GUIDED WAVE DELAMINATION DETECTION AND QUANTIFICATION
WITH WAVEFIELD DATA ANALYSIS

Zhenhua Tian
Department of Mechanical Engineering,
University of South Carolina,
Columbia, SC 29208, tianz@email.sc.edu

Cara A.C. Leckey
Nondestructive Evaluation Sciences Branch,
NASA Langley Research Center,
Hampton, VA 23681, cara.ac.leckey@nasa.gov

Jeffrey P. Seebo
Analytical Mechanics Associates, Inc.
Hampton, VA 23681, jeffrey.p.seebo@nasa.gov

Lingyu Yu
Department of Mechanical Engineering,
University of South Carolina,
Columbia, SC 29208, yu3@cec.sc.edu

ABSTRACT

Unexpected damage can occur in aerospace composites due to impact events or material stress during off-nominal loading events. In particular, laminated composites are susceptible to delamination damage due to weak transverse tensile and interlaminar shear strengths. Developments of reliable and quantitative techniques to detect delamination damage in laminated composites are imperative for safe and functional optimally-designed next-generation composite structures. In this paper, we investigate guided wave interactions with delamination damage and develop quantification algorithms by using wavefield data analysis. The trapped guided waves in the delamination region are observed from the wavefield data and further quantitatively interpreted by using different wavenumber analysis methods. The frequency-wavenumber representation of the wavefield shows that new wavenumbers are present and correlate to trapped waves in the damage region. These new wavenumbers are used to detect and quantify the delamination damage through the wavenumber analysis, which can show how the wavenumber changes as a function of wave propagation distance. The location and spatial duration of the new wavenumbers can be identified, providing a useful means not only for detecting the presence of delamination damage but also allowing for estimation of the delamination size. Our method has been applied to detect and quantify real delamination damage with complex geometry (grown using a quasi-static indentation technique). The detection and quantification results show the location, size, and shape of the delamination damage.

1. INTRODUCTION

Aviation safety is an area of focus in NASA’s aeronautics work. Damage due to impact events must be detected and the damage must be evaluated to determine if repairs are needed for safe operation. Matrix cracking, fiber breakage, fiber–matrix debonding, and delamination are the most common types of damage in fiber composites [1]. In particular, laminated composites are susceptible to delamination damage due to their weak transverse tensile and interlaminar shear strengths (as compared to their in-plane properties) [1]. Delamination damage can occur largely internally to the composite such that a damage indication is barely visible on the composite surface to the naked eye; such damage is known as Barely Visible Impact Damage (BVID) [2]. Damage below the BVID limit is not visible on the composite surface, even if delamination damage exists internally. Such hidden delamination damage must be detected and evaluated before it becomes critical. The problem of how best to detect such material changes in laminated composite components is still being solved, and a solution to this problem will be imperative for safe and functional, optimally-designed next-generation composite aircraft. Current composite “safety margin” design comes with a weight penalty which could be mitigated by the development of accurate, efficient, and reliable structural health monitoring (SHM) methods to locate and quantify the unique damage types that can occur in composite materials.

Guided ultrasonic waves have proven effective for SHM due to their ability to inspect a large area while maintaining the sensitivity to small defects in the structure [3-8]. Advances in guided wave based SHM technologies over the last decade have
demonstrated the feasibility of detecting and locating damages in composite structural components [9-17]. Due to the complex wave interaction that occurs when hidden delamination damage is present, tremendous efforts have been put into delamination detection methodologies and the study of wave interaction with this damage type, such as references [17-23].

In this paper, we study guided wave interactions with the delamination damage and apply wavefield analysis methodologies to analyze the complex wave interaction phenomenon and to quantify the delamination damage. A scanning laser Doppler vibrometer is used to measure the time-space wavefield of guided wave interactions with the delamination. Three dimensional (3D) Fourier transform (FT) was used to transform the wavefield data from the time-space domain into frequency-wavenumber domain where further wave propagation information is revealed. To detect and quantify the delamination damage, we apply a wavenumber field analysis method which can provide the wavenumber value at each spatial location. The wavenumber field analysis method is then applied to inspect a plate with impact induced delamination damage. The detection and quantification results show clear indication of the location, size, and shape of the delamination damage.

2. GUIDED WAVES IN LAMINATED COMPOSITES

When guided waves propagate in a delaminated composite, multiple reflections within the delamination region can occur, as shown in references [24-28]. Hence, a considerable amount of ultrasonic energy is “trapped” above and below delaminated regions until eventually the energy dissipates. Ramadas et al. studied the interaction of the antisymmetric A₀ mode with symmetric delaminations [25]. They also identified multiple reflections in the delamination region. The trapped energy phenomenon of guided wave propagation in delaminated composites has also been studied experimentally through the use of wavefield images obtained from laser vibrometry tests [26, 27]. It is observed that upon entering the delaminated region, the incident waves will be split above and below the delamination and then propagate independently through upper and lower lamina (single delamination scenario being assumed). After that, a significant portion of the waves are reflected back from the far edge of the delamination region. The reflected waves then pass back above (or below) the delaminated area and experience reflections at the original entrance to the delamination region. The process is repeated until the energy is dissipated, as found in the simulation work reported by Hayashi and Kawashima[24]. Glushkov et al. also observed similar wave energy trapping and localization in a strip delamination by using laser vibrometry to record the wavefield [28].

Since the material layers above and below the delamination have different thicknesses from the original plate thickness, the trapped waves will accordingly have different wave propagation characteristics. Therefore, it is expected that by analyzing the trapped wave signals, the delamination dimensions can be quantified. Prior work by Rogge and Leckey demonstrated that wavenumber analysis can be used to determine the approximate depth and size of near-surface delamination damage [23]. This paper demonstrates quantitative characterization of the trapped waves, along with delamination detection and sizing utilizing the trapped wave phenomenon for real delamination damage.

To demonstrate the fundamentals of guided wave propagation and interactions in laminated composites, two 380 mm×380 mm 8-ply IM7/8552 composite laminate plates with layup [0/2/90]₃s are first studied. One plate was pristine, while the other contained a delamination created by inserting a 20mm×20mm Teflon film under the second ply during manufacturing. Guided waves are actuated by a surface bonded 7 mm round PZT patch at 300 kHz, while the time-space wavefield data are acquired by a scanning laser Doppler vibrometer and are used to investigate the wave propagation [29]. Figure 1 shows the schematic of the test plate (detailed experimental setup can be found in [29]).

Figure 2 shows the time-space wavefields of the guided waves propagating along the y-axis (1D wave propagation). For the pristine case in Figure 2a, a faster S₀ mode and a slower A₀ mode can clearly be observed. For the delaminated case in Figure 2b, waves propagating back and forth between the beginning (y=20 mm) and ending (y=40 mm) boundaries of the delamination can be distinctively seen, exhibiting a “trapped wave” phenomenon [27].

Figure 3 shows the snapshots of the wavefields in the scan area. Figure 3a is the wave propagation recorded at 15 μs when the incident S₀ mode interacts with the delamination damage. We see there are waves propagating both upward and downward between delamination boundaries (upper and lower). At 30 μs, as shown in Figure 3b, the incident A₀ mode is interacting with the delamination damage. The figure shows a localized yet complicated interference pattern in the delamination region due to the multiple trapped waves and wave interferences at this time.

![Figure 1. Composite plate setup for the laser vibrometry test.](image-url)
Figure 2. The time-space wavefields of the waves propagating along the y axis: (a) for the pristine plate, and (b) for the delaminated plate. The two solid black lines at 20mm and 40mm are the delamination boundaries.

3. DATA ANALYSIS APPROACHES

Though interesting wave interactions have been observed in the time-space wavefield, a quantitative evaluation is not yet readily obtained. To quantify the complicated wave interactions within the delamination region, further wave data analysis becomes essential. Wave propagation characteristics such as wave mode content, as well as how the waves evolve as with frequency or space are also desired. Prior works reported in the literatures have demonstrated that wavefield data in the frequency-wavenumber representation have abundant information regarding the existence of various wave modes and wave propagation characteristics [21, 30-33]. We therefore develop and apply several quantitative wave analysis approaches based on wavenumber information in order to study wave interactions with delamination type defects, and to detect delamination damage quantitatively.

3.1. Frequency-wavenumber spectral analysis

Frequency-wavenumber information of the guided waves can be obtained from the time-space wavefield by applying a 3D FT, mathematically given as

$$U(f, k) = F[u(t, x)] = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} u(t, x) e^{-j(2\pi f' - kx)} dt dx$$

where the space vector $x$ and the wavenumber vector $k$ in Cartesian coordinates are defined as $(x, y)$ and $(k_x, k_y)$. $u(t, x)$ is the time-space wavefield in terms of the time $t$ and the space vector $x$. $U(f, k)$ is the resulting frequency-wavenumber representation or “spectrum” in terms of the frequency $f$ and the wavenumber vector $k$. As the frequency is the counter part of time, the wavenumber is the counter part of space. The mathematics of the frequency-wavenumber technique can be found in several references [21, 30-34].

Figure 3. Guided wave propagation and “trapping” in the delaminated composite plate: (a) the $S_0$ mode interacting with the delamination at 15 $\mu$s, and (b) the $A_0$ mode interacting with the delamination at 30 $\mu$s. The black solid lines are the delamination boundaries.

Figure 4a and 4b show plots of the frequency-wavenumber spectra of the experimental wavefields for the pristine and delaminated cases, respectively. To identify the wave mode information, the frequency-wavenumber spectra are compared with the theoretical dispersion curves which are plotted as dotted ($A_0$) and solid ($S_0$) lines. The pristine plate frequency-wavenumber spectrum (Figure 4a) shows the lower amplitude $A_0$ and higher amplitude $S_0$ modes, which match well with the theoretical dispersion curves.
In the delaminated plate, the delamination damage splits the originally bonded full laminate into two parts (above and below the delamination). Since the two separated parts have different layups and thinner thicknesses compared to the original pristine laminate, the guided waves in the separated parts will have modified propagation characteristics (such as modified dispersions and wavenumbers).

As expected, the spectrum of the delaminated case (Figure 4b) shows new frequency-wavenumber components in addition to the original A₀ and S₀ modes. The new frequency-wavenumber components include both positive and negative counterparts, which correspond to the forward and backward propagating waves, respectively. We compared the new frequency-wavenumber components with the dispersion curves of the material above the delamination, equivalent to a two ply [0\0] laminate, since only the waves in the top plate surface was measured in the experiment. The comparison in Figure 4b shows the new frequency-wavenumber components match well with the theoretical curves of A₀ mode in the two ply [0\0] laminate. This analysis result agrees well with the real delamination depth which is below the second ply.

3.2. Spatial wave filtering

The frequency-wavenumber analysis result shows that new frequency-wavenumber components appear in the spectrum of the delaminated plate, and are correlated to the waves in the delamination region. To further confirm this result, a wave filtering process is used to extract the new frequency-wavenumber components and transform them back into the time-space domain. The filtering process is mathematically expressed as the product between the frequency-wavenumber spectrum $U(f, k)$ and a filter function $F(f, k)$ as:

$$U_f(f, k) = U(f, k)F(f, k)$$  (2)

where $F(f, k)$ denotes a filter in the frequency-wavenumber domain and $U_f(f, k)$ is the filtered spectrum, which only keeps the delamination induced new wavenumbers. By transforming the filtered spectrum $U_f(f, k)$ back into the time-space domain through inverse 3D FT, we can obtain the filtered time-space wavefield $u_F(t, x)$ as

$$u_F(t, x) = F^{-1}[U_f(f, k)]$$  (3)

Since the filtered spectrum $U_f(f, k)$ only keeps the new frequency-wavenumber components, it is expected that the corresponding time-space wavefield $u_F(t, x)$ only contains the trapped waves induced by the delamination.

Figure 5 shows the filtered time-space wavefield along the y axis. Comparing this result to the wavefield before filtering (Figure 2b), it is seen that the filtered time-space wavefield shows trapped waves that exist between the delamination boundaries.

Figure 6 shows a snapshot at 30μs of the filtered wavefield in the scan area. The filtered wavefield only contains the trapped waves in the delamination region, and shows the feasibility of using the trapped waves for delamination size quantification. Moreover, the wavefield filtering results further confirm that the new frequency-wavenumber components in Figure 4b correspond to the trapped waves in the delamination region.

Figure 4. The frequency-wavenumber spectra of the time-space wavefields in Figure 2: (a) for the pristine plate, and (b) for the delaminated plate. The solid and dotted lines are theoretical dispersion curves for S₀ and A₀ wave modes, respectively.

Figure 5. The filtered time-space wavefield of the waves propagating along y axis. The two solid black lines at 20mm and 40mm are the delamination boundaries.
Figure 6. A snapshot at 30μs of the filtered wavefield in the 2D scan area. The black solid lines are the delamination boundaries.

3.3. Wavenumber field analysis

The frequency-wavenumber analysis presented in the section 3.1 unveils wave propagation characteristics that cannot be explicitly seen in the time-space domain. However, in the resulting frequency-wavenumber representation \(U(f, k)\), the spatial information \(x\) is not available from the result of the 3D FT (see Figure 4).

It is quite often desirable to know how the wavenumber changes in space. To retain the spatial information, a novel short space 3D FT has been applied to acquire a space-frequency-wavenumber representation. The technique is a straightforward extension of the short time FT to multi-dimensional problems, i.e., breaking down the time-space wavefield into small segments over the space dimension before Fourier transformation [35]. To do this, the wavefield data is multiplied by a window function which is non-zero for only a short period in space while constant over the entire time dimension. The 3D FT is then applied to the resulting wavefield segments. When the window slides along the space dimension, a set of windowed wavefield segments is generated. The 3D FT is then applied to the resulting wavefield segments. Mathematically, the short space 3D FT is implemented through spatial windowing technique, as

\[
S(\bar{x}, f, k) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} u(t, x)W(t, x - \bar{x})e^{-j(2\pi f t - k \cdot \bar{x})} dt dx
\]

where \(\bar{x}\) is the retained spatial vector and \(W(t, x)\) is a window function. In our study, a Hanning function is used to construct the window \(W(t, x)\), given as:

\[
W(t, x) = \begin{cases} 
0.5 \left[ 1 + \cos \left( \frac{2\pi |x|}{D_s} \right) \right] & \text{if } |x| \leq D_s / 2 \\
0 & \text{otherwise}
\end{cases}
\]

Then, for a specific frequency \(f_0\), we define the wavenumber field as

\[
k^*(\bar{x}, f_0) = \arg \max_k |S(\bar{x}, f, k)|
\]

For a series of frequencies \(f_i\) \((i=1,2,3,...N)\) within a small frequency band, the wavenumber field is defined as

\[
k^*(\bar{x}) = \frac{1}{N} \sum_{i=1}^{N} |k^*(\bar{x}, f_i)|
\]

The wavenumber field \(k^*(\bar{x})\) contains the local wavenumber information at each spatial point. Figure 7 gives the wavenumber field calculated from the time-space wavefield of the delaminated plate. The wavenumber field shows an area which has larger wavenumber values than the rest. This region matches well with the real delamination location and size. Since the delamination damage affects the wavenumber (as demonstrated in section 3.1), the wavenumber field can be used to detect and quantify the delamination location and size.

Figure 7. The calculated wavenumber field from the experimental time-space wavefield in the delaminated plate. The black solid lines are the delamination boundaries.
4. IMPACT-INDUCED DELAMINATION DETECTION AND QUANTIFICATION

The previous section has shown that the wavenumber analysis approaches yields quantitative information of guided wave interactions and wave trapping in delamination regions; and can also be used as delamination detection tools. In this section, the wavenumber analysis methods are used to detect and quantify real impact-induced delamination damage in laminated composite plates.

4.1. Damage growth in a CFRP plate

A quasi-static indentation technique was used to grow damage in a CFRP plate. The technique has been shown by previous authors to be an ideal method for controlled growth of impact-like damage in composite laminates[36]. The composite sample is a 26 ply IM7/8552 381 mm × 381 mm laminate with a quasi-isotropic layup of [(0/45)-45]/90]S. The composite plate was loaded in a mechanical testing system using a 50.8 mm diameter indenter at a constant displacement rate of 1.27 mm/min. The displacement and load were monitored during the indentation test and the composite was unloaded when the data showed a sudden drop in load (due to damage growth), as shown in Figure 8b. A photo of the CFRP plate after the indentation test is shown in Figure 9a. Figure 9b is a zoomed in view which shows a very slight indentation on the surface with no other surface damages.

Following the quasi-static indentation test, an ultrasonic Cscan was used to quantify the resulting delamination damage under the plate surface. The Cscan data were collected in an immersion tank using a 10 MHz transducer and a scan step size of 0.25 mm. The Cscan image in Figure 9c shows multiple delaminations within the 32.3 mm × 22.6 mm damage zone, occurring at various depths through the plate thickness.

4.2. Delamination detection and quantification

A 7 mm round PZT was installed on the CFRP plate surface (shown in Figure 9a) to generate guided waves at 500 kHz. A scanning laser Doppler vibrometer was used to measure the wavefield in the CFRP specimen containing the impact-induced delamination damage. Figure 10a is a wavefield snapshot at 55 μs showing the guided wave propagations and interactions. The incident guided waves interact with the damage and are trapped in the delamination region. Due to the existence of multiple wave modes and complex wave interactions, it is difficult to detect and quantify the delamination damage only from the original measured time-domain wavefield. Further wavefield processing is required.

To detect and quantify the damage, both the wavefield filtering and wavenumber field analysis methods were used. Figure 10b gives the wavefield filtering result which only retains the trapped waves. The trapped waves clearly indicate the delamination location.

Figure 10c shows the wavenumber field over the test area. The delamination damage is clearly observed as larger wavenumbers in wavenumber field. The detected delamination size in the wavenumber field is approximately 30 mm × 20 mm, which agrees well with the Cscan result. Moreover, the

Figure 8. Quasi-static indentation for delamination damage growth: (a) the indentation setup, and (b) the curve of indentation force versus displacement.

Figure 9. The 26 ply laminate after the quasi-static indentation: (a) a photo of the specimen, (b) a zoomed view of the indentation, and (c) a Cscan image showing the interior delamination damage generated by the indentation test.

Figure 10. Wavefield filtering and wavenumber field analysis for delamination damage quantification: (a) wavefield snapshot, (b) wavefield filtering result, and (c) wavenumber field over the test area.
delamination shape in the wavenumber field closely matches the delamination shape in the Cscan image Figure 9c.

Figure 10. The delamination damage detection and quantification results: (a) the wavefield snapshot at 55 μs shows the guided wave interactions and trappings in the impact-induced delamination damage, (b) the filtered wavefield snapshot at 55 μs shows the trapped waves at the damage, and (c) wavenumber field shows the location and shape of the damage.

5. CONCLUSIONS

This paper presents our studies on guided wave interactions with impact induced delamination damage and damage quantification techniques for laminated composite plates. The wavefield data analysis confirms the wave trapping phenomenon. Quantitative interpretation of the wave behaviors in the delamination region via different wavenumber analysis methods is demonstrated. Among the methods studied, the frequency-wavenumber analysis shows that the frequency-wavenumber spectrum can indicate the presence of new wavenumbers. The reconstructed wavefield images created from the new wavenumber components demonstrate that the new wavenumbers correlate to trapped waves in the delamination region. Additionally, the wavefield shows how the wavenumber changes as a function of the propagation distance. Thus, the location and spatial duration of the new wavenumbers can be identified, providing a useful means not only for detecting the presence of delamination damage but also sizing the damage. Finally, the wavenumber field analysis shows the wavenumber values at each spatial point indicating not only the location and size, but also the shape of the damage.

The developed analysis methods have been applied to detect impact-induced delamination damage in a carbon fiber reinforced polymer plate. The delamination is barely visible even from careful visual inspection while C-scan images show internal delamination of about 30 mm × 20 mm size. By using wavenumber field analysis, interior delamination damage is detected and quantified.

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REFERENCES