Comparison of SMOS and SMAP soil moisture retrieval approaches using
tower-based radiometer data over a vineyard field


a University of Hamburg, Center for Marine and Atmospheric Sciences (ZMAW), Hamburg, Germany
b INRA, Bordeaux Sciences Agro, UMR 1391 ISPA, F-33140 Villenave d’Ornon, France
c Faculty of Physics, University of Valencia, 50 Burjassot. 46100 Valencia, Spain
d Centre d’Etudes Spatiales de la BIOsphère (CESBIO – CNES, CNRS, IRD, Université Toulouse III), Toulouse, France
e Department of Earth Sciences, VU University Amsterdam, the Netherlands.
f NASA GSFC, Greenbelt, MD 20771, USA
g USDA-ARS Hydrology and Remote Sensing Laboratory, Beltsville, MD 20705-2350 USA
h Gamma Remote Sensing, Worbstr. 225, CH-3073 Gümligen, Switzerland
i Swiss Federal Research Institute WSL, Zürcherstrasse 111, 8903 Birmensdorf, Switzerland
j European Centre for Medium-Range Weather Forecasts (ECMWF), Reading, UK

ABSTRACT

The objective of this study was to compare several approaches to soil moisture (SM) retrieval using L-band microwave radiometry. The comparison was based on a brightness temperature \(T_B\) data set acquired since 2010 by the L-band radiometer ELBARA-II over a vineyard field at the Valencia Anchor Station (VAS) site. ELBARA-II, provided by the European Space Agency (ESA) within the scientific program of the SMOS (Soil Moisture and Ocean Salinity) mission, measures multiangular \(T_B\) data at horizontal and vertical polarization for a range of incidence angles (30°-60°). Based on a three year data set (2010-2012), several SM retrieval approaches developed for spaceborne missions including AMSR-E (Advanced Microwave Scanning Radiometer for EOS), SMAP (Soil Moisture Active Passive) and SMOS were compared. The approaches include: the Single Channel Algorithm (SCA) for horizontal (SCA-H) and vertical (SCA-V) polarizations, the Dual Channel Algorithm (DCA), the Land
Parameter Retrieval Model (LPRM) and two simplified approaches based on statistical regressions (referred to as 'Mattar' and 'Saleh'). Time series of vegetation indices required for three of the algorithms (SCA-H, SCA-V and 'Mattar') were obtained from MODIS observations. The SM retrievals were evaluated against reference SM values estimated from a multiangular 2-Parameter inversion approach. The results obtained with the current base line algorithms developed for SMAP (SCA-H and -V) are in very good agreement with the 'reference' SM data set derived from the multi-angular observations ($R^2 \approx 0.90$, RMSE varying between 0.035 and 0.056 m$^3$/m$^3$ for several retrieval configurations). This result showed that, provided the relationship between vegetation optical depth and a remotely-sensed vegetation index can be calibrated, the SCA algorithms can provide results very close to those obtained from multi-angular observations in this study area. The approaches based on statistical regressions provided similar results and the best accuracy was obtained with the 'Saleh' methods based on either bi-angular or bipolarization observations ($R^2 \approx 0.93$, RMSE $\approx 0.035$ m$^3$/m$^3$). The LPRM and DCA algorithms were found to be slightly less successful in retrieving the 'reference' SM time series ($R^2 \approx 0.75$, RMSE $\approx 0.055$ m$^3$/m$^3$). However, the two above approaches have the great advantage of not requiring any model calibrations previous to the SM retrievals.

1. Introduction

Surface soil moisture plays a major role in the water and energy budgets of continental surfaces, which has direct implications for hydrological, climate, and weather forecasting models. L-band passive microwave remote sensing is one of the most promising approaches to monitor this variable at the global scale with frequent revisiting times (Jackson et al., 1995; Kerr et al., 2001, Njoku et al., 2003; De Lannoy et al., 2013). Three recent or planned space missions use this technology: SMOS (launched end of 2009), Aquarius (launched in June of 2011) and SMAP (launch scheduled in November 2014).

The Soil Moisture and Ocean Salinity (SMOS) mission is the first spaceborne mission dedicated to soil moisture (SM) mapping. SMOS has multi-angular capabilities which are exploited by the SM retrieval approach: SM and vegetation optical depth $\tau$ (used to parameterize vegetation attenuation and emission) are retrieved simultaneously based on SMOS multi-configuration observations, in terms of polarizations and incidence angles. Aquarius is a combined passive/active L-band microwave instrument which consists of a set
of three radiometers and a scatterometer, operating at 1.4 GHz and 1.26 GHz respectively (Levine et al., 2010). The primary mission objective of Aquarius is to provide global observations of surface sea salinity once every 7 days. However, Aquarius has also potential capabilities to monitor soil moisture at global scales (Luo et al., 2013, Bindlish et al., 2013).

SMAP incorporates a radar and a radiometer, both operating at L-band and at the incidence (observation) angle $\theta = 40^\circ$. The spatial resolutions of the corresponding active- and passive microwave signatures are $\sim 39$ km x 47 km and $\sim 1$ km x 1 km, respectively. The mission concept is to combine the complementary attributes of the radar observations (high spatial resolution but lower soil moisture accuracy) and radiometer observations (higher soil moisture accuracy but coarse spatial resolution) to retrieve SM at a spatial resolution of 9 km, and the freeze-thaw state at a spatial resolution of 3 km (Entekhabi et al., 2010; O’Neill et al., 2013).

Several SM retrieval approaches have been developed in the context of these L-band space missions. As noted above, in the operational SMOS SM retrieval algorithm, SM and vegetation optical depth at nadir ($\tau_{NAD}$) are retrieved simultaneously based on SMOS multiangular and bipolarization observations (Wigneron et al., 1995, 2000; Kerr et al., 2012). The 2-Parameter (2-P) retrievals of SM and $\tau_{NAD}$ are obtained from inversion of the L-MEB (L-band Microwave Emission of the Biosphere) model (Wigneron et al., 2007). This forward model is based on the so-called $\tau$-$\omega$ model (Mo et al., 1982) and it includes a number of parameterizations to capture effects of vegetation structure and soil roughness on polarization and angular properties of L-band $T_B$ emitted from land surfaces. The inversion of L-MEB considering SM and $\tau_{NAD}$ as the requested parameters (referred to as ‘L-MEB 2-P’ inversion) is implemented in the operational algorithms used to compute the Level 2 (distributed by ESA) and Level 3 (distributed by the Centre Aval de Traitement des Données SMOS (CATDS), Berthon et al., 2012) SMOS products. In parallel to this operational retrieval method, several simplified methods have been developed to exploit the capability of L-band radiometers to provide information on land surface states such as SM. For instance, Wigneron et al. (2004) and Saleh et al. (2006) have evaluated statistical regressions based on bipolarization or bi-angular $T_B$ data. Mattar et al. (2012) have evaluated similar regression methods that also use a vegetation index estimated from ancillary remotely sensed observations (such as the Normalized Difference Vegetation Index (NDVI) or the Leaf Area Index (LAI)) to account for vegetation effects. Moreover, methods based on Neural Networks have been and are currently evaluated (Liu et al., 2002; Rodriguez et al., 2003).
The general retrieval approach proposed for SMAP is different from the operational SMOS SM retrieval: SMAP observations will be available for the sole incidence angle of 40°, but make use of the complementary information provided by the active- (radar) and the passive (radiometer) L-band data. In the initial release of the ATBD (Algorithm Theoretical Basis Document) written for the retrievals from SMAP’s radiometer (O’Neill et al., 2013), four soil moisture retrieval algorithms are suggested for evaluation during the pre- and post-launch calibration and validation activities: (i) the single-channel algorithm at H polarization (SCA-H) which is the current SMAP baseline algorithm, (ii) the single-channel algorithm at V polarization (SCA-V), (iii) the dual-channel algorithm (DCA), and (iv) the Land parameter retrieval model (LPRM). In the SCA-H and –V algorithms, vegetation is accounted for by the \( \tau - \omega \) model as in L-MEB. However, optical depth at nadir \( (\tau_{\text{NAD}}) \) is not retrieved as for SMOS. Instead it is estimated from the linear relation \( \tau_{\text{NAD}} = b \cdot \text{VWC} \) between \( \tau_{\text{NAD}} \) and vegetation water content (VWC) (Jackson et al. (1991)). Thereby, values of the b-parameter are assumed polarization independent and will be provided from a land cover look up table, and the VWC is estimated from values of the NDVI Index. The DCA retrieval approach is very similar to the one used for SMOS. The only difference is that the inversion is based on the minimization of a cost function accounting for the Root Mean Square Error (RMSE) between measured and simulated bi-polarized \( T_B \) observations at one incidence angle, whereas multi-angular observations are used for SMOS. In the LPRM algorithm, the Microwave Polarization Difference Index (MPDI) and the observed emissivities are used to derive the vegetation optical depth \( \tau \) (Meesters et al., 2005). In a second step, SM is retrieved with an optimization routine that minimizes the error between the modelled and observed H-polarized brightness temperatures (Owe et al., 2008; De Jeu et al., 2009).

In this study, these different retrieval algorithms were compared using a 3-year long multiangular \( T_B \) data set acquired by the L-band radiometer ELBARA-II over a vineyard field (MELBEX-III) at the Valencia Anchor Station (VAS) site (Schwank et al., 2012, Wigneron et al., 2012). Applications of the retrieval methods can be made at large scales from satellite observations but also at more local scale for long term SM monitoring from ground based instruments mounted on different types of platforms: towers as for ELBARA-II (de Rosnay et al., 2006; Schwank et al., 2012; Schlenz et al., 2012, etc.); trucks (Hornbuckle et al., 2004; Kurum et al., 2009) or from the top of a mountain as in Pellarin et al. (2013).

ELBARA-II (Schwank et al. 2010), developed by GAMMA Remote Sensing AG (Switzerland) and funded by the ESA, provides \( T_B \) at horizontal and vertical polarization for a
range of observation angles (30°-60°). The ELBARA-II T\textsubscript{B} observations were acquired since 2010 and a 3-year T\textsubscript{B} data set is available for the MELBEX-III site. As an accurate estimation of SM from ground based measurements over the MELBEX-III site could not be achieved because of very frequent agricultural practices within the field, it was considered that representative SM values (referred to as 'reference' SM data set) over the ELBARA-II footprints were obtained from multi-angular 2-P L-MEB retrievals. Moreover, the 2-P L-MEB approach also provided retrievals of optical depth at nadir (τ\textsubscript{NAD}). These latter values were used to calibrate the relationships between τ\textsubscript{NAD} and NDVI, which are required in the SCA-H and SCA-V algorithms. Based on these ‘reference’ SM and τ\textsubscript{NAD} data sets and the ELBARA-II T\textsubscript{B} observations, seven SM retrieval approaches were evaluated and compared: the four methods considered presently in the SMAP ATBD based on bi-polarization observations at one observation angle (θ = 40° for SMAP) and three regression methods (Saleh et al, 2006 and Mattar et al., 2012) developed in the framework of SMOS research activities and based on bi-angular or bipolarization observations. The results of this evaluation are discussed in the context of the improvement and development of the SM retrieval algorithms.

2. Materials and method

2.1. The ELABARA-II radiometer at MELBEX-III (VAS site)

The study was based on T\textsubscript{B} measurements made by the ELBARA-II radiometer over the 2010-2012 period within the VAS site. ELBARA-II was installed in September 2009 at the MELBEX-III vineyard field (referred to as M-III), close to Caudete de las Fuentes, on the Utiel-Requena Plateau at ~ 800 m a.s.l., in the region of Valencia, Spain (39°31'18.18"N, 1°17'29.64"W). This site is one of the reference sites selected by ESA in Europe within the SMOS science program.

All details concerning the ELBARA-II instrument and the M-III experiment set up are given in Schwank et al. (2010, 2012), and Wigneron et al. (2012). Only a brief summary of the main information concerning this experiment is presented here.

The ELBARA-II radiometer was set up 17 meters above ground to monitor a vineyard that is representative of the main land use of the VAS region. The ELBARA-II was equipped with an elevation tracker that allows measurements at specific observation angles θ varying
between $30^\circ \leq \theta \leq 330^\circ$ with $\theta = 180^\circ$ being the zenith direction. Every 30 minutes, automated "elevation scans" are carried out that provide $T_B$ at horizontal and vertical polarizations at observation angles between $\theta = 30^\circ$ and $70^\circ$ with steps of $5^\circ$. Between each elevation scan, measurements are made at the $\theta = 45^\circ$ every 10 minutes. Once a day, at 23:55 local time, the radiometer is automatically positioned at $150^\circ$ to carry out sky calibration measurements. The absolute accuracy of the ELBARA-II measurements was estimated to be better than $\pm 1 \text{ K}$ over the course of 2010-2012. During short time periods, no measurement could be acquired over the vineyard field due to experiments using reflecting foils (Schwank et al., 2012) or due to technical issues: in 2010 (DoY 222 - DoY 245, DoY 312 - DoY 337) and in 2011 (DoY 41 – DoY 62; DoY 84 – DoY 133). The ELBARA-II observations were slightly affected by Radio Frequency Interferences (RFI) caused by active microwave systems violating the protected part of the L-Band (1400 MHz – 1427 MHz). Efforts made by the Spanish administrative authorities in 2010 to mitigate RFI disturbances resulted in a significant decrease since the beginning of July in 2010 (~ DoY 190). Most RFI events result in steep increases in the time variations of the measured $T_B$ (larger than 30K at minimum) and unrealistic $T_B$ values (larger than 330 K). These RFI events were detected manually from the ELBARA-II $T_B$ data set. To be consistent with the overpass times of SMOS and SMAP, only $T_B$ measurements made at 6 am and 6 pm local time are considered in this study.

2.2. In situ measurements

Concurrent with the ELBARA-II observations, ground measurements were obtained within the M-III vineyard. Soil profiles of the volumetric soil moisture [$\text{m}^3 \cdot \text{m}^{-3}$] and temperature were acquired up to about 1 m (Wigneron et al., 2012). Vineyard cultivation practices are carried out frequently within the field (for weeding and pest control, winter and summer pruning, cluster thinning, etc.) so that SM probes could not be installed permanently within the ELBARA-II footprints. Only two Delta-T Theta Probes measuring the volumetric SM of the top 0-6cm soil layer were installed at the border of the field where no field work was carried out. It is our opinion that these SM probes cannot provide SM values representative of the field conditions as seen by the ELBARA-II instrument and have not been used in the analysis presented here (Wigneron et al., 2012).
A meteorological station located at the VAS (coordinates: 39°34′15″N, 1°17′18″W, 813 m a.s.l.), a few kilometres from the M-III site provided the standard meteorological variables (air temperature, wind speed, air humidity, etc.). Over the VAS site, the average value of the total yearly precipitation over the ten years prior to 2010 is $P = 461$ mm. For the three years considered in this study; 2010 was wet ($P = 538.2$ mm) and was followed by a ‘dry’ and a ‘very dry’ year in 2011 and 2012 ($P = 379.2$ mm in 2011 and $P = 288.6$ mm in 2012).

Details concerning the soil and vegetation conditions at the M-III site are provided in Wigneron et al. (2012). The field-site observed with ELBARA-II is typical of vineyards in the VAS region (the spacing between each plant is ~ 2 m and that between each row is ~ 3 m). Two field experiments in 2007 and 2010 led to similar values of the maximum Leaf Area Index, LAI_{\text{MAX}} \approx 2.2. To monitor the time variations in the vegetation characteristics over the growing season, we used the NDVI index from the MODIS products (16 day NDVI composite of 250 m MODIS data; MODIS (2010)). As the field was large enough (larger than 300 m x 300 m), it can considered that the MODIS NDVI time variations are representative of the vegetation conditions as seen by the ELBARA-II radiometer operated at the M-III site.

In order to monitor the evolution of the surface roughness over time, field measurements were made by means of measuring mechanically two-dimensional profiles of the ground surface. For this purpose, a 2 m needle board with 201 needles, movable in the vertical direction and with 1 cm spacing between needles was used (Mialon et al. (2012)). The needle board was leveled and placed on the ground such that the needles were allowed to fall until they touched the soil surface. Subsequently, photos of the profile created by the needle heights were taken and digitized to compute soil roughness parameters. On each of the seven days during 2012 when roughness measurements were performed, approximately 8 to 12 profiles were taken within the ELBARA-II footprints. Different locations and orientations (perpendicular and parallel to the vegetation rows) were considered in computing representative information on the standard deviation of soil surface height ($S_D$, cm), and correlation length ($L_C$, cm). Time variations in the average values of $S_D$ and $L_C$ are shown in Fig. 1 for the seven days of measurements in 2012. The corresponding annual mean values are $\langle S_D \rangle = 2.2$ cm, $\langle L_C \rangle = 6.2$ cm.

### 2.3 L-MEB modelling and inversion
The data set considered as a reference in this study was obtained using the 2-P L-MEB inversion approach to obtain retrievals of SM and $\tau_{\text{NAD}}$ (Wigneron et al., 2000). There are many reasons to use this retrieved data set as a reference.

First, the SM data set retrieved from tower-based remote sensing observations can be considered as representative of the SM conditions over the whole ELBARA-II footprint (this is usually a complex task using field probes distributed within the field). Second, the 2-P L-MEB method, based on multi-angular observations, has been validated in many studies against experimental data sets for a variety of soil and vegetation conditions (Wigneron et al., 1995, 2007; Pardé et al., 2003, 2004, Saleh et al., 2006; Panciera et al., 2009; Cano et al., 2010; Schlenz et al., 2012, etc.), and its accuracy and robustness has been evaluated theoretically (Wigneron et al., 2000). The 2-P L-MEB method is currently implemented in the official SMOS retrieval algorithm (Kerr et al, 2012). Third, the 2-P L-MEB approach has the advantage of providing retrievals of optical depth at nadir ($\tau_{\text{NAD}}$). These latter values were used to calibrate the relationships between $\tau_{\text{NAD}}$ and NDVI, which are required in the SCA-H and SCA-V algorithms. Moreover, it can not be considered that one method can benefit from the use of 2-P L-MEB retrieval method as a reference: the equations of the L-MEB model, used in the 2-P L-MEB approach, are also the basis of the SCA-H, SCA-V, DCA and LPRM algorithms.

A detailed description of the L-MEB model is given in Wigneron et al. (2007) and a brief summary of the main L-MEB equations and of additional parameterizations developed since 2007 is given in the following. The L-MEB model is based on a zero-order solution of the radiative transfer equations: the so called $\tau$-$\omega$ model, where the optical depth $\tau$ accounts for extinction effects within the canopy and the effective scattering albedo $\omega$ (-) accounts for scattering effects (Mo et al., 1982; Kurum et al., 2013). To incorporate the SMOS multi-angular feasibility, several additional parameterizations are used in L-MEB to account for effects of the vegetation structure and soil roughness on L-band brightness temperatures emitted from vegetated land surfaces.

In local thermal equilibrium the emissivity $e_{GP}$ of the ground at horizontal ($p = H$) and vertical ($p = V$) polarization is related to the corresponding reflectivity $r_{GP}$ of the soil (the ground) observed at the angle $\theta$:

$$e_{GP} (\theta) = 1 - r_{GP} (\theta)$$  (1)
The soil reflectivity $r_{GP}$ can be expressed as the reflectivity $r^*_{GP}$ of a specular surface and the roughness model parameters $Q_R$, $H_R$ and $N_{RP}$ as:

$$r_{GP}(\theta) = [(1-Q_R) r^*_{GP}(\theta) + Q_R r^*_{GQ}(\theta)] \exp(-H_R \cos^{N_{RP}}(\theta))$$  \hspace{1cm} (2)

In this equation, $H_R$ parameterizes the intensity of the roughness effects, $Q_R$ parameterizes the polarization mixing effects, and $N_{RP}$ is used to account for the specific effects of roughness on the trend of soil reflectivity $r_{GP}$ as a function of incidence angle and polarization. The reflectivity of a specular surface $r^*_{GP}$ was computed using the Fresnel equations as a function of $\theta$ and of the effective soil dielectric permittivity $\varepsilon_G$. The latter was computed from soil moisture SM, soil effective temperature $T_G$, and from the clay fraction using the dielectric mixing model of Mironov et al. (2012), referred to as the ‘Mironov’ model in the following. This is in contrast to the earlier study Wigneron et al. (2007), where the Dobson model (Dobson et al., 1985) was used to estimate $\varepsilon_G$.

We used the recent results of Lawrence et al. (2013) to estimate the values of the roughness model parameters ($Q_R$, $H_R$ and $N_{RP}$). These parameters were assumed as constants in time, and therefore computed from the annual average value $\langle S_D \rangle$ of the standard deviation of the soil surface height and the corresponding annual mean $\langle L_C \rangle$ of the correlation length (Fig. 1).

To be consistent with the general approach considered for SMAP we assumed that $N_{RV} = N_{RH} = 0$ (O’Neill et al., 2013). On that assumption, the roughness parameters $H_R$ and $Q_R$ were computed as (Lawrence et al., 2013):

$$H_R = 1.762 \left(1 - \exp\left(-\frac{Z_S}{1.85}\right)\right)$$  \hspace{1cm} (3)

where $Z_S = (\langle S_D \rangle)^2 / \langle L_C \rangle$ (cm)

Considering the annual mean values $\langle S_D \rangle = 2.2$ cm and $\langle L_C \rangle = 6.2$ cm measured over the M-III site in 2012, we obtained $Z_S = 0.78$ cm, $H_R = 0.606$, $Q_R = 0.0303$.

In this study, we considered a composite soil-vegetation surface temperature $T_{GC}$ for the effective temperature $T_G$ of the ground (the soil) and the vegetation canopy $T_C$. The composite effective temperature $T_{GC}$ of the ELBARA-II footprints was computed from the ERA-INTERIM 0-7 cm soil temperature product ($T_{E,07}$). ERA-INTERIM is the latest ECMWF (European Centre for Medium-Range Weather Forecasts) global atmospheric reanalysis of the period 1979 to the present (Dee et al., 2011) with a temporal resolution of 3 hours and a
spatial resolution of 0.75° (corresponding to about 100 km resolution over the VAS site). The accuracy of this estimate was considered to be sufficient in several studies investigating SM retrievals from L-band observations (Pardé et al., 2004; Wigneron et al., 2012).

As noted above, we used the $\tau - \omega$ model to compute the upwelling emission ($T_B$) from the two layer soil-vegetation medium. $T_{BP} (p = H, V)$ is the sum of three terms: (1) the direct upwelling vegetation emission, (2) the downwelling vegetation emission reflected by the soil and attenuated by the canopy layer, and (3) upwelling soil emission attenuated by the canopy:

$$T_{BP} = (1-\omega_p) (1-\gamma_p) \left( 1 + \gamma_p r_{GP} \right) T_C + (1-r_{GP}) \gamma_p T_G$$

(4)

where $T_G = T_C = T_{GC} = T_{E-07}$ is assumed in this study, and $r_{GP}$ is the soil reflectivity computed with (2) and (3). $\gamma_p$ is the vegetation attenuation factor which is related to the optical depth $\tau_p$ as (Beer’s law):

$$\gamma_p = \exp\left(-\frac{\tau_p}{\cos \theta}\right)$$

(5)

To account for vegetation anisotropies, the optical depth $\tau_p(\theta)$ at the observation angle $\theta$ is expressed with a parameterization involving the optical depth $\tau_{NAD}$ at nadir ($\theta = 0^\circ$):

$$\tau_p(\theta) = \tau_{NAD} \left( \sin^2(\theta) \cdot tt_p + \cos^2(\theta) \right) \quad \text{(at } p = V, H)$$

(6)

The parameters $tt_V$ ($) and $tt_H$ ($) account for the angular dependence of $\tau_p(\theta)$. As found in Wigneron et al. (2012), we considered that $tt_H = 1$ (default L-MEB value) and that the $tt_V$ parameter is free in the retrieval process, to account for the effects of the vine stocks, with a preferential vertical orientation. So in reality, a 3-Parameter retrieval approach is made in this study, but the notation 2-P is kept, as only SM and $\tau$ can be considered as variables of interest for applications.

The values of the effective scattering albedo $\omega_p$ were found to be close to zero over most of the non-forested vegetation covers (Grant et al., 2008; Kurum et al., 2013). The value of $\omega_p$ was set equal here to 0.02 for both polarizations. A summary of the values of the soil and vegetation L-MEB parameters used in this study over the M-III site and described above is given in Table 1.

The 2-P L-MEB inversions were based on bi-polarization and multiangular $T_B$ measurements using a minimization procedure of a cost function evaluating the difference between the L-
MEB simulations and the \( T_B \) measurements (Wigneron et al., 2000, 2007, 2012). The retrievals were based on ELBARA-II \( T_B \) data acquired with the automated elevation scans (section 2.1) performed for the observation angles \( \theta = 30^\circ, 35^\circ, 40^\circ, 45^\circ, 50^\circ \) (corresponding roughly to the limit of validity of L-MEB at large incidence angles). As noted above, only \( T_B \) measurements made at 6 am and 6 pm will be considered in this study. Especially for the measurements at 6 am temperature gradients across the vegetation and the soil are minimal (Kerr et al., 2001).

### 2.4 Description of the different SM retrieval methods

As mentioned in the introduction, seven SM retrieval approaches were evaluated and compared in this study: the four methods considered presently in the SMAP ATBD for the passive-only product and three regression methods (described in Saleh et al (2006) and Mattar et al. (2012)) developed in the context of SMOS. The retrieved SM values were compared to a 'reference' SM data set obtained from the 2-P L-MEB inversion, which was assumed to be representative of the SM values over the ELBARA-II footprint. The seven SM retrieval approaches are described in the following sections. As is the case for the 2-P L-MEB method, these seven methods use the \( \tau - \omega \) radiative transfer model (described above) to account for the vegetation effects and they all assume \( \tau_{NAD} \) is independent of polarization and incidence angle \( (\tau_V(0^\circ) = \tau_H(0^\circ) = \tau_{NAD}) \). They are based on the same equation (1) to model the roughness effects, considering that \( N_{RV} = N_{RH} = 0 \). Furthermore, as implemented here they all use the ‘Mironov’ equations to compute the effective soil dielectric permittivity \( \varepsilon_G \). All of the parameters listed in Table 1 for the 2-P L-MEB method are accounted for in the seven SM retrieval methods considered. Only a very brief description of the SCA-H, SCA-V, DCA and LPRM methods will be given here as a detailed description of these methods is available in the initial release of the ATBD. All these four methods were applied to the ELBARA-II \( T_B \) data at the incidence angle of 40° corresponding to the SMAP observations. A summary of the input variables required for the seven different retrieval methods, as well as for the reference algorithm 2-P L-MEB, is given in Table 2.

#### 2.4.1 Single Channel Algorithms (SCA-H and SCA-V)
The Single Channel Algorithm (SCA-H), based on horizontally polarized $T_B$ observations, is the current SMAP baseline, but the same algorithm can also be applied to vertically polarized $T_B$ data (SCA-V). In SCA-H, brightness temperatures are converted to emissivity using a surrogate for the temperature of the emitting surface layer (in this study, the soil temperature provided by ECMWF ($T_{E,07}$) is used). The derived emissivity is corrected for vegetation and surface roughness to obtain the soil emissivity. Finally, a dielectric mixing model (the ‘Mironov’ model in this study) is used to obtain soil moisture SM from the soil dielectric constant $\varepsilon_0$ using the Fresnel equations.

In this investigation, SCA-H and SCA-V are based on the same corrections of vegetation (using the $\tau_{-w}$ model), and soil roughness effects (using the $H_R$ and $Q_R$ parameters) as those used for the 2-P L-MEB method.

$\tau_{NAD}$ is estimated from the vegetation water content (VWC) as

$$\tau_{NAD} = b \cdot VWC$$  \hspace{1cm} (7)

where $b$ is a proportionality factor mainly depending on the vegetation structure.

For SMAP, values of $b$ will be provided by means of a land cover lookup table and the baseline approach utilizes a set of land cover-based equations to estimate VWC from values of NDVI. The following equation is used for cropland (O’Neill et al, 2013):

$$VWC = (1.9134 \times NDVI^2 - 0.3215 \times NDVI + \text{Stemfactor} \times (\text{NDVI}_{\text{ref}} - 0.1)) / (1 - 0.1)$$  \hspace{1cm} (8)

where Stemfactor parameter is the product of the average height of a land cover class and the ratio of sapwood area to leaf area; $\text{NDVI}_{\text{ref}}$ is assumed to be equal to the maximum value of NDVI time series (the value of $\text{NDVI}_{\text{ref}}$ was set equal here to 0.4696 from the analysis of the MODIS NDVI observations over the 2010-2012 period). In this study, the $b$ and Stemfactor parameters were calibrated prior to the inversion process, as described in Section 2.5.

### 2.4.2 The Dual Channel Algorithm (DCA)

The Dual Channel Algorithm (DCA) is an extension of the SCA and uses both H-polarized and V-polarized $T_B$ observations to simultaneously retrieve SM and VWC (O’Neill et al, 2013). As in the 2-P L-MEB algorithm, the SM and $\tau_{NAD}$ variables are adjusted iteratively until the root mean square difference between the simulated and observed $T_B$ is minimized.

There are differences between 2-P L-MEB and DCA algorithms. Firstly, $T_B$ data at $\theta = 40^\circ$ are used for DCA, while multiangular data are used for 2-P L-MEB. Secondly, the $t_t V$
parameter (accounting for an angular dependence of τ) is retrieved in 2-P L-MEB, while DCA does not account for this dependence. Except for the \( t_t V \) and \( t_t H \) parameters, all vegetation and soil parameters used in DCA are the same as those used in the 2-P L-MEB method (Table 1).

2.4.3 Land Parameter Retrieval Model (LPRM)

The LPRM approach uses an analytical solution for the derivation of the vegetation optical depth. This solution uses the Microwave Polarization Difference Index (MPDI) and the observed surface emissivity (\( e_H \) and \( e_V \)) as input and is based on the assumption that the values of the vegetation optical depth are the same for both polarization (\( \tau_V = \tau_H \)). The MPDI index is calculated from the brightness temperature at H- and V polarizations as follows (Meesters et al., 2005):

\[
\text{MPDI} = \frac{(T_{BV} - T_{BH})}{(T_{BV} + T_{BH})} \quad (8)
\]

Then based on equation (4) of the \( \tau-\omega \) omega model, soil moisture is retrieved using an optimization routine that minimizes the RMSE between the modelled and observed H-polarized brightness temperatures. As for SMOS, the vegetation optical depth at this optimized soil moisture value is an additional retrieval result. As noted in O’Neill et al. (2013), the LPRM was implemented on multifrequency satellites such as AMSR-E, where also the Ka-band V-polarized channel is used to retrieve physical temperatures of the scene observed. This latter can also be estimated from re-analysis or near real time data from weather prediction centres (Parinussa et al., 2011), as is done in the current SMOS SM retrieval algorithm (Kerr et al., 2012). Only a few studies (e.g. de Jeu et al., 2009) have examined the applicability of this model at L-band frequencies, although the analysis of SMOS data with LPRM is currently underway. All detailed equations of the LPRM approach are given in (Owe et al., 2001; Meesters et al., 2005, Owe et al., 2008, de Jeu et al., 2009, Chung et al., 2013). As for DCA, except for the \( t_t V \) and \( t_t H \) parameters which are not relevant here, all vegetation and soil parameters used in LPRM are the same as those used in the 2-P L-MEB method (Table 1).

2.4.4 Linear regression methods (Saleh et al., 2006; Mattar et al., 2012)
Two methods based on regression equations developed by Saleh et al. (2006) and Mattar et al. (2012) were evaluated in this study. Both methods were numerically derived from the equations of the τ-ω model assuming, as for LPRM, that the value of the effective scattering albedo is \( \omega_p = 0 \), and that the values of optical depth \( \tau_p \) are the same for both polarizations \( p = H, V \). These methods are physically-based. However, as the development of an analytical formulation would be complex, most of the time they are used as regressions methods. As shown by Saleh et al. (2006), a key interest in these regression methods is that they can be used for varying roughness and vegetation conditions over time: no additional information about temporal changes in these two state variables (such as NDVI or LAI for vegetation for instance) is required. These regression methods have been used in several studies based on \textit{in situ}, airborne or spaceborne (SMOS) observations (Albergel et al., 2011; Parrens et al., 2012; Calvet et al., 2011, etc.)

The method of Saleh et al. (2006) can be applied to observations made either at the two incidence angles \( \theta_1 \) and \( \theta_2 \) (referred to as ‘Saleh’ bi-angular):

\[
\ln(SM) = a_2 \ln(\Gamma_p(\theta_1)) + a_1 \ln(\Gamma_p(\theta_2)) + a_0 (\theta_1, \theta_2, p)
\]

(9)

or to bi-polarization observations made at one observation angle \( \theta \) (referred to as ‘Saleh’ bi-polarization):

\[
\ln(SM) = b_2 \ln(\Gamma_H(\theta)) + b_1 \ln(\Gamma_V(\theta)) + b_0 (\theta)
\]

(10)

where \( \Gamma_p(\theta) \) is the reflectivity of the soil-vegetation system at polarization \( p \) (\( p=V \) or \( p=H \)), defined as

\[
\Gamma_p(\theta) = 1 - \frac{T_{BP}(\theta)}{T_{GC}}
\]

(11)

where the composite soil vegetation surface temperature \( T_{GC} \) was estimated from the ERA-INTERIM 0-7cm soil temperature product (T\textsubscript{E-07}).

The method of Mattar et al. (2012) is very similar and can be written as (referred to as ‘Mattar’):

\[
\ln (SM) = c_2 \ln (\Gamma_p(\theta)) + c_1 \text{NDVI} + c_0 (\theta, p)
\]

(12)

where the NDVI is considered here as a proxy for optical depth, as in the SCA-H and SCA-V methods.
In the above equations (9), (10) and (12), the parameters \((a_0, a_1, a_2), (b_0, b_1, b_2)\) and \((c_0, c_1, c_2)\) are regression coefficients, which are assumed to be constant in time and have to be calibrated over each pixel. In this study, in the ‘Saleh bi-polarization’ equation (10), we used the observation angle \(\theta = 40^\circ\) as used in the other retrieval methods. In the ‘Saleh bi-angular’ equation (9), we used H-polarized bi-angular observations at \(\theta_1 = 30^\circ\) and \(\theta_2 = 50^\circ\). In the ‘Mattar’ equation (12), we used H-polarized observations at \(\theta = 40^\circ\). These latter configurations were found to be the best for SM retrievals (results not shown here).

### 2.5 Method calibration

In this study, the SCA-V, SCA-H, DCA and LPRM methods were based on the L-MEB model parameters given in Table 1. In addition, some model parameters specific to some methods had to be calibrated. The DCA and LPRM methods did not require any additional calibration. Conversely, in the SCA-V and SCA-H methods, the two parameters \(b\) and Stemfactor, used to link NDVI and optical depth, had to be calibrated. Moreover, the three ‘regression’ methods ‘Saleh bi-angular’, ‘Saleh bi-polarization’ and ‘Mattar’ did not require any L-MEB parameters but required the calibration of three coefficients \((a_i), (b_i)\) or \((c_i)\) \((i = 0, 1\) and 2) used in equations (8), (9) and (11), respectively.

The calibration of the above parameters and coefficients was performed three times, using one year of data for calibration and the two other years for validation. To calibrate the \(b\) and Stemfactor parameters in SCA-H and SCA-V, a multilinear regression method was used to fit the optical depth derived from equations (6) and (7) to the ‘reference’ optical depth \(\tau_{\text{NAD}}\) retrieved from the 2-P L-MEB method. The obtained values for all three calibration years (2010, 2011 and 2012) are given in Table 3.

Similarly, to calibrate the three coefficients in the regression equations of the ‘Saleh bi-angular’, ‘Saleh bi-polarization’ and ‘Mattar’ methods, a multilinear regression method was used to minimize the difference between the retrieved SM derived from equations (9), (10) or (12) to the ‘reference’ SM values retrieved from the 2-P L-MEB method. The obtained values of the coefficients for all three methods and all three calibration years (2010, 2011 and 2012) are given in Table 3.

### 3. Results
3.1. Reference values of SM and $\tau_{\text{NAD}}$

As outlined above, the ‘reference’ values of soil moisture (SM) and optical depth at nadir ($\tau_{\text{NAD}}$) were retrieved from the multiangular T$_B$ data measured by the ELBARA-II instrument. The T$_B$ measured $\theta = 40^\circ$ for the time period 2010-2012 are shown in Fig. 2. A clear seasonal cycle in the T$_B$ time-series can be seen, with maximum values of T$_B$ during summer and lower T$_B$ values during winter. This annual cycle is related to the vegetation growth cycle, beginning in April and ending in November, and to the soil moisture conditions, which are generally drier during the summer period.

However, as already noted in Section 2.2, significantly wetter/drier conditions were encountered in 2010/2012, respectively, which is reflected in the observed T$_B$ trends over the MELBEX-II site with lower values during summer 2010 compared to summer 2012. Based on these T$_B$ observations, the retrieved values of SM and $\tau_{\text{NAD}}$ were computed from the 2-P L-MEB method and they are illustrated in Fig. 3a-b. As discussed in Jackson et al. (2012), conditions of standing water during or shortly after intensive rainfalls should be flagged. In this study, to avoid these conditions, all retrieved values of SM which were found to be larger than the saturation value SM$_{\text{SAT}}$ were not considered (SM$_{\text{SAT}}$ was set equal to 0.5 m$^3$/m$^3$ over the M-III site as computed by Juglea et al. (2010)). Note that due to this data filtering, the number of SM data used in the comparison may vary slightly from one approach to the other.

In accordance with the above-discussed T$_B$ trends one can see that rainy conditions led generally to higher values of SM throughout the year in 2010 and during the winter period in 2011 and 2012 (Fig. 3a). Drier conditions during the second half of 2011 and 2012 led to rather long time intervals of lower SM values.

The vegetation cycle could be clearly distinguished from the time variations in both the optical depth at nadir ($\tau_{\text{NAD}}$) and NDVI index obtained over the 250 m MODIS pixel including the M-III vineyard (Fig. 3b). Relatively similar maximum values of $\tau_{\text{NAD}}$ were retrieved during the summer of all three years (maximum values of $\tau_{\text{NAD}}$ are close to 0.24 in 2010 and close to 0.22 in 2011 and 2012). During the winter period, after vine pruning and defoliation, values of $\tau_{\text{NAD}}$ close to 0.05 were retrieved for all three years. This latter value corresponds to the estimated value of the optical depth ($\tau_{\text{STOCK}}$) of vine stocks (Schwank et
Superimposed on the long term trend of $\tau_{\text{NAD}}$, short-time changes in the time variations of $\tau_{\text{NAD}}$ can be noted. It is likely that these apparent fluctuations result from unaccounted for changes in the roughness conditions over the field as discussed in Patton and Hornbuckle (2013) and Jackson et al. (2012) for SMOS observations. It can be noted too that very low values of $\tau_{\text{NAD}}$ were retrieved during a short period of time in May of 2011 and 2012, just before the vine vegetation growth. We assumed that this could be caused by specific effects during this period related to soil roughness or to vegetation structure. For instance, this effect could be linked to lower roughness conditions in relation to field works in May. As the roughness parameterization is set as constant over the 3 year period, actual lower roughness conditions in the field would lead to retrievals of lower $\tau_{\text{NAD}}$ values and, to a lesser extent, higher SM values. Our field observations of roughness for the year 2012 (Fig. 1) are not accurate enough to confirm clearly this assumption but they seem to be leaning in that direction.

A maximum value of NDVI is reached in the middle of July (~ DoY 200): $\text{NDVI}_\text{MAX} \approx 0.45$ in 2010 and 2011 and $\text{NDVI}_\text{MAX} \approx 0.36$ in 2012. It is likely the lower value of $\text{NDVI}_\text{MAX}$ in 2012 can be related to the drier conditions during that year. In comparison with the year 2011, it seems that the very dry conditions during 2012 impact the NDVI values, but do not impact the time variations of $\tau_{\text{NAD}}$ considerably.

A scatter plot of the retrieved values of the optical depth $\tau_{\text{NAD}}$ versus the NDVI index is shown in Fig. 4. It can be seen that the results are generally consistent from one year to the other. One specific pattern can be noted in 2011; it corresponds to very low values of $\tau_{\text{NAD}}$ retrieved while vegetation is fully developed ($\text{NDVI} \approx 0.45$), which was already discussed above.

### 3.3 Comparison of SM Retrievals

The retrieved values of SM from all retrieval methods presented in section 2 were compared to the reference SM values retrieved with the 2-P L-MEB method applied to the measurements performed during the years 2010-2012. A summary of this comparison is given in Table 4, in terms of coefficient of determination ($R^2$), bias ($m^3/m^3$), RMSE ($m^3/m^3$) and unbiased RMSE (ubRMSE, $m^3/m^3$) as defined by Entekhabi et al. (2010). To illustrate the
results, scatter plots of retrieved SM values versus ‘reference’ SM values are given for all methods considered in this study (Fig. 5).

All five methods requiring a calibration step, e.g. SCA-V, SCA-H, ‘Saleh’ bi-angular, ‘Saleh’ bi-polarization and ‘Mattar’ (the calibration was made using one year and the evaluation with the two other years), provided SM retrievals that were in good agreement with the ‘reference’ SM data ($R^2$ is generally higher than 0.90, and the RMSE is lower than 0.045 m$^3$/m$^3$). If we consider the years used for calibration, best performances in terms of $R^2$ for all four methods were obtained when year 2010 (corresponding to rather ‘wet’ conditions) was used for calibration, while lower performances were obtained using the year 2012 (corresponding to ‘very dry’ conditions) for calibration. Results for the year 2011 are generally close to those obtained for the year 2010. A closer inspection shows that both the SCA-V and the SCA-H methods provide generally very similar performances in SM retrievals (the SCA-V method providing a slightly better accuracy in terms of $R^2$, bias, RMSE and ubRMSE). The three methods based on regression equations (‘Saleh’ bi-polarization, ‘Saleh’ bi-angular, and ‘Mattar’) provided very similar results too. Slightly lower performances were obtained for the ‘Mattar’ method (especially when using the year 2010 for calibration), while best performances were obtained for ‘Saleh bi-angular’. Considering the ubRMSE criteria, the performances of the SCA and the regression methods were even closer. Except for the DCA and LPRM algorithm, the ubRMSE is always around or below the target accuracy for SMAP of 0.04 m$^3$/m$^3$. This is a direct consequence of the fact that values of the bias were found to be higher for the SCA methods (bias $\approx 0.020$ m$^3$/m$^3$) than for the regression methods (bias $\approx 0.010$ m$^3$/m$^3$).

As could be expected, results obtained from methods which did not require parameter calibration (DCA and LPRM) provided results with a lower accuracy: the RMSE was similar for both methods (RMSE $\approx 0.55$ m$^3$/m$^3$), while slightly better $R^2$ values were obtained for DCA ($R^2 = 0.79$) than for LPRM ($R^2 = 0.725$). For both methods, the bias in the retrievals was found to be very low (bias $= 0.021$ m$^3$/m$^3$ for DCA, and bias $= 0.013$ m$^3$/m$^3$ for LPRM).

The scatter plots (Fig. 5) showing the comparison between retrieved SM values versus ‘reference’ SM values are given to illustrate these different results. For methods requiring calibration (SCA-V, SCA-H, ‘Saleh’ bi-angular, ‘Saleh’ bi-polarization and ‘Mattar’), we used the year 2010 in Fig. 5 (this year provided best performances in terms of $R^2$). Note that
the number of data used in the comparison may vary from one approach to the other. This can be explained by two reasons. First, for DCA and LPRM, the comparison was made over three years (2010 - 2012), while it was made over two years (2011 -2012) for the other methods. Second, retrieved SM values larger than the saturation value SM_{SAT} (SM_{SAT} = 0.5 \text{ m}^3/\text{m}^3) were removed in the comparison (a very low number of observations was concerned by this filtering).

It can be seen that a very low bias was obtained generally. However, in wet conditions, the methods LPRM and DCA provided underestimated SM values (for SM > 0.3 \text{ m}^3/\text{m}^3); while the ‘Saleh’ and ‘Mattar’ methods provided overestimated SM values (for SM > 0.2 \text{ m}^3/\text{m}^3) with respect to the reference SM. For DCA and LPRM (methods with do not require any calibration), it can be seen that the SM retrieval performances are lower in a small SM interval, for values of SM comprised between ~ 0.1 and 0.15 \text{ m}^3/\text{m}^3. These SM conditions generally correspond to periods of vegetation growth at the end of spring and of full vegetation development in the summer period.

4. Discussion and conclusion

This study presents an inter-comparison of several SM retrieval methods based on a three year data set of passive L-band microwave observations acquired over a vineyard site at the VAS site.

A careful interpretation of the results should be made, and the results cannot be easily generalized to operational applications for spaceborne sensors. We will discuss these different aspects and the main conclusions of the study in the following. First, it is important to consider that the results were obtained at the field scale and over only one type of vegetation (a vineyard canopy) with some specific features (no litter layer, relatively low LAI and biomass conditions, frequent agricultural practices leading to changes in soil roughness, etc.). Several effects related to changes in the soil roughness conditions or in the vegetation structure (in relation with the crop growth and the agricultural practices) may have a significant impact on the results of the present study. It is likely that the impact of these effects would average out and, therefore, become much less important if we had considered larger footprints of spaceborne radiometric observations, including a large variety in the types of vegetation (natural or cultivated canopies), in the soil conditions and in the agricultural
practices. For instance, specific effects related to the vegetation structure could be revealed over the vineyard field and the values of optical depth for both polarizations ($\tau_H(0)$ and $\tau_V(0)$) could not be considered as equal for that canopy type (Wigneron et al., 2012). This result has frequently been obtained from *in situ* radiometric observations (Pardé et al., 2003, 2004; Wigneron et al., 2004) but it has never been noted, to our knowledge, from spaceborne observations. For instance, Owe et al. (2001) found that $\tau_V = \tau_H$ over test sites in the US over a variety of land covers based on SMMR (Scanning Multichannel Microwave Radiometer) observations at C-band. It is likely that these vegetation structure effects can be a limitation for presented evaluation of the methods, which all assume $\tau_H = \tau_V$. So, several similar studies based on *in situ* observations over a variety of vegetation types are required to provide a more in-depth evaluation of the method performances.

It should be noted too that the performances of the different methods cannot be compared directly as some methods had to be calibrated while some methods did not require any parameter calibration step (DCA and LPRM). The two methods SCA-H and SCA-V, require the calibration of the relationship between optical depth and a remotely sensed vegetation index (NDVI); the three methods based on regression equations, ‘Saleh bi-angular’, ‘Saleh bi-polarization’ and ‘Mattar’, require the calibration of three coefficients. This calibration step could be done in the present study as we considered that a ‘reference’ data set describing the time variations in SM and $\tau_{NAD}$ (and derived from multi-angular observations) was available from the ELBARA-II tower-based observations. However, for operational spatial applications, it is generally very difficult to obtain such a reference data set.

In spite of the limitations discussed above, some key results obtained in this study from tower-based observations could be of value to future operational applications. It was found that the two methods, which did not require any a priori calibration (DCA and LPRM) could provide good SM retrievals and have relatively similar performances ($R^2 \sim 0.72-0.79$; $\text{RMSE} \sim 0.054-0.58$ m$^3$/m$^3$) over the three year period. The methods requiring parameter calibration (two parameters in SCA-H and SCA-V; three coefficients in the three regression methods) provided results closer to the reference: for instance the $R^2$ coefficient increased generally to values larger than 0.90 for all methods. The methods which require additional information concerning the vegetation development (the NDVI variable is required in the SCA-H, SCA-V and ‘Mattar’ algorithms) provided slightly lower performances when year 2012 was used for calibration. For that year the NDVI values were lower than for the two
other years (maximum NDVI values ≈ 0.45 in 2010 and 2011 and ≈ 0.36 in 2012), while the
maximum values of $\tau_{\text{NAD}}$ were found to be relatively similar over all three years ($\approx 0.22 - 0.24$). It is likely that nonlinearities between $\tau_{\text{NAD}}$ and NDVI led to these slightly lower performances in SM retrievals for the year 2012 for the SCA and ‘Mattar’ algorithms.

In the present study, the computed performances are “optimal” performances as it is assumed that a good parameter calibration can be made from a SM data set which can be considered as a reference. This calibration step was possible in this study based on in situ tower-based observations obtained over a homogeneous vineyard field, but this step is much more complex for operational applications based on space borne sensors. Several options are possible to calibrate these different retrieval methods for spaceborne applications. For instance, the reference SM or $\tau_{\text{NAD}}$ values which are required in the calibration step can be estimated:

(i) from networks of in situ measurement sites such as SCAN in the USA (Schaefer et al., 2007), OZNET in Australia (Smith et al., 2012) or SMOSMANIA in France (Albergel et al., 2012), etc. Then, based on results obtained over a variety of soil and vegetation conditions, a look up table providing the calibrated parameters as function of the land cover types can be built.

(ii) from model re-analyses (ERA-Interim (Dee et al., 2011) or MERRA Land (Reichle et al., 2012) for instance), in regions where the simulated SM values can be considered to be accurate. As mentioned above, in a second step, a look up table can be built for a variety of land covers.

(iii) by combining observations from different remote sensing sensors. For instance, the estimation of optical depth $\tau_{\text{NAD}}$ retrieved from SMOS or other satellites (e.g. AMSR-2) could be used to calibrate the vegetation parameters required in the SCA-H and SCA-V algorithms (Lawrence et al., 2014).

Future work will consider these different options to evaluate the retrieval capabilities of the different methods requiring calibration (SCA, ‘Saleh’ or Mattar’) for operational applications based on spaceborne sensors.
Acknowledgments

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References


\url{http://www.esa-soilmoisture-cci.org/}


Table 1.

L-MEB soil and vegetation parameters over the M-III vineyard (VAS site). All these parameters, except \( t_t \) and \( t_v \) which are specific to L-MEB, are valid for the other SM retrieval methods.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Value or used Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Soil dielectric permittivity ( \varepsilon_s )</td>
<td>(-)</td>
<td>Mironov et al. (2012)</td>
</tr>
<tr>
<td>Clay fraction</td>
<td>(-)</td>
<td>0.26 (in situ measurements; Juglea et al., 2010)</td>
</tr>
<tr>
<td>( T_G = T_c = T_GC )</td>
<td>K</td>
<td>ECMWF ERA Interim temperature ( T_{E407} )</td>
</tr>
<tr>
<td>( H_R )</td>
<td>(-)</td>
<td>0.6060 (calibrated, Lawrence et al., 2013)</td>
</tr>
<tr>
<td>( Q_R )</td>
<td>(-)</td>
<td>0.0303 (calibrated, Lawrence et al., 2013)</td>
</tr>
<tr>
<td>( N_{RH} )</td>
<td>(-)</td>
<td>0</td>
</tr>
<tr>
<td>( N_{RV} )</td>
<td>(-)</td>
<td>0</td>
</tr>
<tr>
<td>( t_t )</td>
<td>(-)</td>
<td>1</td>
</tr>
<tr>
<td>( t_v )</td>
<td>(-)</td>
<td>Free parameter in the retrieval process</td>
</tr>
<tr>
<td>( \omega )</td>
<td>(-)</td>
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</tr>
<tr>
<td>( \tau )</td>
<td>(-)</td>
<td>Free parameter in the retrieval process</td>
</tr>
<tr>
<td>SM</td>
<td>m(^3)/m(^3)</td>
<td>Free parameter in the retrieval process</td>
</tr>
</tbody>
</table>
Table 2.
Input variables required in the different retrieval algorithms

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Input variables</th>
</tr>
</thead>
<tbody>
<tr>
<td>SCA-H</td>
<td>$T_{BH}(\theta=40^\circ)$</td>
</tr>
<tr>
<td></td>
<td>ECMWF temperature ($T_{E-07}$)</td>
</tr>
<tr>
<td></td>
<td>NDVI</td>
</tr>
<tr>
<td>SCA-V</td>
<td>$T_{BV}(\theta=40^\circ)$</td>
</tr>
<tr>
<td></td>
<td>ECMWF temperature ($T_{E-07}$)</td>
</tr>
<tr>
<td></td>
<td>NDVI</td>
</tr>
<tr>
<td>DCA</td>
<td>$T_{BH}(\theta=40^\circ), T_{BV}(\theta=40^\circ)$</td>
</tr>
<tr>
<td></td>
<td>ECMWF temperature ($T_{E-07}$)</td>
</tr>
<tr>
<td>LPRM</td>
<td>$T_{BH}(\theta=40^\circ), T_{BV}(\theta=40^\circ)$</td>
</tr>
<tr>
<td></td>
<td>ECMWF temperature ($T_{E-07}$)</td>
</tr>
<tr>
<td>‘Saleh’</td>
<td>$T_{BH}(\theta=40^\circ)$</td>
</tr>
<tr>
<td>bi-polarization</td>
<td>ECMWF temperature ($T_{E-07}$)</td>
</tr>
<tr>
<td>‘Saleh’,</td>
<td>$T_{BH}(\theta=40^\circ)$</td>
</tr>
<tr>
<td>bi-angular</td>
<td>ECMWF temperature ($T_{E-07}$)</td>
</tr>
<tr>
<td>‘Mattar’</td>
<td>$T_{BH}(\theta=40^\circ)$</td>
</tr>
<tr>
<td></td>
<td>ECMWF temperature ($T_{E-07}$)</td>
</tr>
<tr>
<td></td>
<td>NDVI</td>
</tr>
</tbody>
</table>
Table 3.

Calibrated parameters of the different retrieval algorithms: one year (2010, 2011 or 2012) is used for calibration; the two other years are used for validation

**SCA H/V, T_{BH}(\theta=40) or T_{BV}(\theta=40)**

<table>
<thead>
<tr>
<th>Calibration</th>
<th>b</th>
<th>Stemfactor</th>
</tr>
</thead>
<tbody>
<tr>
<td>2010</td>
<td>0.61679</td>
<td>0.20874</td>
</tr>
<tr>
<td>2011</td>
<td>0.31756</td>
<td>0.44014</td>
</tr>
<tr>
<td>2012</td>
<td>0.92819</td>
<td>0.05840</td>
</tr>
</tbody>
</table>

**‘Saleh bi-angular’, T_{BH}(\theta=30), T_{BH}(\theta=50)**

<table>
<thead>
<tr>
<th>Calibration</th>
<th>a₀</th>
<th>a₁</th>
<th>a₂</th>
</tr>
</thead>
<tbody>
<tr>
<td>2010</td>
<td>1.4171</td>
<td>-0.3560</td>
<td>0.8374</td>
</tr>
<tr>
<td>2011</td>
<td>1.0972</td>
<td>-0.2806</td>
<td>0.2613</td>
</tr>
<tr>
<td>2012</td>
<td>2.2857</td>
<td>-1.5674</td>
<td>0.1300</td>
</tr>
</tbody>
</table>

**‘Saleh bi-polarization’, T_{BH}(\theta=40), T_{BV}(\theta=40)**

<table>
<thead>
<tr>
<th>Calibration</th>
<th>b₀</th>
<th>b₁</th>
<th>b₂</th>
</tr>
</thead>
<tbody>
<tr>
<td>2010</td>
<td>0.3524</td>
<td>0.7734</td>
<td>1.1401</td>
</tr>
<tr>
<td>2011</td>
<td>0.2595</td>
<td>0.6208</td>
<td>0.4879</td>
</tr>
<tr>
<td>2012</td>
<td>-0.3914</td>
<td>1.1927</td>
<td>0.7263</td>
</tr>
</tbody>
</table>

**‘Mattar’, T_{BH}(\theta=40)**

<table>
<thead>
<tr>
<th>Calibration</th>
<th>c₀</th>
<th>c₁</th>
<th>C₂</th>
</tr>
</thead>
<tbody>
<tr>
<td>2010</td>
<td>1.2530</td>
<td>0.9491</td>
<td>0.9147</td>
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<tr>
<td>2011</td>
<td>0.9844</td>
<td>0.5748</td>
<td>0.3702</td>
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<tr>
<td>2012</td>
<td>1.0954</td>
<td>2.6578</td>
<td>0.0183</td>
</tr>
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</table>
Table 4.

Performances of the different SM retrieval algorithms in terms of coefficient of determination ($R^2$), bias (m$^3$/m$^3$), RMSE (m$^3$/m$^3$) and ubRMSE (m$^3$/m$^3$). For SCA-H, SCA-V, ‘Saleh bi-angular’, ‘Saleh bi-polarization’ and ‘Mattar’, one year (2010, 2011 or 2012) is used for calibration; the two others are used for validation. For LPRM and DCA, no calibration is required.

<table>
<thead>
<tr>
<th>Method</th>
<th>Calibration</th>
<th>Validation</th>
<th>$R^2$</th>
<th>Bias (m$^3$/m$^3$)</th>
<th>RMSE (m$^3$/m$^3$)</th>
<th>ubRMSE (m$^3$/m$^3$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SCA-H</td>
<td>2010</td>
<td>2011, 2012</td>
<td>0.915</td>
<td>-0.025</td>
<td>0.050</td>
<td>0.043</td>
</tr>
<tr>
<td></td>
<td>2011</td>
<td>2010, 2012</td>
<td>0.905</td>
<td>-0.041</td>
<td>0.054</td>
<td>0.035</td>
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<tr>
<td></td>
<td>2012</td>
<td>2010, 2011</td>
<td>0.852</td>
<td>-0.020</td>
<td>0.056</td>
<td>0.052</td>
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<tr>
<td>SCA-V</td>
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<td>2011, 2012</td>
<td>0.928</td>
<td>-0.014</td>
<td>0.035</td>
<td>0.032</td>
</tr>
<tr>
<td></td>
<td>2011</td>
<td>2010, 2012</td>
<td>0.919</td>
<td>-0.024</td>
<td>0.040</td>
<td>0.032</td>
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<tr>
<td></td>
<td>2012</td>
<td>2010, 2011</td>
<td>0.861</td>
<td>-0.010</td>
<td>0.045</td>
<td>0.043</td>
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<tr>
<td>DCA</td>
<td></td>
<td></td>
<td>0.789</td>
<td>0.021</td>
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<tr>
<td>LPRM</td>
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<td></td>
<td>0.725</td>
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<td>0.004</td>
<td>0.037</td>
<td>0.037</td>
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<tr>
<td></td>
<td>2011</td>
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<td>0.941</td>
<td>0.007</td>
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<td>0.027</td>
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<tr>
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<td>2012</td>
<td>2010, 2011</td>
<td>0.934</td>
<td>0.009</td>
<td>0.036</td>
<td>0.035</td>
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<tr>
<td>Saleh Bi-polarization</td>
<td>2010</td>
<td>2011, 2012</td>
<td>0.946</td>
<td>0.010</td>
<td>0.040</td>
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<tr>
<td></td>
<td>2011</td>
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<td>0.924</td>
<td>-0.001</td>
<td>0.031</td>
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<tr>
<td></td>
<td>2012</td>
<td>2010, 2011</td>
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<td>0.033</td>
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<tr>
<td>Mattar</td>
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<td>0.041</td>
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<tr>
<td></td>
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<td></td>
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<td>0.869</td>
<td>0.017</td>
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<td>0.045</td>
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</table>
Fig. 1. Temporal variations in the standard deviation of soil surface heights $S_D$ and correlation length $L_C$ estimated from measurements during seven days in 2012 performed at the M-III vineyard field. The annual mean values are $\langle S_D \rangle = 2.2$ cm, $\langle L_C \rangle = 6.2$ cm.

Fig. 2. Time-series of measured ELBARA-II $T_B$ over the M-III vineyard during three years (2010-2012) at H (‘o’) and V (‘x’) polarizations and at the observation angle $\theta = 40^\circ$. The $T_B$ data are acquired ~ every 30 minutes but only data measured at 6 am are shown. Diurnal precipitation $P$ is represented with vertical lines.

Fig. 3. Soil moisture SM (a) and optical depth $\tau_{\text{NAD}}$ (b) retrieved with the multiangular 2-P L-MEB method applied to the measurements at the M-III site. The diurnal retrievals are shown for 6 am and 6 pm, respectively. These retrieved values are considered as a reference in this study. Diurnal precipitation is represented with vertical lines. In Fig 3b, the time-series of NDVI index obtained over the 250 m MODIS pixel including the M-III vineyard is shown.

Fig. 4. Scatter plot of retrieved values of the optical depth $\tau_{\text{NAD}}$, retrieved with the multiangular 2-P L-MEB method, versus the NDVI index obtained over the 250 m MODIS pixel including the M-III vineyard. Retrieved values of $\tau_{\text{NAD}}$ computed at 6 am and 6 pm are used.

Fig. 5. Scatter plots of the retrieved SM values versus the reference SM values for all methods: SCA-H (a), SCA-V (b), DCA (c), LPRM (d), ‘Saleh’ bi-angular (e), ‘Saleh’ bi-polarization (f) and ‘Mattar’ (g). Retrieved values of SM are computed at 6 am and 6 pm. In Fig. 5a-b-e-f-g, retrieved values of SM for years 2011 and 2012 are shown (the year 2010 was used for calibration). In Fig. 5c-d (for DCA and LPRM) retrieved values of SM for years 2011, 2012 and 2013 are shown (no calibration was required).
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a)
Optical Depth (TAU) and NDVI

YEAR

Mar/10 Jun/10 Sep/10 Dec/10 Apr/11 Jul/11 Oct/11 Feb/12 May/12 Aug/12 Nov/12
Fig. 4. Scatter plot of retrieved values of the optical depth $\tau_{NAD}$, retrieved with the multiangular 2-P L-MEB method, versus the NDVI index obtained over the 250m MODIS pixel including the M-III vineyard. Retrieved values of $\tau_{NAD}$ computed at 6 am and 6 pm are used.

$\text{TAU} = a_1 \times \text{NDVI} + a_0$

$a_1 = 0.484$

$a_0 = -0.055$
Fig. 5. Scatter plots of the retrieved SM values versus the reference SM values for all methods: SCA-H (a), SCA-V (b), DCA (c), LPRM (d), ‘Saleh’ bi-angular (e), ‘Saleh’ bi-polarization (f) and ‘Mattar’ (g). Retrieved values of SM are computed at 6 am and 6 pm. In Fig. 5a-b-e-f-g, retrieved values of SM for years 2011 and 2012 are shown (the year 2010 was used for calibration). In Fig. 5c-d (for DCA and LPRM) retrieved values of SM for years 2011, 2012 and 2013 are shown (no calibration was required).
b)

![Graph showing the relationship between retrieved soil moisture (SM) and reference SM. The graph includes statistical metrics such as R2, bias, and RMSE.](image)

- N = 1106
- R2 = 0.921
- Bias = -0.014 m³/m³
- RMSE = 0.038 m³/m³
N = 1286
R² = 0.812
bias = 0.017 m³/m³
RMSE = 0.059 m³/m³

DCA
d)

![Graph showing scatterplot with LPRM text]

- N = 1378
- $R^2 = 0.763$
- bias = 0.009 m³/m³
- RMSE = 0.062 m³/m³
e) N = 1108
R^2 = 0.942
bias = 0.005 m^3/m^3
RMSE = 0.040 m^3/m^3

Saleh biangular
N = 1108
R² = 0.939
bias = 0.010 m³/m³
RMSE = 0.044 m³/m³