Tracking the momentum flux of a CME and quantifying its influence on geomagnetically induced currents at Earth

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[1] We investigate a coronal mass ejection (CME) propagating toward Earth on 29 March 2011. This event is specifically chosen for its predominately northward directed magnetic field, so that the influence from the momentum flux onto Earth can be isolated. We focus our study on understanding how a small Earth-directed segment propagates. Mass images are created from the white-light cameras onboard STEREO which are also converted into mass height-time maps (mass J-maps). The mass tracks on these J-maps correspond to the sheath region between the CME and its associated shock front as detected by in situ measurements at L1. A time series of mass measurements from the STEREO COR-2A instrument is made along the Earth propagation direction. Qualitatively, this mass time series shows a remarkable resemblance to the L1 in situ density series. The in situ measurements are used as inputs into a three-dimensional (3-D) magnetospheric space weather simulation from the Community Coordinated Modeling Center. These simulations display a sudden compression of the magnetosphere from the large momentum flux at the leading edge of the CME, and predictions are made for the time derivative of the magnetic field (dB/dt) on the ground. The predicted dB/dt values were then compared with the observations from specific equatorially located ground stations and showed notable similarity. This study of the momentum of a CME from the Sun down to its influence on magnetic ground stations on Earth is presented as a preliminary proof of concept, such that future attempts may try to use remote sensing to create density and velocity time series as inputs to magnetospheric simulations.


1. Introduction

[2] The influence of a southward oriented magnetic field of the solar wind impinging onto the Earth’s magnetosphere is known to be the main driver for coupling the solar wind to the terrestrial system [e.g., Gonzalez and Mozer, 1974; Bargatze et al., 1985; Tsurutani et al., 1992a]. In this case, the oppositely oriented magnetic fields between the solar wind and the magnetosphere are more easily able to reconnect and thereby transfer energy, mass, and momentum to the Earth. For this reason, significant emphasis on understanding and predicting the magnetic field orientation has been pursued to improve our space weather predictive capabilities.

[3] The role of the solar wind density, \( N_{sw} \), in space weather studies is more complex. Statistical studies aimed at coupling the solar wind density to geomagnetic indices such as \( Dst \) show a weak correlation [O’Brien and McPherron, 2000]. Others suggest that \( N_{sw} \) should be significant in mediating the energy transferred to the magnetosphere [Borovsky et al., 1998; Thomsen et al., 1998]. The density has been demonstrated to affect the magnetospheric response by way of the solar wind dynamic pressure (momentum flux) [e.g., Xie et al., 2008]. A sharp
increase in solar wind dynamic pressure can rapidly compress the Earth’s magnetopause causing a large time rate of change in the local ground-based magnetic field intensity. While this effect is not often considered as a measure of “geo-effective” events, the space weather consequences can be severe. An example of this can be found in the 4 August 1972 event, where the peak Dst index was moderate compared to the resulting outage of the AT&T telecommunications cable and the geosynchronous satellite solar cell damage [Anderson et al., 1974; Lanzerotti, 1992; Tsurutani et al., 1992b].

[4] When investigating the drivers of space weather at Earth and in particular geomagnetically induced currents (GICs), it is important to distinguish between the different solar wind structures that initiate the chain of events that may lead to significant socioeconomic losses. Different interplanetary structures have been previously reported to produce significantly varying responses in the Earth magnetosphere [e.g., Huttunen et al., 2008; Miyoshi and Kataoka, 2005; Borovsky and Denton, 2006; Denton et al., 2006; Lavraud and Borovsky, 2008], and it is therefore reasonable to expect different responses for GICs. The two main drivers of GICs are from intense magnetic storms associated with interplanetary coronal mass ejections (CMEs) and co-rotating interaction regions (CIRs). Kataoka and Pulkkinen [2008] and Borovsky and Denton [2006] both found that the biggest problems for ground-based conducting systems were from CME drivers, whereas CIR-driven storms had a relatively minor effect.

[5] Fast-moving interplanetary CMEs can be considered to be made of two primary constituents: (i) the sheath region between the shock front and the leading edge of the CME and (ii) the ejecta itself. The ejecta is often magnetically dominated (i.e., plasma $\beta < 1$) and displays the magnetic properties of a flux rope (FR) when seen in situ [Burlaga, 1988]. The sheath region however contains denser compressed plasma with a higher value of plasma $\beta$. The direction of the magnetic fields within this region is variable, but is often found to vary within a 2-D plane [Nakagawa et al., 1989; Jones et al., 2002; Kataoka et al., 2005; Savani et al., 2011]. The momentum flux, $P_{\text{dyn}} = N_{sw}V^2$ within the sheath is typically high. Huttunen et al. [2008] concluded that as a geo-effective CME propagates over the Earth (usually for a period of ~24 hours), the most intense GIC activity recorded on the ground is most likely to occur at the beginning, during the passage of the sheath region, and between the shock and the leading edge of the magnetic obstacle.

[6] A high solar wind density can cause a change in the compression ratio of the bow shock, as is frequent within a geomagnetic storm [Lopez et al., 2004]. For southward magnetic field, this serves to increase the sensitivity of the predicted effects to $N_{sw}$ [see also Lavraud and Borovsky, 2008]. Recent studies have considered the effect of preconditioning the magnetosphere to increase the space weather effects. For geomagnetic storms driven by both CMEs and CIRs, Lavraud et al. [2006] showed that the Dst were underpredicted by a model for intervals that were preceded by an extended period of northward IMF. This is consistent with the hypothesis that a preconditioned high density plasma sheet will cause a larger than expected geomagnetic storm, as also expected from simulations [Lavraud and Jordanova, 2007]. The density of the Earth’s plasma sheet is regulated by the solar wind density and lags behind by a few hours [Borovsky et al., 1998]. For CME-driven storms, the plasma sheet is generally more dense and persists longer than those driven by CIRs [Denton et al., 2006]. A magnetohydrodynamic (MHD) simulation studied by Siscoe et al. [2002] found that the polar cap potential saturation follows a power law with $P_{\text{dyn}}$. This then led Xie et al. [2008] to develop a model where the magnetosphere can be preconditioned by $P_{\text{dyn}}$.

[7] The Dst index is often used as a measure of the severity of a geomagnetic storm. This index is an average estimate of the global response as determined by four equatorially located ground stations. The Dst measures the horizontal component of Earth’s ground magnetic field and is predominately monitoring the strength of the ring current in the magnetosphere [Fukushima and Kamide, 1973; Liemohn et al., 2001]. Since a denser and cooler plasma sheet produces a stronger ring current, CME-driven storms often produce more intense Dst values. Also, low latitude ($< 56^\circ$) aurora, as measured in Japan was found to be predominately CME associated [Shiokawa et al., 2005]. During a CME-triggered geomagnetic storm, the Dst profile often begins with a short duration rise which is triggered by the arrival of the CME shock front (sudden storm commencement, SSC). The duration of the rise phase between the SSC and storm onset (SO) often corresponds to the sheath region upstream of the magnetic ejecta of the CME. The main phase of the geomagnetic storm, which corresponds to the magnetic ejecta traversing over the magnetosphere, is where a large decrease in the Dst value occurs. However, the phases of a geomagnetic storm can be time shifted under conditions where a strong southward Bz persists within the sheath region. The amplitude of the Dst decrease during the main phase is closely related to the southward magnetic field in the IMF and its subsequent magnetic reconnection with the magnetosphere.

[8] The momentum flux of a CME, and in particular the sheath region, is higher than that of the ambient solar wind. This introduces a changing pressure onto the magnetosphere, and in the case of a CME-driven shock front, the change is abrupt. The subsequent compression of the magnetosphere is expected to generate currents within the terrestrial system which are then detected on the ground as magnetic field fluctuations. As displayed by a Dst time profile during a geomagnetic storm, the geomagnetic field undergoes fast changes over a short time period. The largest time derivative of the ground magnetic field, $db/dt$, occurs during the initial phase (between SSC and SO) or during substorms. As indicated by Faraday’s law of induction, $db/dt$ is key in estimating the geomagnetically induced currents in technological conductor systems like power grids [Pulkkinen et al., 2006; Committee On
The Societal and Economic Impacts Of Severe Space Weather Events, 2008). Therefore, dB/dt is often considered as a reasonable proxy for localized GIC activity [Viljanen et al., 2001]. In order to calculate the geo-electric field, additional information on the ground conductivity and specifics on the technological systems involved are required [Pirjola, 2002; Pulkkinen et al., 2007]. In this paper, we will focus on tracking the effects of CME momentum flux to the proxy of GICs, namely dB/dt.

[9] Significant geomagnetically induced currents have been observed to affect technological systems in middle- and low-latitude regions [e.g., Ngwira et al., 2008; Liu et al., 2009; Watari et al., 2009], and therefore, it is becoming increasingly clear that these geoelectrically driven GICs are not just a high-latitude phenomenon [Pulkkinen et al., 2010a]. The extent to which GICs can be expressed by dB/dt is also not as straightforward as first expected due to the complications of estimating the ground conductivity and how this varies at different depths. Pulkkinen et al. [2010a] showed that in Japan where the tectonic plates are geologically active, the local subduction zone is able to affect GICs in an unusual way by following the amplitude of the local geomagnetic field rather than the time derivative; this highlights the complexity of predicting GICs.

[10] In this paper, we focus on better characterizing the N_{\text{geo}} from remote observations as a solar wind driver for dB/dt of the geomagnetic field. We take steps toward creating a time series of the solar wind density and show that the momentum flux of a CME is an important parameter when predicting space weather incidents. We show this by comparing the ground station data with predicted estimates from the space weather modeling framework (SWMF) [Tóth et al., 2005].

2. Remote-Sensing Observations

[11] The STEREO mission, launched in 2006 [Kaiser et al., 2008], consists of two spacecraft that follow a trajectory similar to that of the Earth. As they separate from each other at a rate of \( \approx 45^\circ \) per year, one spacecraft travels ahead of the Earth (ST-A) while the other lags behind (ST-B). Each spacecraft carries the Sun Earth Connection Coronal and Heliospheric Investigation [Howard et al., 2008] imaging package, which contains an Extreme Ultraviolet Imager, two coronagraphs (COR-1 and COR-2), and the Heliospheric Imager (HI). The HI instrument on each STEREO spacecraft is made up of two wide-field visible-light imagers, HI-1 and HI-2 [Eyles et al., 2009]. The fields of view of HI-1 and HI-2 are of 20° and 70° angular extent, respectively, and under ordinary operation are nominally centered at 13.7° and 53.4° elongation in the ecliptic plane. Thus, the ecliptic plane corresponds to a horizontal line that runs through the center of the fields of view. Figure 1 displays the location of the STEREO spacecraft in relation to the Sun and Earth on 27 March 2011. The shaded regions indicate the field of view for the HI-1 cameras on both spacecraft. The direction of propagation for the CME nose is estimated from Jmap techniques [e.g., Sheeley et al., 1999; Rouillard et al., 2008; Davies et al., 2009; Savani et al., 2009, 2012a] and detailed below in section 2.3.

2.1. CME Mass Calculation

[12] In order to convert the white-light images that contain photometric information per pixel into mass per pixel, we exploit the Thomson scattering properties of electrons from the corona and inner heliosphere. The total light observed by the coronagraphic and heliospheric imagers onboard STEREO is from photospheric photons scattered by all the electrons along the entire line of sight (LOS). The difference in contributions of each electron along the LOS depends on the distance and the Thomson scattering mechanism [Billings, 1966; Vourlidas and Howard, 2006]; therefore, an estimate of the total number can be generated from white-light images [Hayes et al., 2001]. In order to estimate the mass of a CME, the brightness contribution of the transient must be isolated from the background coronal signal. Previous studies have achieved this by subtracting a suitably chosen pre-event image from an image containing the CME [Stewart et al., 1974; Howard et al., 1985; Poland et al., 1981]. A comprehensive explanation of the procedures required to make estimates of a CME mass from the raw telemetry data received on the ground is given by Vourlidas et al. [2010]. However for completeness, the main key points in the procedure are given below:

[13] 1. First, the relevant time stamps for images containing the CME are chosen as well as a pre-event image. The pre-event image is ideally the last possible image prior to the CME entering the field of view in order to make the appropriate corrections for background. It is important to minimize the effects from evolutionary changes and solar rotation, and not to include another CME or other transient effects in the pre-event.
2. The pre-event image is subtracted from the sequence of CME event images. These calibrated images now display information on the excess (depletion) of light in units of mean solar brightness, MSB (i.e., a base-difference sequence).

3. The excess (depletion) of MSB within each pixel in the image is converted into a number of electrons by using the Thomson scattering equations and by assuming all the electrons are located on a single plane determined by the fixed-phi J-map technique.

4. The mass per pixel is calculated from each image by assuming a solar wind distribution of 90% H and 10% He. This corresponds to a mass of $1.97 \times 10^{-24}$ g per electron [Hildner et al., 1975].

5. The mass of the CME is then estimated by summing up the values of all the pixels containing the CME.

Figure 2 is a combined and cropped image from the ST-A and includes a frame from COR-2, HI-1, and HI-2. Practically speaking, the pre-event image is usually subtracted from the frames which occur later in time (i.e., when the CME has entered the field of view). However, this frame may also be subtracted from images that occurred earlier. In Figure 2, the image from the HI-2A camera is one that is actually earlier in time than the pre-event image. Therefore, we are demonstrating the feasibility of using the pre-event image as a static background for frames earlier and later in time.

2.2. Semi-automated CME Mass

1. The sector method [Vourlidas et al., 2010]. The observer manually defines a set of four boundaries that can be used for the entire sequence of images. These boundaries are defined between two position angles (PAs) and the inner and outer radial boundary.

2. Region of interest (ROI) method [Vourlidas et al., 2000; Subramanian and Vourlidas, 2007]. The observer manually draws an outline of the CME. All the pixels within this ROI are considered to contribute toward the CME mass. This method calculates the total mass more accurately than the sector method but requires each frame to be considered individually and is therefore more time consuming.

3. Graduated cylindrical shell model (GCS) method. This method uses the forward modeling technique developed by Thernisien et al. [2009] and Thernisien [2011].
to define the outer boundary of the CME. The different parameters in the model apart from the radial distance are manually chosen from comparing the model shape with both STEREO COR-2 images simultaneously. These parameters are then fixed and the radial distance is varied over the sequence of images as the CME propagates. The outer edge which is traced out by the model is used in the same manner as the ROI method defined above. This new GCS method is used in our paper.

[25] The CME enters the COR-2A camera at 21.24 UT, on 24 March 2011, and approaches a mass of \( \sim 3 \times 10^{12} \) kilograms, which is of the order of magnitude of a typical CME [Vourlidas et al., 2010]. The mass estimates as measured from the GCS model are displayed in Figure 3 and show the typical increasing mass time profile due to the CME entering the field of view. This method enables the CME mass calculations to be made in a semi-automated fashion similar to the sector method, while using a more reliable ROI method for tracing the CME contour. In our example, the mass of the CME was slightly overestimated by \( \lesssim 5\% \) compared to using method 2. This is because we ensured that the entire CME structure was enclosed. For our event, which may not always be the case, it was relatively simple as the CME had well-defined boundaries. However, as the CME propagated, the leading edge became slightly flattened in comparison to the idealized GCS model. This meant the nose of the GCS was progressively further into the heliosphere than the observations. This meant a few extra pixels of mass were included but less than would have been encountered by method 1. It was found that the accuracy of the mass measurements compared to method 2 depended on ensuring that at least the entire area of the CME was included rather than minimizing the surplus area of background solar wind.

[26] The GCS method used in this paper requires several parameters to be defined for each image. The results of propagation direction and flux rope axis were compared to the fixed-phi method (from remote observations) and constant-alpha force-free flux rope model (from in situ data; see section 3.1 for more details), respectively. The results were consistent with each other. The independently estimated propagation directions were within 10° of each other and the three independently estimated flux rope axes were within 30°.

[27] Another option for measuring the mass flow is to investigate a fixed location in the heliosphere by defining a small narrow rectangular box a few pixels wide (slit method). This method emulates a time series of mass over a fixed location such as a spacecraft at a few pixels wide (slit method). This method emulates a time series of mass over a fixed location such as a spacecraft at the L1 position (see section 2.4). Currently, the minimal image processing used in this study does not allow for an accurate estimate to be made at L1. However, future studies using more advanced image processing and better tempo-spatial resolution as expected from the Solar Orbiter should provide the necessary data to advance the techniques in preparation for a possible mission to L5.

2.3. Mass J-Maps

[28] Originally developed for LASCO coronagraphic images, Sheeley et al. [1999] calculated that a small plasma packet moving at uniform speed would have an apparent acceleration and deceleration which is dependant on two variables: the radial velocity, \( V_r \), and the angle of propagation between the CME-Sun-spacecraft, \( \beta \). Moreover, the observed acceleration profile (measured in time and elongation angle away from the Sun, \( \alpha \)) is unique; therefore by using an optimization routine [e.g., Savani et al., 2009, 2010], an estimate of the propagation direction of the CME can be made. This technique (called fixed-phi method) has been shown to be much more useful over a large range of elongation angles [Williams et al., 2009; Davis et al., 2010] and produced very effective results in tracking CMEs from the Sun to planetary systems where they were detected in situ [e.g., Davis et al., 2009; Rouillard et al., 2009; Möstl et al., 2009]. As the premise on which this technique is built relies on the idea of a spatially narrow plasma packet and not a large three-dimensional (3-D) object traveling through the heliosphere, other attempts have been developed to mitigate against some of the simplified assumptions [Kahler and Webb, 2007; Lugaz et al., 2009; Davies et al., 2012].

[29] The propagation direction is estimated by measuring the elongation angle as a function of time. This is most conveniently done by tracking a single feature within a CME through the field of view of all the cameras by using a time-elongation map (J-map). As a plasma packet can be assumed to propagate radially away from the Sun, the radial cuts used in J-maps can be varied to suite the CME direction if it is away from the ecliptic.
plane. In the case of our event, we choose a PA of 97° from ST-A, which corresponds to the direction to Earth. Until this paper, these J-maps have been created by processing MSB images into a running difference sequence, as shown in the top panel of Figure 4. The blue crosses are manually chosen from the image and are the points used in estimating the speed and propagation direction of the CME. Using the fixed-phi method, the radial speed and propagation direction were estimated as 371 kilometers per second and 80°, respectively. The bottom panel displays the same time-elongation tracks but created with a sequence of mass images. As can be seen between the two versions, the white-light J-map is clearer at identifying the propagation of the CME. This is partly because further smoothing and image processing were undertaken on the white-light J-map. It is hoped that further studies into mass J-maps will be used to provide a time series estimate of the mass propagating over the Earth in a process similar to the slit method described above. This is because the slit method would effectively represent a horizontal line along a mass J-map. Although the tracks in the mass J-map displayed in our paper are “noisy,” future studies may implement advanced image processing techniques that are currently under development [e.g., Howard et al., 2012] to find interesting discoveries.

The tracking of the mass estimates can be used with a minimal number of assumptions about the expansion process to estimate the density of the CME. With improvements to the image processing, this information may be used as inputs to space weather forecasting models, instead of using L1 in situ data. Although this will clearly be less reliable than L1 data itself, it has the big advantage of being measured remotely and of the order of ~48 hours in advance. This may prove to be a significant improvement for our forecasting capabilities.

Figure 5 displays the mass J-map along with the in situ measurements of density and velocity at L1. The track, which was made from the white-light J-map, is overplotted onto the mass J-map along with a dashed line to show the position of Earth. The track clearly intercepts the position of Earth at the same time as the CME-driven shock (and the associated density increase from the sheath) arrives at L1. The shock arrival at L1 displays a sudden increase in momentum flux which then compresses the Earth’s magnetosphere (see section 4).

2.4. Mass Time Series

Under the premise that the CME momentum can be tracked and possibly be used as early solar wind input into space weather simulations, it is important to observe how a typical mass time series may look like and how it compares to the in situ density profile currently being used as simulation inputs. Figure 5 shows a normalized times series of the mass measurements (green dashed curve) taken at 3.8° elongation from ST-A, which is within the COR-2 field of view. The mass measurements were taken using the slit method at a plane of sky distance between 13.7 and 14 Rs for each frame. The data were then ballistically time shifted to the L1 position by assuming the CME traveled at 370 kilometers per second and was
Figure 5. (top) The time series of the WIND proton density and velocity for the period 25 March to 01 April 2011. A normalized mass time series from the mass images are overlaid onto the density axis (green). The mass time series is generated from the slit analysis at 3.8° elongation within the COR-2A camera. The time series is ballistically propagated to L1 at a speed of 400 kilometers per second at the leading edge and 370 kilometers per second at the trailing edge, with a linearly decreasing speed profile. Qualitatively, the normalized mass time series shows a remarkable resemblance to the in situ density of the CME sheath. (bottom) The mass J-map with the manually selected CME leading edge.

linearly expanding [Owens et al., 2005] so that the trailing edge of the mass measurements propagated 30 kilometers per second slower than the sheath leading edge (see also Figures 6 and 7). As our event initially propagates with a slow speed, we are able to assume the CME was swept into the solar wind and merely advected out to 1 AU [Siscoe and Schwenn, 2006]. However for faster CMEs, it is important to consider deceleration due to drag effects that change the arrival times at Earth [Gopalswamy et al., 2000; Cargill, 2004]. The units of mass displayed have been normalized to suit the density profile. This has simply been carried out by dividing the measurements by $1.5 \times 10^{11}$ grams per cubic centimeter. A simple method of an expanding volume during the CME’s propagation is used to justify this value (see Appendix A for more details).

Currently only minimally processed images are being used and even with our simplified propagation technique [e.g., Owens and Cargill, 2004; Lugaz and Kintner, 2012], and the qualitative profile of the mass measurements made from remote observations is remarkably similar to that observed in situ. It is clear that CMEs may undergo interactions during propagation to Earth by either solar wind distortions [e.g., Lugaz et al., 2008; Savani et al., 2010], deflections [Lugaz et al., 2012; Wood et al., 2012], or possible rotations [e.g., Shiota et al., 2005; Vourlidas et al., 2011; Nieves-Chinchilla et al., 2012]. This could be the cause of the larger predicted mass measurements within the CME when compared to the in situ values. Or more simply that the CME expanded more during the propagation and is more rarified by the time it reaches Earth.

3. In Situ Observations

The shock associated with our case study event was detected at L1 at 15.09 on 29 March 2011 with a jump in velocity of ~70 kilometers per second (the upstream speed was ~330 kilometers per second). Figure 6 shows the in situ parameters of the solar wind during the propagating interplanetary CME. The three vertical lines indicate the locations of the shock front (14.58 on 29), CME leading edge (23.39 on 29), and rear edge (09.52 on 31), respectively. The CME leading and rear edges were manually chosen by focusing on looking for a duration that includes a smooth field rotation and a discontinuity on density. The focus on the smooth field rotation is in order to produce reliable results from an in situ flux-rope fitting process. The magnetic field vectors are displayed in the RTN coordinate system such that the Normal (N) component is the measure of the magnetic field in the out-of-ecliptic direction (i.e., the north-south direction that is crucial in space weather predictions). This case study shows that the magnetic field in the CME and sheath region is predominately northwardly directed and strongly so in the earliest half of the CME just behind the leading edge. This
CME topology was specially chosen for our analysis as it allows our study to isolate the space weather effects (e.g., potential strength of GICs) that are caused by the momentum flux and not from the resulting magnetic reconnection from a southwardly directed interplanetary magnetic field (IMF).

3.1. Modeling Results for March 2011

[35] Figure 6 displays the magnetic field profile of the optimized CAFF model (see Appendix B for details) within the first to sixth panels as black curves. The first to third panels represent the Cartesian vectors in the RTN coordinate system and the fourth to sixth panels represent the field vectors in the spherical coordinate system. The smooth rotation in the field is often more clearly seen in spherical coordinates while the importance of a southward Bz for predicting space weather events is better observed in the Cartesian coordinates. The orientation of the estimated flux rope axis direction is \((0.4, -0.7, 0.6)\) in RTN and has a right-handed chirality. The optimized parameters for the axial magnetic field and the impact parameter are 14.0 nanotesla and 0.1, respectively. This indicates the spacecraft travel close to but slightly above the FR axis. The mean square error between the optimized model and the data, \(\chi^2\), was <0.1, which represents a good fit to the data [Lynch et al., 2003]. The model fits were also compared to a non-force-free elliptical model [Hidalgo and Nieves-Chinchilla, 2012] to show consistent results (e.g., the axis orientation were within 30° of each other).

3.2. Dst Index

[36] There is a variety of ground responses at Earth from space weather disturbances, and measurements are often focused on different geographically localized processes/positions (e.g., due to local noon time, latitude, or ground resistivity). The disturbance time (Dst) index measures the hourly values of the horizontal component of the Earth’s magnetic field averaged from four near-equatorial
geomagnetic observatories. The $Dst$ index has historically been used as an approximation of the global response to a space weather disturbance. The fluctuations in the $Dst$ closely relate to the ring current and the other current systems (including the magnetotail current) within the terrestrial environment. The inverse proportionality relationship between the horizontal component of the magnetic field and the energy content of the ring current is known as the Dessler-Parker-Sckopke relation [Dessler and Parker, 1959; Sckopke, 1966].

[37] The stereotypical time profile of the $Dst$ index during a geomagnetic storm driven by a fast CME displays an initial positive sharp rise (called the sudden storm commencement, SSC) which defines the arrival of the leading shock front onto the magnetosphere, a drop in value to zero (called the storm onset, SO), and then the main phase is characterized by a large negative decrease which represents the period of strong southward Bz magnetic field. The sheath region between the leading edge of a CME and the shock front is often considered to be related to the period between the SSC and the SO (initial phase) during a geomagnetic storm. However, the phases of a geomagnetic storm can be time shifted under conditions where a strong southward Bz persists within the sheath region.

[38] The case study CME analyzed in this paper was chosen to better understand the significance of its momentum flux as a driver of geomagnetic storms. As such, we chose to investigate a CME with a predominately northward Bz field. This allowed us to isolate the observed geomagnetic disturbance and assume the disturbance is solely due to the momentum flux and not due to reconnection between the CME and magnetosphere. For this reason, the usual main phase of a storm as seen in the $Dst$ is not seen in our event (Figure 7). However, Figure 7 shows a significant rise in the $Dst$ value and sharp fall during the initial phase, which represents the location of a sudden increase in momentum flux from the CME sheath region. The sudden changes in the $Dst$ show that the momentum flux of the CME leading edge is capable of making sudden changes to the ground magnetic field (i.e., cause a large $dB/dt$).

4. Terrestrial Response

[39] Sophisticated MHD simulations in 3-D are becoming an increasingly effective tool for modeling solar wind transients such as CMEs and for predicting their geoeffectiveness at Earth. In this paper, we have employed the Space Weather Modeling Framework (SWMF) [Tóth et al., 2005] package which was executed at the Community Coordinated Modeling Center (CCMC) and operated at NASA Goddard Space Flight Center. The solar wind input data were chosen from the WIND spacecraft at L1 and was ballistically mapped to the outer boundary of the BATS-R-US magnetospheric MHD model that was coupled to the Rice Convection Model in our simulations. The auroral conductances are driven by solar irradiance observations of Fi0.7 and field-aligned electric currents.

[40] Figure 8 displays a 2-D cut of Earth’s magnetosphere (top) before the arrival of the CME-associated shock front and (bottom) when the sheath region of the CME is traveling over Earth’s bow shock. The color table represents the density of the plasma and a few selected magnetic field lines are drawn to help distinguish between the terrestrial and heliospheric systems. The vectors show the solar wind direction. In the 3 hours between the frames shown in Figure 8, the bow shock is severely compressed from a location of approximately 16 Rs to ~10 Rs. This compression significantly increased the density within the magnetosheath and was due to the sudden arrival of a larger momentum flux from within the sheath region of the CME.

[41] Currently, this study uses the in situ data measured at L1 as the inputs into the SWMF simulations in order to predict realistic geomagnetic disturbances. However, it is envisaged that with further development to the mass images, a reasonable density time series calculated remotely may be used as an input into the BATS-R-US code (see section 2.4). This may prove to be a valuable tool in improving any early warning systems by being able to provide an observationally predicted result that is at least ~24 hours earlier than is currently possible.

4.1. Observations of Magnetic Fluctuations

[42] In order to better understand the geomagnetic effects driven by CMEs and in particular to predict the socioeconomic impacts from GICs, it is important to study the localized effects observed at specific locations on Earth during the arrival of the CME. In this paper, we study the momentum flux of CMEs and therefore choose to investigate the equatorially based ground stations. The higher latitude stations are likely to display magnetic field fluctuations that can be partly associated with auroral...
Figure 8. Two-dimensional cut of the Earth’s magnetosphere and bow shock from the BATS-R-US simulation at CCMC. The color scale of the density is the same in both panels. (top) The shape and structure of the magnetosphere prior to the arrival of the CME shock. (bottom) The compressed magnetosphere at the time when the CME sheath is affecting the bow shock.

magnetosphere-ionosphere dynamics, and are therefore not the focus of this paper. The shock arrival at L1 (~15.00 UT) defines the start of the geomagnetic disturbance. We investigate two locations on Earth that are determined to be locally noon and midnight at the shock arrival. The Vassouras (VSS) station in Brazil is used as the locally noon station. The Kanoya (KNY) and Kakadu (KDU) stations in Japan and Australia, respectively, are studied as the locally midnight stations for our investigation.

In order to investigate the possible effects that a CME may have on GICs, the time derivative of the ground magnetic field (dB/dt) must be studied. Figure 9 displays the dB/dt at both local times and shows significant fluctuations at the arrival of the shock onto Earth’s system. The vertical dashed line displays the time the shock arrived at L1 and therefore the delay of ~1 hour on the ground stations predominately represents the propagation time of the solar wind between L1 and the bow shock. The data are displayed with 1 minute temporal resolution in the Cartesian geographic (GEO) coordinate system provided by INTERMAGNET (www.intermagnet.org).

4.2. Simulated dB/dt

Quantifying and predicting ground magnetic field perturbations are vital to the space weather community. As such, the CCMC has developed a tool that is able to extract the ground magnetic field perturbations from the global MHD model outputs by integrating the results from the magnetospheric and ionospheric current systems. In particular, a summation of four separate current systems is used to make the predictions: (1) the current system in the magnetosphere (and magnetotail) above 2.5 Re, (2) field-aligned currents between 2.5 Re and 110 kilometers, (3) Hall current from the ionosphere, and (4) Pederson currents in the ionosphere [Rastatter et al., 2004; Pulkkinen et al., 2010b]. The performance and metric-based analyses between various modeling approaches were part of the Geospace Environment Modeling (GEM) 2008–2009 challenge and is reported by Pulkkinen et al. [2011].

Figure 9 shows the predicted estimates of the ground field as purple curves overlapped on the data. The simulated time series have been shifted earlier in time by 15 minutes which we attribute to a small uncertainty in the input data which resulted from ballistically shifting the input L1 data to the outer boundary of the simulation. We show that the simulated data also display a significant spike in the dB/dt at the storm commencement which coincides with a similar magnitude to the “ground truth” observed by the magnetometer ground stations. Qualitatively, the biggest limitation in the simulated results appears to occur in the inaccuracy of the negative dBz/dt component seen during the time derivative “spike.” This could be due to the Bz component being especially sensitive to geomagnetic induction effects which are not taken into account in our simulation.

It is worth noting that only middle- and high-latitude magnetometer stations were included in the earlier GEM challenges even though the Dst index addresses the low-latitude disturbances. This is due to the global MHD approach being implemented in the first-principle models; they could only capture the ionospheric output at high latitudes by using the Biot-Savart law to integrate over the ionospheric electric currents system. In this paper, we have alleviated such a constraint by coupling the global MHD models to the inner magnetospheric models and thereby capturing the ring current dynamics and magnetospheric current systems, therefore providing the required ionospheric response at low latitudes [Yu et al., 2010].

4.3. Geomagnetically Induced Currents, GICs

Reliable estimates of GICs and the geoelectric field require accurate knowledge of the local geological conditions as well as the dB/dt. As the global distribution of the conductivity from the surface to the upper mantle (depths of several hundred kilometers) is not well known, estimating GICs cannot be arbitrarily made for
any location on Earth. However, for local environments that have historically been susceptible to GIC events [e.g., Pulkkinen et al., 2005; Ngwira et al., 2008; Pulkkinen et al., 2010a; Torta et al., 2012], the ground structure is known and therefore this study could be replicated for larger geoeffective CME events and early warning predictions can be made as to their level of susceptibility. It is envisaged that as the ground structure for more locations around the globe become recognized, the framework presented in this paper will provide the necessary steps to improve GIC forecasting. Of course, a simple approach may be created to estimate the extrema of possible GICs by using realistic extreme ends of the conducting (British Columbia, Canada) and resistive (Quebec, Canada) ground structures [Pulkkinen et al., 2008]. But detailed investigation into these possibilities goes beyond the scope of this work.

5. Discussion

Currently, observations of the solar magnetic fields are used as inputs for the background solar wind when simulating the heliosphere for space weather predictions. However, the CME itself is usually set to an approximate and generic size. Details of the CME that is included in the magnetospheric simulations are only provided by measurements made in situ at L1, which is ~1 hour before its arrival at the Earth’s bow shock. By using remote observations from coronagraphs (~15 \( R_\odot \)), observational estimates of the CME can be made for both the Enlil heliospheric simulation and as early initial-attempt inputs to BATS-R-US magnetospheric simulations. The use of remote observations means that BATS-R-US simulations can be carried out ~48 hours prior to waiting for the CME to propagate to L1.

The focus of this paper was to estimate the CME mass as a time series close to the Sun, which was then ballistically propagated to L1. While previous studies have been carried out to better estimate the arrival times of a CME [Owens and Cargill, 2004; Takakishvili et al., 2009, 2011], extensive plane-of-sky speed measurements have been made over a large number of CMEs [St. Cyr et al., 2000; Yashiro et al., 2004]. These studies could be used to remotely estimate a velocity time series which can then be used to propagate the CME to L1. The ability to remotely estimate both the velocity and mass allows early prediction of the momentum flux arriving to Earth.

Figures 5 and 7 display the remotely observed mass time series which have been artificially normalized to suit the in situ number density. The mass time series were arbitrarily divided by \( 1.5 \times 10^{11} \text{ g} \) in order to display a qualitative profile of the same order of magnitude. Clearly, if these mass time series are to be used as inputs to early space weather simulations, then an appropriate method to scale the mass estimates to a density value is required. Three basic methods can be used as follows: (1) defining the CME’s 3-D volume by, for example, using the GCS model [Thernisien et al., 2006], this volume can then be radially propagated out to 1 AU where the density can be estimated; (2) using the empirical formulas proposed by Vourlidas et al. [2010]; and (3) using a combination of white-light images and off-limb spectroscopy to directly measure the densities across the CME body. Future investigations may attempt to solve the most appropriate method with more events. Method 1 has been used in Appendix A to justify the order of magnitude used in this paper. With appropriate density and velocity estimates made remotely to first approximation, the results can be adjusted in an ensemble.
method for making space weather predictions along with variety of magnetic field estimates [e.g., Lin et al., 2000; Gopalswamy and Yashiro, 2011; Savani et al., 2012b].

6. Conclusions

[51] In this paper, we show the first results for producing density measurements from remote observations that are comparable to their equivalent in situ time series. Therefore, this paper for the first time shows that a time series of data can be estimated remotely and be used to make forecasts of GICs at Earth, while a previous attempt by Pulkkinen et al. [2009] to forecast GICs from remote observations only used a generic pressure pulse for a CME within the Enil model. We also confirm that the compression of the magnetosphere from the momentum flux of a CME is a significant variable in predicting geomagnetically induced currents. Our results are capable of producing qualitatively reliable estimates of the densities upstream of Earth’s bow shock. These results indicate the possibility of using remote observations at a heliocentric distance of ~15 Rs to estimate the solar wind density profile arriving at Earth and show that these estimates can be used as part of a preliminary early warning system for space weather predictions.

[52] This paper focuses on a case study event of a CME which displays a strong northward Bz component in the magnetic field rather than a fast geo-effective event. The CME propagated in the inner heliosphere between 25 and 31 March 2011 and is observed in both ST-A and ST-B. The event allowed our study to attribute all the ground-based measurements at L1 is remarkably similar for the sheath region between the shock front and leading edge. Future studies to investigate CMEs may not necessarily have the capabilities to track the CME along the entire Sun-Earth line. As such, our ballistic propagation approach for the mass measurements from ~15 Rs to L1 may serve as a useful tool for estimating a time series for the mass.

Appendix A: Density Normalization

[56] In this paper, we have chosen to artificially divide the time series of the mass measurements by a constant value of 1.5 × 10^11 g. This was used to convert a mass times series that was estimated remotely into a density times series which was later compared with the in situ measurements. Here we carry out some preliminary work to justify the number used with a simple volume expansion method. The work below is intended to provide an order of magnitude justification; however, further work would benefit from a more detailed approach as suggested in section 5.

[57] We assume that a small volume (defined by the size of a few pixels in the COR-2A camera) measured at ~10 Rs has a shape of a cylinder, such that the circular cross section is within the plane of sky and the length (W0) is defined along the line of sight. First, we assume that the length of the cylinder can be estimated from the GCS model (see Figure A1 for details). At 15:24 UT on 25 March 2011, the height of the legs (h) and the half-angular width (a) from GCS as defined by Thernisien et al. [2006] were estimated as 9.78 Rs and 32.55°, respectively. With trigonometry, we calculate that the cylindrical length should be 10.51 Rs. For this time, we noted that the plane of sky position of the CME nose was 10.5 Rs. The same process was carried out for an image at 17:24 UT to deduce that the heliocentric distance of the CME was to first approximation equal to the cylindrical length,
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Figure A1. (a) The parameters from Thernisien et al. [2006] that are used to estimate the length of the CME along the line of sight. (b) The initial volume element defined to be observed with the COR-2A camera. (c) The final dimensions of the volume element at L1, where the in situ measurements are taken.

Therefore, at L1 where the in situ measurements are made, we estimate the cylindrical length as \(W_1 = 210 \, R_S\).

To estimate the cross-sectional area, we assume the cross section expands at a uniform speed of \(V_{ex} = 30\) kilometers per second (which we estimated from the in situ measurements). The total time of expansion, \(t\), is the same as the propagation time and dependent on the bulk flow speed which we assume to be 370 kilometers per second. Assuming the propagation distance, \(R = 200 \, R_S\), we find that the radius of the circular cross section at L1 is 16.22 \(R_S\) and follows

\[
\gamma_1 = \left( \frac{V_{es}}{V_{bulk}} \right) \times R.
\] (A1)

Therefore, our final volume element (\(\Gamma_f\)) can be estimated by

\[
\Gamma_f = \pi \left( \frac{V_{es}}{V_{bulk}} \right)^2 R^2 W_1,
\] (A2)

to give 5.85 \(\times 10^{27}\) cubic centimeters.

It therefore follows that a first approximation for a normalization constant (\(\kappa_0\)) is

\[
\kappa_0 = \frac{1}{m_f \Gamma_f}.
\] (A3)

From the constants used in our example, \(\kappa_0 = 1.02 \times 10^{-11} \, g^{-1} \, \text{cm}^3\). This is similar to the normalization value of 1.5 \(\times 10^{11}\) used in this paper and is certainly of the correct order of magnitude. This small discrepancy might be solved with more advanced calculations.

Appendix B: Flux Rope Fitting

Simple determination of parameters from a model fitting procedure is one of the best ways to quickly estimate the global properties of an interplanetary CME (ICME) from in situ measurements. The first model to be successfully optimized to magnetic clouds (MCs) was a constant \(\alpha\), force-free (CAFF) flux rope model by Lepping et al. [1990]. Since then, several other attempts have been made to improve the results between observations and models [Owens et al., 2006; Mulligan and Russell, 2001; Hidalgo et al., 2002; Hidalgo and Nieves-Chinchilla, 2012; Owens et al., 2012]. We use a simplified modification of the Lepping et al. [1990] model. The magnetic field of the model is described by the Cartesian form of the Bessel function for a force-free flux rope. In fitting the flux rope model to the data, the first step is to estimate the orientation of the cylindrical axis. Then by determining the chirality and varying both the distance of closest approach and axial magnetic field strength as free parameters within a computational code, we are able to make predictions of ICME parameters.

The method employed to determine the MC axis direction involves a technique called minimum variance analysis (MVA) [Sonnerup and Cahill, 1967; Steed et al., 2008]. MVA was originally developed to determine the local normal for a tangential discontinuity (TD) in the magnetic field. This method calculates the orthogonal set of vectors in which the variance of the magnetic field in question is at minimum (e1), maximum (e3), and intermediate (e2). For each of these eigenvectors, there is a corresponding eigenvalue, often represented as \(\lambda_1\), \(\lambda_3\), and \(\lambda_2\), respectively.

For the purposes of investigating TDs, the minimum eigenvector calculated provides the normal to the plane. Here the ratios of eigenvalues (\(\lambda_1\)) and the other two are of concern as they indicate the reliability in the normal. For investigating the axial direction of a MC, we must concern ourselves with the intermediate direction, with MVA applied to the time period that contains the flux rope only. The axis of the MC therefore lies in the intermediate direction, but the distinction of the field variance along the coordinate axes reduce as the spacecraft trajectory moves further from the central MC axis.

When investigating the intermediate direction, the eigenvalue ratios between \(\lambda_2/\lambda_1\) and \(\lambda_3/\lambda_2\) are of concern. Ideally, both ratios should be \(> 10\), but recent work using MVA has shown that ratios greater than 2 are adequate in ICME context [Bothmer and Schwenn, 1998]. If the ratio of either \(\lambda_2/\lambda_1\) or \(\lambda_3/\lambda_2\) is small, then the axial
direction becomes ambiguous within the plane of the two eigenvectors.

[66] The scenario above is described for the ideal case, where the spacecraft passes through the center of the flux rope. However, this is usually not true. The distance of closest approach, $Y_0$, is an important parameter in determining the predicted field profile. It is defined in dimensionless units as the closest approach distance divided by the radius of the flux rope. Thus, $Y_0$ varies between 1 and ~1 for a spacecraft traveling above and below the MC center, respectively. Rees [2003] simulated idealized flux ropes with spacecraft trajectories away from the center and then carried out MVA over the time profiles. He found that the error in the axis angle increased with an increasing $|Y_0|$. The results suggest that an impact parameter of $>0.5$ should be dealt with caution as the error may be of the order of $\sim 15\%$. The uncertainty in ascertaining the axis orientation [Al-Haddad et al., 2013] is one of the reasons why more complex models choose to begin their analysis with MVA and then later find the optimal direction by introducing two extra free variables.

[67] High-frequency noise is a source of error for MVA in the interplanetary CME context. MVA analyzes the variance in the magnetic field, and therefore the large noise fluctuations can yield incorrect eigenvectors. To limit this effect, 10 or 15 minute averaged data are often used when fitting a modeled rope to the data. It has been shown that for good events, the time resolution between 10 and 60 minutes has a negligible effect on the axis orientation [Lepping et al., 2003]. Subtly, the lower resolutions are often used for large events, with a reason to maintain the total number of data points within the MC to about $N = 40$ [Lepping et al., 2006]. Although this is not essential, it is desirable when comparing various cases against each other in a statistical manner.

[68] Once the axis of the model MC is determined, the in situ magnetic field data are rotated into the frame of the MVA axes. A sequence of flux ropes is then created and compared to the data by analyzing the mean square error ($\chi$) coefficient. The $\chi$ coefficient measures how well each rope fits to the data and is defined in the same manner as Lynch et al. [2003].

[69] The time interval between the start and end of the MC is identified manually by eye. This defines the data range which is compared to the model and fixes the size of the MC model. By using the distance of closest approach, the axial field strength, and chirality (a concept of rotation in the magnetic field, either clockwise or anticlockwise) as free parameters, various simulated MCs can be generated. Each simulated MC is compared to the data by measuring the $\chi$ coefficient. The simulated MC with the smallest $\chi$ value is regarded as the best fit result. The free variables that create the model are varied by using a downhill simplex method developed by Nelder and Mead [1965]; this is a nonlinear optimization routine designed to minimize the $\chi$ coefficients. This approach is faster than a standard grid search and can be easily manipulated to determine the free variables to larger significant figure. The optimized free parameters are the outputs of the model. These results are used again to re-create the optimized model. The field vectors from this model are then rotated into the spacecraft frame and plotted on top of the observed data for visual confirmation.

[70] It is worth noting here that the CAFF model described above assumes a static ICME. That is to say, the model plotted shows a time series obtained by taking a radial cut through a flux rope at a fixed time. Many ICMEs observed at terrestrial distances take ~24 hours to transit over a spacecraft; therefore, it is important to note that ICME seen at the end of the transit has evolved and is different from the same object at the beginning of the transit. A more accurate representation would be to include a time series of a flux rope evolving in time past a fixed point in space.

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