Elemental Water Impact Test: Phase 1
20-inch Hemisphere

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Acknowledgments

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Abstract

Spacecraft are being designed based on LS-DYNA simulations of water landing impacts. The Elemental Water Impact Test (EWIT) series was undertaken to assess the accuracy of LS-DYNA water impact simulations. Phase 1 of the EWIT series featured water impact tests of a 20-inch hemisphere dropped from heights of 5 feet and 10 feet. The hemisphere was outfitted with an accelerometer and three pressure gages. The focus of this report is the correlation of analytical models against test data. Three analytical models were used:

1. Closed-Form Solution
2. 2-D Axisymmetric LS-DYNA Model
3. 3-D Quarter Symmetry LS-DYNA Model

The closed form solution was found to over-predict the peak acceleration. The peak pressure from the closed-form solution is infinite; however, the solution does provide a reasonable prediction for the late-time pressure decay.

The 2-D axisymmetric LS-DYNA model was evaluated for a broad range of modeling parameters. The two parameters that were found to be the most critical were mesh density and fluid-structure coupling stiffness. The 2-D model provided reasonable predictions for the acceleration histories. Pressure histories were poorly predicted; however, reasonable predictions were obtained for the impulse as determined by integrating the pressure history. Increasing mesh density resulted in better predictions for the late-time pressure decay, but did not improve the predictions of the early-time peak pressure.

The 3-D quarter symmetry LS-DYNA model was used for further evaluations of mesh density and fluid-structure coupling stiffness. The 3-D model produced predictions for the acceleration histories that better matched the test data than the 2-D model. The pressure histories from the 3-D model were equally as poor as the 2-D model. Again, the impulse was predicted far more accurately than the pressure.

The following guidelines were proposed for defining the fluid mesh density and fluid-structure coupling stiffness for LS-DYNA simulations. These guidelines might not be feasible for spacecraft water landing design simulations due to limits in available computer resources.

1. The element size of the fluid mesh should be no larger than 1/200th of the radius of curvature of the structure.
2. The coupling stiffness curve should be established based on the maximum expected coupling pressure at a penetration equal to 1/10th the size of the fluid elements.

Guidelines were also offered for judging the adequacy of the fluid-structure coupling definition.

1. The coupling stiffness is too soft if the peak coupling pressure is toward the middle of the contact patch rather than at the perimeter.
2. The coupling stiffness is too soft if the acceleration time history exhibits oscillations that can be related to the structure bouncing on the coupling surface.
3. The coupling stiffness is too stiff if the coupling pressure distribution appears as a checkerboard pattern of isolated pressure spikes.
4. The coupling stiffness is too stiff if the coupling pressure histories appear as a series of isolated spikes.
# Table of Contents

1. **Introduction**......................................................................................................................... 1
2. **Simulations**........................................................................................................................... 1  
   2.1. LS-DYNA............................................................................................................................... 1  
   2.2. ALE Solution Parameters ...................................................................................................... 1  
   2.3. Element Section Parameters ............................................................................................... 2  
   2.4. Material Parameters ............................................................................................................ 2  
   2.5. Equation of State Parameters ............................................................................................. 2  
   2.6. Fluid Structure Coupling Parameters .................................................................................. 2  
   2.7. Boundary Conditions ......................................................................................................... 2  
   2.8. Gravity and Atmospheric Preload ...................................................................................... 3  
3. **Tests**...................................................................................................................................... 3  
   3.1. Test Configuration ................................................................................................................ 3  
   3.2. Test Article .......................................................................................................................... 4  
   3.3. Test Results ........................................................................................................................ 5  
4. **Simulation Models**............................................................................................................. 8  
   4.1. Closed-Form Solution .......................................................................................................... 8  
   4.2. 2-D LS-DYNA Simulation ................................................................................................... 9  
   4.3. 3-D LS-DYNA Simulation .................................................................................................. 11  
5. **Test and Simulation Correlation**.......................................................................................... 13  
   5.1. Closed-Form Results ......................................................................................................... 13  
   5.2. 2-D LS-DYNA Results ....................................................................................................... 15  
   5.3. 3-D LS-DYNA Results ....................................................................................................... 30  
6. **Establishing Simulation Parameters without Test Data**...................................................... 38  
   6.1. Width of Pressure Pulse ...................................................................................................... 38  
   6.2. Establishing Mesh Density and Coupling Stiffness ............................................................ 39  
   6.3. Evaluating Model Performance without Test Data ............................................................. 40  
7. **Conclusions and Recommendations**................................................................................ 43  

References........................................................................................................................................ 44  

Appendix A: Two-Dimensional Axisymmetric Model .................................................................... 45  
Appendix B: Three-Dimensional Quarter Model ........................................................................... 48
List of Figures

Figure 1. Test Set-Up ..................................................................................................................... 4
Figure 2. Hemisphere Configuration ............................................................................................. 4
Figure 3. Pressure Transducer Locations ....................................................................................... 5
Figure 4. Raw Acceleration Histories for 5-foot Drops ................................................................. 5
Figure 5. Filtered Acceleration Histories for 5-foot Drops ............................................................. 6
Figure 6. Raw Acceleration Histories for 10-foot Drops ............................................................... 6
Figure 7. Filtered Acceleration Histories for 10-foot Drops .......................................................... 7
Figure 8. Pressure Histories for 5-foot Drops ................................................................................ 8
Figure 9. Pressure Histories for 10-foot Drops .............................................................................. 8
Figure 10. Two-Dimensional Axisymmetric Model .................................................................... 10
Figure 11. Mesh Variants for Two-Dimensional Axisymmetric Model ...................................... 11
Figure 12. Three-Dimensional Quarter Model ............................................................................ 12
Figure 13. 0.025-inch Fluid Element Mesh Variant .................................................................... 13
Figure 14. Closed-Form Solution Acceleration History for 5-foot Drop .................................... 14
Figure 15. Closed-Form Solution Acceleration History for 10-foot Drop .................................. 14
Figure 16. Closed-Form Solution Pressure History for 5-foot Drop ........................................... 15
Figure 17. Closed-Form Solution Pressure History for 10-foot Drop ........................................ 15
Figure 18. Acceleration Histories for 5-foot Drop for 0.025-inch Element Size ....................... 16
Figure 19. Acceleration Histories for 5-foot Drop for 0.05-inch Element Size .......................... 16
Figure 20. Acceleration Histories for 5-foot Drop for 0.1-inch Element Size ............................ 17
Figure 21. Acceleration Histories for 10-foot Drop for 0.025-inch Element Size ....................... 17
Figure 22. Acceleration Histories for 10-foot Drop for 0.5-inch Element Size .......................... 18
Figure 23. Acceleration Histories for 10-foot Drop for 0.1-inch Element Size .......................... 18
Figure 24. Peak Accelerations for Mesh and Coupling Stiffness Variants for 5-foot Drops ...... 19
Figure 25. Peak Acceleration for Mesh and Coupling Stiffness Variants for 10-foot Drops ...... 19
Figure 26. Pressure in Fluid versus DBFSI Pressure at Coupling Surface ................................ 20
Figure 27. Pressure Histories for 5-foot Drop for 0.025-inch Element Size ............................... 21
Figure 28. Pressure Histories for 5-foot Drop for 0.05-inch Element Size .................................. 21
Figure 29. Pressure Histories for 5-foot Drop for 0.1-inch Element Size ................................... 22
Figure 30. Pressure Histories for 10-foot Drop for 0.025-inch Element Size ............................. 22
Figure 31. Pressure Histories for 10-foot Drop for 0.05-inch Element Size ............................... 23
Figure 32. Pressure Histories for 10-foot Drop for 0.1-inch Element Size ................................... 23
Figure 33. Pressure Histories for 5-foot Drop for 10 x Curve 10 Mesh Variants ........................ 24
Figure 34. Pressure Histories for 10-foot Drop for 10 x Curve 10 Mesh Variants ..................... 24
Figure 35. Peak Pressure for Mesh and Coupling Stiffness Variants for 5-foot Drops ............... 25
Figure 36. Peak Pressure for Mesh and Coupling Stiffness Variants for 10-foot Drops ............. 25
Figure 37. Impulse for Mesh and Coupling Stiffness Variants for 5-foot Drops ........................ 26
Figure 38. Impulse for Mesh and Coupling Stiffness Variants for 10-foot Drops ....................... 26
Figure 39. Pressure Contours for Coupling Stiffness Variants for 5-foot Drop ......................... 27
Figure 40. Peak Filtered Accelerations for Sensitivity Study Variants ........................................ 28
Figure 41. Peak Pressures for Sensitivity Study Variants ............................................................. 29
Figure 42. Pressure Pulse Caused by a 0.02-inch Divot .............................................................. 30
Figure 43. Acceleration History for 5-foot Drop Simulations ..................................................... 31
Figure 44. Acceleration History for 10-foot Drop Simulations ................................................... 31
Figure 45. Pressure Histories for 5-foot Drop Simulations .......................................................... 32
Figure 46. Pressure Histories for 10-foot Drop Simulations .......................................................... 33
Figure 47. Pressure Distribution at 0.001 seconds after Impact for 5-foot Drop Simulations .... 34
Figure 48. Pressure Distribution at 0.001 seconds after Impact for 10-foot Drop Simulations .. 35
Figure 49. Acceleration Histories for Mesh Variants for 5-foot Simulations.............................. 36
Figure 50. Acceleration Histories for Mesh Variants for 10-foot Simulations............................ 36
Figure 51. Pressure Histories for Mesh Variants for 5-foot Simulations .................................... 37
Figure 52. Pressure Histories for Mesh Variants for 10-foot Simulations .................................. 37
Figure 53. Pressure Transducer Arrangement ............................................................................. 38
Figure 54. Pressure Histories for Multiple Pressure Transducers................................................ 39
Figure 55. Description of Penetration and Leakage................................................................. 41
Figure 56. Symptoms of an Excessively Soft Coupling Stiffness ............................................... 42
Figure 57. Symptoms of Excessively High Coupling Stiffness.................................................... 43

List of Tables

Table 1. Parameters Varied for Sensitivity Study ........................................................................ 28
Table 2. Pressure Transducer Locations ...................................................................................... 38
Table 3. Pressure Pulse Width Estimate ...................................................................................... 39
Table 4. Recommendations for Element Size and Coupling Stiffness ........................................ 40
1. Introduction

Spacecraft are being designed based on LS-DYNA [1] simulations of water landing impacts. The Elemental Water Impact Test (EWIT) series was undertaken to assess the accuracy of LS-DYNA water impact simulations. Phase 1 of the EWIT series featured water impact tests of a 20-inch hemisphere dropped from heights of 5 feet and 10 feet.

2. Simulations

2.1. LS-DYNA

LS-DYNA is a general purpose transient dynamic finite element code capable of simulating complex real world problems. LS-DYNA’s strength is in the modeling of impact problems. An explicit time integration scheme is used in which there is no equilibrium check and iteration of the solution between time steps. This approach works only because the time step is restricted to be smaller than the shortest stress wave transit time for any element in the model.

The modeling of contact between bodies in LS-DYNA is accomplished via a penalty method. Contact is detected when the nodes of one body pass through the face or edges of the elements of another body. Preloaded penalty springs are then inserted to push the bodies apart. One consequence of this approach is one body must always penetrate another body before contact is detected. Another consequence is that there is a finite contact stiffness at the interface between the bodies that is entirely nonphysical.

LS-DYNA has a limited capability to model a fluid using Arbitrary Lagrangian-Eulerian (ALE) meshes. In the ALE approach, each time step begins with a mesh that is conceptually similar to the Lagrangian meshes used to model structures. LS-DYNA determines the deformation of the fluid that occurs during the time step, then moves, or advects, the mesh back to its original configuration and treats the fluid as having moved through the mesh. The result is that the nodes of the mesh do not move. Instead, the volume fraction of the fluid in each element is changed. The fluid in the ALE mesh can flow, compress, and impart momentum; however, the ALE mesh does not offer a full Navier-Stokes fluid flow solution.

LS-DYNA features many parameters that can be adjusted in modeling of fluid-structure interaction problems. An overarching parameter is the mesh density. As with all finite element codes, a smaller element size generally produces results that are more accurate. In addition to mesh density, there are many other solution parameters that can be selected. Several of these are discussed in the following sections.

2.2. ALE Solution Parameters

The *CONTROL_ALE card includes several parameters, most of which should be allowed to take default values. The number of solution cycles per mesh advection step, NADV, should ideally be specified as 1, though it can be set to a higher value if necessary to reduce solution time. Various options for the mesh advection method, METH, are available. The developer recommends METH=2, which is second order accurate. Other options can be tried if necessary to reduce solution time. Several parameters are available for mesh advection smoothing. The developer warns that the smoothing algorithm is not based in physics. It is recommend that smoothing be turned off, AFAC=-1.
2.3. Element Section Parameters

For a 2-D mesh, *SECTION_ALE2D offers two axisymmetric element formulations. ELFORM=14 is area weighted and ELFORM=15 is volume weighted. The code developer strongly recommends ELFORM=14. For a 3-D mesh, *SECTION_SOLID offers two treatments of an air space above a fluid. ELFORM=11 allows the air to be treated as a fluid with its own equation of state. ELFORM=12 treats the air as a void space. The code developer recommends ELFORM=11.

2.4. Material Parameters

Fluids with an equation of state utilize *MAT_NULL. The most important material property for the impact problem is the material density, RO. The tensile pressure cutoff, PC, is typically set to either zero or a very small negative number. If the air is treated as a void space (ELFORM=12), it may be desirable to set PC equal to negative one atmosphere (-14.7 psi) in order to mimic the fact that cavitation does not occur until the pressure drops to zero absolute pressure. The LS-DYNA Keyword User's Manual [2] implies that a non-zero value must be specified in order for the fluid to be able to cavitate.

2.5. Equation of State Parameters

The two most commonly used equations of state for water are *EOS_GRUNEISEN and *EOS_LINEAR_POLYNOMIAL. *EOS_GRUNEISEN is required for water at high pressure as would occur in the simulation of an underwater explosion. For the range of pressures seen in the water impact problem, the two options provide similar relationships between pressure and volumetric strain. *EOS_LINEAR_POLYNOMIAL is readily usable for both water and air.

2.6. Fluid Structure Coupling Parameters

The *CONSTRAINED_LAGRANGE_IN_SOLID card features many options. The default for the number of fluid-structure coupling points on the surface of each structural element, NQUAD, is a 2 x 2 array of coupling points. If the structural elements are larger than the fluid elements, a larger number of NQUAD points should be specified. Perhaps the most important coupling parameter is the coupling stiffness, PFAC. If PFAC is a positive value, the coupling stiffness is based on the solution time step and the mass of the nodes on either end of the penalty coupling springs. The default is PFAC=0.1. A negative value for PFAC points to a user-specified coupling stiffness curve. The curve specifies the coupling pressure as a function of the distance the fluid penetrates past the coupling surface. The user can also specify the fluid element minimum volume fraction at which coupling is activated, FRCMIN. The default is FRCMIN=0.5. Problems with excessive penetration of fluid into the structure can be addressed by reducing FRCMIN; however, there is no firm physical basis for this. Simulations with low values of FRCMIN have been observed to show the fluid moving away from the structure prematurely.

2.7. Boundary Conditions

The typical approach for modeling a water or soil block in an impact problem is to restrain the sides and bottom of the mesh in the directions normal to each face. The problem with this approach is that stress waves are reflected when they reach the mesh boundary. Usually, dispersion of the stress waves results in negligible pressure amplitude by the time the stress wave returns back in the area of the impact. An alternative approach is to designate a layer of elements along the sides and bottom of the mesh as ambient
pressure reservoir elements. This is done via the ambient element type option, AET=4, on the
*SECTION cards. The ambient pressure reservoir elements allow material to flow in and out of the mesh
while holding the pressure constant.

2.8. Gravity and Atmospheric Preload

It is customary in water and soil impact problems to initialize gravity at 1g instantaneously at the start of a
simulation. The result is that stress waves oscillate through the material throughout the solution duration.
This typically has negligible effect on the solution as the amplitude of the pressure oscillations is similar
to the hydrostatic head at the base of the mesh, which is much less than the pressure due to the impact. A
more accurate method is to ramp gravity to 1g prior to the impact. The result is a stable hydrostatic stress
state in the material provided that the ramp time is much longer than the time required for a stress wave to
propagate through the depth of the mesh. If there is no atmospheric overpressure, the pressure in the
material at the surface will be zero, which could allow material to cavitate prematurely. If the air is
treated as a void (ELFORM=12), premature cavitation can be prevented by setting the tensile cutoff
pressure on the *MAT_NULL input, PC, equal to negative one atmosphere (-14.7 psi). If the air is
modeled as a fluid (ELFORM=11), the *INITIAL_HYDROSTATIC_ALE and
*ALE_AMBIENT_HYDROSTATIC options can be used to preload the air and water meshes with
atmospheric and hydrostatic pressure. For the *INITIAL_HYDROSTATIC_ALE and
*ALE_AMBIENT_HYDROSTATIC options, *EOS_LINEAR_POLYNOMIAL must be used to define
the equation of state for the air and water.

3. Tests

3.1. Test Configuration

The drop tests were performed in a 15-foot diameter above-ground swimming pool located in the Room
123 high-bay area of Building 1293A at NASA Langley Research Center (LaRC). The depth of the water
in the pool was approximately four feet. The test pool was located inside a 24-foot diameter above-
ground swimming pool to catch any over splash. A foam pad was placed under the liner at the bottom of
the inner pool to cushion bottom impacts. The test article was suspended above the test pool on a boom
extended from a forklift. A line hanging from the test article was used to measure the drop height. The
test set-up is illustrated in Figure 1.
3.2. Test Article

The test article was a hemispherical aluminum shell with an outside diameter of 20 inches. The general configuration of the test article is illustrated in Figure 2. The hemisphere had a shell thickness of 0.19 inches and was filled with bismuth ballast to an approximate depth of 2.5 inches at the apex. Eight phenolic ribs served as internal attachment points for instrumentation, which included an accelerometer at the center and three pressure transducers at a distance of approximately 2.25 inches from the apex. The locations of the pressure transducers are illustrated in Figure 3. An aluminum lid with a thickness of 0.25 inches served to keep water away from the instrumentation. The hemisphere was lifted into position for the drop test via three lift points at the perimeter of the lid. The weight of the hemisphere with instrumentation was 48 lb.

Figure 1. Test Set-Up

Figure 2. Hemisphere Configuration
3.3. Test Results

Three tests were performed at a 5-foot drop height and three were performed at a 10-foot drop height. For comparison with simulation data, the acceleration histories were filtered using a 180 Hz Butterworth filter to remove the vibratory structural response. Figures 4 and 5 show raw and filtered acceleration histories for the 5-foot drops. Figures 6 and 7 show the acceleration histories for the 10-foot drops. An artifact of the filtering is a small negative dip in acceleration prior to impact.
Figure 5. Filtered Acceleration Histories for 5-foot Drops

Figure 6. Raw Acceleration Histories for 10-foot Drops
Histories from the pressure transducers for the 5-foot and 10-foot drops are shown in Figures 8 and 9. The sampling rate for both pressure and acceleration data was 50,000 Hz. The TDAS PRO data acquisition system used for the tests is equipped with an analog anti-aliasing filter with a cutoff frequency of 4300 Hz. The anti-aliasing filter can be bypassed, but it was used for these tests. The sampling rate was relatively high for this type of test; however, the duration of the pressure peaks is so short that even this relatively high sampling rate provides just a few points to define the pressure peaks. As a consequence, some of the pressure histories exhibit truncated peaks. Even for the pressure histories that do not show truncated peaks, it is inevitable that the data points sampled during the test did not capture the absolute pressure peak.

One pressure history from each test that does not show a truncated peak was chosen for comparison against simulation data. The chosen pressure histories are Gage 3 of Test 1, Gage 3 of Test 2, and Gage 2 of Test 3 for the five-foot drops, and Gage 1 of Test 4, Gage 2 of Test 5, and Gage 3 of Test 6 for the ten-foot drops. The peaks of the pressure histories do not occur simultaneously due to small angles of pitch that exist upon impact of the hemisphere with the water. In the figures, the relative timings of the peaks are as they occurred during the test. For comparisons between tests, the pressure histories have been arbitrarily shifted so that several peaks from different tests align.
4. Simulation Models

4.1. Closed-Form Solution

A closed-form solution for the acceleration and pressure histories of a sphere impacting water was developed by A.P. Cappelli and J.P.D. Wilkinson [3]. The equations are as follows.
\[ A = -\left(4\sqrt{2} \frac{\rho V_0^{5/2} R^{3/2} t^{1/2}}{M}\right) (1 + \gamma)^{-2} \quad \text{Equation 1} \]

\[ P = \frac{\sqrt{2} \rho V_0^{3/2} R^{1/2}}{\pi t^{1/2} \left(1 - \frac{r^2}{c^2}\right)^{1/2} (1 + \gamma)^2} - \frac{\rho V_0^2}{2(1+\gamma)^2} \left[ 1 + \frac{4r^2}{2c^2} \left(1 - \frac{r^2}{c^2}\right)^{-1} \right] \quad \text{Equation 2} \]

\[ c = (2 R V_0 t)^{1/2} \quad \text{Equation 3} \]

\[ \gamma = \frac{9\sqrt{2} \rho (RV_0t)^{3/2}}{3M} \quad \text{Equation 4} \]

Where:

\[ A = \text{Acceleration} \]
\[ P = \text{Pressure} \]
\[ \rho = \text{Water Mass Density} \]
\[ V_0 = \text{Initial Velocity} \]
\[ M = \text{Mass} \]
\[ R = \text{Radius of Curvature at Impact Point} \]
\[ r = \text{Polar Distance from Impact Point} \]
\[ c = \text{Maximum Radius of Wetted Shell Surface} \]
\[ t = \text{Time after Impact} \]
\[ \gamma = \text{Non-Dimensional Parameter} \]

Cappelli and Wilkinson note problems with Equation 2. The predicted pressure is singular at the time that the contact patch radius, \( c \), reaches the polar distance, \( r \), which results in the equation producing no real answer for the highest pressure at a given polar distance. Cappelli and Wilkinson recommend dropping the second term of the pressure equation as it is small everywhere except for a negative singularity at the perimeter of the contact patch. Cappelli and Wilkinson further note that the remaining term of the pressure equation predicts nonphysical negative pressure in the late time.

### 4.2. 2-D LS-DYNA Simulation

A model of a two-dimensional axisymmetric slice of the penetrator was used to evaluate the sensitivity of the acceleration and pressure to several LS-DYNA parameters. The model configuration is illustrated in Figure 10.
The hemisphere was treated as linear elastic. Aluminum material properties were specified for the shell and the cover. The internal ballast was bismuth. The material density of the bismuth ballast was adjusted to achieve the desired total weight of 48 lb. The water was modeled with an equation of state. The air was treated as a vacuum. Gravity was ramped to 1g during the first 0.01 seconds to obtain a stable hydrostatic pressure state in the water prior to impact. The initial height and velocity of the hemisphere were adjusted so that impact occurred at the desired velocity at 0.01 seconds. The LS-DYNA cards that describe the coupling stiffness, material properties, and initial conditions are provided in Appendix A.

Three mesh variants of the model were used with element edge lengths of 0.1, 0.05, and 0.025 inches in the area of the initial contact for both the hemisphere shell and the water. The meshes are illustrated in Figure 11.
The pressure transducers used for the tests had a diameter of approximately one-eighth inch. For the simulations, coupling pressure was recorded using the DBFSI option in LS-DYNA. The pressure was averaged for the elements that span 0.1 inches at the pressure transducer location. This was one element for the 0.1-inch mesh, two elements for the 0.05-inch mesh, and four elements for the 0.025-inch mesh.

The baseline coupling stiffness was designated Curve 10. Curve 10 featured 100 psi at a penetration of 0.005 inches. Simulations were also performed with variants of Curve 10 with the stiffness scaled by factors of 0.1, 10, and 100.

### 4.3. 3-D LS-DYNA Simulation

A three-dimensional quarter model of the hemisphere was used for further evaluations of coupling stiffness and mesh density. The three-dimensional model was considered necessary because the 2-D and 3-D sections of the LS-DYNA code were written by different developers. The theory is the same for both, but there is no certainty that the implementation behaves in exactly the same manner, so there is no certainty that the findings concerning one modeling approach are directly applicable to the other. The three-dimensional model is illustrated in Figure 12.
The hemisphere was treated as rigid. Both the air and the water were modeled with equations of state. Gravity was initiated instantaneously and options within LS-DYNA were employed to initiate the air at one atmosphere and the water at one atmosphere plus hydrostatic pressure. The initial height of the hemisphere above the water was set so that impact occurred immediately after the start of the simulation. The bottom and outermost layers of elements of the water and air meshes were defined as reservoir elements. The reservoir elements allow material to flow in or out of the mesh in order to maintain constant pressure at the boundary. The LS-DYNA cards that describe the coupling stiffness, material properties, and initial conditions are provided in Appendix B.

Three water meshes were used. The baseline mesh featured an element size of 0.1 inches near the initial impact. The overall mesh radius was 15 inches, the air height was 1.2 inches, and the water depth was 13.2 inches. The first variant featured an element size of 0.05 inches near the initial impact and the same overall mesh radius and depth as the baseline mesh. The second variant was created by halving the dimensions of the 0.05-inch mesh. This resulted in an element size of 0.025 inches near the initial impact and an overall mesh radius of 7.5 inches, an air height of 0.6 inches, and a water depth of 6.6 inches. The 0.025-inch element model is illustrated in Figure 13. Due to the limited extent of the mesh, the 0.025-inch element model was suitable only for short duration simulations to determine early-time impact response.
For all simulations, the element size for the hemisphere was 0.1 inches, which is similar to the size of the pressure transducer used in the tests. Pressures from the simulations were recorded for a single element using the DBFSI option.

The baseline coupling stiffness was designated Curve 12. Curve 12 featured 100 psi at a penetration of 0.01 inches. This was half the stiffness of the baseline Curve 10 used for the 2-D simulations. The rationale for halving the coupling stiffness for the 3-D simulations was that the baseline 3-D mesh featured elements with edge lengths twice as large as the baseline 2-D mesh. For the baseline mesh with an element size of 0.1 inches, simulations were performed with variants of Curve 12 that were scaled by factors of 0.1 and 10 for the stiffness. Simulations were also performed with the coupling stiffness default, PFAC = 0.1. LS-DYNA determines the default coupling stiffness based on the stiffness required to achieve a vibration period equal to the critical time step size for solution stability.

5. Test and Simulation Correlation

5.1. Closed-Form Results

Accelerations for the closed-form solution for the 5-foot and 10-foot drops are plotted with test data in Figures 14 and 15. The test data was filtered using a 180-Hz Butterworth filter to eliminate vibratory structural response not represented in the analytical models. The closed-form solution exhibits no noise and requires no filtering. The results show that the closed-form solution substantially overpredicted the peak acceleration. This is partly due to the closed-form solution not taking into account the reduction in the velocity that occurs as a consequence of the deceleration during the early stages of the impact. For the 5-foot drop, the velocity would have reduced from 215 in/sec at impact to 168 in/sec at 0.01 seconds after impact. For the 10-foot drop, the velocity would have reduced from 304 in/sec to 206 in/sec.
The closed-form solution pressure histories are plotted with test data in Figures 16 and 17. The closed-form solution is asymptotic at the perimeter of the contact patch, but provides a reasonable prediction of the pressure decay.
5.2. 2-D LS-DYNA Results

Acceleration histories for the three mesh variants are compared to test accelerometer histories in Figures 18 through 20 for the 5-foot drops and Figures 21 through 23 for the 10-foot drops. All acceleration histories were filtered using a 180-Hz Butterworth filter and were time-shifted to facilitate comparison. The figures for the 5-foot drops show close agreement with the test results. For the 10-foot drops, the simulations over-predicted the acceleration peak. Both the 5-foot and 10-foot drops show the simulations had a much slower acceleration decay rate in the late time, after approximately 0.008 seconds.
Figure 18. Acceleration Histories for 5-foot Drop for 0.025-inch Element Size

Figure 19. Acceleration Histories for 5-foot Drop for 0.05-inch Element Size
Figure 20. Acceleration Histories for 5-foot Drop for 0.1-inch Element Size

Figure 21. Acceleration Histories for 10-foot Drop for 0.025-inch Element Size
The acceleration histories show that the filtered peak acceleration is relatively insensitive to both the mesh density and the coupling stiffness for the range of element sizes and coupling stiffnesses considered. This is illustrated in the bar charts shown in Figure 24 for the 5-foot drops and Figure 25 for the 10-foot
drops. The tests produced filtered peaks of approximately 11g for the 5-foot drops and 22g for the 10-foot drops.

![Figure 24. Peak Accelerations for Mesh and Coupling Stiffness Variants for 5-foot Drops](image)

![Figure 25. Peak Acceleration for Mesh and Coupling Stiffness Variants for 10-foot Drops](image)

Pressure histories were extracted from the LS-DYNA simulations using the DBFSI option, which translates the coupling forces into an interface pressure. The DBFSI pressure does not necessarily match the pressure seen in the fluid. This is illustrated in Figure 26 for a 5-foot drop of the 0.025-inch mesh model with the 10 x Curve 10 coupling stiffness. The DBFSI pressure reflects the actual loading on the coupling surface whereas the fluid pressure represents the pressure at the center of the elements of the fluid mesh. The relative mesh densities for the fluid and structure along with the density of the fluid
coupling points on the structure (NQUAD) all factor into how closely the pressure in the fluid matches the interface pressure. Further mesh refinement would lead to better agreement between the pressure in the fluid and the pressure at the coupling surface.

![Image: Figure 26. Pressure in Fluid versus DBFSI Pressure at Coupling Surface]

Pressure histories for the three mesh variants are compared to test pressure histories in Figures 27 through 29 for the 5-foot drops and Figures 30 through 32 for the 10-foot drops. The pressure histories are unfiltered. Pressure histories for the 10 x Curve 10 simulations are shown in Figure 33 for the 5-foot drops and Figure 34 for the 10-foot drops. The simulation pressure histories have been averaged over an edge length of 0.1 inches, which approximates the pressure transducer size of 0.125 inches. The simulation results show that refining the mesh results in better agreement with the test data for the late time decay of the pressure history; however, there is no convergence in matching the peak pressure of the test data.
Figure 27. Pressure Histories for 5-foot Drop for 0.025-inch Element Size

Figure 28. Pressure Histories for 5-foot Drop for 0.05-inch Element Size
Figure 29. Pressure Histories for 5-foot Drop for 0.1-inch Element Size

Figure 30. Pressure Histories for 10-foot Drop for 0.025-inch Element Size
Figure 31. Pressure Histories for 10-foot Drop for 0.05-inch Element Size

Figure 32. Pressure Histories for 10-foot Drop for 0.1-inch Element Size
The pressure histories show that the peak pressure is highly sensitive to both the mesh density and the coupling stiffness. The results also show that this sensitivity is reduced as the mesh is refined; however, this does not mean that the peak pressures from the simulations converge toward the peak pressures from the test. This is illustrated in the bar charts shown in Figure 35 for the 5-foot drops and Figure 36 for the...
10-foot drops. The tests produced peak pressures of approximately 120 psi for the 5-foot drops and 200 psi for the 10-foot drops.

![Bar graph showing peak pressures for different mesh and coupling stiffness variants for 5-foot drops.](image1)

**Figure 35. Peak Pressure for Mesh and Coupling Stiffness Variants for 5-foot Drops**

![Bar graph showing peak pressures for different mesh and coupling stiffness variants for 10-foot drops.](image2)

**Figure 36. Peak Pressure for Mesh and Coupling Stiffness Variants for 10-foot Drops**

Figures 37 and 38 show the impulse at the pressure transducer locations from the LS-DYNA simulations. The impulse was calculated by integrating the pressure history for the first 0.01 seconds following impact. Despite the drastic differences in the shapes of the pressure histories, the impulse is relatively insensitive to the mesh density and the coupling stiffness. The impulse varies between 0.069 psi-sec and 0.073 psi-sec for the simulations of the 5-foot drops and between 0.112 psi-sec and 0.117 psi-sec for the simulations of the 10-foot drops. This explains why the acceleration histories were very similar despite drastic
differences in the pressure histories. For simulation of the response of the overall structure, the exact profile of the pressure pulse is probably not important as long as the impulse is correct; however, the profile of the pressure pulse may be important for the design of small penetrations or crushable materials.

A similar computation was performed for the pressure histories from the tests. The impulse for the 5-foot drops was 0.116 psi-sec for Gage 3 of Test 1 and 0.084 psi-sec for Gage 3 of Test 2. The impulse for the 10-foot drops was 0.122 psi-sec for Gage 2 of Test 5 and 0.119 psi-sec for Gage 3 of Test 6. The pressure histories for Gage 2 of Test 3 and Gage 1 of Test 4 were not long enough to determine the impulse for the full period.

---

**Figure 37. Impulse for Mesh and Coupling Stiffness Variants for 5-foot Drops**

---

**Figure 38. Impulse for Mesh and Coupling Stiffness Variants for 10-foot Drops**
In addition to the effect the coupling stiffness has on the peak of the pressure history, it also affects the shape of the pressure contours within the fluid. Also, a coupling stiffness that is too soft can result in substantial penetration of fluid through the fluid-structure interface. This is illustrated in Figure 39 for the simulation of a 5-foot drop of the 0.05-inch mesh. The 0.1 x Curve 10 coupling stiffness produces smooth pressure contours but shows significant penetration of the fluid into the structure. The 100 x Curve 10 coupling stiffness shows no penetration, but the pressure contours show multiple isolated patches of high pressure. For the 100 x Curve 10 coupling stiffness, the impact occurs as a series of localized hits rather than as one continuous impact.

Figure 39. Pressure Contours for Coupling Stiffness Variants for 5-foot Drop

Sensitivity studies were performed for several simulation parameters. The parameters varied are listed in Table 1. The baseline simulation for the study was the 0.05-inch element model dropped from 5 feet. An exception was made for the divot model, which was based on the 0.025-inch element model in order to provide a finer mesh for defining the divot. Bar charts illustrating the peak filtered acceleration and peak
pressure are shown in Figures 40 and 41. Most of these parameters had relatively little effect on the peak filtered acceleration and peak pressure.

*Table 1. Parameters Varied for Sensitivity Study*

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Baseline</th>
</tr>
</thead>
<tbody>
<tr>
<td>ELFORM</td>
<td>Element formulation for 2-D axisymmetric mesh.</td>
<td>14</td>
</tr>
<tr>
<td>EOS_GRUNEISEN</td>
<td>Form of the equation of state for the water.</td>
<td>EOS_LINEAR_POLYNOMIAL</td>
</tr>
<tr>
<td>FRCMIN</td>
<td>Volume fraction at which a fluid element is considered to be coupled to the structure.</td>
<td>0.5</td>
</tr>
<tr>
<td>METH</td>
<td>Method for advecting fluid mesh between solution time steps.</td>
<td>3</td>
</tr>
<tr>
<td>PC</td>
<td>Tensile cutoff pressure for fluid.</td>
<td>14.7 psi</td>
</tr>
<tr>
<td>Instantaneous Gravity</td>
<td>Method of applying gravity.</td>
<td>Gravity ramped over 0.01 seconds prior to impact.</td>
</tr>
<tr>
<td>Rigid Model</td>
<td>Treating the hemisphere model as rigid rather than flexible.</td>
<td>Flexible model.</td>
</tr>
<tr>
<td>61.3 lb Model</td>
<td>Weight of hemisphere.</td>
<td>48.0 lb</td>
</tr>
<tr>
<td>Divot</td>
<td>Adding a divot with a depth of 0.02 inches in way of the pressure transducer location.</td>
<td>No divot.</td>
</tr>
</tbody>
</table>

*Figure 40. Peak Filtered Accelerations for Sensitivity Study Variants*
Regarding these parameters, the following should be noted.

- ELFORM=15 does not compute the stress correctly and should not be used according to the LS-DYNA developers at LSTC.
- The value of FRCMIN should be changed with caution as a low value can result in the fluid mesh moving before the impacting object arrives.
- METH=2 is described in the LS-DYNA Keyword User’s Manual [2] as “second order accurate”, whereas METH=1 and METH=3 (Baseline) are described as “first order accurate”.
- PC=-14.7 is used to mimic the overpressure of the atmosphere. The result is that the water at the surface of the fluid mesh does not cavitate until a tensile pressure of 14.7 psi is reached.
- Initiating gravity instantaneously results in an oscillating pressure field in the fluid whereas ramping gravity results in a stable hydrostatic pressure field.
- The measured weight of the hemisphere was 48 lbs. The 61.3 lb weight was based on the basic geometry assuming that the bismuth was sold rather than machined away to accommodate instrumentation.

Increasing the weight of the hemisphere would be expected to reduce the peak deceleration. This is consistent with the simulation results. The reduced deceleration would result in a modestly higher velocity at the time that the pressure pulse reaches the transducer location, which would be expected to result in a higher pressure peak. The simulation showed negligible change in the peak pressure. The effect of the increased weight on the pressure history was so small that no clear effect was perceptible in the simulation.

The idea of adding a divot to the simulation model stemmed from the difficulty of obtaining a perfectly flush mounting for a pressure transducer in the test article. For the 2-D axisymmetric model, the
representation of a recessed transducer mounting as a divot was not exactly correct as the divot actually represented an axisymmetric groove; however, the effect was expected to be similar. The 0.02-inch divot resulted in a significant spike in the pressure as the water passed over it. This is illustrated in Figure 42 for a 5-foot drop of the 0.025-inch mesh with the 10 x Curve 10 coupling stiffness. This was consistent with findings from experiments with pressure transducers that showed that slightly recessing the pressure transducer resulted in a higher pressure reading.

![Peak average pressure across pressure transducer = 139 psi.](image)

Figure 42. Pressure Pulse Caused by a 0.02-inch Divot

The conclusion from the results from the 2-D model was that the most important parameters for the study of test versus analysis correlation are mesh density and coupling stiffness. Other parameters either have little effect or lack any physical basis for making a change. As a consequence, mesh density and coupling stiffness were the focus of further studies performed with the three-dimensional model of the hemisphere.

### 5.3. 3-D LS-DYNA Results

A series of coupling stiffness variants for the baseline mesh (0.1-inch elements) were analyzed. In Figures 43 and 44, the acceleration histories for the 5-foot and 10-foot drops are compared to test data. For both drop heights, the simulation acceleration histories correlate well with the test data. The variant with the lowest coupling stiffness (0.1 x Curve 12) shows oscillatory behavior, which resulted from the hemisphere bouncing on the coupling surface.
Figure 43. Acceleration History for 5-foot Drop Simulations

Figure 44. Acceleration History for 10-foot Drop Simulations
The pressure histories from the simulations are compared to test data in Figures 45 and 46. The simulation pressure histories show a strong sensitivity to coupling stiffness. The baseline coupling stiffness (Curve 12 x 1) shows the closest match to the peak pressures measured in the test; however, the shape of the curve from the simulation does not match the shape of the curves from the test.

Figure 45. Pressure Histories for 5-foot Drop Simulations
For simulations of the 5-foot drops, the impulse during the first 0.01 seconds after impact varied between 0.052 psi-sec for the Curve 12 x 10 variant and 0.067 psi-sec for the Curve 12 x 1 variant. For the 5-foot drop test data, the range was 0.084 psi-sec to 0.116 psi-sec. For simulations of the 10-foot drops, the impulse varied between .098 for the Curve 12 x 10 variant and 0.100 for the PFAC Default variant. For the 10-foot drop test data, the range was 0.119 psi-sec to 0.122 psi-sec.

Figures 47 and 48 illustrate the distribution of the coupling pressure in the simulations of the 5-foot and 10-foot drops. The softest coupling stiffness (0.1 x Curve 12) produced a broad pressure patch without a well-defined “Coliseum Effect” ring of high pressure at its perimeter. The highest coupling stiffness (PFAC Default) produced a scattering of high pressure spikes rather than continuous rings of pressure.
Figure 47. Pressure Distribution at 0.001 seconds after Impact for 5-foot Drop Simulations
Simulations were run for fluid mesh variants with element sizes of 0.05 inches and 0.025 inches. The element size of the hemisphere was 0.1 inches for all simulation variants. The 0.05-inch fluid mesh was created by subdividing the 0.1-inch elements of the baseline fluid mesh. The 0.025-inch fluid mesh was created by halving the dimensions of the 0.05-inch mesh. As a consequence, the 0.025-inch fluid mesh has just half the overall extent of the 0.1-inch and 0.05-inch fluid meshes. For the 0.025-inch fluid mesh, the hemisphere began to interact with the mesh boundary at approximately 0.002 seconds. This limited the 0.025-inch fluid mesh simulation to the very early time response.

For the 0.05-inch fluid mesh, the coupling stiffness was made twice as stiff as the Curve 12 baseline. For the 0.025-inch fluid mesh, coupling stiffness was made four times as stiff as the Curve 12 baseline. The increase in coupling stiffness for the finer meshes was motivated by the belief that the maximum allowable penetration distance should be a function of the fluid element size rather than an absolute dimension. Also, the number of fluid coupling points (NQUAD) was increased from 2 for the 0.1-inch baseline fluid mesh to 3 for the 0.05-inch fluid mesh and 6 for the 0.025-inch fluid mesh. This was necessary to avoid the smaller fluid elements slipping between the coupling points of the 0.1-inch elements of the hemisphere.

*Figure 48. Pressure Distribution at 0.001 seconds after Impact for 10-foot Drop Simulations*
Acceleration histories for the 5-foot and 10-foot drops for the fluid mesh variants are compared to test data in Figures 49 and 50. The 0.025-inch fluid mesh is not included in the acceleration comparison because the hemisphere begins interacting with the fluid mesh boundary before the peak acceleration was reached. The results show that the refinement from a 0.1-inch mesh to a 0.05-inch mesh makes negligible difference in the acceleration histories.

Pressure histories for the fluid mesh variants are compared to test data in Figures 51 and 52. The pressure histories show that the baseline 0.1-inch mesh offers the best prediction for the peak pressure, but does not follow the pressure decay curves from the tests and has a second peak that is not physically reasonable. Refinement to a 0.05-inch mesh reduces the pressure peak below the value from the tests and results in a pressure history that oscillates about the pressure decay curves from the tests. Further
refinement to a 0.025-inch mesh further reduces the peak pressure and results in a pressure history that closely follows the pressure decay curves from the tests.

![Figure 51. Pressure Histories for Mesh Variants for 5-foot Simulations](image)

The simulation results for the 3-D model had peak filtered accelerations that were very similar to the test results. For the 5-foot drops, the simulations under-predicted the peak accelerations by less than 15%. For the 10-foot drops, the simulations modestly over-predicted the peak accelerations. The acceleration results support the use of a 15% allowance for design for loads that are proportional to the acceleration. The same cannot be concluded for the pressure histories. The peak pressures can be either over-predicted or under-predicted based on the mesh density and the coupling stiffness.

![Figure 52. Pressure Histories for Mesh Variants for 10-foot Simulations](image)
6. Establishing Simulation Parameters without Test Data

6.1. Width of Pressure Pulse

A series of tests were performed with additional pressure transducers mounted in the hemisphere. The time required for the pressure pulse to propagate from one transducer location to another provides an indication of the speed at which the pressure pulse travels. This can be used in conjunction with the observed time duration of the pressure pulse to estimate of the width of the pressure pulse. Figure 53 shows the arrangement of pressure transducers. Table 2 lists the coordinates of the pressure transducers.

![Figure 53. Pressure Transducer Arrangement](image)

<table>
<thead>
<tr>
<th>Sensor ID</th>
<th>X (in)</th>
<th>Y (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MS1</td>
<td>0.8125</td>
<td>2.125</td>
</tr>
<tr>
<td>MS2</td>
<td>1.250</td>
<td>-3.1875</td>
</tr>
<tr>
<td>MS3</td>
<td>0.875</td>
<td>-2.0625</td>
</tr>
<tr>
<td>PCB1</td>
<td>-0.875</td>
<td>-2.0625</td>
</tr>
<tr>
<td>PCB2</td>
<td>3.0625</td>
<td>0.875</td>
</tr>
<tr>
<td>PCB3</td>
<td>-1.750</td>
<td>-4.1875</td>
</tr>
</tbody>
</table>

The histories for the pressure transducers for a 10-foot drop are shown in Figure 54. The peak pressure decreases, and the time duration increases, as the pressure pulse moves away from the apex. Table 3 provides an estimate of the width of the pressure pulse based on the time duration of the pulse and the
velocity of the pulse as determined from the arrival time at subsequent transducer locations. The calculation suggests a pulse width of approximately 0.2 inches, which is approximately 1/50th of the radius of the hemisphere.

Figure 54. Pressure Histories for Multiple Pressure Transducers

Table 3. Pressure Pulse Width Estimate

<table>
<thead>
<tr>
<th>Gage</th>
<th>Arrival Time (sec)</th>
<th>X (in)</th>
<th>Y (in)</th>
<th>Radius (in)</th>
<th>Velocity (in/sec)</th>
<th>Pulse Width (sec)</th>
<th>Pulse Width (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PCB1</td>
<td>4.711</td>
<td>-0.875</td>
<td>-2.0625</td>
<td>2.2404</td>
<td>986.17</td>
<td>0.0002</td>
<td>0.197</td>
</tr>
<tr>
<td>MS2</td>
<td>4.7122</td>
<td>-1.25</td>
<td>-3.1875</td>
<td>3.4238</td>
<td>857.41</td>
<td>0.0002</td>
<td>0.171</td>
</tr>
<tr>
<td>PCB3</td>
<td>4.7135</td>
<td>-1.75</td>
<td>-4.1875</td>
<td>4.5385</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

6.2. Establishing Mesh Density and Coupling Stiffness

The ability of the model to adequately simulate the pressure pulse is dependent on having a mesh density that adequately describes the shape of the pressure pulse. If it is assumed that a minimum of four elements are needed across the width of the pressure pulse, and it is estimated that the width of the pressure pulse is approximately 1/50th of the radius of curvature of the structure, then the fluid element size should be no larger than 1/200th of the radius of curvature. This leads to a fluid element size of 0.05 inches for the hemisphere. This is the element size for the middle mesh variant for the 2-D axisymmetric model. It is half the element size of the baseline 3-D quarter model.
The approach recommended by LSTC in the LS-DYNA Keyword User’s Manual [2] for defining the coupling stiffness curve is as follows.

“The curve consists of \( \{0,0\} \) as the first point and \( \{\text{maximum allowable penetration (MAP), estimated maximum coupling pressure (EMCP)}\} \) as a second point. MAP may be a small penetration with respect to the minimum ALE element width (maybe 10% or less). EMCP can be estimated from a maximum fluid pressure observed from a previous run when leakage first occurs. This curve may be scaled to vary the stiffness of the coupling spring. The approach is to gradually increase the coupling stiffness until leakage stops. The best coupling stiffness is one which provides just enough force to prevent leakage and not more.”

LSTC subsequently amended this recommendation in e-mail and verbal communications. The amended recommendation is to base EMCP on the maximum pressure observed in a simulation with the PFAC default (PFAC = 0.1). There remains ambiguity as to whether this is the peak pressure seen anywhere in the model or at a presumed pressure transducer location and whether it should be the pressure seen in the fluid or at the fluid-structure interface. LS-DYNA does permit the specification of different fluid-structure coupling definitions (*CONSTRAINED_LAGRANGE_IN_SOLID) for different regions of the model; however, the coupling definition cannot be changed during the simulation.

For the hemisphere, the recommended mesh density and coupling stiffness are described in Table 4.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Criteria</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Radius of Curvature, R</td>
<td>Known Dimension</td>
<td>10 in</td>
</tr>
<tr>
<td>Fluid Element Size, L</td>
<td>( L = R/200 )</td>
<td>0.05 in</td>
</tr>
<tr>
<td>Maximum Allowable Penetration, MAP</td>
<td>( MAP = L/10 )</td>
<td>0.005 in</td>
</tr>
<tr>
<td>Estimated Maximum Coupling Pressure, EMCP</td>
<td>From LS-DYNA simulation with PFAC = 0.1</td>
<td>100 psi</td>
</tr>
</tbody>
</table>

The maximum pressure is expected to be more than 10 psi but less than 1000 psi, so 100 psi was chosen as an order of magnitude estimate for EMCP. This resulted in a curve that is identical to Curve 10 (100 psi at 0.005 inch) used for the 2-D axisymmetric model. It is twice as stiff as Curve 12 (100 psi at 0.01 inch) used for the 3-D quarter model. It is recognized that even with these guidelines, the peak pressure is not likely to be predicted with a high degree of accuracy.

### 6.3. Evaluating Model Performance without Test Data

When test data is unavailable, the analyst must make judgments on the performance of the fluid-structure interaction to determine whether the coupling stiffness is too high or too low. Through the course of these and other simulations, several aspects of the model performance have been observed that provide indications regarding whether the behavior of a simulation is physically reasonable.

One way to assess the adequacy of the fluid-structure interaction is to observe the degree of penetration and leakage through the structure. The following distinction is made between penetration and leakage.
- Penetration is fluid that passes through the coupling interface but is still resisted by the coupling force.
- Leakage is fluid that escapes through the coupling interface and is not resisted by the coupling force.

Figure 55 illustrates the distinction between penetration and leakage.

Since LS-DYNA utilizes a penalty method in which springs are added to resist the passage of material through the coupling interface, some degree of penetration must always occur in order for there to be a coupling force. Penetration can be reduced by increasing the coupling stiffness (PFAC).

Leakage should not occur at a properly functioning fluid-structure interface. Leakage may occur if the relative mesh size is such that not every fluid element is resisted by coupling points on the structural elements. Leakage can be alleviated by increasing the density of the coupling points (NQUAD).

Two symptoms of an excessively soft coupling stiffness were observed. The first was a coupling pressure pattern that lacks a well-defined “Coliseum Effect” ring of high pressure at the outer perimeter of the contact patch. The second was low frequency oscillation of the acceleration history as a consequence of the oscillatory system created by the mass of the structure and the coupling stiffness. These symptoms are illustrated in Figure 56.
Two symptoms were also observed for an excessively stiff coupling stiffness. The first was an interface coupling pressure pattern that appears as a set of isolated point loads. The second was a pressure history that appears as a series of isolated high pressure spikes. These symptoms are illustrated in Figure 57.
These criteria can be used to evaluate coupling stiffnesses that are at the extremes. Unfortunately, this still leaves a broad range of coupling stiffnesses that are either too stiff or too soft but give results that are not obviously wrong.

7. Conclusions and Recommendations

The results for the hemisphere model demonstrate that LS-DYNA can accurately predict acceleration histories for a broad range of mesh densities and coupling stiffnesses. The prediction of pressure histories is a more difficult problem. LS-DYNA predictions of pressure histories improve as the fluid mesh is refined; however, the required mesh size for a real world problem may be impractical due to large model size requiring excessive disk space and unacceptably long run times.
The simulation results for the 3-D hemisphere model had peak filtered accelerations that were very similar to the test results. For the 10-foot drops, the simulations modestly over-predicted the peak accelerations. For the 5-foot drops, the simulations under-predicted the peak accelerations by less than 15%. This supports the use of a 15% allowance for design for loads that are proportional to the acceleration. The same cannot be concluded for the pressure histories. The peak pressures can be either over-predicted or under predicted based on the mesh density and the coupling stiffness.

In the absence of test data, the analyst must make a judgment regarding whether the fluid-structure coupling interface is performing adequately. The following guidelines are proposed.

1. The element size of the fluid mesh should be no larger than 1/200th of the radius of curvature of the structure.
2. The coupling stiffness curve should be established based on the maximum expected coupling pressure at a penetration equal to 1/10th the size of the fluid elements.

It is recognized that the above guidelines may result in an impractical model size with impractical run time and that the pressure histories are not likely to be realistic even if the guidelines are followed. As a consequence, the following guidelines for judging the adequacy of the performance of the coupling surface are offered.

1. The coupling stiffness is too soft if the peak coupling pressure is toward the middle of the contact patch rather than at the perimeter.
2. The coupling stiffness is too soft if the acceleration time history exhibits oscillations that can be related to the structure bouncing on the coupling surface.
3. The coupling stiffness is too stiff if the coupling pressure distribution appears as a checkerboard pattern of isolated pressure spikes.
4. The coupling stiffness is too stiff if the coupling pressure histories appear as a series of isolated spikes.

References

Appendix A: Two-Dimensional Axisymmetric Model

The following are the LS-DYNA cards that control the material properties, contact, and initial conditions for the axisymmetric model. These particular cards are for the 0.05-inch mesh for the 10-foot drop with the Curve 10 x 1 coupling stiffness. Node numbers and the number of set segments for pressure output differ depending on the mesh density.

*KEYWORD 8000000000
$ IMPACT AT 0.01 SECONDS
$ RAMPED GRAVITY
$ ELFORM=14 FOR AIR AND WATER
$ VARIABLE D3PLOT TIME STEP
*TITLE
2-D Axisymmetric Model of 20" Hemisphere
*CONTROL_TERMINATION
$ ENDTIM ENDCYC DTMIN ENDENG ENDMAS
 0.0200 0.0 0.0 0.0
$*CONTROL_PARALLEL
$4
*CONTROL_HOURGLASS
1 0.1
*CONTROL_ENERGY
$# HGEN RWEN SLNTEN RYLEN
 2 2
*CONTROL_OUTPUT
$# NPOPT NEECHO NREFUP IACCOP OPIFS IPNINT IKEDIT IFLUSH
1 3
$# IPRTF
0
$*DATABASE_RBDOUT
$ 0.0000020
*DATABASE_NODOUT
0.0000020
*DATABASE_HISTORY_NODE
$ id1 id2 id3 id4 id5 id6 id7 id8
 4000020 4000024 4001553 4001557 4001975
*DATABASE_BINARY_D3PLOT
$# dt lcdt beam npltc
0.0000200 7778
*DEFINE_CURVE
7778 0 1.0 1.0 0.0 0.0 0
0.00000 0.002000
0.00990 0.002000
0.01000 0.000020
0.01210 0.000020
0.01212 0.002000
0.02000 0.002000
*DATABASE_BINARY_D3THDT
999.999
$*SET_MULTI-MATERIAL_GROUP_LIST
$ 3=Vacuum 2=Soil
123
*ALE_MULTI-MATERIAL_GROUP
2 1
3 1
$
*SET_PART_LIST
1 2
*SET_PART_LIST
11 11 12 21 22
*CONTROL_ALE
$ DCT NADV METH AFAC BFAC CFAC DFAC EFAC
3 1 3 -1.0
$ START END AAFAC VFACT PRIT EBC PREF NSIDBEC
$*CONSTRAINED_LAGRANGE_IN_SOLID_EDGE$
$#   slave    master     sstyp     mstyp     nquad     ctype     direc     mcoup$
11         1         0         0         3         4         2      -123
$#   start end   pfac fric frcmin norm normtyp   damp$
0         0       -10        0         0         0         0         0
$#   cq   hmin   hmax     ileak    pleak     lcidpor nvent   iblock$
0         0         0         0       0.1
$#   iboxid   ipenchk    intforc  ialesof    lagmul     pfacmm      thkf$
0         0         1         0         0
$*
$*DEFINE_CURVE$
$*SECTION_SHELL$
$      SID    ELFORM      SHRF       NIP     PROPT      IRID     ICOMP     SETYP$
1        14   0.83333                                                 1
$       T1        T2        T3        T4      NLOC     MAREA      IDOF    EDGSET
1.        1.        1.        1.  
$*SECTION_SHELL$
$      SID    ELFORM      SHRF       NIP     PROPT      IRID     ICOMP     SETYP$
98        14   0.83333                                                 1
$       T1        T2        T3        T4      NLOC     MAREA      IDOF    EDGSET
1.        1.        1.        1.  
$*SECTION_SHELL$
$      SID    ELFORM      SHRF       NIP     PROPT      IRID     ICOMP     SETYP$
99        14   0.83333                                                 1
$       T1        T2        T3        T4      NLOC     MAREA      IDOF    EDGSET
1.        1.        1.        1.  
$*SECTION_ALE2D$
$      SID   ALEFORM       AET    ELFORM$
2        11                  14
$*SECTION_ALE2D$
$      SID   ALEFORM       AET    ELFORM$
3        11                  14
$*
$*PART$
Vacuum
$      PID     SECID       MID     EOSID      HGID      GRAV     ADAPT      TMID$
2         3         3         3         3         3         3
$*PART$
Water
$      PID     SECID       MID     EOSID      HGID      GRAV     ADAPT      TMID$
3         2         2         2         2         2         2
$*PART$
Hemisphere
$      PID     SECID       MID     EOSID      HGID      GRAV     ADAPT      TMID$
1         1         1         1         1         1         1
$*
$*MAT_VACUUM$
$      mid       rho$
3 1.116E-11
$*MAT_NULL$
$      mid        ro        pc        mu     terod     cerod        ym        pr$
2 9.3365e-5     -14.7 1.6300E-7 0.0000000 0.0000000
$*MAT_ELASTIC$
1  0.000253    10.2E6      0.33                             0

Bismuth

Cover

$*
$*MAT_VACUUM$
$      mid       rho$
98 3.324E-5
$*MAT_NULL$
$      mid        ro        pc        mu     terod     cerod        ym        pr$
98 0.000253    10.2E6      0.33                             0

Cover
*MAT_ELASTIC
98  0.0006279  4.6E6  0.33  0

*MAT_ELASTIC
99  0.000253  10.2E6  0.33  0

$  
*EOS_LINEAR_POLYNOMIAL
2  0.0000000  3.11574e5  0.0000000  0.0000000  0.0000000  0.0000000  0.0  1.0
$

*Hourglass
HGID I HQ QM
3  1  1.E-6
2  1  1.E-6
1  1  0.1

*SET_NODE_LIST_GENERATE
sid
111
$  
b1beg blend
4000001  4100000

*INITIAL_VELOCITY
nsid
111
$  
vx vy vz vxr vyr vzar
0. -302.48 0.  

*LOAD_BODY_Y
1  386.1

*DEFINE_CURVE
1  0  1.0  1.0  0.0  0.0  0  0

0.0  0.0
0.01  1.0
100.0  1.0

$

*INCLUDE
2d_hemisphere_water_block_rev4_0p050.k

*DEFINE_TRANSFORMATION
100
$  
a1 a2 a3 a4 a5 a6 a7
TRANSL 0.0 13.04 0.
$

*INCLUDE_TRANSFORM
2d_20inch_hemisphere_0p050.k
$  
idoff ideoff idpoff idmoff idsoff idfoff iddoff
4000000  4000000
$idoff

$fctmas fcttim fctlen fcttem incout1 1
$ tranid 100
$

*END
Appendix B: Three-Dimensional Quarter Model

The following are the LS-DYNA cards that control the material properties, contact, and initial conditions for the three-dimensional quarter model. These particular cards are for the 0.1-inch mesh for the 10-foot drop with the Curve 12 x 1 coupling stiffness. For the 0.05-inch mesh, the number of fluid-structure coupling points, NQUAD, is increased to 3. For the 0.025-inch mesh, NQUAD is increased to 6.

```
*KEYWORD 800000000
*TITLE
3D QUARTER MODEL OF HEMISPHERE
*CONTROL_TERMINATION
  $   ENDTIM    ENDCYC    DTMIN    ENDENG    ENDMAS
      0.02    0.0      0.0      0.0
*CONTROL_HOURGLASS
  1       0.1
*CONTROL_ENERGY
  $#    HGEN    RWEN    SLNTEN    RYLEN
      2         2
*CONTROL_OUTPUT
  $#    NPOPT    NEECHO    NREFUP    IACCOP    OPIFS    IPNINT    IKEDIT    IFLUSH
      1         3
  $#    IPRTF
      0
  $
*DATABASE_GLSTAT
  0.0000020
*DATABASE_MATSUM
  0.0000020
*DATABASE_RBDOUT
  0.0000020
*DATABASE_BINARY_D3PLOT
  $#    dt    Tc*dt    beam    npltc
      0.0002
*DATABASE_BINARY_FSIFOR
  $   dt
  0.0000200      7778
  0.0002
*DATABASE_BINARY_D3THDT
  999.999
$
*SET_PART_LIST
  1
  2       3        22        23
*SET_PART_LIST
  222
  2       22
*SET_PART_LIST
  323
  3       23
*ALEMENT_MULTI-MATERIAL_GROUP
  $    sid    idtype
        222    0
        323    0
*SET_MULTI-MATERIAL_GROUP_LIST
  123
  2
*CONTROL_ALE
  $#    dct    nadv    meth    afac    bfac    cfac    dfac    efac
      2         1         2      -1.0
  $#    start    end    aafac    vfact    prit    ebc    pref    nsidebc
      14.7
$
*CONSTRAINED_LAGRANGE_IN_SOLID
  $#    slave    master    ssstyp    mstyp    nquad    ctype    direc    mcoup
      1          1           1           0          2         4         2    -123
  $#    start    end    pfac    fric    frcmin    norm    normtyp    damp
      0          0      -12          0         0         0         0
  $#    cq    hmin    hmax    ileak   pleak    lcidpor    nvent    iblock
      0          0         0          0          0          0          0
  $#    iboxid    ipenchk    intforc    ialesof    lagmul    pfacmm    thkf
```
*DEFINE_CURVE
$ lcid sidr sfa sfo
12 1.0 1.00
0.000 0.0
0.010 100.0
$

*SECTION_SHELL
$ sid elform shrf nip propt irid icomp setyp
1 1 0.8333333
1 1 t1 t2 t3 t4 nloc marea idof edgset
0.1875 0.1875 0.1875 0.1875

*SECTION_SOLID
$ SID ELFORM AET
2 11
$ SID ELFORM AET
3 11
$ SID ELFORM AET
22 11 4
$ SID ELFORM AET
23 11 4

*PART
Hemisphere
$ PID SECID MID EOSID HGID GRAV ADAPT TMID
1 1 1 1

*PART
Vacuum
$ PID SECID MID EOSID HGID GRAV ADAPT TMID
2 2 2 2 2 0

*PART
Water
$ PID SECID MID EOSID HGID GRAV ADAPT TMID
3 3 3 3 3 0

*PART
Vacuum
$ PID SECID MID EOSID HGID GRAV ADAPT TMID
22 22 2 2 2 0

*PART
Water
$ PID SECID MID EOSID HGID GRAV ADAPT TMID
23 23 3 3 3 0

*MAT_NULL
$ mid rho pc mu terod cerod ym pr
2 1.127E-7 0.0

*MAT_NULL
$ mid rho pc mu terod cerod ym pr
3 9.3365e-5 0.0 1.6300E-7 0.0000000 0.0000000

*MAT_RIGID
$ mid ro e pr
1 0.001075 1e+07 0.3
$ cmo con1 con2
1 5 7
$ a1 a2 a3 v1 v2 v3

*EOS_IDEAL_GAS
$$ eosid cv cp c1 c2 t0 v0
2 6.179E5 8.651E5 0.0 0.0 527.67 1.0

*EOS_LINEAR_POLYNOMIAL
$ eosid c0 c1 c2 c3 c4 c5 c6
2 0.0 0.0 0.0 0.0 0.4 0.4 0.0
$ e0 v0
1 36.74 0.0

*EOS_LINEAR_POLYNOMIAL
$  eosid  c0   c1   c2   c3   c4   c5   c6
  3  14.7  3.11574e5  0.0000000  0.0000000  0.0000000  0.0000000
$  e0  v0
    0.0  0.0
$
*Hourglass
$  HGID   IHQ   QM
  2   1  1.E-6
  3   1  1.E-6
*SET_NODE_LIST_GENERATE
$  sid
  111
$  b1beg  b1end
  4000001  4900000
*INITIAL VELOCITY
$  nsid
  111
$  vx   vy   vz   vxr   vyr   vzr
  304.41  0.   0.   0.   0.   0.
*LOAD_BODY_X
  1  -386.1
*DEFINE_CURVE
  1   0  1.0  1.0  0.0  0.0  0.0
  100.0  1.0
*SET_PART_LIST
$  sid
    781
$  pid1  pid2
    2  3
*INITIAL_HYDROSTATIC_ALE
$  SID  SIDTYPE  VECID  GRAVITY  PBASE
  781  0   789   386.1   14.7
$  NID  MMGBELOW
  103067  1
     44  2
*SET_PART_LIST
$  sid
    782
$  pid1  pid2
    22  23
*ALE_AMBIENT_HYDROSTATIC
$  SID  SIDTYPE  VECID  GRAVITY  PBASE
  782  0   789   386.1   14.7
$  NID  MMGBELOW
  103067  1
     44  2
*DEFINE_VECTOR
$  vid  xt   yt  zt  xh  yh  zh  cid
  789  0.   0.   0.   1.   0.   0.   0.
$
$  *INCLUDE
  water_air_quarter_0p1.k
  *DEFINE_TRANSFORMATION
  100
  $  a1  a2  a3  a4  a5  a6  a7
  TRANSL -10.01  0.0  0.0
$  *INCLUDE_TRANSFORM
  hemisphere_mesh_rev0.k
  $  idnoff  ideoff  idpoff  idmoff  idsoff  idfoff  iddoff
    40000000  40000000
  $  idoff
  $  fctmas  fcttim  fctlen  fcttem  incout1
    1
  $  tranid
    100
$
  *END
Spacecraft are being designed based on LS-DYNA simulations of water landing impacts. The Elemental Water Impact Test (EWIT) series was undertaken to assess the accuracy of LS-DYNA water impact simulations. Phase 1 of the EWIT series featured water impact tests of a 20-inch spherical hemisphere dropped from heights of 5 feet and 10 feet. The hemisphere was outfitted with an accelerometer and three pressure gages. The focus of this report is the correlation of analytical models against test data.