Assimilation of Freeze/Thaw Observations into the NASA Catchment Land Surface Model

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Abstract

The land surface freeze/thaw (F/T) state plays a key role in the hydrological and carbon cycles and thus affects water and energy exchanges and vegetation productivity at the land surface. In this study, we developed an F/T assimilation algorithm for the NASA Goddard Earth Observing System, version 5 (GEOS-5) modeling and assimilation framework. The algorithm includes a newly developed observation operator that diagnoses the landscape F/T state in the GEOS-5 Catchment land surface model. The F/T analysis is a rule-based approach that adjusts Catchment model state variables in response to binary F/T observations, while also considering forecast and observation errors. A regional observing system simulation experiment was conducted using synthetically generated F/T observations. The assimilation of perfect (error-free) F/T observations reduced the root-mean-square errors (RMSE) of surface temperature and soil temperature by 0.206 °C and 0.061 °C, respectively, when compared to model estimates (equivalent to a relative RMSE reduction of 6.7% and 3.1%, respectively). For a maximum classification error ($C_{E_{\text{max}}}$) of 10% in the synthetic F/T observations, the F/T assimilation reduced the RMSE of surface temperature and soil temperature by 0.178 °C and 0.036 °C, respectively. For $C_{E_{\text{max}}}=20\%$, the F/T assimilation still reduces the RMSE of model surface temperature estimates by 0.149 °C but yields no improvement over the model soil temperature estimates. The F/T assimilation scheme is being developed to exploit planned operational F/T products from the NASA Soil Moisture Active Passive (SMAP) mission.
1. Introduction

Over one-third of the global land area undergoes a seasonal transition between predominantly frozen and non-frozen conditions each year (Kim et al. 2011). This land surface freeze/thaw (F/T) transition is closely linked to the timing and length of the vegetation growing season (e.g. Black et al. 2000; Grippa et al. 2005; Kimball et al. 2006), the seasonal evolution of land-atmosphere carbon dioxide exchange (Goulden et al. 1998) and the timing of seasonal snowmelt, soil thaw and spring flood pulses (Kimball et al. 2001; Rawlins et al. 2005; Kane et al. 2008). The land surface F/T state thus acts as a natural on/off switch for hydrological and biospheric processes over northern land areas and upper elevations where seasonal frozen temperatures represent a significant portion of the annual cycle (Kim et al. 2011).

Studies show that the growing season, vegetation productivity and land-atmosphere CO$_2$ exchange patterns are shifting as a result of global warming (e.g. Randerson et al. 1999; Nemani et al. 2003). For example, Smith et al. (2004), McDonald et al. (2004) and Kimball et al. (2006) found consistency between these patterns and changes in seasonal F/T dynamics observed by satellite microwave remote sensing. Thus, for more accurate modeling and prediction of land surface hydrological and biospheric processes, a good representation of the landscape F/T state in land surface schemes is needed. Recent efforts to enhance F/T modeling through improved and more expansive representation of permafrost include work on the Community Land Model (CLM; Lawrence et al. 2008; Lawrence et al. 2012), ORCHIDEE (Koven et al. 2009), the joint UK Land Environment Simulator (JULES; Dankers et al. 2011) and the pan-Arctic Water Balance Model (Rawlins et al. 2013).

Surface air temperature measurements from regional weather stations can provide an indication of the landscape F/T state. However, the limited coverage of global weather station
networks, especially at higher latitudes and elevations, severely limits the capability for global monitoring and the ability to capture F/T spatial and temporal patterns (Kim et al. 2011). Satellite observations of passive and active microwaves are well suited for characterizing the landscape F/T state (Frolking et al. 1999; Bateni et al. 2012; Kontu et al. 2010). Lower frequency (≤ 37 GHz) microwave observations vary significantly between frozen and thawed landscapes as a result of the strong sensitivity to contrasting dielectric properties. A number of algorithms have been developed to detect the landscape F/T state at 25 – 50 km resolution using brightness temperature measurements from the Advanced Microwave Scanning Radiometer for the Earth Observing System (Zhao et al. 2011), the Scanning Multichannel Microwave Radiometer (Zuerndorfer et al. 1992), the Special Sensor Microwave Imager (Zhang et al. 2001) and the Soil Moisture and Ocean Salinity mission (Kontu et al. 2010). Similarly, radar backscatter data have been utilized in several studies for the detection of the land surface F/T state (Frolking et al. 1999; Kimball et al. 2001; Bartsch et al. 2011). The L-band (1.4 GHz) radar observations from the Soil Moisture Active Passive (SMAP) mission (to be launched in 2014) will provide a global classification of the F/T state at a 3 km spatial resolution and with a 3-day temporal fidelity (Entekhabi et al. 2012).

The assimilation of remotely sensed F/T retrievals into land surface models might improve the simulation of carbon and hydrological processes that are especially relevant during F/T transitions. In this study the potential of the F/T assimilation to improve estimates of land surface (skin) and soil temperature is investigated. To this end, an algorithm was developed for the assimilation of binary F/T observations into the NASA Catchment land surface model (Koster et al. 2000) within the NASA Goddard Earth Observing System, version 5 (GEOS-5) modeling and assimilation framework. The assimilation algorithm includes a newly developed
observation operator that diagnoses the F/T state of the Catchment model and is compatible with the information contained in the remotely sensed landscape F/T state at different microwave frequencies. The F/T analysis consists of a rule-based approach that updates Catchment model prognostic variables for surface and soil temperature in response to binary F/T observations and considers forecast and observation errors. In order to test the methodology, an observing system simulation experiment is conducted using synthetically generated F/T observations. The ultimate goal of this study is to provide a framework for the assimilation of F/T retrievals from SMAP into the Catchment model in the context of the SMAP Level 4 Surface and Root Zone Soil Moisture (L4_SM) algorithm (Reichle et al. 2012) and the SMAP Level 4 Carbon algorithm (Kimball et al. 2012). Future research will explore the direct assimilation of brightness temperature or backscatter measurements to analyze the landscape F/T state.

2. F/T detection using remote sensing

At microwave frequencies, the landscape dielectric constant and thus the radar backscatter and the emission of passive microwaves undergo large temporal changes associated with corresponding changes in the predominant landscape F/T state within the satellite footprint (Mironov et al. 2010), which makes space-borne microwave measurements well suited for global F/T monitoring (Kim et al. 2011). In most studies, 0 °C is considered the temperature threshold between the frozen and thawed states (Colliander et al. 2012). The temperature at which the F/T transition occurs, however, varies with the water solute concentration and shows strong heterogeneity across different landscape elements and within the satellite field of view. Thus, the 0 °C threshold is only an approximation of the landscape F/T transition point.
The contribution of different land surface elements to the retrieved F/T index depends on the microwave frequency used for the F/T classification. Colliander et al. (2012) used QuickScat Ku band (13.4 GHz) backscatter measurements to investigate the relationship between individual land surface elements (e.g. soil, snow cover, and vegetation) and the aggregate landscape F/T state indicated by the surface backscatter. It was observed that the temperature of the soil and that of vegetation stems and branches are generally better indicators of Ku band F/T dynamics than surface air temperature, with soil temperature being a better indicator than vegetation temperature. Colliander et al. (2012) did not consider the effect of snow cover despite the fact that for their study domain the frozen condition is dominated by a snow-covered landscape. The rationale for their approach is the fact that the landscape thawing can be detected even under snow-covered conditions, as demonstrated by Kimball et al. (2004a,b) using Ku-band measurements from the NASA Scatterometer. Due to their longer wavelength, L-band (1.4 GHz) observations from SMAP should be less sensitive to snow and vegetation scattering effects under dry/frozen snow conditions and penetrate more deeply into the soil than Ku-band measurements. This increases the sensitivity of the microwave signals to the F/T state of the underlying surface soil layer.

However, for wet snow the penetration depth of microwaves is drastically reduced to a few centimeters or less (Mätzler et al. 1984). Thus, sensitivity to soil conditions is minimal under wet snow and the satellite signal will largely reflect snow cover conditions when a significant amount of wet snow is present on the surface.
3. F/T diagnosis using the Catchment land surface model

This section first provides a brief description of the NASA GEOS-5 Catchment model (Koster et al. 2000; Ducharne et al. 2000; Reichle et al. 2011; Reichle 2012), a state-of-the-art global land surface model. Next, an observation operator is introduced for the diagnosis of the landscape F/T state in the model. This observation operator is needed for the F/T analysis (section 4) and designed to be compatible with the information contained in remotely sensed F/T observations at different microwave frequencies.

a. Catchment model overview

The Catchment model’s basic computational unit is the hydrological catchment (or watershed). In each catchment, the vertical profile of soil moisture is determined by the equilibrium soil moisture profile from the surface to the water table and by two additional variables that describe deviations from the equilibrium profile in a 1-m root zone layer and in a 2-cm surface layer, respectively. Based on soil moisture, each catchment is separated into three distinct and dynamically varying subareas: a saturated region, an unsaturated region and a wilting region. The Catchment model also includes a three-layer snow model that accounts for snow melting and refreezing, dynamic changes in snow density, snow insulating properties, and other physics relevant to the growth and ablation of the snowpack (Stieglitz 1994).

In the snow-free portion of the catchment, the surface energy balance is computed separately for the saturated, unsaturated, and wilting subareas of each catchment. In each of these three subareas, the land surface temperature is modeled with surface temperature prognostic variables that are specific to the soil moisture regime ($T_{C1}$ for the saturated region, $T_{C2}$ the for unsaturated region and $T_{C4}$ for wilting region). For tropical forest land tiles, the $T_{C1}$, $T_{C2}$ and $T_{C4}$ fields are tied
to approximately the top 5 cm of soil, whereas for all other tiles the effective soil depth associated with these variables is negligible (Reichle 2012). The area-weighted average of the three prognostic surface temperature variables determines the surface temperature in the absence of snow, $T_{\text{surf}}^{\text{no-snow}}$, which is then averaged (again area-weighted) with the surface snow temperature, $T_{\text{surf}}^{\text{snow}}$, to provide the land surface temperature $T_{\text{surf}}$ of the entire catchment:

$$T_{\text{surf}} = (1 - \text{asnow})T_{\text{surf}}^{\text{no-snow}} + (\text{asnow})T_{\text{surf}}^{\text{snow}}$$

The surface snow temperature and the snow area fraction (asnow) are themselves diagnosed from the model’s snow prognostic variables (snow water equivalent, snow depth, and snow heat content).

Subsurface temperatures are modeled using a soil heat diffusion model that consists of six layers. The thicknesses of the layers are about 10, 20, 40, 75, 150, and 1,000 cm starting from the top-most soil temperature layer. The layer thicknesses are the same for all land tiles. (For tropical forests, the layers of the heat diffusion model are shifted downward by the 5 cm thickness of the surface layer; see above.) The prognostic variables for the heat diffusion model are the ground heat contents ($ght$) in the six layers from which the soil temperatures ($T_{\text{soil}}$) in each layer are diagnosed. For the remainder of this paper, $ght$ and $T_{\text{soil}}$ refer to the values in the top-most (10 cm thick) soil layer only.

b. Freeze/thaw state in the Catchment model
The F/T analysis (section 4) requires diagnosing the landscape F/T state of the Catchment model based on its prognostic variables. As outlined in section 2, the landscape F/T state observed by L-band microwave remote sensing is assumed to be primarily related to the near-surface soil and vegetation canopy temperature under dry/frozen snow condition. Under wet snow, however, the satellite F/T signal will largely reflect snow cover conditions. We therefore first define an effective temperature that vertically averages the (snow-free) portion of the surface temperature, $T_{\text{surf}}^{\text{no-snow}}$, and the top-layer soil temperature $T_{\text{soil}}^{\text{top}}$:

$$T_{\text{eff}} = (1 - \alpha) T_{\text{soil}} + \alpha T_{\text{surf}}^{\text{no-snow}}$$  \hspace{1cm} (2)

Given the wavelengths used for F/T remote sensing, which typically range from 1 cm to 20 cm, and the resulting penetration depths, the contribution of the lower-layer soil temperatures to the microwave signal is small and neglected here. The parameter $\alpha$ determines the relative contributions of the surface temperature and the soil temperature and can be adjusted according to the microwave frequency used for the F/T classification so that it better reflects sensor signal penetration depth. Besides the (snow-free) effective temperature, $T_{\text{eff}}^{\text{no-snow}}$, additional information on the landscape F/T state is contained in the modeled snow conditions. Here, the snow cover area fraction, $a_{\text{snow}}$, is most relevant. In the Catchment model, the snow cover fraction increases linearly with the snow water equivalent (SWE) during the accumulation phase and reaches full cover ($a_{\text{snow}}=100\%$) when the total amount of SWE accumulated over the catchment reaches a model constant of $W_{\text{MIN}}=26$ kg m$^{-2}$ (Reichle et al., 2011).

The landscape F/T state is then diagnosed from the Catchment model variables via the following observation operator, which is also illustrated in Figure 1:
Thawed (F/T=1) \( \text{if } T_{\text{eff}} \geq T_{\text{eff-threshold}} \text{ and } asnow < asnow_{\text{threshold}} \) (3)

Frozen (F/T=-1) \( \text{if } T_{\text{eff}} < T_{\text{eff-threshold}} \text{ or } asnow \geq asnow_{\text{threshold}} \)

The effective temperature that determines the transition between frozen and thawed conditions is \( T_{\text{eff-threshold}} = 0^\circ C \). The snow cover threshold value \( asnow_{\text{threshold}} \) determines the maximum modeled snow cover fraction that is still compatible with a thawed condition. This value is fixed at 10% in this study and depends on the microwave frequency and the associated penetration depth through snow. The penetration depth at C-band (5.6 GHz) can be as large as several meters in dry snow conditions (Bingham and Drinkwater 2000, Dall et al. 2001) and is likely even larger at L-band (1.27 GHz; Rignot et al. 2001). For wet snow, however, the penetration depth of microwaves is drastically reduced to a few centimeters or less (Mätzler et al., 1984).

4. F/T data assimilation module (F/T analysis)

The assimilation of F/T observations is conceptually similar to the assimilation of snow cover observations. In both cases, the observed variable is, at least at a finer spatial scale, essentially a binary observation. Binary observations cannot be assimilated with a Kalman filter, because this requires continuous variables. For the assimilation of F/T observations, we propose a rule-based assimilation approach, similar to the rule-based assimilation of binary snow cover observations (Rodell and Houser 2004). In short, if the model forecast and the corresponding SMAP observations disagree on the F/T state, that is, if the model indicates frozen conditions and observation indicates thawed conditions (or vice versa), the model prognostic variables
related to the soil temperature ($T_{soil}$) and the snow-free surface temperature ($T_{surf}^{no-snow}$) are adjusted to match the observed F/T condition more closely. To account for model and observation errors, the delineation between frozen and thawed regimes is defined with some uncertainty in the assimilation algorithm, as will be detailed below.

a. Uncertainty in F/T simulations and observations

The perhaps simplest F/T analysis could use the observation operator defined in Equation (3) to determine the F/T state of the model forecast and then apply increments to switch the model’s F/T state whenever the model’s F/T state differs from that of the observations. However, such an analysis would ignore any uncertainty associated with the formulation of the observation operator (Equation (3)). It would also ignore any errors in the observations themselves.

For the purpose of the F/T analysis, we therefore refine the observation operator by introducing a regime of undetermined F/T status, which is defined by upper and lower bounds for the effective temperature and snow cover thresholds, as illustrated in Figure 2. Specifically, the model F/T state for the purpose of the F/T analysis is:

\[
\begin{align*}
\text{Completely Thawed (F/T=1)} & \quad \text{if } T_{\text{eff}} > UB_{T_{\text{eff}}} & \text{and } asnow < LB_{asnow} \\
\text{Completely Frozen (F/T=-1)} & \quad \text{if } T_{\text{eff}} < LB_{T_{\text{eff}}} & \text{or } asnow > UB_{asnow} \\
\text{Undetermined (F/T=0)} & \quad \text{otherwise}
\end{align*}
\]

In this study, $UB_{T_{\text{eff}}}$ and $LB_{T_{\text{eff}}}$ are fixed at -1°C and +1°C, and $LB_{asnow}$ is set to 5%. A value of 100% was chosen for $UB_{asnow}$. This assigns an “undetermined” F/T regime to situations with considerable snow cover on soil that is thawed or close to thawing. Under these
circumstances, it is difficult to determine whether the model F/T state should be thawed or frozen in a manner that would be fully consistent with the retrieval algorithm that was used to determine the value of the F/T observation.

The “undetermined” regime impacts the computation of the increments in two ways. Firstly, if the model forecast F/T state is “undetermined”, no increments will be applied. Secondly, the upper and lower bounds for the effective temperature threshold \((UB_{T_{eff}}, LB_{T_{eff}})\) will be used to formulate the rule-based increments that result from the F/T analysis (section 4b). In either case, the “undetermined” regime implicitly assigns weight to the model forecast in the analysis update and thus assumes imperfect observations.

\[\text{b. Update rules}\]

The assimilation of F/T observations is based on a number of rules. No updates are performed (i) if both the model and the observations agree on the F/T state, or (ii) if the model F/T state is undetermined per Equation (4). When the observations and simulations indicate a contrasting F/T state, then the model prognostic variables associated with \(T_{eff}\) are updated (i.e., \(T_{C1}, T_{C2}, T_{C4},\) and \(ght;\) section 3). Specifically, if the observations indicate a thawed condition (F/T=1) whereas the model is in a frozen regime, then \(T_{eff}\) is increased to the lower bound \(LB_{T_{eff}}\). Conversely, if the observations indicate freezing (F/T=-1) and the model is in a thawed regime, then \(T_{eff}\) is decreased to the upper bound \(UB_{T_{eff}}\). The updates can be summarized as follows:

\[\text{If obs F/T=1, model F/T=-1 and } \Delta T = (UB_{T_{eff}} - T_{eff}) < 0, \text{ then } T_{eff}^+ = T_{eff}^- + \Delta T\]

\[\text{If obs F/T=-1, model F/T=1 and } \Delta T = (LB_{T_{eff}} - T_{eff}) > 0, \text{ then } T_{eff}^- = T_{eff}^+ + \Delta T\]

\[\text{(5)}\]
In this equation, $T_{eff}^-$ represents the a priori estimate and $T_{eff}^+$ represents the analysis. The same increment $\Delta T$ is applied to the prognostic temperature variables $T_{C1}$, $T_{C2}$ and $T_{C4}$ (the weighted average of which determines $T_{\text{surf}}^{\text{no-snow}}$) and the soil temperature, $T_{\text{soil}}$. For the latter, the ground heat content ($g_{ht}$, the model prognostic variable that determines the soil temperature) is adjusted accordingly to match the updated soil temperature, $T_{\text{soil}}^+$. Note that the updates to $T_{C1}$, $T_{C2}$ and $T_{C4}$ also adjust $T_{\text{surf}}$ following Equation (1). In this study we are only updating the surface temperature and the soil temperature (and ground heat content) of the top-most soil layer. For future studies, updating the temperature of lower soil layers can also be considered.

The update rules (Equation (5)) intentionally do not adjust the snow variables directly. As mentioned in section 4a, an upper bound of $UB_{\text{asnow}}=100\%$ has been selected to avoid uncertainties related to the role of snow in determining the F/T state. This choice is supported by several experiments that were performed with smaller threshold values for $UB_{\text{asnow}}$ and in which a portion of the snow was removed if the observed F/T state indicated thawed conditions. These additional experiments (not shown) indicated that (error-prone) F/T observations sometimes mistakenly removed the model snow, which resulted in large subsequent forecast errors. It is difficult to recover from such errors, because once the model snow has been removed, the missing snow cannot easily be re-deposited at future analysis times due to the lack of quantitative information about snow mass in the F/T observations. Consequently, in the following the snow prognostic variables are not adjusted as part of the F/T analysis update. Nevertheless, at later time steps the model’s snow conditions will respond to the adjusted soil temperatures and corresponding updated hydrological fluxes.
5. Synthetic twin experiment

The twin experiment consists of several components. A Catchment land surface model integration serves as the “truth” and is used (i) to generate synthetic F/T observations and (ii) to validate the analysis results. The data assimilation experiment is performed with imperfect simulations and observations. The synthetic observed F/T state is obtained by adding classification error to the true F/T state (Section 5b). The imperfect Catchment land surface model integration is produced with a different forcing dataset to mimic forcing errors. This imperfect model simulation without data assimilation is referred to as the open loop (OL) (see discussion in section 5b). The F/T analysis is performed by assimilating the synthetic F/T observations into the imperfect model simulation using erroneous forcing data, and is referred to as the data assimilation (DA) integration. The OL and DA results are compared against the truth and the relative importance of assimilating observed F/T data is investigated (section 6).

a. Study domain and time period

The study domain is a region in North America between 45-55°N and 90-110°W (Figure 3). The simulations are performed on a 36 km Equal-Area Scalable Earth (EASE) grid, covering 1,137 grid cells in the study domain. The Catchment model integration is conducted using the GEOS-5 land data assimilation system (Reichle et al. 2014) with a time step of 20 min. The selected period of investigation is 8 years (1 January 2002 - 1 January 2010) and the temporal resolution of the model output is 3-hourly. The model was spun up by cycling ten times through the 1-year period from 1 January 2001 to 1 January 2002.
b. Synthetic truth, synthetic observations, and open loop

The synthetic truth is based on a Catchment model simulation that uses surface meteorological forcing data from the Modern-Era Retrospective analysis for Research and Applications (MERRA; Rienecker et al. 2011). The MERRA data product is provided at an hourly temporal resolution and a 1/2°×2/3° (latitude/longitude) spatial resolution. The resulting 8 years of synthetic true hydrological state variables and fluxes are used for the validation of the F/T analysis (DA). The synthetic true F/T state is obtained by applying the observation operator (Equation (3)) using $\alpha = 0.5$, $\text{snow}_{\text{threshold}} = 10\%$, and $T_{\text{f-threshold}} = 0^\circ\text{C}$.

The synthetic observed F/T indices are obtained by corrupting the true F/T data set with synthetic classification error. Specifically, the classification error is defined by the probability of misclassification. The SMAP mission requirements call for a F/T product with no more than 20% mean spatial classification error (McDonald et al. 2012). Here, we assume that the classification error is greatest near $0^\circ\text{C}$, where it reaches $CE_{\text{max}}$, linearly tapers off towards colder and warmer temperatures and vanishes below -10°C and above +10°C. That is, the classification error is given by a piecewise linear function of the land surface temperature, $T_{\text{surf}}$, as follows:

\[
\begin{align*}
    CE_{\text{max}} & \left( \frac{T_{\text{surf}} + 10}{10} \right) & & \text{-10°C} < T_{\text{surf}} < 0°C \\
    CE_{\text{max}} & \left( \frac{10 - T_{\text{surf}}}{10} \right) & & 0°C < T_{\text{surf}} < 10°C \\
    0 & & & T_{\text{surf}} > 10°C \text{ or } T_{\text{surf}} < -10°C
\end{align*}
\]  

This parameterization of the classification error is illustrated in Figure 4.
The synthetic F/T observations are generated at each time and for each location (or grid cell) by obtaining the probability of misclassification based on the land surface temperature $T_{\text{surf}}$ from Equation (6). We then randomly select a number from a uniform distribution between 0 and 1. If the selected random number is less than the specified classification error for that land surface temperature, then the observed F/T index is obtained by changing the sign of true F/T classification. Otherwise, the observed F/T index is equal to the true F/T state. The sensitivity of the data assimilation experiments to different levels of observation classification errors will be investigated below.

The open loop data set is obtained from an integration of the Catchment model with forcing data that differ from those used for the truth. Forcing errors were imposed by replacing the MERRA surface meteorological forcing fields with data from the Global Land Data Assimilation System (GLDAS; Rodell et al. 2004) as used in a former version of the NASA GMAO seasonal prediction system at 3-hourly temporal resolution and at $2.0^\circ \times 2.5^\circ$ (latitude/longitude) spatial resolution. The hydrological response associated with the differences between MERRA and GLDAS in precipitation and radiation timing and intensity results in considerable differences in the diagnosed F/T state at the grid scale.

c. F/T assimilation setup

The F/T assimilation experiment uses the same model settings as described for the open loop model, that is, it uses GLDAS forcings to mimic forcing errors relative to the MERRA truth. No additional perturbations are imposed and a single deterministic integration is performed for a period of 8 years (1 January 2002 – 1 January 2010). In this study, the synthetic observed F/T index is assimilated into the imperfect model integration at 6:00am and 6:00pm local time (F/T
The proposed assimilation time steps are compatible with the planned overpass times of SMAP.

The various tunable parameters in the diagnosis of the (uncertain) F/T state and the update rules are as follows. The parameter $\alpha$ (which determines the weight of the components of the effective temperature, Equation (2)) is set to 0.5 for the generation of F/T observations. This parameter is tunable and the sensitivity of data assimilation experiments to this parameter in the observation operator (Equation (3)) will be explored in section 6b. The values for the lower and upper bounds on the snow cover threshold $[LB_{asnow}; UB_{asnow}]$ are 5% and 100% snow cover, respectively. The uncertainty range for $asnow$ accounts for the combined uncertainty associated with the diagnosis of the modeled F/T state and the classification of the F/T observations in the presence of snow. In order to account for the uncertainty of the $0^\circ$C threshold value resulting from water solute concentration across different landscape elements within the satellite field of view, the upper and lower bounds for the effective temperature thresholds are $+1^\circ$C and $-1^\circ$C, respectively. The F/T analysis may benefit from adjusting these uncertainty bounds in response to the F/T classification error in the synthetic observations, but in the present paper we keep the bounds fixed.

**d. Validation of temperature estimates**

By design, the analysis update (Equation (5)) does not alter the F/T state of the model forecast, but the update rules will alter the temperature variables whenever the model forecast F/T state differs from the observed F/T index. It is expected that the differences in surface and soil temperatures (with respect to the truth) are smaller in the assimilation estimates than in the
open loop estimates. We therefore focus the validation on the computation of root-mean-square errors (RMSE) of surface and soil temperatures versus the truth data set.

F/T data assimilation is expected to be most relevant when temperatures are near 0°C because it is straightforward to estimate the F/T state accurately during clearly warm or cold conditions. We thus limit the validation to time steps where the air temperature is above -7°C and below +7°C (as indicated by the MERRA surface air temperatures). Furthermore, we restrict the validation to 6:00 am and 6:00 pm local time only, compatible with the time of the SMAP overpasses.

6. Results and discussion

a. Open loop (OL) and data assimilation (DA) with standard settings

To assess the impact of the imperfect forcing on the diagnosis of the F/T state without data assimilation, we first examine the OL results. As mentioned in section 5, the OL utilizes GLDAS forcings and the “truth” utilizes MERRA forcings. When compared to the truth, the OL has a F/T classification error of 4.85% (Table 1). The table also shows that the RMSE value for the OL surface temperature ($T_{\text{surf}}$) is 3.1°C and that of the first soil layer temperature ($T_{\text{soil}}$) is 2.0°C.

Again, by design the F/T analysis update does not alter the F/T state of the model forecast, and consequently the F/T classification error of the assimilation estimates is the same as that of the OL. But through the assimilation of the F/T observations, we hope to reduce the OL temperature errors. The F/T analysis involves adjusting the land surface effective temperature ($T_{\text{eff}}$), and subsequently $T_{\text{surf}}$ and $T_{\text{soil}}$, if the observed and simulated F/T states do not agree. Table 2 summarizes the reduction in RMSE ($\Delta$RMSE = RMSE OL – RMSE DA) by
assimilating synthetic F/T observations with 4 different levels of classification error ($CE_{max}$), and assuming default values for the tunable parameters, as introduced in section 5c.

Assimilating observed F/T indices without classification error results in an RMSE improvement of 0.206°C for the land surface temperature ($T_{surf}$) and an RMSE improvement of 0.061°C for the first layer soil temperature. When compared to the OL results for these two variables, the F/T analysis results in relative RMSE improvements of 6.7% and 3.1% for $T_{surf}$ and $T_{soil}$, respectively. The skill improvement decreases monotonically with increasing classification error in the observations. For a maximum classification error of $CE_{max}=20\%$ the assimilation of F/T observations still reduces the surface temperature RMSE by 0.149°C but it no longer improves the soil temperature estimates.

Figure 5 shows the $T_{surf}$ and $T_{soil}$ skill improvements in the study domain for the assimilation of F/T observations with $CE_{max}=0\%$, 5% and 20%. Figures 5a and 5b show that as a result of assimilating perfect F/T observations, the skill of $T_{surf}$ and $T_{soil}$ improves for almost all grid cells within the study domain. However, the efficiency of the F/T analysis deteriorates as the classification error is increased (Figures 5c-d). For $CE_{max}=20\%$, many grid cells in the study domain have negative or no improvement in $T_{soil}$ skill. As mentioned above, the F/T analysis may benefit from adjusting the uncertainty bounds in response to the classification error of the synthetic F/T observations, but the above results indicate that using a single set of uncertainty bounds already provides reasonable assimilation estimates.

Figure 6 shows the skill improvement for each grid cell binned as function of the number of analysis updates per grid cell (that is, the skill improvement is spatially averaged across grid cells experiencing a similar number of analysis updates in time within the study domain). The data
points are assigned to 6 bins with equal numbers of grid cells. Each bin center is assigned the average number of analysis updates for the grid cells in that particular bin. When more error-free observations (Figure 6a,b) or observations with modest classification errors (Figure 6c,d) are assimilated, the average skill improves with the number of analysis updates for both the temperatures, $T_{\text{surf}}$ and $T_{\text{soil}}$. However, as the maximum classification error is increased to 20% (Fig 6e,f), the average skill in the temperature variables does not improve with the number of analyses. This is due to the negative effect of assimilating misclassified observed F/T indices into the model.

b. Sensitivity of assimilation results to the formulation of the effective temperature

The effective temperature, $T_{\text{eff}}$, which is an important variable in diagnosing the F/T state, is a weighted average of the surface temperature in the absence of snow, $T_{\text{surf}}^{\text{no-snow}}$, and the soil temperature, $T_{\text{soil}}$ (Equation (2)). The weight ($\alpha$) should be a function of the microwave penetration depth. An increase (decrease) in penetration depth results in a decrease (increase) in parameter $\alpha$ and hence an increase (decrease) in the weight of the soil temperature component of effective temperature $T_{\text{eff}}$. In this study, the synthetic true F/T state was obtained based on the assumption that the parameter $\alpha$ equals 0.5. Thus, $T_{\text{surf}}^{\text{no-snow}}$, and $T_{\text{soil}}$ have similar weights in determining the effective temperature, $T_{\text{eff}}$, and thus the F/T state of the soil.

However, when determining the F/T index from (real) remote sensing observations, the relative effect of $T_{\text{surf}}^{\text{no-snow}}$ and $T_{\text{soil}}$ in those observations is not known a priori. Here we investigate the sensitivity of the DA performance to the choice of this factor in the observation operator. A
physically meaningful range of $\alpha$ between 0.25 and 1 was selected. This means that the weight of soil temperature, $T_{\text{soil}}$, ranges between 0.75 and 0 in the model.

The sensitivity of the assimilation results to the value of $\alpha$ in the forecasted F/T state is illustrated Figure 7. The skill improvements ($\Delta$RMSE) are shown for the case where no classification error ($CE_{\text{max}}=0\%$) is associated with the assimilated F/T indices. As expected, the maximum skill improvement for both $T_{\text{surf}}$ and $T_{\text{soil}}$ occurs when the parameter $\alpha$ is 0.5, that is, when the $\alpha$ value that is used in the observation operator of the assimilation system matches the $\alpha$ value that was used to generate the synthetic F/T observations. The figure shows that the sensitivity of $T_{\text{surf}}$ to the parameter $\alpha$ seems to be higher than that of $T_{\text{soil}}$. The skill of $T_{\text{surf}}$ is reduced by up to 50% when $\alpha$ is not selected correctly, while the skill is reduced by at most 8% for $T_{\text{soil}}$. It is thus important to understand how different land surface variables contribute to the observed F/T and to mimic this relationship adequately in the F/T observation operator used in the data assimilation scheme.

7. Conclusions

In this study an algorithm for the diagnosis of the F/T state in the NASA Catchment land surface model was developed. The algorithm is compatible with the information contained in remotely sensed retrievals of landscape F/T state at different microwave frequencies. The GEOS-5 land data assimilation system in offline mode was updated with the newly designed F/T assimilation module. The ultimate goal of this research is to provide a framework for the assimilation of SMAP (Soil Moisture Active Passive) F/T observations into the Catchment model.
The performance of the method for a synthetic experiment showed encouraging improvements in the skill of soil temperature and land surface temperature estimates. However, the average skill improvement depends on the classification error in the F/T observations. In our synthetic study, the open loop simulation has a modeled F/T classification error of 4.85% error compared to the truth. When assimilating perfect (error-free) F/T observations, the RMSE for land surface temperature ($T_{surf}$) and soil temperature ($T_{soil}$) improves by 6.7% and 3.1%, respectively. Yet, the skill improvement decreases monotonically with increasing classification error in the assimilated F/T observations. No more improvements in soil temperature were found with maximum classification errors of $CE_{max}=20\%$.

The results also discuss the sensitivity of the data assimilation (DA) to the $\alpha$ parameter in the observation operator. This parameter controls the relative contribution of the snow-free surface temperature and the top-layer soil temperature to the F/T state in the modeling system and impacts the temperature increments applied during the F/T analysis. The maximum skill improvement can only be expected if the observation operator in the modeling system closely mimics the relative importance of various landscape components, including the surface and soil temperatures, in the determination of the satellite F/T observations. Therefore, the observation operator could also benefit from further tuning to improve the linkage between the modeled snow cover and the expected F/T index retrieved from the microwave signal. Moreover, the limitations of the present study could perhaps be overcome in the future by directly assimilating backscatter or brightness temperature observations (instead of F/T retrievals).

The regional domain of the experiment investigated in this research represents a relatively flat terrain area of central North America. In this region, the model without assimilation (open loop) produced a F/T classification error of only 4.85%. This modeling error is a direct result of
the assumption that all F/T classification errors are solely due to errors in the forcing data (as reflected in the difference between the GLDAS and MERRA data). When the F/T assimilation method is applied to satellite observations (instead of synthetic retrievals), we expect larger errors in the simulated F/T state, especially over regions with more complex topography (e.g., regions in Western North America) where global forcing fields do not resolve the considerable heterogeneity of the surface conditions. In applications, the benefit of assimilating high-resolution (3 km) SMAP F/T retrievals is therefore expected to be greater for improving the simulation of eco-hydrological processes.

Acknowledgments

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Table 1. Metrics for OL vs. truth estimates for a period of 8 years (2002-2010) and at 6am and 6pm local time. The RMSE for $T_{\text{surf}}$ and $T_{\text{air}}$ is computed excluding times and locations where $T_{\text{air}} > 7^\circ C$ or $T_{\text{air}} < -7^\circ C$.

<table>
<thead>
<tr>
<th>Variables</th>
<th>Metric</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T_{\text{surf}}$</td>
<td>RMSE</td>
<td>3.08 °C</td>
</tr>
<tr>
<td>$T_{\text{soil}}$</td>
<td>RMSE</td>
<td>1.97 °C</td>
</tr>
<tr>
<td>F/T</td>
<td>Classification error</td>
<td>4.85%</td>
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</table>
Table 2. RMSE improvement (ΔRMSE = RMSE OL – RMSE DA, in °C) for $T_{surf}$ and $T_{soil}$ for different maximum classification errors ($CE_{max}$), excluding times and locations where $T_{air} > 7°C$ or $T_{air} < -7°C$, for a period of 8 years (2002-2010) and at 6am and 6pm local time.

<table>
<thead>
<tr>
<th>$CE_{max}$ (%)</th>
<th>0%</th>
<th>5%</th>
<th>10%</th>
<th>20%</th>
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<tbody>
<tr>
<td>ΔRMSE (°C)</td>
<td>0.206</td>
<td>0.192</td>
<td>0.178</td>
<td>0.149</td>
</tr>
<tr>
<td>$T_{surf}$</td>
<td>0.061</td>
<td>0.049</td>
<td>0.036</td>
<td>0.006</td>
</tr>
</tbody>
</table>
Figure captions

Figure 1. Schematic representation of the model diagnosis of the land surface F/T state as a function of (snow-free) effective temperature ($T_{eff}$) and the snow cover fraction ($a_{snow}$).

Figure 2. Schematic representation of three distinct F/T state regimes defined by upper and lower uncertainty bounds on the effective temperature and snow cover thresholds for the purpose of the F/T analysis. The upper bound for the snow cover threshold is set to $UB_{asnow}=100\%$.

Figure 3. Map of study domain.

Figure 4. Classification error function.

Figure 5. $\Delta$RMSE (= RMSE OL – RMSE DA) in (a, c, e) $T_{surf}$ and (b, d, f) $T_{soil}$ across the study domain for assimilation of synthetic F/T observations with (a, b) $CE_{max}=0\%$, (c, d) $CE_{max}=5\%$, and (e, f) $CE_{max}=20\%$. A positive $\Delta$RMSE indicates a skill improvement in the assimilation results.

Figure 6. Spatially averaged $\Delta$RMSE for (a,c,e) $T_{surf}$ and (b,d,f) $T_{soil}$ with 1 spatial standard deviation around the mean as a function of the number of analysis updates for the assimilation of synthetic F/T observations with (a,b) $CE_{max}=0\%$, (c,d) $CE_{max}=5\%$, and (e,f) $CE_{max}=20\%$. A positive $\Delta$RMSE indicates a skill improvement in the assimilation results.
Figure 7. ΔRMSE for (a) $T_{\text{surf}}$ and (b) $T_{\text{soil}}$ as a function of the $\alpha$ parameter chosen in the observation operator. A positive ΔRMSE indicates a skill improvement in the assimilation results.
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40
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Figure 7. \( \Delta \text{RMSE} \) for (a) \( T_{\text{surf}} \) and (b) \( T_{\text{soil}} \), as a function of the \( \alpha \) parameter chosen in the observation operator. A positive \( \Delta \text{RMSE} \) indicates a skill improvement in the assimilation results.