Early expectations of a high-luminosity phase associated with the formation of spheroids on a free-fall timescale (Eggen et al. 1962) have long given way to a framework in which the spheroids are assembled over an extended period of time. The identification of fairly high

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space densities of massive and passively evolving galaxies at $z \gtrsim 1.5$ (e.g., Glazebrook et al. 2004; Cimatti et al. 2004) revealed weaknesses in the early semi-analytic models of their formation. Large-scale surveys, both locally and out to $z \sim 1$, provide a fairly clear view of the evolution in the number density of red sequence galaxies and the global stellar mass density in passive systems (e.g., Bell et al. 2006; Faber et al. 2007; Brown et al. 2003, 2007).

Deep spectroscopic studies of red galaxies (e.g., McCarthy et al. 2004; Cimatti et al. 2006, 2008) estimated stellar ages consistent with early formation redshifts ($z_{\text{form}} \gtrsim 4$), potentially at odds with the rapid evolution in stellar mass density at these epochs (e.g., Rudnick et al. 2003). It is now clear that the red
sequence was in place at fairly early epochs (Bell et al. 2004; Bremer et al. 2006; Kriek et al. 2008), but evolved strongly in the $1 \lesssim z \lesssim 3$ era (e.g., Demarco et al. 2010) and likely since $z \sim 1$ as well (e.g., Faber et al. 2007). The emerging picture in which massive galaxies are assembled via mergers followed by a rapid quenching of star formation addresses many of the salient properties of the red sequence galaxies (Faber et al. 2007).

In light of these results it was quite surprising that high spatial resolution studies showed that the passive red galaxies at intermediate redshifts are systematically smaller than their likely present-day counterparts (e.g., Daddi et al. 2005; Toft et al. 2007; Cimatti et al. 2008; Damjanov et al. 2009), while observations of red galaxies at $z \gtrsim 2$ suggest even more dramatic evolution (e.g., van Dokkum et al. 2008; Saracco et al. 2010).

The primary interest in determining the characteristic sizes of passive galaxies is the insight that it provides into the dynamical state of the system. As one projection of the fundamental plane (Djorgovski & Davis 1987; Dressler et al. 1987), the Kormendy relation (Kormendy 1977) provides a probe of the dynamics of hot stellar systems. The Kormendy diagram for the $z \gtrsim 1$ red sequence galaxies is nearly as tight as it is locally, but is offset in both surface brightness and size (e.g., Damjanov et al. 2009), even when the effects of passive fading of the stellar populations are taken into account. The compact sizes and high surface brightness of the red galaxies imply stellar densities in the centers of these galaxies that are two to three orders of magnitude higher than present-day massive red galaxies (e.g., van Dokkum et al. 2008; Damjanov et al. 2009).

The challenge in understanding these results stems from the apparent conflict between the requirement for a factor of $\sim 3$ growth in size during an epoch in which the stellar masses, population ages, and overall morphologies show little or no evolution. A number of models are under active discussion (e.g., Naab et al. 2006; Fan et al. 2008; Damjanov et al. 2009), but most involve large numbers of late-stage minor mergers that grow the galaxies in size without contributing large amounts of mass. While it is difficult to conclusively rule out various measurement biases which might give rise to this apparent trend (e.g., underestimated effective radii or overestimated masses), most interpretations are astrophysical in origin: major or minor merging occurring at different phases (e.g., Naab et al. 2006), or expansion due to a significant mass loss, either by an active galactic nucleus (Fan et al. 2008) or stellar winds (Damjanov et al. 2009). Recently, Hopkins et al. (2010) presented a semi-analytic model based on high-resolution hydrodynamic simulations (Cox et al. 2006), which incorporates several astrophysical and observational mechanisms for this trend, and concluded that for galaxies with a stellar mass of $M_\star \gtrsim 10^{11} M_\odot$, the late-stage minor merging is the dominant mechanism, accounting for $\sim 50\%$ of the apparent size evolution. Certainly many of these high-redshift systems do in fact show merger-like features (e.g., van Dokkum & Brammer 2010) or have (multiple) companions (e.g., Bell et al. 2006), and so merging is an attractive explanation for the observed size evolution.

The merging scenario implies that some non-negligible fraction ($\lesssim 10\%$; Hopkins et al. 2009) of compact galaxies should remain at $z \sim 0$. However, Trujillo et al. (2009) find that only $0.03\%$ ($\approx 48/152, 083$) of galaxies at $z \sim 0.2$ have stellar densities comparable to these high-redshift galaxies, arguing against the merger scenario. To further confound the issue, these galaxies are generally young ($\sim 3$ Gyr old), giving an approximate formation redshift of $z_{\text{form}} \sim 0.3$, suggesting that they are not the relics of the early universe, but formed from gas-rich, recently merged disks. Conversely, Saracco et al. (2010) find that $\sim 62\%$ ($\approx 21/34$) of their galaxies at $1 < z_{\text{spec}} < 2$ are within $1\sigma$ of the local $K - M_\star$ relation (Shen et al. 2003). Based on this finding, they suggest that the compact high-redshift galaxies are not the progenitors of large field galaxies, but of compact brightest cluster galaxies. The absence of compact early-type galaxies at $z \sim 0$ (e.g., Taylor et al. 2010) seems to suggest that the simple picture of galaxy merging with some mass-loss expansion is not completely correct, in stark contrast to the simulated results (e.g., Naab et al. 2009; Hopkins et al. 2010). In this paper, we present results from the Early Release Science (ERS) program with Wide-Field Camera 3 (WFC3) which suggest that the size evolution from $z \sim 2$ to the present depends on stellar mass. This finding should provide an additional observational constraint to further refine the theoretical models.

This paper is organized as follows. In Section 2, we describe the observations and ancillary data, in Section 3 we define our sample, in Section 4 we detail our stellar population modeling and morphological analysis, in Section 5 we describe our mass-dependent size evolution model, in Section 6 we discuss several key results, and in Section 7 we give a brief summary of this work with thoughts for future surveys. Throughout this paper, we assume a $\Lambda$CDM cosmology with $\Omega_0 = 0.27, \Omega_\Lambda = 0.73$, and $H_0 = 73 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Spergel et al. 2003) and will quote all magnitudes in the AB magnitude system (Oke & Gunn 1983).

2. OBSERVATIONS

2.1. The Wide-Field Camera 3 Early Release Science

For this work, we analyze the ERS (PropID: 11359, PI: R. W. O’Connell) observations conducted with the WFC3 recently installed on the HST. This field covers roughly the northern 40 arcmin$^2$ of the Great Observatories Origins Deep Survey southern field (GOODS-S; Giavalisco et al. 2004), and leverages the existing ACS optical data with near-ultraviolet (NUV) and near-infrared (NIR) data with equivalent space-based imaging. The main details regarding the data collection, reduction, calibration, and mosaicking are presented by Windhorst et al. (2011). We briefly summarize the observational aspects critical to this work.

The ERS program utilizes the two complementary modes of the WFC3: UVIS and IR channels. The data were collected between 2009 September and November and form a $2 \times 4$ and $2 \times 5$ mosaic, respectively. The final data set consists of $\sim 40$ arcmin$^2$ of 10-band HST imaging covering 2250 Å to 1.6 $\mu$m in wavelength. The v2.0 GOODS high-level science products had an original pixel scale of 30 mas and were 3 $\times$ 3 block summed to produce science and weight maps of equal pixel scale to the WFC3 observations (see Windhorst et al. 2011, for a more detailed discussion on the rebinning process and its motivation). Therefore, our final HST mosaics have 90 mas pixels. We refer hereafter to the 10-band WFC3 and ACS filter set in the F225W, F275W, F336W, F435W, F606W, F775W, F850LP, F980M, F125W, and F160W as $U_1U_2U_3BVizY_JH$ to simplify the bandpass notation.
2.2. Source Catalogs

We created source catalogs using SExtractor (Bertin & Arnouts 1996) with the \( H \)-band mosaic as the detection image and each of the \( HST \) mosaics as measurement images. We use the weight maps produced by MultiDrizzle (Koekemoer et al. 2002), modified to account for correlated pixel noise (Dickinson et al. 2004). For object detection, we require a minimum of 5 connected pixels each greater than 0.6\( \sigma \) above the local background and apply a 3 pixel Gaussian smoothing filter. For deblending, we adopt a contrast parameter of \( 10^{-4} \) with 64 sub-thresholds. For photometry, we adopt the MAG\_AUTO measurements with a Kron factor of 2.5, and minimum object radius of 3.5 pixels, which reliably recover total fluxes to within \( \sim 6\% \) (Bertin & Arnouts 1996). We use the AB zero points given by Kalirai et al. (2009a, 2009b) for the UVIS and IR data, respectively.

3. SAMPLE SELECTION

We select our passively evolving galaxies using a variation on the standard \( pBzK \) selection (Daddi et al. 2004), designed to identify galaxies at \( z \sim 2 \) with little ongoing star formation and stellar population ages of \( \sim 1 \) Gyr (Daddi et al. 2005). However, to take full advantage of our high spatial resolution and significantly deeper ERS data set, and avoid issues associated with cataloging images with markedly different angular resolution, we use our \( H \)-band imaging instead of the ground-based \( K \)-band images. Therefore, we modify the classical \( pBzK \) selection criteria to an equivalent \( pBzH \) scheme:

\[
(z' - H) - (B - z') < -0.2 - \langle (H - K) \rangle, \quad (1)
\]

\[
(z' - H) > 2.5 - \langle (H - K) \rangle, \quad (2)
\]

As these \( pBzK \) galaxies have maximally old, passively evolving systems, we derive a typical color of \( \langle (H - K) \rangle = 0.7 \) mag based on a stellar population with an instantaneous star formation history formed at \( z_{\text{form}} = 10 \) based on S. Charlot & G. Bruzual (2007, in preparation) and Bruzual (2007, hereafter CB07). In Figure 1, we show the \( (B - z′) \) and \( (z′ - H) \) colors with these criteria illustrated as a shaded polygon. To rule out any potential image artifacts associated with the ERS field edges, we require the object images to be in the portion of the \( H \)-band mosaic which received the full complement of two orbits per pointing. We restrict the \( H \)-band magnitude to a relatively conservative limit of \( H \leq 25 \) mag to ensure a complete and reliable sample (Windhorst et al. 2011). With these requirements, we identify a final sample of 30 galaxies in \( 43.1 \text{ arcmin}^2 \) and present their photometry (Table 1). Of these galaxies, 15 objects have very little (or no) flux in the \( B \) band. To highlight their red colors and visual morphologies, we show a \( 4.5 \), three-color stamp of each object in Figure 2.

We show the source counts of \( BzH \) galaxies in Figure 3. The counts plateau around \( H \simeq 22.5 \) mag, which is roughly 4 mag brighter than the \( H \)-band completeness limit (Windhorst et al. 2011). Furthermore, since the GOODS \( z' \)-band imaging is complete to \( z' \sim 27.3 \) mag (Dahlen et al. 2010) and our effective color limit is \( (z' - H) \gtrsim 1.8 \) mag, this plateau is unlikely due to incompleteness in the \( z' \)-band data, suggesting that the faint end of their luminosity function is relatively flat or declining at low luminosities. Stutz et al. (2008) note a similar dearth of low-mass systems (\( \lesssim 2 \times 10^{10} M_\odot \)), further supporting a flat or declining faint-end slope. At the bright end (\( H \lesssim 22 \) mag), our survey and modified \( pBzK \) selection method produces source counts consistent with Lane et al. (2007), based on the UKIRT Infrared Deep Sky Survey (UKIDSS) Ultra Deep Survey (UDS). While the UKIDSS/UDS survey is much wider (\( \sim 0.6 \) deg\(^2\)), the ERS data push \( \gtrsim 2 \) AB mag deeper into a regime not routinely possible from the ground.

4. ANALYSIS

4.1. Surface Brightness Models

To determine the rest-frame optical morphologies of our galaxies, we model the two-dimensional light distribution in the \( H \) band using GalFit (Peng et al. 2002). We determine an empirical point-spread function (PSF) from a median stack of 75 stars identified in the field, based on their full width at half-maximum (FWHM) and brightness determined by SExtractor (Windhorst et al. 2011). We fit the standard Sérsic profile:

\[
\Sigma(r) = \Sigma_e e^{-b_\gamma (r/r_e)^{\gamma - 1}}, \quad (3)
\]

where \( r_e \) is the effective radius,\(^23\) \( \Sigma_e \) is the surface brightness at the effective radius, \( n \) is the Sérsic index, and \( b_\gamma \) is a constant found by numerically solving \( \Gamma(2n) = 2\gamma(2n, b_\gamma) \) with \( \Gamma(x) \) and \( \gamma(x, y) \) representing the gamma and incomplete gamma functions, respectively. Since GalFit is minimizing a goodness-of-fit statistic, modeling the uncertainty in each pixel is critical for meaningful estimate of the uncertainty in each of the fit parameters. Therefore, we transform the scaled weight maps produced by MultiDrizzle into uncertainty maps and

\[^{23}\text{We refer to the effective radius as } r_e \text{ when in angular units and as } R_e \text{ when converted to physical units.}\]
explicitly include the shot noise from the objects. We perform all fits with GaIFit in units of counts using the H-band mosaic effective exposure time of 5017.7 s. We excise an 81 × 81 pixel² stamp centered on each galaxy; this size was chosen as a compromise between a sufficient number of sky pixels for a robust sky estimation by GaIFit, and the number of (generally unassociated) nearby galaxies. Neighboring galaxies can bias the parameter estimation of the primary galaxy, therefore one must carefully mask out the unmodeled objects, or simultaneously fit all the objects in the stamp. We opt for the latter, since it avoids the ambiguities in pixel masking, and permits the flux in a given pixel to be represented as the sum of independent components. However, without good initial conditions, the GaIFit algorithm may not converge to a meaningful solution, since the number of degrees of freedom can be very large. Therefore, to estimate better initial conditions for each galaxy in the stamp and ultimately ensure convergence in the final simultaneous solution, we fitted the two-dimensional light profiles of the primary BzH galaxy in question and any neighboring galaxies in a multi-stage process as follows.

1. We identify all neighboring galaxies and their associated pixels with SExtractor, using the same settings mentioned in Section 2.2. Any sources with FWHM_IMAGE_HI < 1 arcsec are eliminated from the SExtractor segmentation maps and object catalogs, since they are likely cosmic rays or other artifacts. These objects are masked in all subsequent fitting processes.

2. The pixels of any galaxy whose isophotes are truncated (based on the SExtractor flags) are masked, by setting the uncertainty maps to 10¹⁶ ADU. These galaxies are no longer considered in the GaIFit process.

3. We model the light distribution of each remaining galaxy (including the primary BzH galaxy) individually, while masking all the pixels associated with every other galaxy. For any neighboring galaxy with semi-minor axis of B_IMAGE_HI < 1 pixel from SExtractor, we switch from fitting a Sérsic profile to a PSF model, in order to eliminate degenerate degrees of freedom. Our results are robust to the choice of semi-minor axis limit, provided that we do not permit it to be larger than the size of the empirical PSF (discussed in more detail below). It is important to note that this step is only present to get reasonably accurate initial conditions for subsequent simultaneous object fitting.

4. We refit a GaIFit model, which contains a combination of point sources and Sérsic profiles, to the stamp as a whole using the results from the previous step as the initial guesses.

In a few cases, we manually masked diffraction spikes or stellar halos clearly associated with foreground stars, which were just
Figure 2. $BzH$ color images. Each stamp is $4.5'(\approx 38$ kpc at $z = 1.6)$ on a side, has north up and east left, and has a pixel scale of 0.090 pixel$^{-1}$. All images are shown with the same color and logarithmic intensity scale. We find the object just to the south of 2750 (and 2749) is just barely too blue to have been included in our sample, which is consistent with the suggestion that this object has recently ($\sim 150$ Myr) undergone an intense burst of star formation of $500-2000 M_{\odot}$ yr$^{-1}$ (van Dokkum & Brammer 2010; Ferreras et al. 2011).

outside the field of view of the stamp before proceeding through the above procedure.

For the individual and simultaneous fits, we placed constraints on various GalFit parameters to prevent the algorithm from diverging into an unphysical regime. We constrained the centroid of any component to be within the $\pm 2\sigma$ of the centroid determined by SExtractor, and the total magnitude to be $35 \leq H_{\text{tot}} \leq \text{MAG}_{\text{AUTO}}H - 2$ mag. In general, these constraints are so weak that they generally play no role in the fitting whatsoever, but they reduce the sensitivity to the pixel masking with the segmentation maps. We additionally constrain the Sérsic index and effective radius to be $0.01 \leq n \leq 8$ and $0.01 \leq r_e/A_{\text{IMAGE}} \leq 5$, respectively. These constraints are considerably stronger, and we recognize that the model is likely incorrect when GalFit converges to a solution which is on these boundaries. These cases are rare, and generally a sign that additional astrophysical components are needed (e.g., bulge/disk separately, nuclear point sources, or merger signatures), that the frame was inappropriately sized, that the object was unresolved, and/or that there was some additional light component or image defect present in the image (e.g., diffraction spikes, stellar halos, and/or cosmic rays).

As our primary interest here is on the sizes of these galaxies, it is imperative that we ensure the effective radii are robustly measured. While GalFit reliably determines the random uncertainty which follows from the maximum likelihood analysis, the total uncertainty should include a systematic term as well. To estimate the contribution from the systematic uncertainty, we construct a grid of simulated galaxies with brightnesses $20$ mag $\leq H \leq 25$ mag, effective radii $0.5$ pixel $\leq r_e \leq 5.5$ pixel, and a fixed Sérsic index of $n = 4$ (for simulation only). These galaxies are convolved with the PSF and embedded in a blank region of the $H$-band mosaic. We then fitted these simulated galaxies with GalFit using the above procedure and find that
GalFit typically overestimates the effective radii by $\sim 10\%$ and underestimates the uncertainties by $\sim 10\%$. Both the systematic bias and uncertainty are weakly brightness dependent, where fainter galaxies are more biased and uncertain. We remove the brightness-dependent bias and quadratically add the uncertainty to our effective radii measurements reported in Table 2.

Many of the these red galaxies are very small and, even with the space-based imaging, may still be unresolved. Therefore, it is critical to properly identify which galaxies are resolved and have reliable effective radii measurements. We begin by swapping the fully variable Sérsic model for the primary galaxy with a pure PSF model, which can only vary in position and brightness. However, as we have simultaneously fitted every object in our postage stamps, we anticipate that GalFit may incorrectly change the parameters of neighboring (unrelated) galaxies to compensate for the poor primary model, particularly in the case of a well-resolved primary galaxy. Therefore, when we use the PSF model for the primary galaxy, we hold the parameters of the neighboring sources fixed at the values found previously by GalFit. We now compare the goodness-of-fit statistics for these Sérsic and PSF models by considering the quantity:

$$F = \frac{\chi^2_{\text{PSF}} - \chi^2_{\text{Sérsic}}}{\chi^2_{\text{Sérsic}}}$$

and expect that sources with low values of $F$ are equally well characterized by a PSF model as by the more complex Sérsic profile. We calibrate this quantity by computing the $F$-values of the known ERS stars, which were used to derive the empirical PSF used above. In Figure 4, we show the $F$-values as a function of the GalFit-derived PSF magnitude, with the galaxies plotted as filled-blue points and the stars as red asterisks. The trend is as expected: nearly all point sources can be found at $-0.5 < F < 0$, while the $BzH$ galaxies are generally at $F < 0$ which depends on brightness. Therefore, we define objects which can be equally characterized by a PSF as by a Sérsic fit as having $F < F_{\text{crit}}$, while objects with $F > F_{\text{crit}}$ are more extended than the known ERS stars. We adopt $F_{\text{crit}} = 0.025$ and note that only 475 stars have $F > F_{\text{crit}}$, which is consistent with Bond et al. (2009). We give the GalFit results in Table 2.

### 4.2. Stellar Populations and Photometric Redshifts

We fit the matched-aperture HST photometry with a library of stellar population synthesis models to simultaneously determine the stellar mass, population age, and redshift with our own software. Our model grid consists of a four-dimensional parameter space spanned by redshift ($z$), stellar population age ($t$), $V$-band extinction ($A_V$), and star formation timescale ($\tau$) for an exponentially declining star formation history. We assume solar metallicity, a Salpeter initial mass function (IMF), and adopt the CB07 population synthesis models. The allowed photometric redshifts ranged from $0 \leq z < 7$ with $\Delta z = 0.01$, the ages presented by CB07, extinctions of $0 \leq A_V < 2$ mag with $\Delta A_V = 0.2$ mag, and star formation timescales of $\tau \in [10^{-3}, 1, 2, 3, 5, 15, 30, 10^3]$ Gyr. We include a 10% systematic uncertainty on the observed fluxes to account for uncertainties in the zero points and assumed templates. We compute the $\sigma$ uncertainties on the stellar population parameters (e.g., mass, age, etc.) by use of a simple Monte Carlo calculation. For each band for a given galaxy, we draw a normal random variable with mean and standard deviation equal to the flux and flux uncertainty (without the systematic term) and catalog the new population parameters. By repeating for $10^4$ iterations, we build

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24 We impose the usual self-consistency constraint that the a galaxy be younger than the age of the universe.
up a distribution of each stellar population parameter and take the mean and standard deviation as the measured quantity and uncertainties, respectively.

We apply this approach to the complete sample of 30 $BzH$ galaxies. In Figure 5, we show the photometric redshift distribution and the comparison to a spectroscopic redshift, when available. As expected, the median redshift of the sample is $z_{\text{phot}} = 1.6 \pm 0.6$ \cite{2009}, where the uncertainty reflects the standard deviation of the distribution. To estimate our typical redshift uncertainty, we compare to the published spectroscopic redshifts in the lower panel of Figure 5. Based on the root-mean-squared scatter of the seven objects with known spectroscopic redshifts, we estimate our uncertainties in $(1+z)$ are $\sim 3.3\%$. We do recover many of the known galaxy cluster members at $z \sim 1.6$ (Kurk et al. 2009). We present our resulting photometric redshifts and stellar population parameters in Table 3.

5. $BzH$ GALAXY SIZE EVOLUTION

Based on the photometric redshift estimates and the spectroscopic data (where available), the $BzH$ selection reliably identifies galaxies in the interval $z_{\text{phot}} \sim 1.6$. However, to study...
the evolution of their sizes with redshift, we must compare to 
other similarly selected samples. The high-redshift ($z \gtrsim 1.5$) samples are generally derived from similar color criteria pre-
icted here and have effective radii measured in the $H$ band, for 
a rest-frame wavelength of $\lambda_{rest} \approx 6500$ Å. To ensure fair com-
parisons with lower redshift samples, we require sizes measured 
at similar rest-frame wavelengths. For the low-redshift data, we 
use the sample of 8666 early-type galaxies at $z < 0.2$ with 
effective radii measured in the $i'$ band (Bernardi et al. 2003) 
selected from the Sloan Digital Sky Survey, Early Data Re-
lease (SDSS-EDR; York et al. 2000). The stellar masses for the 
7th Data Release 26 galaxies were determined following Salim 
et al. (2007). By cross matching these samples, we obtain 8595 
galaxies suitable for our low-redshift comparison. We select 
three mass ranges which are volume limited based on the upper 
and lower flux limits imposed by detector saturation in SDSS 
and the Bernardi et al. (2003) brightness criterion, respectiv-
ely. In Figure 6, we show these volume-limited selections (black 
boxes) and the flux limits (dashed lines). If these limits are not 
strictly imposed, then an artificial redshift dependence on the 
effective radii will be introduced as the radii are tightly correlated 
with the stellar masses, which roughly scale with luminosity. 
For example, without these volume limits, the effective radii of 
the SDSS galaxies will seem to increase with redshift since the 
survey is not sensitive to the lower mass (smaller) galaxies at 
the higher redshifts. Eliminating this critical Malmquist-like bias in 
the low-redshift sample ensures a fair comparison between the 
high- and low-redshift data.

To investigate the passively evolving galaxy size evolution 
at a fixed stellar mass, we show in Figure 7 the effective radii as 
a function of redshift for this work (filled circles) and a 
host of published measurements as described in the caption. 
We convert all mass estimates from the literature to the Salpeter 
IMF based on corrections discussed in the Appendix. For clari-
ty, we do not show three objects whose measured effective 
radii are $r_e \lesssim 0.5$ pixel as marked by the gray shaded 
region. While these objects are formally consistent with being 
extended, such small sizes are dubious and highly degenerate 
with the Sérsic index and local sky estimation. Furthermore, 
there are 11 objects from our sample which are either outside 
our mass range (10.3 $\leq $ log $(M_*/M_\odot) \leq $ 11.5) or have photometric 
redshifts at $z_{phot} \gtrsim 2.6$, as the spectral energy distribution 
fits are highly suspect. We overplot the power-law models of 
the form $R_e \propto (1 + z)^{-\alpha}$ (thick black line) where $\alpha$ is determined 
for each mass range separately and present the goodness-of-
fit statistic for the two models in the lower-left corner of each 
panel. We treat the canon of SDSS as a single low-redshift 
constraint, using their mean and error in the mean for the fits. 
For comparison, we show the mass-independent model (dashed 
blue line) in each panel, which was determined by fitting the 
data in all three panels simultaneously. We note that fits of the 
form $R_e \propto H(z)^{-\beta}$ (where $H(z)$ is the Hubble parameter 
give a similar qualitative result: the amount by which galaxies 
are smaller in the past depends on their stellar mass. Newman 
et al. (2010) identified a similar result for 12 galaxies with dy-
namical masses determined from measured velocity dispersions. 

Our preliminary estimate of a mass-dependent size evolution 
model is qualitatively similar to the predictions from the semi-
analytic models of Hopkins et al. (2009), where the power-
law index varies with mass as $\alpha(M_\ast) \approx 0.23 \log (M_\ast/10^9 M_\odot)$. 
However, their model underpredicts our measured power-law 

![Figure 6](http://www.mpa-garching.mpg.de/SDSS/DR7/)

#### Table 3

<table>
<thead>
<tr>
<th>ID</th>
<th>$z_{phot}$</th>
<th>$z_{spec}$</th>
<th>log Age$^a$ (log yr)</th>
<th>log Mass$^b$ ($M_\odot$)</th>
<th>$\chi^2_0$</th>
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<td>408</td>
<td>1.58 ± 0.05</td>
<td>...</td>
<td>8.7 ± 0.2</td>
<td>10.6 ± 0.1</td>
<td>0.9</td>
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<tr>
<td>606</td>
<td>1.89 ± 0.19</td>
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Notes.

$^a$ Population age assuming an exponential star formation history.

$^b$ Stellar mass.
indices in our three mass regimes, but does give the same qualitative steepening of $\alpha$ with mass. Following their approach, we derive tentative relationships for the power-law indices:

$$\alpha(M_*) \approx (-0.6 \pm 0.7) + (0.9 \pm 0.4) \times \log \left( \frac{M_*}{10^9 M_\odot} \right)$$

and caution that with only three independent mass bins, this scaling should be considered preliminary at best. However, this result gives indices consistent with the reported value of Buitrago et al. (2008), who find that $\alpha(M_*) > 10^{11} M_\odot \approx 1.5$. In Section 7, we discuss some potential shortcomings of the current data and propose experiments for future data sets.

6. DISCUSSION

It has become relatively well established that early-type galaxies are indeed smaller at high redshift than their local counterparts for a given stellar or dynamical mass (e.g., Trujillo et al. 2009; Newman et al. 2010). However, the causes for this result are far less clear, or agreed upon. The likely mechanisms can be broadly characterized as astrophysical effects (early-time major mergers, late-time minor mergers, adiabatic expansion, or stellar mass-to-light relations, or observational biases (underestimating the effective radius, overestimating the stellar mass, or incorrectly assuming that the high- and low-redshift populations are directly comparable). Using a semi-analytical model, Hopkins et al. (2010) find that the factor of $\sim 5$ increase in the effective radii over the last $\sim 10$ Gyr for galaxies with $M_* \gtrsim 10^{11} M_\odot$ can be explained by a combination of these effects, with the late-time minor merging playing the largest role. However, we find that lower mass systems exhibit notably weaker redshift evolution, suggesting a different mixture of the main processes may be at work. For example, the adiabatic expansion mode may become more critical given the shallower gravitational potentials in the low-mass systems.

As noted above, the tentative stellar mass-dependent size evolution presented in this work is similar to the findings of Newman et al. (2010) for dynamical masses estimated from velocity dispersions, and has an interesting consequence for the $R_e - M_*$ relation. Shen et al. (2003) find that SDSS elliptical galaxies follow the scaling relation $R_e = R_{e,11}(M_*/10^{11} M_\odot)^{\gamma}$, where $R_{e,11} = 4.16$ kpc and $\gamma = 0.56$. However, the mass-dependent size evolution found by us and by Newman et al. (2010) imply either a fundamental change in the $R_e - M_*$ scaling relationship at high redshift (such as a flattening of the effective radius for decreasing stellar mass) or a redshift-dependent value of $\gamma$, in addition to the usual lower value of $R_{e,11}$. Unfortunately, at this stage the high-redshift data cannot distinguish these two scenarios or shed light on the cause for this change. In fact, given the large scatter in $R_e - M_*$ at high redshift ($z \sim 1.5$), most of the size evolution is driven by the Bernardi et al. (2003) sample at $z < 0.2$.

The favored red galaxy formation paradigm suggests that passively evolving galaxies have come from a population of more active systems in their recent past. These systems originate from mergers of gas-rich disks that trigger intense starbursts which are later quenched by active galactic nuclei (AGNs), finally resulting in dead spheroidal systems spent of their gas and no longer forming stars (e.g., Faber et al. 2007, and references therein). The Lyman break galaxies (LBGs) observed at $z \gtrsim 3$ are a possible progenitor system (e.g., Overzier et al. 2010). While their stellar masses are far less well constrained due to the lack of rest-frame IR data, the majority of LBGs have $M_* \sim 10^{10} M_\odot$ between $3 \lesssim z \lesssim 6$ (e.g., Papovich et al. 2001; Yan et al. 2006). Therefore, the typical LBG at $3 \lesssim z \lesssim 6$ belongs to the lower panel of Figure 7 and has effective radii of $R_e \sim 1$ kpc (e.g., Ferguson et al. 2004; Bouwens et al. 2006; Hathi et al. 2008; Oesch et al. 2010), after transforming to an equivalent rest-frame wavelength (Barden et al. 2005). The LBGs are then consistent with our size evolution model, possibly suggesting that similar physical mechanisms driving the passive galaxy evolution may be at work for the LBGs as well. Given their increased star formation rates, larger gas content, and lower total mass, the mass-loss modes, whether driven by AGNs (e.g., Fan et al. 2008) or stellar winds (e.g., Damjanov et al. 2009), are potentially more important. However, we recognize that these samples (LBGs and passive galaxies) are quite different and that the next generation of space-based infrared instruments (Near-Infrared Camera and Mid-Infrared
Instrument on James Webb Space Telescope, JWST) will provide a much clearer picture for the high-redshift (z \gtrsim 3) size comparisons.

7. SUMMARY

We identified 30 passively evolving galaxies to H \leq 25 mag from a set of color criteria similar to the pBzK selection. We measure rest-frame optical (\lambda_{rest} \sim 6500 Å) effective radii as two-dimensional fits to the H-band image. By comparing with several other comparable samples at similar redshifts, we find that the size evolution depends on the stellar mass. We give tentative scalings between the power-law index of the R_e-z relation and stellar mass. While we have made every attempt at matching the selection biases between the high- and low-redshift samples, subtle differences may remain (such as the requirements on spectroscopic redshift and visual classification on the low-redshift data not matched at high redshift). Given the various requirements on placing SDSS fibers and the seeing-limited imaging, it is easy to believe that there may be systematic differences in the way the samples are created. Using future surveys with ultraviolet imaging with HST (such as planned observations with CANDELS and of the Hubble Ultra-Deep Field), we can extend the redshift range to 0.3 \lesssim z \lesssim 1.3 while consistently selecting galaxies of identical rest-frame spectral properties and removing any potential differences between the high- and low-redshift samples.

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Facilities: HST (WFC3, ACS)

### APPENDIX

#### STELLAR MASS CONVERTIONS

In most cases when authors determine stellar masses from population synthesis techniques, they adopt a single IMF and metallicity with the understanding that the stellar masses are dependent on these choices. Since there is no clear indication of which IMF may be appropriate, and modeling an arbitrary IMF and metallicity with broadband observations is prone to large degeneracies (Conroy et al. 2009), we are left to convert all stellar masses taken from the literature to a common set of assumptions. To derive these conversions, we refit our 30 objects with a different IMF and metallicity and compute

\[
\left( \log \frac{M_{\ast, i}}{M_{\ast, j}} \right) = C_{ij},
\]

where \(M_{\ast, i}\) and \(M_{\ast, j}\) are the resulting stellar masses for the different input models \(i\) and \(j\), respectively. We extend this analysis to include the Bruzual & Charlot (2003, BC03) models, which did not include flux contributions for thermally pulsating asymptotic giant branch stars. In Table 4, we tabulate the \(C\) matrix to convert the mass estimates obtained from the literature (as discussed in Section 5), where a model is encoded by three characters: the first indicates the vintage (3 = BC03 and 7 = CB07), the second indicates the metallicity (5 = 0.4 Z_☉, 6 = 1.0 Z_☉, and 7 = 2.5 Z_☉), and the third indicates the IMF (S = Salpeter or C = Chabrier).

### REFERENCES


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