Session 6
Dynamic Modeling and Systems Analysis

1:00 – 1:05p  Overview – Jeffrey Csank
1:05 – 1:30p  Dynamic Systems Analysis – Jeffrey Csank
1:30 – 1:55p  T-MATS (Toolbox for the Modeling and Analysis of Thermodynamic Systems) – Jeffrieses Chapman

4th Propulsion Control and Diagnostics Workshop
Ohio Aerospace Institute (OAI)
Cleveland, OH
December 11-12, 2013
Dynamic Systems Analysis

• Preliminary Engine Design
  – Systems Analysis (Steady state)
  – Lack of dynamic performance information
    • Historical data (past experiences)
    • Additional conservatism in the design

• Dynamic Systems Analysis
  – Better predict/account for dynamic operation in PED
  – Allow for trade-offs between performance and operability margins to meet future engine performance requirements
  – Enabled through the Tool for Turbine Engine Closed-loop Transient Analysis (TTECTrA)
T-MATS (Toolbox for the Modeling and Analysis of Thermodynamic Systems)

• Simulation System designed to give a user a library containing building blocks that may be used to create dynamic Thermodynamic systems. Includes:
  - Iterative Solving capability
  - Generic Thermodynamic Component models
    Turbomachinery components (compressor, turbine, burner, nozzle, etc.)
  - Control system modeling (controller, actuator, sensor, etc.)

• MATLAB/Simulink Based
• Open Source (free of proprietary and export restrictions)
• Development of T-MATS is being led by NASA Glenn Research Center

  - NASA’s focus for this project is on the modeling of aerospace applications, however the T-MATS framework is extremely general and can be applied to any thermodynamic model.
Reducing Conservatism in Aircraft Engine Response Using Conditionally Active Min-Max Limit Regulators

- Typical aircraft engine control is based on a Min-Max scheme
- Designed to keep the engine operating within prescribed mechanical and operational safety limits
  - Compares fuel flow to determine the limit that is closest to being violated
  - Conservative
- Improve engine performance by allowing the limit regulators to only be active when a limit is in danger of being violated.
Dynamic Systems Analysis

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4th Propulsion Control and Diagnostics Workshop
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• Alicia Zinnecker, N&R Engineering
• Georgia Institute of Technology
Outline

• Preliminary Engine Design
• Systems Analysis
• Tool for Turbine Engine Closed-loop Transient Analysis (TTECTrA)
• Dynamic Systems Analysis
• Conclusion
Preliminary Engine Design

- Huge commitments are made based on results
- A completely new engine is relatively rare
- Most programs focus on derivative engines
Systems Analysis

- Complex process that involves system-level simulations to evaluate system-level performance, weight, and cost (optimize system, compromise component)
- Focus on steady-state design cycle performance
- Dynamic considerations and issues are incorporated through the use of operating margins
  - Stall margin
Tool for Turbine Engine Closed-loop Transient Analysis (TTECTrA)

- Capable of automatically designing a controller
- Easily integrates with users engine model in MATLAB/Simulink environment
- Provide an estimate of the closed-loop transient performance/capability of a conceptual engine design

Requirements:
- MATLAB®/Simulink® (Release R2012b or later)
  - MATLAB® Version 8.0 (R2012b)
  - Simulink® Version 8.0 (R2012b)
  - Control Systems Toolbox® Version 9.4 (R2012b)
- Engine Model compatible with Simulink
- State space linear model in MATLAB
• TTECTrA software automatically designs:
  – Set Point
  – Set Point Controller
  – Limit Controller

• Simulates different thrust profiles
TTECTra - Set Point Function

- Flight condition (altitude, Mach, temperature)
- Define set point bounds and number of breakpoints
  - Fuel flow
  - Thrust
TTETrA – Set Point Controller

- Bandwidth (Hz)
- Phase Margin
- Feedback filter (Hz)
- Throttle Filter (Hz)
TTECTrA – Limit Controller

- **Acceleration Minimum Surge Margin (HPC)**
  - $N_{\text{cdot}}$ vs $N_{cR25}$
- **Deceleration Minimum Surge Margin (LPC)**
  - $W_f/P_s3$
**TTECTrA - Selector Logic / Actuator**

- **Selector Logic (Min/Max scheme)**
  - Min (Set Point, Acceleration)
  - Max (Min, Deceleration)

- **Actuators**
  - Currently only models fuel flow
  - First order filter
Commercial Modular Aero Propulsion System Simulator 40,000 (C-MAPSS40k)

- 40,000 Lb Thrust Class High Bypass Turbofan Engine Simulation
- Matlab/Simulink Environment
- Publically available
- Realistic controller
- Realistic surge margin calculations
Burst and Chop Thrust Profile

- Idle (14% of max thrust) to Take-off thrust profile to test the TTECTrA controller
- Compare the thrust response to the Federal Aviation Administrations (FAA) Federal Aviation Regulation (FAR) Part 33, Section 33.73(b)
Burst and Chop Thrust Profile

![Graphs showing Burst and Chop Thrust Profile](image-url)
Engine Deterioration

- Thrust, lbf
- Control Variable
- HPC SM, %
- LPC SM

Time, s
The Benefit of TTTECTrA

Do we have enough margin? Too much margin?

<table>
<thead>
<tr>
<th>Stack</th>
<th>%</th>
</tr>
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<tbody>
<tr>
<td>Uncertainty</td>
<td>11</td>
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<tr>
<td><em>Reynolds Number</em></td>
<td>2</td>
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<tr>
<td><em>Distortion</em></td>
<td>4</td>
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<tr>
<td><em>Tip Clearances</em></td>
<td>1.5</td>
</tr>
<tr>
<td><em>Deterioration</em></td>
<td>1.5</td>
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<tr>
<td><em>Random</em></td>
<td>2</td>
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<tr>
<td>Transient Allowance</td>
<td>12</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td>23</td>
</tr>
</tbody>
</table>

Corrected Flow (Wc) vs Pressure Ratio (PR)

- Uncertainty
  - SA
  - DSA
The Benefit of TTTECTrA

- **Combustor Stability**

- **Low Pressure Compressor**

- **Turbine life**
Future Work

• NPSS Model in Simulink
  – Georgia Institute of Technology

• Integrate TTECTrA with the NPSS Simulink model
  – NASA/RHC

• Integrate TTECTrA/NPSS Simulink with a larger systems analysis optimization algorithm
  – NASA/RHC and NASA/RTM
Conclusion

• Dynamic systems analysis:
  – Enables engine transient performance to be accounted for in the optimization of the engine design and early in the preliminary design of turbine engines.
  – Allows trading of overly conservative surge margin for better performance through system redesign (or online).

• Developed the Tool for Turbine Engine Closed-loop Transient Analysis (TTECTrA)
  – Capable of automatically designing a controller at a single flight condition.
  – Easily integrates with users engine model in MATLAB/Simulink environment.
  – Open source
Thank you

Questions?
Toolbox for the Modeling and Analysis of Thermodynamic Systems (T-MATS)

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4th Propulsion Control and Diagnostics Workshop
Ohio Aerospace Institute (OAI)
Cleveland, OH
December 11-12, 2013
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Outline

• T-MATS Description
• Background
• Framework
• Block Sets
• Examples
• Conclusion
• Future work
T-MATS Description

• **Toolbox for the Modeling and Analysis of Thermodynamic systems, T-MATS**
  – Modular thermodynamic modeling framework
  – Designed for easy creation of custom Component Level Models (CLM)
  – Built in MATLAB®/Simulink®

• **Package highlights**
  – General thermodynamic simulation design framework
  – Variable input system solvers
  – Advanced turbo-machinery block sets
  – Control system block sets

• **Development being led by NASA Glenn Research Center**
  – Non-proprietary, free of export restrictions, and open source
    • Open collaboration environment
Background

- Thermodynamic simulation examples

<table>
<thead>
<tr>
<th>Model Type</th>
<th>Examples</th>
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<tbody>
<tr>
<td><strong>Steady-State</strong> (system convergence may be required)</td>
<td>Gas turbine cycle model</td>
</tr>
<tr>
<td></td>
<td>• e.g., performance models</td>
</tr>
<tr>
<td><strong>Dynamic with Quasi-steady-state variables</strong> (multi-iteration simulation; time and system convergence)</td>
<td>Gas turbine model with spool dynamics only. (real time running capability)</td>
</tr>
<tr>
<td></td>
<td>• e.g., control models</td>
</tr>
<tr>
<td><strong>Fully Defined Dynamic Simulation</strong> (iteration over time)</td>
<td>Dynamic gas turbine model with spool and volume dynamics (typically runs more slowly)</td>
</tr>
<tr>
<td></td>
<td>• e.g., near stall performance models</td>
</tr>
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</table>
# Background: Industry Study

<table>
<thead>
<tr>
<th>Package</th>
<th>User Friendly*</th>
<th>Flexibility*</th>
<th>Export Restricted</th>
<th>Source code available</th>
<th>Dynamic</th>
<th>Control System</th>
<th>Cost</th>
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<td>C-MAPSS40k, NASA</td>
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<td>Low</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>MATLAB</td>
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<tr>
<td>Matlab: Thermlib toolbox, Eutech</td>
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<td>No</td>
<td>Yes</td>
<td>No</td>
<td>MATLAB + $4900</td>
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<td>T-MATS, NASA</td>
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<td>No</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>MATLAB</td>
</tr>
</tbody>
</table>

**Definitions:**

1* User Friendly, Controls Perspective
   - Low: Code based
   - Med: Model based
   - High: Model based with package implemented in a platform that is an industry standard

2* Flexibility
   - Low: Plant configuration set
   - Med: Object oriented, objects difficult to update
   - High: Object oriented, objects easily adaptable by user
T-MATS Framework

• T-MATS is a plug-in for a MATLAB/Simulink platform
  – additional blocks in the Simulink Library Browser:

  ![Simulink Library Browser](image)

  Added Simulink Thermodynamic modeling and numerical solving functionality

  – additional diagram tools for model development in Simulink:

  ![Block Parameters](image)

  Faster and easier model creation
T-MATS Framework

- **Dynamic Simulation Example:**
  - Multi-loop structure
  - The “outer” loop (green) iterates in the time domain
    - Not required for steady-state models
  - The “inner” loop (blue) solves for plant convergence during each time step
Blocks: Numerical Solver

- Many Thermodynamic models are partially defined and require a solver to ensure model conservation (e.g., mass, energy, etc.).
  - In many gas turbine simulations, component flow will typically be solved by an independent solver.

- T-MATS contains solvers that perform in two main steps:
  - Automated Jacobian (system gradient) Calculation
    \[
    J = \begin{bmatrix}
    \frac{\partial f_1}{\partial x_1} & \cdots & \frac{\partial f_1}{\partial x_n} \\
    \vdots & \ddots & \vdots \\
    \frac{\partial f_m}{\partial x_1} & \cdots & \frac{\partial f_m}{\partial x_n} 
    \end{bmatrix}
    \]
  - Each plant input is perturbed to find the effect on each plant output.
  - Newton-Raphson method is used to “converge” the system.

\[
x(n + 1) = x(n) - \frac{f(x(n))}{f'(x(n))}
\]
where,
\[
f'x(n) = J
\]
Blocks: Turbo-machinery

• T-MATS contains component blocks necessary for creation of turbo-machinery systems
  – Models based on common industry practices
    • Energy balance modeling approach
    • R-line compressor maps in Compressor model
    • Pressure Ratio maps in Turbine model
    • Single fuel assumption
    • Flow errors generated by comparing component calculated flow with component input flow
  – Includes blocks such as; compressor, turbine, nozzle, flow splitter, and valves among others.
  – Built with S-functions, utilizing compiled MEX functions
 Blocks: Controls

- **T-MATS** contains component blocks designed for fast control systems creation

  - **Sensors:**

  - **Actuators:**

  - **PI controllers:**
Blocks: Settings

- The T-MATS Simulation System is a highly tunable and flexible framework for Thermodynamic modeling.
  - T-MATS block Function Block Parameters
    - fast table and variable updates
  - Open source code
    - flexibility in component composition, as equations can be updated to meet system design
  - MATLAB/Simulink development environment
    - user-friendly, powerful, and versatile operation platform for model design
Dynamic Gas Turbine Example: Objective System

Simple Turbojet
Dynamic Gas Turbine Example: Creating the Inner Loop
Dynamic Gas Turbine Example: Inner Loop Plant

Turbojet plant model architecture made simple by T-MATS vectored I/O and block labeling
Dynamic Gas Turbine Example: Creating the Solver
Dynamic Gas Turbine Example: Solver

Simulink While Iterator block

Inner Loop Plant from previous slide

Iterative Solver

Plant flow errors driven to zero by iterative solver block in parallel with While Iterator
Dynamic Gas Turbine Example: Creating the Outer Loop

Outer Loop

Effectors

Inner Loop

Plant

X_ol(t+dt)

Outputs

Do While

Simulink Block

y(t)

f(x(n))

Iterations

Iterations to ensure convergence, n

X_il(n+1)

Iterative Solver

T-MATS Block

X_ol(t+dt)

Outer Loop

Plant

Iteration over time, t

Iteration over time, t
Dynamic Gas Turbine Example: Outer Loop Plant

Environmental conditions

Simple Control System

Shaft speed integration

Shaft integrator and other Outer Loop effectors added to create full system simulation
Verification and Release

• Verification was performed by matching T-MATS simulation data with other established simulations.
  – Models chosen for verification
    • NPSS steady-state turbojet model
    • C-MAPSS – High bypass turbofan engine model
  – In all cases differences in simulation performance were within acceptable limits.

• Expected Release: Q4,2013 or Q1,2014.
  – Pre-built examples will include:
    • Newton-Raphson equation solver
    • Steady state turbojet simulation
    • Dynamic turbojet simulation
Conclusions

- T-MATS offers a comprehensive thermodynamic simulation system
  - Thermodynamic system modeling framework
  - Automated system “convergence”
  - Advanced turbo-machinery modeling capability
  - Fast controller creation block set
Future Work

• Increase thermodynamic modeling capability
  – Introduce Cantera to T-MATS
    • “Cantera is a suite of object-oriented software tools for problems involving chemical kinetics, thermodynamics, and/or transport processes”
    • Open source
    • Increases thermodynamic modeling capability to include:
      – Non-fuel specific gas turbine modeling
      – Fuel cells
      – Combustion
      – Chemical Equilibriums

\[ O + CH \rightleftharpoons H + CO \]
Reducing Conservatism in Aircraft Engine Response Using Conditionally Active Min-Max Limit Regulators

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Overview

• Introduction
• Baseline Control Architecture
• Conditionally Active Limit Regulator Approach
• Simulation Examples
• Conclusions & Future Work
Introduction

• The primary task of an engine control system is to deliver the guaranteed performance while ensuring safe operation throughout operating envelope over the life of the engine.

• Guaranteed performance is defined as meeting the FAA certification requirements for engine responsiveness – maximum allowed 95% rise time for idle to max thrust command.
Baseline Control Architecture

- Typical aircraft engine control is based on a Min-Max scheme
- Designed to keep the engine operating within prescribed mechanical and operational safety limits
Engine Response with Baseline Control

- C-MAPSS40k Full throttle burst at sea-level static conditions with an end-of-life engine

- Acceleration limit regulator is active immediately even though it is far from the limit - Conservative Response
Is the Conservative Response an issue?

• No:
  • Not during normal flight as long as it meets the FAA response requirements

• Yes:
  • On aircraft where primary flight control surfaces are damaged (e.g. UAL 232, Bagdad DHL, AA 587)
  • On aircraft with integrated flight/propulsion control

• Can we improve the engine response while maintaining the current architecture?
The Case for Conditionally Active Limit Regulators

- The baseline Min-Max selection control approach is inherently conservative
- Every limit regulator is capable of limiting fuel flow to engine – regardless of proximity to current limit
- Depending on how the individual PI regulators are tuned, the regulator may intervene when there is no danger of a limit being violated
- To reduce conservatism, limit regulators should become active only when a limit is in “danger” of being violated.
Conditionally Active Limit Regulators

• For operation with reduced conservatism while still ensuring safety, following two criteria must both be satisfied to enable a limit regulator:
  1) The regulated variable must be “close” to the specified limit
  2) The rate of change of the regulated variable is such that the regulated variable will reach the limit within a specified number of control update time steps
Conditionally Active Limit Regulators

- The conditions for the limit regulator to be active can be stated as:
  For a maximum limit variable $y_1$ with limit $y_{1\text{max}}$:

  $$y_1 \geq (1 - \alpha_1) \times y_{1\text{max}}$$

  \[y_1 + \frac{d}{dt} y_1 \times \beta_1 \times \Delta T \geq y_{1\text{max}}\]

  - where $\alpha_1$ and $\beta_1$ are positive design parameters

- Similar equations can be developed for minimum limit variables
Conditionally Active Limit Regulators

Graphical interpretation:

- Criteria 1 is satisfied at \( t_A \)
- Criteria 2 is satisfied at \( t_B \)
- Therefore the limit \( y_1 \) regulator is enabled at \( t_B \)

\[
y_{1\text{max}} - (1-\alpha_1)y_{1\text{max}}
\]

\[
t_A + \beta_1 \Delta T
\]

\[
 t_A + \beta_1 \Delta T
\]

\[
 t_B + \beta_1 \Delta T
\]
CA Architecture Modification

Uses the existing Min-Max architecture, but each regulator's output is only considered if the associated criteria are satisfied.
Choice of CA Design Parameters

• We currently do not have an analytical approach to selecting the CA limit regulator design parameters $\alpha$ and $\beta$
• The CA parameters are tuned empirically
  – $\alpha$ value selected first to ensure limit is not violated for operation under worst case conditions
  - With a fixed $\alpha$, the $\beta$ value is selected to provide fastest possible response without violating limit
• Numerical optimization algorithm has been developed
Simulation Results

- Full throttle burst at sea-level static conditions with an end-of-life engine

- Reduced conservatism resulting in much faster response
Simulation Results

- Case when a limit (Nc) is reached
Conclusions

- The use of properly tuned Conditionally Active limit regulators can improve the engine response without compromising safety.
- This approach should simplify the tuning and validation of the limit regulator gains as the regulators are only active in a small number of possible cases.
- The CA limit regulator does not require modifications to any other aspect of the well established control architecture.
Future Work

• Formulate the CA limit regulator approach in a proper mathematical framework

• Investigate development of analytical approach to determining the CA design parameters so as to satisfy performance and safety requirements
References

