THE CONTRIBUTION OF $z \lesssim 6$ SOURCES TO THE SPATIAL COHERENCE IN THE UNRESOLVED COSMIC NEAR-INFRARED AND X-RAY BACKGROUNDS

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ABSTRACT

A spatial clustering signal has been established in Spitzer/IRAC measurements of the unresolved cosmic near-infrared background (CIB) out to large angular scales, $\sim 1{'}$. This CIB signal, while significantly exceeding the contribution from the remaining known galaxies, was further found to be coherent at a highly statistically significant level with the unresolved soft cosmic X-ray background (CXB). This measurement probes the unresolved CXB to very faint source levels using deep near-IR source subtraction. We study contributions from extragalactic populations at low to intermediate redshifts to the measured positive cross-power signal of the CIB fluctuations with the CXB. We model the X-ray emission from active galactic nuclei (AGNs), normal galaxies, and hot gas residing in virialized structures, calculating their CXB contribution including their spatial coherence with all infrared emitting counterparts. We use a halo model framework to calculate the auto and cross-power spectra of the unresolved fluctuations based on the latest constraints of the halo occupation distribution and the biasing of AGNs, galaxies, and diffuse emission. At small angular scales ($\lesssim 1{'}$), the $4.5\,\mu$m versus 0.5–2 keV coherence can be explained by shot noise from galaxies and AGNs. However, at large angular scales ($\sim 10{'}$), we find that the net contribution from the modeled populations is only able to account for $\sim 3\%$ of the measured CIB×CXB cross-power. The discrepancy suggests that the CIB×CXB signal originates from the same unknown source population producing the CIB clustering signal out to $\sim 1{'}$.

Key words: cosmic background radiation – dark ages, reionization, first stars – diffuse radiation – large-scale structure of universe

Online-only material: color figures

1. INTRODUCTION

Background radiation is produced by a variety of sources that dominate different parts of the electromagnetic spectrum and includes contributions from sources inaccessible to individual telescopic studies. The near-IR cosmic infrared background (CIB) probes the history of starlight and associated emission falling into the 1–5 $\mu$m range (see review by Kashlinsky 2005), whereas the cosmic X-ray background (CXB) probes emissions from accretion-powered sources and hot ionized gas. Spatial correlations between the two can arise from sources emitting at both IR and X-ray wavelengths or from separate IR and X-ray sources that share the same large-scale structures. Angular fluctuations in the CIB have been revealed after carefully masking resolved sources in deep near-infrared (near-IR) exposures and Fourier analyzing the pixels remaining in the maps. This technique has led to measurements using Spitzer/IRAC, Hubble Space Telescope/NICMOS, and AKARI/InfraRed Camera (Kashlinsky et al. 2005, 2007a; Thompson et al. 2007; Matsumoto et al. 2011; Kashlinsky et al. 2012; Cooray et al. 2012b). The amplitude of the CIB fluctuations in the Spitzer and AKARI data, now extending to $\sim 1{'}$, is well above the expected contribution of local foregrounds, such as the Zodiacal Light and Galactic cirrus, and implies an unresolved extragalactic CIB component which significantly exceeds the power from the remaining known galaxy populations (Helgason et al. 2012). The minimal CIB flux implied by the new sources responsible for these fluctuations is of order 0.5–2 nW m$^{-2}$ sr$^{-1}$ (Kashlinsky et al. 2007a) and is well below the claimed direct CIB flux measurements from DIRBE (Dwek & Arendt 1998), Infrared Telescope in Space (Matsumoto et al. 2005), and AKARI (Tsumura et al. 2013), being consistent with limits placed by $\gamma$-ray attenuation from very high energy sources (Meyer et al. 2012; Ackermann et al. 2012; H.E.S.S. Collaboration 2013). The power spectrum of the Spitzer fluctuations is highly isotropic on the sky and is consistent with that of high-$z$ $\Lambda$CDM clustering out to $\sim 1{'}$ (Kashlinsky et al. 2012); it appears, within the statistical uncertainties, with the same amplitude and spatial shape at both deeper (lower shot-noise; Kashlinsky et al. 2007b) and shallower (larger shot-noise; Cooray et al. 2012b) IRAC maps.

The measured spatial power spectrum of the source-subtracted CIB fluctuations rises at angular scales $\gtrsim 20{'}$. The amplitude and shape of this rise is a direct measurement of the clustering properties of the underlying source populations and thus a primary key of understanding their nature. The interpretation of these power spectra has been a matter of debate (Salvaterra et al. 2006; Kashlinsky et al. 2007b; Fernandez et al. 2010; Cooray et al. 2012a; Yue et al. 2013a). It is now firmly established that the extragalactic signal is inconsistent with the emission of presently resolved galaxies ($z < 6$) with extrapolation to low luminosities (Helgason et al. 2012). On the other hand, it was proposed that CIB fluctuations from the first light era could be measurable thus making the signal a critical tool for studying the high-$z$ universe (Kashlinsky et al. 2004; Cooray et al. 2004). The CIB fluctuations show...
no spatial correlations with deep Hubble/Advanced Camera for Surveys (ACS) maps \( \lesssim 0.9 \mu m \) implying that the sources are extremely faint and/or that their Lyman-break is redshifted well into the near-IR, \( 1+z \) \( 0.1 \mu m \gtrsim 0.9 \mu m \) (Kashlinsky et al. 2007c). Current measurements show strong clustering on large scales coupled with the low shot noise levels on small scales (Kashlinsky et al. 2007b). This is consistent with a high redshift origin, although an alternative scenario has recently been proposed to explain some of these measurements as arising from the intrahalo light from stars stripped of their parental halos at intermediate redshifts of \( z \sim 1–4 \) (Cooray et al. 2012b; see Section 4.3 for full discussion).

The large-scale clustering of the source-subtracted CIB fluctuations does not provide direct information on whether the underlying sources are powered by stellar nucleosynthesis or accretion onto compact objects. Cappelluti et al. (2013, hereafter C13) provided observational evidence for a substantial population of accreting sources among the CIB sources, raising the intriguing possibility of extensive black hole activity in the early Universe. C13 used deep source-subtracted Spitzer/IRAC and Chandra maps of a common region to reveal a highly significant cross-power (3.8 \( \sigma \) 5.6 \( \sigma \)) between the unresolved CIB at 3.6, 4.5 \( \mu m \) and the soft 0.5–2 keV CXB, arguing for a high-\( z \) origin of the sources. An interesting and specific model for the discovered CIB\( \times \)CXB signal explained it in terms of direct collapse black holes at \( z \gtrsim 12–15 \) (Yue et al. 2013b) by a mechanism which is capable of reproducing both the unexplained CIB and cross CIB\( \times \)CXB fluctuation signals without violating constraints imposed by the total measured soft CXB. However, before models of such hypothetical high-\( z \) sources can be favored as leading explanations for the measured signal, a more quantitative analysis of known, and proposed, source classes at \( z \lesssim 6 \) is needed. There exists a variety of known mechanisms of X-ray production which can spatially correlate with optical/IR emitting counterparts in complex ways.

The deepest Chandra surveys have been able to resolve \( \sim80\%–90\% \) of the [0.5–8] keV CXB into individual point sources, the majority of which is made up of active galactic nuclei (AGNs; Hickox & Markevitch 2006; Lehmer et al. 2012). However, at the faintest fluxes, the abundance of sources identified as normal galaxies rapidly approaches that of AGNs and is likely to dominate at fainter levels. The X-ray emission within galaxies comes predominantly from X-ray binaries (XRBs), a compact object accreting from a companion star, which have been found to scale well with galaxy properties, such as star formation rate (SFR) and stellar mass (e.g., Ranalli et al. 2003; Persic & Rephaeli 2007; Lehmer et al. 2010). These sources have recently been detected out to deeper levels and higher redshifts by stacking analyses (Cowie et al. 2012; Basu-Zych et al. 2013). Cappelluti et al. (2012b) studied the unresolved CXB fluctuations \( \gtrsim 2 \times 10^{-16} \) erg s\(^{-1}\) cm\(^{-2}\) remaining in deep Chandra exposures and determined that the bulk is produced by gas residing in galaxy groups and clusters (\( \sim50\% \)), with the rest being contributed by AGNs and galaxies. At these levels, any contribution from high-\( z \) miniquasars would be overwhelmed by these low-\( z \) components (\( <5\% \)), although the systematic uncertainty in the mean level of the CXB increases such constraints by a large factor. The signal measured in C13 is revealed only after eliminating undetected X-ray sources down to unprecedented flux levels, \( \ll5 \times 10^{-17} \) erg s\(^{-1}\) cm\(^{-2}\), using the deep source-subtracted Spitzer maps.

In this paper, we explore the contribution of the intermediate \( z \) sources to the measured level of the CIB\( \times \)CXB coherence (C13) by modeling components from different populations: galaxies, AGNs, and diffuse emission in both IR and X-rays. We also discuss the intrahalo model of Cooray et al. (2012b) versus the full set of CIB constraints and its measured coherence with the unresolved CXB. This exhausts the set of known and proposed populations out to \( z \lesssim 4–6 \). We present a formalism for reconstructing the cross-power spectrum of the fluctuations produced by each source class using the latest observational evidence for their clustering and abundance.

The paper is organized as follows. Following Section 2, which defines the basic parameters, Section 3 discusses the CIB\( \times \)CXB measurement of C13 in more detail. Section 4 addresses contributions to the CIB and presents population modeling of optical/IR emitting sources. In Section 5, we do the same for CXB contributions with X-ray population models. In Section 6, we develop the formalism for reconstructing the CIB\( \times \)CXB fluctuation signal and present our results in Section 7, followed by discussion in Section 8.

### 2. DEFINITIONS AND PARAMETERS

Throughout, all quantities referred to as “X-ray” or denoted by “X” correspond to the emission in the soft X-ray band 0.5–2 keV, unless noted otherwise. The suffix IR refers to the near-IR wavelengths 3.6 \( \mu m \) and 4.5 \( \mu m \), i.e., the effective wavelengths of Spitzer/IRAC bandpasses 1 and 2, whereas FIR refers to the total infrared quantities, integrated over 10–1000 \( \mu m \). We assume standard \( \Lambda \)CDM cosmology using the cosmological parameters from the Planck experiment (Planck Collaboration et al. 2013). All magnitudes are in the AB system.

Background fluctuations are characterized by the spatial power spectrum as a function of the spatial frequency \( q \) (or spatial scale \( 2\pi/q \), defined as \( P(q) = \langle |\Delta(q)|^2 \rangle \)), where \( \Delta(q) \) is the two-dimensional Fourier transform of the source-subtracted CIB. The mean square fluctuation in CIB flux on angular scale \( \theta = 2\pi/q \) is defined as \( \langle |\Delta(q)|^2 \rangle = q^2 P(q)/(2\pi) \). The cross-power describing the correlations between fluctuations at different wavelengths \( m \) and \( n \) is \( P_{mn}(q) = \langle \Delta_m(q) \Delta_n^*(q) \rangle \) with \( R \) standing for the real, imaginary parts of the Fourier transform, \( \Delta(q) \). The cross-power spectrum is a real quantity which can assume positive or negative values. Coherence is then defined in its usual way as in Kashlinsky et al. (2012), \( \mathcal{C}(q) = (P_{mn}(q))^2/P_m(q)P_n(q) \). In the absence of common (coherent) populations at wavelengths \( m \) and \( n \), the cross-power, measured from a map of \( N_{pix} \) pixels, will oscillate around zero with a random statistically uncertainty of order \( P_m P_n/\sqrt{N_{pix}} \). Table 1 summarizes the definitions of the quantities used throughout the paper.

The source-subtracted CIB fluctuations have two components: (1) large scales \( >20''–30'' \) are dominated by the clustering of an unresolved population of unknown sources, while (2) small scales are dominated by the shot(white) noise,\(^7\) which arises mainly from unresolved galaxy populations. The two components may arise from different populations of unresolved sources.

### 3. THE MEASURED CIB\( \times \)CXB COHERENCE

The spatial coherence measured between the source-subtracted CIB fluctuations and the unresolved CXB used data

\(^7\) This refers to the net white noise component, which includes the counting noise and, in some models, also the one-halo component.
from the deep Chandra ACIS-I AEGIS-XD survey and the Spitzer Extended Deep Survey (SEDS) in the EGS field, where the two data sets overlap in a $\pm 8' \times 45'$ region of the sky (for details, see Cappelluti et al. 2013). The measured cross-power between the source-subtracted IRAC maps at (3.6, 4.5) $\mu$m and Chandra [0.5–2] keV maps was detected at angular scales of $10'-1000'$, with an overall significance of $\pm 3.8 \sigma$, $5.6 \sigma$, respectively. At the same time, no significant signal was detected between the IRAC source-subtracted maps and the harder Chandra bands. The measured coherence signal has been detected after jointly masking resolved sources down to $m_{AB} \simeq 25$ and $7 \times 10^{-17}$ erg s$^{-1}$ cm$^{-2}$ in IR and X-rays, respectively. The signal is characterized by the cross-power spectrum, $P_{XIR}(q)$ shown in Figure 10, and exhibits a broadband averaged cross-power in the $10'-1000'$ angular range (see definitions in Table 1)

$$\langle P_{X,0.5-2\text{keV}} \rangle = 6.4 \pm 1.7, $$

$$\langle P_{X,4.5\mu m,0.5-2\text{keV}} \rangle = 7.3 \pm 1.3,$$

in units of $10^{-20}$ erg s$^{-1}$ cm$^{-2}$ nW m$^{-2}$ sr$^{-1}$. We refer to the opposite ends of the measured angular interval $[10', 1000']$ as small and large angular scales, respectively.

In this paper, we examine the contribution to this signal from extragalactic populations at $z \leq 6$ with the putative high-$z$ populations deferred to a forthcoming paper. We decompose the total power spectrum of the fluctuations into the sum of power from sources of types known to emit both in X-rays and optical/IR

$$P_{\text{total}} = P_{\text{galaxies}} + P_{\text{AGN}} + P_{\text{diffuse}}$$

with each of these components contributing both in terms of their large-scale clustering on the sky as well as shot noise dominating small-scale power. We refer to sources of X-ray emission arising collectively from stars, stellar remnants, and gas within galaxies as “normal galaxies” whereas the term “AGN” is used in its broadest sense referring to any black hole activity in the centers of galaxies regardless of subclasses. We also consider nonpoint sources, such as hot diffuse gas and dispersed light around galaxies, which we collectively refer to as “diffuse” components.

The measured coherence can be interpreted as the product of the fraction of the emission due to common populations, i.e., $C = \xi_{m} \xi_{m}$, where $\xi_{m}$ is the fraction contributed by the common populations in band $m$. At large angular scales ($\sim 20''$), the level of the measured coherence between 4.5 $\mu$m and [0.5–2] keV is measured to be $C(q) \sim 0.03$–0.05, implying that at least 15%–25% of the large scale power of the CIB fluctuations is correlated with the spatial power spectrum of the X-ray fluctuations, i.e., $\sqrt{C} \gtrsim 15%–25%$. This implies that the true nature of the signal lies somewhere in between two limiting scenarios:

1. 100% of the large-scale CIB fluctuations are contributed by common X-ray sources, which make up $\sim 15%–25%$ of CXB fluctuations, and
2. $\sim 15%–25%$ of the large scale CIB fluctuations are contributed by common X-ray sources, which make up 100% of CXB fluctuations.

Note that $\sqrt{C(q)}$ is a scale-dependent value. It is important to stress that the term “common sources” does not necessarily imply that the corresponding parts of the CIB and CXB are produced by the same physical sources emitting at both IR and X-rays. The IR and X-ray emitters may simply be separated by an angle smaller than the Chandra Gaussian beam of $\pm 10''$ corresponding to a physical scale of $\sim 0.1$ h$^{-1}$ Mpc at $z = 1$. This defines the scale of the individual “objects” in the analysis that follows.

C13 also note that the unresolved CXB fluctuations may be contaminated by ionized gas in the Milky Way. Unfortunately, this component is difficult to model and subtract but it is not expected to exhibit positive cross-correlation with the Galactic cirrus and should rather anticorrelate with infrared emitting dust clouds. Therefore, the observed X-ray fluctuations are an upper limit for the extragalactic CXB component, and its coherence with the CIB, quoted at $C \sim (0.15–0.25)^{2}$, should be considered a lower limit.

### Table 1

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**Notes.**

$^a$ These are the units we use throughout the paper.

$^b$ Refers to Spitzer/IRAC 3.6 $\mu$m and 4.5 $\mu$m flux.

$^c$ Refers to soft X-ray 0.5–2 keV band flux.
can be obtained from population studies and deep observations at other wavelengths.

4.1. Galaxies

The extrapolation of faint galaxy populations suggests an unresolved CIB of $\sim 0.1$–$0.3$ nW m$^{-2}$ sr$^{-1}$ at 3.6 $\mu$m which is mostly produced in the $1 < z < 4$ range (Helgason et al. 2012). The large-scale clustering of these populations, $\delta F/F \lesssim 0.05$, was found to be insufficient to account for the observed CIB fluctuations at large scales (see Figure 6). However, provided that unresolved galaxies dominate the unresolved CXB fluctuations, they could, in principle, produce enough coherence with the CXB to reach $\mathcal{C} \sim 0.02$–$0.05$ while remaining an underdominant component in the CIB fluctuations. In this paper, we use the empirical calculation of Helgason et al. (2012) in which the CIB from galaxy populations was reconstructed using over 230 observed multiwavelength luminosity functions (LFs) measured at $z \lesssim 5$. The faint-end regime of this original reconstruction was extrapolated to low luminosities, and its accuracy has since been verified in deep near-IR source counts from the SEDS survey reaching 26 AB mag Ashby et al. (2013). We address the X-ray emission from these unresolved galaxies in Section 5.1.

4.2. AGNs

The AGNs fraction of the resolved CIB sources is small, $\lesssim 8$%–$10$% (Treister et al. 2006), but their leading role for the CXB makes them important for the interpretation of the CIB×CXB correlation. Here, we estimate the CIB production from AGNs by constructing an AGN population model from J-band LFs of Assef et al. (2011). This sample consists of 1838 AGNs (Type 1 and 2) at $0 < z \lesssim 6$ selected in both IR and X-ray and is therefore less affected by incompleteness and biases seen in purely optical or infrared selected samples. The choice of rest-frame J-band (1.25 $\mu$m) LFs minimizes the uncertainty in the $k$ correction, as distant populations observed at 3.6–4.5 $\mu$m emit light at rest frames $0.7 \lesssim \lambda \lesssim 4.5$ $\mu$m for $z < 4$. We use the pure luminosity evolution parameterization of the AGN LF given by Assef et al. (2011), which includes both host galaxy emission and reddening, extrapolating the parameterized evolution beyond $z > 5$ (assuming LDDE model instead does not affect our results). The inclusion of the host galaxy is important since the X-ray faint AGN tend to be optically obscured and dominated by their host galaxy light, which also contributes to the CIB. At every distance, the 1.25 $\mu$m emission is corrected to $\lambda_{em} = \lambda_{obs}/(1+z)$ using the average low-resolution AGN spectral template of Assef et al. (2010), where $\lambda_{obs}$ is either 3.6 and 4.5 $\mu$m for this paper (see also Richards et al. 2006). Figure 1 shows a reasonable agreement between this projected population and Spitzer/IRAC AGN counts of Treister et al. (2006). Inaccuracies in the shape of the counts may arise from the fact that our mean AGN spectrum is corrected for host galaxy contribution and reddening.

The typical faint-end slope measured for AGN LFs ranges from $-1.6$ to $-1.3$, showing marginal evidence for flattening at higher redshifts (Croom et al. 2009; Glikman et al. 2011). In our model, we conservatively extrapolate a nonevolving faint-end slope of $\beta = -1.4$ to account for unresolved AGNs but this likely overestimates the AGN contribution for several reasons. First, we use LFs uncorrected for host galaxy contribution that bias the faint-end slope and increase the number of faint objects (Hopkins et al. 2007). This effect can be particularly pronounced in the near-IR, as the ratio of host to AGN in unobscured objects has a typical maximum at 1.6 $\mu$m. Second, the 0.5–2 keV versus 3.6 $\mu$m flux ratio turns toward $\chi/O < 0$ at faint fluxes, suggesting a decreasing importance of AGN contribution (Civano et al. 2012). This is consistent with a significant number of optically normal galaxies that are seen as hosts of low-luminosity X-ray AGNs, (e.g., Barger et al. 2005). Diminishing nuclear activity makes the host galaxy dominate at low luminosities, and the distinction between galaxy and AGN becomes less meaningful. Then, these sources should be largely accounted for by our treatment of IR galaxies (see previous subsection). In addition, our treatment of normal galaxies (see Section 4.1) is based on a compilation of observed galaxy LFs which do not typically exclude AGNs.

From Figure 1, it is clear that normal galaxies are far more numerous than AGNs at all flux limits regardless of the extrapolation to faint levels. The CIB contribution of AGNs is always $\lesssim 10$% of the galaxy contribution, and their sky surface density is $\sim 2$–3 orders of magnitude smaller than the $\sim 1$ arcsec$^{-2}$ required to explain the measured CIB fluctuations (Kashlinsky et al. 2007b). AGNs would need to live in low-luminosity X-ray AGNs, (e.g., Treister et al. 2006, circles). The dotted lines show the cases in which the faint-end slope of the AGN LF is extrapolated with a constant slope of $-1.6$ (upper) and $-1.2$ (lower). The green line shows the galaxy reconstruction of Helgason et al. (2012) compared with SEDS data (Ashby et al. 2013, diamonds).

Figure 1. Cumulative source number counts of galaxies (green line) compared with AGNs (blue line). The models for AGNs are constructed from J-band LFs and are uncorrected for host galaxy contribution (explained in the text). Corresponding AGN counts data is from Treister et al. (2006, circles). The dotted lines show the cases in which the faint-end slope of the AGN LF is extrapolated with a constant slope of $-1.6$ (upper) and $-1.2$ (lower). The green line shows the galaxy reconstruction of Helgason et al. (2012) compared with SEDS data (Ashby et al. 2013, diamonds). (A color version of this figure is available in the online journal.)

4.3. Diffuse Emission, Intrahalo Light

Recently, some modeling of the origin of the CIB fluctuations has focused on a form of “missing light” associated with galaxy
populations but distributed in diffuse structures around masked sources. There are several empirical lines of observational evidence that argue strongly against such an origin.

1. There are no spatial correlations between the source-subtracted Spitzer/IRAC maps and galaxies detected in deep Hubble/ACS maps (0.5–0.9 μm)  \( \lesssim 28 \) mag (Kashlinsky et al. 2007c). However, there are very significant correlations between the ACS galaxies and the unmasked Spitzer maps. This means that ACS galaxies and any associated diffuse emission, cannot contribute significantly to the large-scale CIB fluctuations found in source-subtracted Spitzer data.

2. Arendt et al. (2010) show that the large-scale CIB fluctuations are not sensitive to increasing/decreasing the size of masked regions around resolved galaxies. Indeed, Figure 17 of Arendt et al. (2010) shows that there is little variation in the CIB fluctuation as the source masking is eroded or dilated to masking fractions varying from 5% to 7%.

3. Kashlinsky et al. (2005) and Arendt et al. (2010) show that there are no correlations between the source-subtracted CIB fluctuations and the identified removed extended sources. Moreover, Arendt et al. (2010) constructed artificial halos around masked sources and demonstrated that the diffuse emission in the final image does not correlate spatially with the halos around masked sources that mimic missing light. These arguments contradict scenarios invoking any form of “missing light” associated with masked galaxies.

One such scenario was proposed by Cooray et al. (2012b), who considered diffuse starlight scattered around and between galaxies at \( z \sim 1–4 \) as an alternative explanation for the origin of the unresolved CIB fluctuations. This can arise from stars stripped in mergers or ejected via other processes. In this paper, we consider such a diffuse component following definitions in Cooray et al. (2012b), deriving the CIB production history as

\[
\frac{dF_{\text{IHL}}}{dz} = \frac{c}{4\pi} \int_{M_{\text{min}}}^{M_{\text{max}}} L_{\text{IHL},\lambda}(M, z) \frac{dn}{dM} dM \frac{dt}{dz} (1 + z)^{-1},
\]  

(2)

where \( \lambda' = \lambda_{\text{abs}}(1+z) \) using a spectral template of a typical elliptical galaxy containing old stellar populations from Starburst99 (Leitherer et al. 1999). This template assumes a 900 Myr old stellar population forming at the same time with a Salpeter initial mass function (IMF) (1–100 M_\odot) and metallicity \( Z = 0.008 \). In Figure 4, we show that different choices of spectral energy distribution (SED) parameters do not affect the intrahalo light (IHL) flux to a great extent (unless the population is very young < 20 Myr). In all other respects, we follow the formulation in Cooray et al. (2012b) recovering a flux of 1 nW m^{-2} sr^{-1} at 3.6 μm which is consistent with but slightly higher than the 0.75 nW m^{-2} sr^{-1} quoted in Cooray et al. (2012b). We are unable to get the large-scale clustering up to the quoted \( \delta F/F = 10\%–15\% \) and, as a result, our large-scale fluctuations are a factor of ~2–3 lower; this actually provides a somewhat better fit to the measured signal 4.5 μm (see Figure 6).

As is shown in Figure 4, the CIB from this component, Equation (2), exceeds the total CIB from all galaxies already at \( z \gtrsim 2 \) according to the reconstruction of Helgason et al. (2012). Although this by itself makes the model nonviable, we calculate the coherence levels between CIB and diffuse X-ray emission for this component.

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8 The empirical results 1–3 above were omitted from the discussion by Cooray et al. (2012b).

5. SOURCES OF THE CXB

5.1. Normal X-Ray Galaxies

The bulk of the CXB (~80%–90%) has been resolved into point sources, most of which is contributed by AGNs (Hickox & Markevitch 2006; Lehmer et al. 2012). However, the number counts from the Chandra deep fields reveal that the contribution of normal galaxies (mostly XRBs) approaches that of AGNs at the faintest levels (Xue et al. 2011; Lehmer et al. 2012). A simple extrapolation of the slope of galaxies implies that they will ultimately dominate AGNs at \( \lesssim 10^{-17} \) erg s^{-1} cm^{-2} (see Figure 5); this is in fact suggested by deep stacking analyses (Cowie et al. 2012). Although Helgason et al. (2012) demonstrated the low contribution of known galaxy populations to the unresolved CIB, their CXB × CIB amplitude ultimately depends on their X-ray properties.

The X-ray galaxy luminosity function (XLF) derived from Chandra and XMM-Newton data is limited to small samples of local galaxies of \( L_X \sim 10^{40} \) erg s^{-1} (Norman et al. 2004; Tzanavaris & Georgantopoulos 2008) with luminosity evolution consistent with \( L^* \propto (1 + z)^{3.3} \) out to \( z \sim 1 \). The X-ray emission in galaxies is dominated by a population of compact objects accreting from a stellar companion, although hot gas can contribute substantially to the soft X-ray flux (\( \lesssim 1 \) keV). To gain a better understanding of the X-ray galaxy population and its evolution, a popular approach takes advantage of empirical correlations of X-ray luminosity with various galaxy properties derived from longer wavelength data. The XLF can be related to LFs measured at other wavelengths following Avni & Tananbaum (1986):

\[
\Phi(\log L_X) = \int_{-\infty}^{\infty} \Phi(\log L_Y) P(\log L_X | \log L_Y) d\log L_Y \quad (3)
\]

(in num Mpc^{-3} dex^{-1}), where \( Y \) represents a rest-frame band which correlates with X-ray luminosity via some specified \( L_X-L_Y \) relation, and \( P(\log L_X | \log L_Y) \) describes the probability of a source of \( L_Y \) having an X-ray luminosity of \( L_X \). Here, we assume the probability distribution to be Gaussian:

\[
P(\log L_X | \log L_Y) = \frac{1}{\sqrt{2\pi}\sigma} \exp \left[ -\frac{(\log L_X(L_Y) - \log L_X)^2}{2\sigma^2} \right].
\]

where \( L_X(L_Y) \) is the X-ray luminosity predicted by a \( L_X-L_Y \) relation, and \( \sigma \) is the standard deviation of the scatter in the measured correlation.

We consider the X-ray luminosity of normal galaxies to be the sum of contributions from high-mass X-ray binaries (HMXBs), low-mass X-ray binaries (LMXBs), and hot gas

\[
L^\text{rad}_X = L_X(\text{HMXB}) + L_X(\text{LMXB}) + L_X(\text{gas}).
\]

Other forms of galaxy-wide X-ray emission, such as from white dwarf binaries and supernova remnants, have been found to be at least 10 times weaker, so we ignore their contribution in this paper (Boroson et al. 2011). A strong correlation is found between the SFR and the overall X-ray emission of the galaxy which is attributed to active star forming regions producing bright, short-lived (< 100 Myr) HMXBs. On the other hand, long-lived (\( > 1 \) Gyr) LMXBs have been found to correlate well with the net stellar mass in galaxies. For a full census of X-ray galaxies and their different emission mechanism, it is helpful to decompose the population into late (active) and early (quiescent)-type
The tight correlation between X-ray luminosity and SFR has established HMXBs as the dominant mechanism for X-ray production in late-type galaxies (e.g., Ranalli et al. 2003). For the purpose of reconstructing the evolving population of X-ray galaxies, we rely on the total infrared LF (8–1000 μm).\(^9\) This choice is motivated by several points: (1) reradiated dust emission in the FIR is an established tracer of star formation that bypasses uncertainties in UV tracers due to obscuration, (2) the \(L_X-L_{\text{FIR}}\) correlation is both very significant and well calibrated, and (3) the evolution of the FIR LF has been probed out to \(z \sim 3\) allowing the estimation of HMXB activity for four-fifths of the cosmic time. Since the bulk CXB from galaxies comes from late-type galaxies (e.g., Ranalli et al. 2003). For the template LF for early-type galaxies, we have chosen the local \(K\)-band LF of Kochanek et al. (2001) (Two Micron All Sky Survey) for \(z < 0.05\) and the evolving LF Arnouts et al. (2007) from combined SWIRE–VDVS–CFHTLS data reaching \(z = 2\). These measurements separate the contribution from the early-types and late-type to the total LF. The bright (high-mass) end of the LF (stellar mass function) is dominated by early-types, whereas late-types are much more numerous at the faint (low-mass) end. All of the \(K\)-band LFs are well described by the Schechter function, with parameters \(L^*, \phi^*, \sigma\) measured out to \(z = 2\). We fit the evolving parameters in the \(0 < z < 2\) range using the functional forms in Helgason et al. (2012) and extrapolate them beyond \(z > 2\).

\(9\) We denote the total infrared (8–1000 μm) as “FIR” to avoid confusing with “IR”, which we use to refer to the near-IR.

\(10\) We have replaced SFR with \(L_{\text{IR}}\) (in solar units) based on the original relation used by Lehmer et al. (2010), \(\text{SFR} = 9.8 \times 10^{-11} L_{\text{FIR}}\).
To demonstrate this, we use the hot gas properties predicted in semi-analytic models (SAMs) of Guo et al. (2011) mapped onto the Millennium Simulations. The hot gas mass is calculated based on the baryon content, cooling, and infall rate onto the halo (see Guo et al. 2011 for details). We assume a density profile of $\propto (1 + (r/r_0)^2)^{-3\beta/2}$ with a constant $r_0 = R_{vir}/10$ and $\beta = 2/3$ (Anderson et al. 2013) and apply $k$ corrections assuming a thermal continuum spectrum of $\propto T_{vir}^{-1/2} \exp(-E/kT_{vir})$. In this description, the observed [0.5–2 keV] counts are reproduced when all systems with masses below $10^{13} M_\odot$ are included, which is roughly the mass scale of the most massive galaxies. However, the hot gas counts flatten toward lower fluxes where they are dominated by the HMXB component. This is shown as a red dotted line in Figure 5. In Section 5.3 we consider diffuse X-ray emission in more complex environments such as groups and filaments, including the warm–hot intergalactic medium (WHIM).

5.1.4. The Unresolved CXB from Galaxies

The cumulative source density seen on the sky is

$$N(> S) = \int \int S dS' d\Omega' = \int \int S dS' dz,$$

where the differential is expressed in terms of the XLF as

$$d^3N/dS dz = 4\pi d^2(z)K(z) dV/dz,$$

where $dV/dz = c d^2(z)(1 + z)^{-1} dt/dz$ is the comoving volume element and $K(z)$ is the k-correction. For a power-law spectrum, $E^{-\Gamma}$, with a spectral index $\Gamma$, the k-correction becomes $(1+z)^{\Gamma-1}$. The power-law slope of X-ray galaxy spectra has been found to lie in the $1 < \Gamma < 3$ range with a mean of $\approx 1.8$, which is what we assume for the HMXB and LMXB contribution. For the hot gas component, we k-correct using a thermal continuum spectrum, $\propto T^{-0.5} \exp(-E/kT)$.

Figure 2 shows the predicted cumulative X-ray counts of our galaxy population models (Equation (8)) and compares them with the observed deep counts of Lehmer et al. (2012) showing both the early- and late-type contribution. The bright counts rise with a near-Euclidian slope and start turning over toward the faint regime as expected from both the LF turnover and cosmic expansion. At the flux limit of today’s deepest measurements, $\sim 10^{-17}$ erg s$^{-1}$ cm$^{-2}$, the source counts are dominated by $L_{IR}$ galaxies (at the knee of the LF) gradually turning over to the faint-end regime, which only becomes relevant at much fainter levels ($\lesssim 10^{-19}$ erg s$^{-1}$ cm$^{-2}$). As long as the flux converges, the unresolved CXB fluctuations are not very sensitive to the faint-end slope of the XLF.

The spatial CIB×CXB correlation signal is detected by C13 after masking sources resolved in both the Chandra and Spitzer/IRAC maps. The common IR/X-ray mask leaves $\sim 68\%$ of the pixels in the overlapping $8' \times 4'$ region for the Fourier analysis. The superior resolution and depth reached in the Spitzer exposure maps causes faint X-ray sources to be subtracted well below the detection threshold of the Chandra maps. The depth of the joint CXB×CXB analysis is therefore mostly determined by the IR source subtraction. In this paper, we assume a fixed magnitude limit in the Spitzer/IRAC maps with X-ray sources removed according to a selection function $\eta(S_X|m_{lim})$, where $m_{lim}$ refers to the IRAC magnitude limit of the near-IR mask. We also tried relaxing the assumption of a fixed $m_{lim}$ and instead used the complement of the source selection completeness in the SEDS EGS field. This has little effect on our results. In order to obtain $\eta(S_X|m_{lim})$ at flux levels inaccessible to current X-ray observatories, we look at the distribution of $f_X/f_{IR}$ predicted in the SAM of Guo et al. (2011) mapped onto the Millennium Simulation (for a detailed description, we refer to Guo et al. 2011). Mock lightcones based on this model were constructed by Henriques et al. (2012). Although mostly consistent with galaxy counts in the optical, the SAM tends to overestimate the number of small systems causing the abundance of faint galaxies to overpredict observed 3.6 $\mu$m and 4.5 $\mu$m counts. We therefore apply a post-correction
From Figure 3, it is clear that most of the background light by a factor to the galaxy population by shifting excess sources of magnitude $m$ by a factor

$$\Delta m = \frac{|m(n_{\text{obs}}) - m(n = n_{\text{obs}})|}{\delta},$$

(10)

where $m(n)$ are the Millennium SAM derived counts, and $n_{\text{obs}}$ are the observed counts. We find that for a modification factor of $\delta = 1.05$, the population of Henriques et al. (2012) is brought into a good agreement with the observed counts while conserving the total number of systems and their redshift distribution. Figure 3 shows the 4.5 $\mu$m versus 0.5–2 keV brightness distribution of normal galaxies according to the Millennium SAM where we have used the SFR and $M^*$ to predict the X-ray luminosity via $L_X = \alpha M^* + \beta \text{SFR}$ of Lehmer et al. (2010) and include a scatter of $\sigma = 0.4$. This is essentially the same relation as the $L_X-L_{\text{IR}}$ in Equation (6) with the conversion $\text{SFR}/L_{\text{IR}} = 9.8 \times 10^{31}$. The approximate detection limit of the Spitzer maps is shown in Figure 3 as a horizontal line and the color scheme scales with flux per solid angle, i.e., depicting the contribution to the total CXB×CIB background. From Figure 3, it is clear that most of the background light is resolved and eliminated in the masking process with a diminishing contribution from the remaining unresolved sources toward the bottom left. We define the selection function of 0.5–2 keV source removal as the unresolved galaxy fraction

$$\eta(S_X|m_{\text{lim}}) = \frac{N(S_X|m > m_{\text{lim}})}{N(S_X|m)}$$

(11)

display it in the bottom panel in Figure 3. This shows that, for an IR limit of 25 mag, 90% of sources are removed at $\approx 3 \times 10^{-18}$ erg s$^{-1}$ cm$^{-2}$ which is considerably fainter than the flux limit of CDF-S (Xue et al. 2011). Systems identified as subhalos in the Millennium catalog were removed together with its parent halo, provided it is brighter than $m_{\text{lim}}$. The subhalos have little effect on our results.

Our XLF model allows us to construct the flux production rate per solid angle from undetected galaxies as

$$\frac{dF_X}{dz} = \int \eta(S) S \frac{d^3N}{dSdzd\Omega} dS,$$

(12)

where $d^3N/dSdzd\Omega$ comes from Equation (9)b and $F_X$ is the X-ray flux per solid angle. Figure 4 shows the history of the emitted X-rays from galaxies remaining after removing IR sources brighter than 25 mag. Very little CXB remains at $z \lesssim 0.5$ after source subtraction but rises thereafter and peaks at $z \sim 1$, close to the peak of the star formation history.

### 5.2. X-Ray AGN

The resolved CXB is dominated by AGN populations, which have been studied in detail by Chandra and XMM-Newton out to $z \sim 3$. For X-ray AGNs, we use the population model of Gilli et al. (2007) based on XLFs and evolution of AGNs. The models consider the observed XLFs, $k$ corrections, absorption distribution, and spectral shapes of AGNs and return the observed X-ray flux distribution at any redshift. The models have been shown to adequately reproduce source counts, redshift distribution, and intrinsic column densities. Our adopted AGN population contains sources in the $0 < z < 8$ range with a wide range in luminosity, $38 < \log(L_X/\text{erg s}^{-1}) < 47$, to allow for very faint unresolved sources. Column densities are
20 < \log(N_H/cm^2) < 26. The evolution of the AGN XLF in Gilli et al. (2007) is modeled with and without an exponential decay at z > 2.7 on top of the extrapolated evolution from lower redshift parameterization of Hasinger et al. (2005), i.e., \( \phi(L, z) = \phi(L, z_0)10^{-0.43(z-z_0)} \) with \( z_0 = 2.7 \). We do not include the decrease at high-z, which results in a CIB×CXB signal within a factor of two of the case with a decline. In Figure 5, we show the counts from our adopted AGN model and compare with data.

The extent to which AGN are removed by the joint IR/X-ray mask of C13 is estimated based on data from Civano et al. (2012) who provide X/IR flux ratios for 1761 sources in the COSMOS survey reaching \( S_{0.5-2\text{keV}} = 1.9 \times 10^{-16} \text{erg s}^{-1} \text{cm}^{-2} \). Toward faint fluxes AGN trend to become brighter at 3.6 \( \mu \text{m} \) deviating from the classic X/O = 0. We fit a linear relation to the 3.6 \( \mu \text{m} \) versus 0.5–2 keV distribution, \( m_{\text{IR}} = -1.5 \log S_X - 1.7 \), and extrapolate to the faint regime with a large Gaussian dispersion of \( \sigma = 1.5 \text{mag} \). We then apply \( m_{\text{IR}} = 25 \) to extract the selection \( n(S) \) for the X-ray removal (see Equation (11)). The scatter \( \sigma = 1.5 \text{mag} \) is chosen such that the resulting shot noise \( P_{\text{SN}}^X \) in the X-ray power spectrum matches the data. The selection is shown in the top panel in Figure 5 which demonstrates the extended tail of unresolved X-ray AGN caused by the wide dispersion in their IR flux (see Civano et al. 2012). In Figure 4 we show the unresolved AGN CXB production rate as function of the redshift. The bulk of the CXB flux from undetected AGN comes from \( z \sim 1 \).

### 5.3. Diffuse Hot Gas and WHIM

In Section 5.1, we calculated the CXB contribution of hot gas heated within galaxies. However, diffuse gas in groups and filaments (including the WHIM) also contributes to the CXB and was found to dominate the unresolved 0.5–2 keV CXB fluctuations of (Cappelluti et al. 2012b). Scaling relations indicate that the X-ray masking of C13 removes galaxy clusters and groups down to \( \log(M/M_\odot) = (12.5-13.5) \) (i.e., \( kT < 1.5 \text{keV} \), Finoguenov et al. 2007). Thus, only the low luminosity (low mass) and warm population of galaxy groups and filaments contributes to the unresolved CXB.

Since this class of objects is difficult to model analytically, we describe their properties using a set of mock maps from Roncarelli et al. (2012), who used a cosmological hydrodynamical simulation to define the expected X-ray surface brightness due to the large-scale structures. The original hydrodynamical simulation (see the details in Tornatore et al. 2010) follows the evolution of a comoving volume of \( 37.5 h^3 \text{Mpc}^3 \) considering gravity, hydrodynamics, radiative cooling, and a set of physical processes connected with the baryonic component, among which a chemical enrichment recipe that allows to follow the evolution of seven different metal species of the intergalactic medium (IGM). From its outputs, Roncarelli et al. (2012) simulated 20 lightcones with a size of \( \sim 0.25 \text{deg}^2 \) each, covering the redshift interval \( 0 < z < 1.5 \). Each pixel of the maps contains information about the expected observed spectrum in the 0.3–2.0 keV band with an energy resolution of 50 eV. The emission coming from the IGM was computed assuming an emission from an optically thin, collisionally ionized gas (Apec in XSPEC) model and considering the abundances of the different metal species provided by the simulation.

These maps/spectra have been convolved with the Chandra response in order to reproduce the effective Chandra count rates. Since the CXB data of C13 are masked for galaxy clusters, we apply a source masking on the simulated maps. We have simulated observations with the actual depth of the C13 field. We have added an artificial isotropic particle and cosmic background according to the levels estimated directly from the maps of C13. Random Poisson noise was artificially added to the image, and we ran a simple wavelet detection with a signal-to-noise ratio threshold of 4. We have then excluded all of the regions within which the overall encircled signal from sources is above 4\( \sigma \) with respect to the background. The unresolved CXB production rate averaged over all the realizations is shown in Figure 4.

### 6. THE ANGULAR AUTO/CROSS-POWER SPECTRUM OF MULTIPLE POPULATIONS

Cosmic background fluctuations can be described by the angular power spectrum, \( P(q) \). This can be written as the sum of the clustering and shot noise of the underlying source populations:

\[
P_{\text{tot}}(q) = P(q) + P_{\text{SN}},
\]

where \( q \) is the angular wavenumber in rad\(^{-1}\). The first term, representing the clustering, can be related to the three-dimensional power spectrum of the underlying sources, \( P(k,z) \), by projection via the Limber equation (Limber 1953):

\[
P(q) = \int \frac{H(z)}{cd^2(z)} \sum_i \sum_{j>i} \left[ \frac{dF}{dz} \right] \left[ \frac{dF}{dz} \right] P_{ij}(qd_c^{-1}, z)dz,
\]

where \( d_c(z) \) is the comoving distance and \( H(z) = H_0 \sqrt{\Omega_M (1 + z)^3 + \Omega_r} \). The quantities in the square brackets are the comoving distance \( (1 + z) \) units for different source populations, which are denoted by the indices \( i \) and \( j \) running over our three populations: (1) galaxies, (2) AGN, and (3) diffuse emission. The summation

---

**Figure 5.** Upper: the selection of the unresolved regime for galaxies (darkest gray shade) and AGNs (gray shade). Note that, for a constant \( m_{\text{IR}} \) limit, a larger fraction of AGN remain unresolved due to their higher X/O ratio and greater dispersion. The complement of the X-ray source selection in AEGIS-XD (Goulding et al. 2012) is shown for comparison (lightest gray shade). This essentially defines the unresolved regime in C13 for X-ray source removal, i.e., without additional IR masking. Lower: the source counts from our adopted AGN model and comparison with data. The dotted line shows the hot gas contribution from virialized halos.

(A color version of this figure is available in the online journal.)
results in six terms, three auto power terms \((i = j)\), and three cross terms \((i \neq j)\) which represent the coupling of different populations that live at the same epochs sharing the same environments. The shot noise arises from the fluctuation in the number of sources within the instrument beam. It only depends on the flux distribution of sources and can be expressed as

\[
P_{\text{SN}} = \int_{S_{\text{lim}}}^{S_{\text{max}}} S^2 \sum_i \left[ \frac{dN}{dS} \right]_i dS, \tag{15}
\]

where \(S_{\text{lim}}\) is the minimum detected source brightness, and \(i\) denotes the source population as before. Note that the shot noise, sometimes called Poisson term, does not have coupling terms as it represents a random process and is uncorrelated between different populations. Figures 6 and 7 show the modeled auto power spectrum of the angular fluctuations in the CIB and the CXB respectively, comparing them with current measurements.

In the description above, “coupling” terms \((i \neq j)\) refer to the correlation of different populations at the same wavelength, not cross-power between two wavelengths. The CIB×CXB cross-power spectrum can be written\(^{11}\)

\[
P_{\text{tot}}^{\text{IR}, \text{X}}(q) = \int \frac{H(z)}{cd^2(z)} \sum_i \sum_j \left[ \frac{dF^\text{IR}}{dz} \right]_i \left[ \frac{dF^\text{X}}{dz} \right]_j P_{ij}(qd_c^{-1}, z)dz, \tag{16}
\]

where the summation results in nine terms representing all combinations of cross-correlated X-ray and IR contributions from different source populations (note the different summation over \(j\) compared to the conditional \(j \geq i\) in Equation (14)). The cross-power of the shot noise term is

\[
P_{\text{SN}}^{\text{IR}, \text{X}} = \int_0^{S_{\text{IR}}} \int_0^{S_{\text{X}}} S_{\text{IR}}^2 S_{\text{X}}^2 \frac{d^2N}{dS_{\text{IR}}dS_{\text{X}}} dS_{\text{IR}} dS_{\text{X}}, \tag{17}
\]

which is added to \(P_{\text{tot}}^{\text{IR}, \text{X}}(q)\). However, this expression requires additional knowledge of the \(dS_{\text{IR}}/dS_{\text{X}}\) dependence of each population in order to be evaluated. As our model construction lacks this information, we instead use

\[
P_{\text{SN}}^{\text{IR}, \text{X}} = \int \left[ \frac{dP_{\text{SN}}^{\text{IR}}}{dz} \frac{dP_{\text{SN}}^{\text{X}}}{dz} \right]^{1/2} dz. \tag{18}
\]

We test the accuracy of this equation using the Millennium lightcones, which give \(P_{\text{SN}}^{\text{IR}, \text{X}}\) directly, and find it to be a good approximation to Equation (17) (see Figure 9).

6.1. Halo Model

Our description of angular fluctuations requires knowledge of the power spectrum of luminous sources, \(P_{ij}(k)\)

\[^{11}\text{Just as the two-point correlation function is related to the auto power spectrum, the cross power spectrum is simply the Fourier transform of the cross-correlation function, } C_{\text{xx}}(\theta) = \langle \delta F_{\text{y}}(x) \delta F_{\text{y}}(x + \theta) \rangle.\]
where \(i \neq j\) describing the correlated fluctuations between sources within the same parent halo; and a two-halo term, \(P^{2h}\), arising from the spatial correlation of two sources hosted by separate parent halos. As before, the \(i \neq j\) terms represent coupling terms between different populations, whereas for \(i = j\) the expressions reduce to the more familiar form of Cooray & Sheth (2002). For source populations \(i\) and \(j\), these can be written as

\[
P^{1h}_{ij}(k) = \int \frac{d n}{d M} \frac{\langle N^c_i N^j_0 + N^j_i N^c_0 \rangle u(k|M)}{\bar{n}_i\bar{n}_j} d M \tag{19}
\]

\[
P^{2h}_{ij}(k) = P^{\text{lin}}(k)(B^c_i + B^j_i)(B^c_j + B^j_j), \tag{20}
\]

where

\[
B^c_i = \int \frac{d n}{d M} \frac{N^c_i}{\bar{n}_i} b(M) d M \tag{21}
\]

\[
B^j_i = \int \frac{d n}{d M} \frac{N^j_i}{\bar{n}_i} b(M) u(k|M) d M, \tag{22}
\]

where \(i \neq j\) represents cross terms, and \(i = j\) reduces these expression to the more familiar form of Cooray & Sheth (2002). The individual quantities are defined as follows.

1. \(P^{\text{lin}}(k, z)\) is the linear \(\Lambda\)CDM power spectrum computed using the transfer function of Eisenstein & Hu (1998) and the adopted cosmological parameters;
2. \(\langle N^c_i(M, z) \rangle\) (\(N^c_i\) shorthand) is the average halo occupation of central sources;
3. \(\langle N^j_i(M, z) \rangle\) (\(N^j_i\) shorthand) is the average halo occupation of satellite sources;
4. \(\bar{n}_i(z)\) is the average number density of population \(i\) such that

\[
\bar{n}_i = \int \left\langle \left( N^c_i(M, z) + N^j_i(M, z) \right) \right\rangle \frac{d n}{d M} d M; \tag{24}
\]

5. \(P^{\text{lin}}(k, z)\) is the linear \(\Lambda\)CDM power spectrum computed using the transfer function of Eisenstein & Hu (1998) and the adopted cosmological parameters;
6. \(u(k|M)\) is the normalized Fourier transform of the Navarro–Frenk–White (NFW) halo profile (Navarro et al. 1996; Cooray & Sheth 2002); and
7. \(b(M, z)\) is the linear halo bias adopted from the ellipsoidal collapse formalism of Sheth et al. (2001).

It should be kept in mind that all quantities in Equations (19)–(22) are evolving with redshift but we have omitted this dependence in the expressions to keep the notation tidy.

\[\text{Figure 8. Upper: the approximate lowest halo mass removed by the IR mask as a function of redshift obtained from the Millennium SAM of Guo et al. (2011). The three lines correspond to 80%, 90%, and 95% of systems in the Millennium catalog being removed (top to bottom). The dashed line indicates the approximate removal threshold of groups/clusters in the X-ray maps (see Erfanianfar et al. 2013)). Lower: the large scale bias, \(b_{\text{gal}}\) (Equation (30)), from galaxies, AGNs, and diffuse components. The solid lines show the biasing for a masked density field with the mass selection function in the upper panel, whereas the dotted lines show the case of no source subtraction. Notice that at low redshift, the density field of undetected systems is underbiased. (A color version of this figure is available in the online journal.)}\]

6.2. Halo Occupation, Bias, and Mass Selection

The HOD has been widely investigated for both galaxies and AGNs. We adopt standard parameterizations of \(N^c_i(M)\) and \(N^j_i(M)\), which have been found to match observed data. For galaxies, we assume the four parameter description of Zheng et al. (2005)\(^{12}\):

\[
N^c_{\text{gal}} = \frac{1}{2} \left[ 1 + \text{erf} \left( \frac{\log M - \log M_{\text{min}}}{\sigma_{\log M}} \right) \right], \tag{25}
\]

\[
N^j_{\text{gal}} = \frac{1}{2} \left[ 1 + \text{erf} \left( \frac{\log M - \log 2M_{\text{min}}}{\sigma_{\log M}} \right) \right] \left( \frac{M}{M_{\text{sat}}} \right)^{\alpha}, \tag{26}
\]

where \(M_{\text{min}}\) is the minimum halo mass that can host a central galaxy, and \(\sigma_{\log M}\) controls the width of the transition of the step from zero to one central galaxy. The satellite term has a cutoff mass which is twice as large as the one for central galaxies and grows as a power law with a slope of \(\alpha\) and is normalized by \(M_{\text{sat}}\). The amplification of the fluctuations through large-scale biasing is most sensitive to the choice of \(M_{\text{min}}\), which is not well known as galaxies in the lowest mass halos are not detected. However, at a given redshift, the source subtraction removes the massive halos from the top down and limits the range of mass scales where the unresolved fluctuation signal arises, \(M_{\text{min}} < M < M_{\text{cut}}(z)\), where \(M_{\text{cut}}(z)\) is the lowest mass halo removed at \(z\) (see Figure 8, upper). We have adopted the

\(^{12}\) \(N^j\) is a shorthand notation for \(\langle N^j_i(M, z) \rangle\) and is in general redshift dependent.
following parameters of the HOD model motivated by Sloan Digital Sky Survey measurements of Zehavi et al. (2011): $\sigma_{\log M} = 0.2$, $M_{\text{min}} = 10^{10} M_\odot$, $M_{\text{cut}} = 5 \times 10^{10} M_\odot$, and $\alpha = 1$, where we have deliberately chosen a low cutoff mass, $M_{\text{min}}$, allowing low-mass halos hosting galaxies well into the unresolved regime.

The HOD of AGNs is less certain due to low number statistics but AGNs seem to be preferentially found in halos of $\sim 10^{12.5} M_\odot$. The HOD has been measured for X-ray selected AGNs at $z \lesssim 1$ (Miyaji et al. 2011; Allevato et al. 2012; Richardson et al. 2013) and optical quasars out to $z \sim 3$ (Shen et al. 2013; Richardson et al. 2012). Previous studies suggest that, compared to optical quasars, X-ray selected AGNs are more strongly clustered and reside in more massive host halos but the host halo mass range is insufficiently constrained for a definitive conclusion (Cappelluti et al. 2012a). Like galaxies, the central AGNs are modeled as a softened step function at $M_{\text{min}}$ but the satellites are described by a power law with a low-mass rolloff:

$$N_{\text{AGN}}^S = \frac{1}{2} \left[ 1 + \exp \left( \frac{\log M - \log M_{\text{min}}}{\sigma_{\log M}} \right) \right], \hspace{1cm} (27)$$

$$N_{\text{AGN}}^S = \left( \frac{M}{M_1} \right)^{\alpha} \exp \left( - \frac{M_{\text{cut}}}{M} \right). \hspace{1cm} (28)$$

This description has five free parameters: $M_{\text{min}}$, the characteristic mass scale of the step where the HOD goes from zero to a single AGN per halo, with the transition width controlled by $\sigma_{\log M}$. The mass at which a halo contains on average one satellite AGN is described by $M_1$; $\alpha$ is the power-law index controlling the steepness of the satellite HOD with increasing host mass; and $M_{\text{cut}}$ is the mass scale below which the satellite HOD decays exponentially. We have chosen parameters obtained in a numerical study of Chatterjee et al. (2012) that agree with measured values when a selection of $L_{\text{bol}} > 10^{42}$ erg s$^{-1}$ is applied. We interpolate the redshift evolution of the $L_{\text{bol}} > 10^{42}$ erg s$^{-1}$ parameters given in Table 2 of Chatterjee et al. (2012).

The HOD of our diffuse component is somewhat uncertain as it does not describe the same population in X-rays and IR, i.e., hot/warm gas as opposed to diffuse starlight. We allow the diffuse component to trace the NFW halo profile by considering a satellite term only, setting the HOD of central sources to zero. For diffuse IR, we adopt the parameters from the IHL model of Cooray et al. (2012b), discussed in Section 4.3, and assume that this component arises in halos in the $\sim 10^9$ to $10^{12.5} M_\odot$ range. However, gas does not reach sufficient temperatures in such small halos but we neglect this by allowing hot gas to live in halos anywhere below the mass limit of detected (and removed) groups and clusters identified by Erfanianfar et al. (2013) in the EGS field (see dashed line in Figure 8).

When faced with source-subtracted images, the density field is modified in the process of masking the brightest sources which live in the most massive, and consequently, most biased halos. This effect can be accounted for by knowing the mass-dependent luminosity distribution, i.e., the conditional LF. Since we do not have this information, we use the semi-analytical model of Guo et al. (2011) mapped onto the Millennium Simulations to explore the halo mass dependence of source removal in deep IR maps. We eliminate all galaxies brighter than $m_{\text{lim}} = 25$ and construct a mass selection function defined as the fraction of unresolved systems as a function of host halo mass:

$$\eta(M, z) = \frac{N(M, z) > m_{\text{lim}})}{N(M, z)}.$$

We display this function in Figure 8 (upper panel), which shows the mass scale at which 80%, 90%, and 95% of the systems are removed as a function of redshift. We multiply our galaxy HOD (Equation (25)) by this function, thereby subtracting the massive halos from the density field (including their satellites). Since this function is derived from galaxies, we do not apply this mass selection to the AGN and diffuse component and instead use the X-ray cluster/group detection limits of Erfanianfar et al. (2013) as the upper mass limits. The overall effect of this is shown in Figure 8.

The amplification of fluctuations through large scale biasing of the sources follows from Equation (22) in the limit where $u(k|M) \rightarrow 1$, or equivalently

$$b_M^\text{eff}(z) = \int \frac{dM}{dM} \frac{N_s^c + N_s^d}{n} b(M, z) dM,$$

where the mass-dependent bias comes from the prescription of Sheth et al. (2001). The quantity is shown in Figure 8 for galaxies, AGNs, and diffuse emission. We also show the bias without halo subtraction due to $\eta(M)$, i.e., in the absence of source masking. Note how the density field becomes underbiased at low redshifts where the mask is most effective.

6.3. Comparing Fluctuation Models with N-body Simulations

In real measurements, the angular power spectrum is obtained directly from the masked and Fourier transformed image, $P_m(q) = \langle \Delta_m(q) \Delta^*_m(q) \rangle$. However, our calculation of $P(q)$ relies on the projection of emitting populations via the Limber equation with empirically motivated assumptions for their HOD. A more sophisticated treatment would link the source luminosities to host halo masses in a conditional LF, $\Phi(L|M)$ (see, e.g., Cooray 2006; Béthermin et al. 2013). In order to test the validity of the approximations made, we make use of the Millennium Simulation SAM of Guo et al. (2011) to derive the unresolved CIB × CXB power spectrum from galaxy populations. The evolving simulation box has been projected to construct lightcones which provide 2 deg$^2$ mock images of the extragalactic sky based on the SAM (Henriques et al. 2012). From the mock catalogs, we remove all galaxies brighter than IRAC3,6,4.5 magnitude 25 AB, including substructure associated with the parent halo. The X-ray emission is calculated using the relation of Lehmer et al. (2010): $L_X = \alpha M^\ast + \beta \text{SFR} + (1 + z)^{0.5}$, where we have added the last term to account for evolution (see Section 5.1).

We calculate the source-subtracted fluctuations directly from the mock images, $\langle \Delta_s(q) \Delta^*_s(q) \rangle$, and compare the results with our fluctuation model in Figure 9. Despite the difference in approach, this SAM and our population model predict consistent fluxes and CIB × CXB cross-power. Caveats worth mentioning include the halo resolution limit of Millennium $\sim 10^{10} M_\odot$ and the possibility of spurious power arising from the replication of the simulation box required for the lightcone construction (see Blaizot et al. 2005). The agreement with our model is nevertheless encouraging.

7. RESULTS

7.1. CIB Fluctuations

Figure 6 shows the auto power spectrum of CIB fluctuations from unresolved galaxies, AGNs, and IHL, comparing them with the measurements of C13. The contribution from unresolved galaxies (green) is discussed in detail in Helgason.
et al. (2012), the IHL (red) is close to that of Cooray et al. (2012b). We only use the default model from Helgason et al. (2012) which has been validated in the SEDS survey (Figure 34 in Ashby et al., 2013), reducing the uncertainties of the faint-end extrapolation of the LF. The contribution from AGNs (blue) is much smaller due to their low numbers compared to IR galaxies, <10%. In addition, C13 found that their source-subtracted CIB power spectrum is independent of the X-ray mask. This means that X-ray flux that may be missed by the IR mask, such as from the wide wings of the extended Chandra point-spread function (PSF), will show up in the CIB power spectrum but will not contribute to the cross-power CIB×CXB.

7.2. CXB Fluctuations

We find that the CIB power spectrum is dominated by shot noise from unresolved AGN (see Figure 7) with the contribution from galaxies and gas being considerably lower. However, a different study (Cappelluti et al. 2012b) finds the largest contribution to come from hot gas. There are various reasons for the different findings. First, the X-ray maps of Cappelluti et al. (2012b) are deeper (4 Ms) than C13 (800 ks), allowing Cappelluti et al. (2012b) to directly mask AGNs to much fainter levels. Second, Cappelluti et al. (2012b) modeled AGNs in the luminosity range $42 < \log (L/L_\odot) < 47$, whereas we include AGNs all the way down to $\log (L/L_\odot) = 38$. This makes a substantial difference in the abundance of faint AGNs.

The net CIB from unresolved galaxies and AGNs is $2.1 \times 10^{-13}$ and $7.9 \times 10^{-14}$ erg s$^{-1}$ cm$^{-2}$, respectively. Whereas the CXB power spectrum is consistent with being entirely due to shot noise from unresolved AGNs, there is a hint of additional clustering toward large scales which is not accounted for. No reasonable amount of clustering (bias $\lesssim 30$) is sufficient to account for enhanced CXB fluctuations on scales >200$'$.

This component is real and extragalactic in nature, it could indicate the source of the coherence with the CIB fluctuations. However, it is important to note that the 0.5–2 keV fluctuations are contaminated by foreground emission from the Galaxy, which is not sensitive to the removal of extragalactic point sources. Therefore, any interpretation of the CXB power spectrum carries an intrinsic source of uncertainty due to the contribution of the Galaxy. A non-negligible Galaxy component at $<1$ keV could explain why C13 measure a low level of cross-correlation between [0.5–2] keV and [2–4.5]–[4.5–7] keV maps. While irrelevant for the CXB×CIB cross-power spectrum, correcting for the Galaxy would reduce the measured CXB power spectrum. Additionally, the extended PSF of Chandra could spread some fraction of the X-ray point source flux outside the finer IR mask. This would not show up in the CIB×CXB cross-power, as the large scale CIB fluctuations do not correlate with either IR or X-ray removed sources.

7.3. CIB×CXB Fluctuations

We start with summarizing the resultant contributions to the cross-power from three main components appearing in Figure 10: galaxies, AGNs, and diffuse.

1. Galaxies. The largest contributions to the cross-power comes from galaxies (galIR × galX, green line) and AGNs (galIR–AGNX, purple line). A significant galaxy–galaxy component is expected because (1) they make up a substantial unmasked CIB component and (2) dominate AGNs at faint X-ray fluxes (see Figure 5). The small-scale cross-power is in good agreement with the data, the galIR × galX shot noise making up $\sim 30\%$. However, this fraction decreases toward large scales. In order to explain the shape of the CIB×CXB fluctuations at all scales in terms of galaxies only, one needs to alleviate the problem of the low clustering with respect to shot noise, as is the case with the CIB fluctuations. Simply increasing the flux of the unresolved populations would overproduce the small-scale power. A way of increasing the large-scale power without affecting the shot noise is to enhance the galaxy bias. However, this requires bias of $\gtrsim 10$, which is not expected for faint, low-mass systems. We therefore conclude that the entire CIB×CXB signal cannot originate from normal galaxies unless future measurements show that the cross fluctuations (g$^2 P(q)/2/\pi$) decrease toward large scales as opposed to staying roughly flat, as indicated by the C13 data.

2. AGN. Shot noise from unresolved AGNs provides the largest contribution, $\sim 60\%$, to the small-scale CIB×CXB power (Figure 10, blue line). This is because a greater fraction of bright AGNs remains unresolved after IR masking (see Figure 5). At large scales, their AGNIR×AGNX contribution is small due to lower flux in both IR and X-rays compared with galaxies. However, a substantial contribution comes from X-ray AGNs correlating with IR galaxies (purple line). As shot noise does not appear in this term, the cross-power spectrum has a shape that resembles the data but with an amplitude which is more than an order of magnitude below the data. To test whether this term could be enhanced, we examined the case in which the IR source subtraction removes no additional AGNs, i.e., only AGNs detected in X-rays are removed. This gives an amplitude that is one order of magnitude below the data points. Enhancing the clustering of the AGN population to the levels of very biased high-z quasars, corresponding to AGNs living in $>10^{13} M_\odot$ halos, still falls below the measured levels. In fact, both our AGN population model (Gilli et al. 2007) and our AGN removal selection (Civano et al. 2012) are chosen conservatively and should, if anything, give a smaller signal (see Figure 5).

3. Diffuse. Dispersed starlight around and between masked galaxies can share the same environment with diffuse warm gas in collapsed halos and filaments. For distant structures, however, the thermal spectrum of the ionized gas, $\sim 1$ keV, quickly redshifts out of the 0.5–2 keV band (see Section 5.3) and therefore has limited correlations with the IHL that
mostly arises at different epochs, $z \sim 1–4$. Despite this, the large scale CIB×CXB component arising between IHL and warm gas at $z < 1$ is comparable to that of galaxies and AGNs (see Figure 10, red). The diffuse component could be made larger if the bulk of IHL emission arose at low-$z$ in halos $\gtrsim 10^{12.5} M_\odot$ but this would be unlikely to explain the entire CIB×CXB data. Coherence between IHL and X-ray galaxies/AGNs is also difficult to accommodate for the following reasons. In the resolved regime, the point sources are masked so any X-ray emission originating in the central regions is eliminated with no correlation with diffuse IR light outside the mask. In the unresolved regime, the IR galaxies themselves should dominate over IHL which can only constitute a fraction of the total galaxy light. We already account for the coherence of unresolved IR galaxies with X-ray galaxies/AGNs. Furthermore, the fact that the CIB fluctuations are not sensitive to the X-ray mask argues against the removed X-ray sources being responsible for the CIB×CXB signal. We note the additional problems with the IHL hypothesis in Section 4.3.

Despite the large uncertainties in the data, there seems to be a systematic lack of cross-power at large scales $> 300''$, where the source clustering is in the linear regime. At small scales, our modeled shot noise term is in agreement with the data. To better understand these results, we consider a simple model composed of linear $\Lambda$CDM clustering and a noise term, $P(q) = a_1 P_{\Lambda\text{CDM}} + a_2$, with the two individual terms shown as light gray regions. Our model of net contribution from galaxies, AGNs, and diffuse emissions is shown as a black dashed line. (black line) is a poor fit to the data ($\chi^2/8 = 2.8$), falling more than an order of magnitude below the best-fit model. A quantitative comparison is shown in Table 2. This distinction is not significant at $3.6 \mu$m versus [0.5–2 keV] due to the

Figure 10. X-ray vs. IR cross-power terms of all source populations compared to measurements from Cappelluti et al. (2013). The total cross-power spectrum from all terms is shown as a solid black line. The individual terms are galaxiesIR–galaxiesX (green), galaxiesIR–AGNX (purple), galaxiesIR–diffuseX (orange), AGNIR–galaxiesX (turquoise), AGNIR–AGNX (blue), and diffuseIR–diffuseX (red). Auto terms are shown as dashed lines ($i = j$), whereas coupling terms ($i \neq j$) are shown as dashed-dotted lines.

(A color version of this figure is available in the online journal.)
large uncertainties but the systematically growing discrepancy toward large scales suggests the same behavior as 4.5 μm versus [0.5–2 keV]. This is illustrated in Figure 12.

8. CONCLUSIONS AND DISCUSSION

In this paper, we have considered known populations of X-ray sources at z < 6 in an attempt to explain the measured spatial coherence of the unresolved CIB and CXB. The dominant contribution to the modeled CIB × CXB signal comes from unresolved galaxies containing XRBs and IR galaxies associated with X-ray emitting AGNs found within the same large-scale structures. However, we find that the combined contribution from galaxies, AGNs, and hot gas is unable to produce the large-scale cross-power needed to explain the data. At 4.5 μm versus 0.5–2 keV, the large-scale cross-power is only (2.6% ± 1.0%) of the best-fit model but the discrepancy decreases toward small angular scales where the shot noise becomes consistent with the best fit. At 3.6 μm versus 0.5–2 keV, these identifications are not robust due to larger uncertainties in the data.

Warm gas in $10^{13.5}$ M$_\odot$ systems can be bright at $z \lesssim 0.5$ but IR sources are eliminated down to $\sim 10^{11}$ M$_\odot$ in this redshift range. A significant source of coherence may arise at low z in association with diffuse starlight (IHL). However, the correlation of IHL with unresolved X-ray galaxies/AGNs at higher redshifts is problematic. Whereas at $z = 0$, the IHL corresponds to $\sim 1\%$ of the total CIB produced by galaxy populations, at $z \gtrsim 2$, it seems to exceed the total CIB from all galaxies (see Figure 4). The lack of correlation between the source-subtracted CIB fluctuations and (1) deep Hubble/ACS maps (Kashlinsky et al. 2007c) and (2) test halo images (Arendt et al. 2010), also makes it difficult to favor missing starlight as a dominant component of the fluctuations.

While other mechanisms capable of producing a correlation between X-rays and IR may exist, they are generally expected to be much weaker than the dominant forms considered in this work: galaxies, AGNs, and hot gas. Thermal emission from hot dust $\sim 700$ K would have to arise in the local universe as it would otherwise redshift out of the near-IR bands and it is also inconsistent with the observed blue color of the source-subtracted CIB fluctuation in the 2.4–4.5 μm range. Because of its red colors, any dust dominated component would have to be underdominant in the CIB fluctuations while being associated with X-ray emission from the dominant CXB component, i.e., the Galaxy foreground or obscured AGN. Infrared cirrus emission in the Galaxy should absorb X-rays and exhibit a negative cross-power contrary to the measurements of C13. In the case of obscured AGN, they make up a greater fraction of the hard CXB and are less significant in soft X-rays. This is not consistent with the fact that C13 detect CIB × CXB cross-correlation in the 0.5–2 keV band but not in the harder bands. Furthermore, the cross-correlation between the [0.5–2] keV band and both [2–4.5] and [4.5–7] keV are small. There is a hint of clustering in the CXB power spectrum at $> 10^4$, which may or may not be the source of coherence with the CIB. However, the component producing the large scale CIB × CXB cannot constitute less than $\sim 15\%$–20% of the CXB clustering.

The possibility that the CIB × CXB signal is contributed by high-z miniquasars is discussed in C13. Such objects are expected to form early and grow rapidly in order to explain the population of bright quasars already in place at $z \sim 6$. Yue et al. (2013b) have constructed a population model of highly obscured direct collapse black holes that is able to account for (1) net CIB measurements and γ-ray absorption constraints; (2) the shape and amplitude of the source-subtracted CIB fluctuations; (3) the unresolved soft CXB level; and (4) the shape and amplitude of the spatial coherence in the unresolved CIB × CXB. The inclusion of such a component improves the CIB × CXB best fit considerably (see Figure 11). Whether these requirements can be realistically satisfied physically by other types of high-z mini-quasars, and at the same time stay within limits imposed by reionization and black hole mass growth, will be investigated in future work.

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REFERENCES


Figure 12. Systematic discrepancy of the cross-power spectra of our model and the data as a function of angular scale. $P_{\text{data}}(q)/P_{\text{model}}(q)$. The normalized model is indicated by the dashed line. The 1σ regions of the best-fit, two-parameter model is shown in light gray.

| Table 2 |
| Comparison of our Net Model with the Best-fit Model $P(q) = a_1 P_{\Lambda CDM} + a_2$ |

<table>
<thead>
<tr>
<th>Clustering ($a_1 \times 10^{17}$)</th>
<th>Shot Noise ($a_2 \times 10^{19}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(3.6 μm)</td>
<td>(4.5 μm)</td>
</tr>
<tr>
<td>Best fit</td>
<td>2.5 ± 2.1</td>
</tr>
<tr>
<td>This work</td>
<td>1.0 ± 0.4</td>
</tr>
</tbody>
</table>

Notes. The power is in units of erg s$^{-1}$ cm$^{-2}$ nW m$^{-2}$ sr$^{-1}$. * Clustering at 1000″.