Computational Investigation of Novel Tip Leakage Mitigation Methods for High Pressure Turbine Blades

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This paper presents preliminary findings on a possible approach to reducing tip leakage losses. In this paper a computational study was conducted on the EEE (Energy Efficient Engine) HPT (High Pressure Turbine) rotor tip geometry using the commercial numerical solver ANSYS FLUENT. The flow solver was validated against aerodynamic data acquired in the NASA Transonic Turbine Blade Cascade facility. The scope of the ongoing study is to computationally investigate how the tip leakage and overall blade losses are affected by 1. injection from the tip near the pressure side, 2. injection from the tip surface at the camber line, and 3. injection from the tip surface into the tip separation bubble. The objective is to identify the locations on the tip surface at which to place appropriately configured blowing keeping in mind the film cooling application of tip blowing holes. The validation was conducted at Reynolds numbers of 85,000, 343,000 and 685,000 and at engine realistic flow conditions. The coolant injection simulations were conducted at a Reynolds number of 343,000 based on blade chord and inlet velocity and utilized the SST turbulence model in FLUENT. The key parameters examined are the number of jets, jet angle and jet location. A coolant to inlet pressure ratio of 1.0 was studied for angles of +30°, -30° and 90° to the local free stream on the tip. For the 3 hole configuration, 3 holes spaced 3 hole diameters apart with length to diameter ratio of 1.5 were used. A simulation including 11 holes along the entire mean camber line is also presented (30 degrees toward suction side). In addition, the effect of a single hole is also compared to a flat tip with no injection. The results provide insight into tip flow control methods and can be used to guide further investigation into tip flow control. As noted in past research it is concluded that reducing leakage flow is not necessarily synonymous with reducing losses due to leakage.

Nomenclature

\[ C_p = \frac{2(P_T - P)}{\rho U_e^2}, \text{ pressure coefficient} \]

\[ C_x = \text{blade axial chord (132.59 mm)} \]

\[ P = \text{pressure} \]

\[ P_s = \text{upstream static pressure} \]

\[ P_T = \text{upstream stagnation pressure} \]

\[ Re = \text{Reynolds number based on inlet conditions and axial chord} \]

\[ U_e = \text{nominal exit freestream velocity, based on inviscid solution} \]

\[ Z = \text{spanwise coordinate} \]

\[ X = \text{axial coordinate, axial distance from leading edge} \]

\[ Y = \text{pitchwise coordinate} \]

\[ \rho = \text{density} \]

\[ \phi = \frac{(P_T - P_f)(P_T - P_S)}{(P_T - P_S)}, \text{ total pressure loss coefficient} \]

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I. Introduction

NASA’s N+3 notional engines are expected to be characterized by high operating pressure ratios and turbine inlet total temperatures. The more compact highly loaded turbines will result in large pressure difference across the turbine rotor tips. The pressure distribution set up around the rotor blade results in a pressure gradient across the tip gap of the rotor. This is a significant concern due to the occurrence of aerodynamic loss due to tip leakage. The high pressure gas on the pressure side of the blade has a tendency to flow towards the suction side, which is at a lower pressure, across the tip. The path of the tip flow depends on several parameters such as blade rotational rate, blade geometry (tapering, twist, camber, tip gap height, and tip contouring) and flow inlet angle. These parameters can be reduced to the ratio of tip width to tip gap height, tip inlet Mach number and flow direction. No matter what the cause of the leakage flow, it results in a drop in efficiency and aerodynamic loss. The loss due to the interaction of the tip leakage vortex with the passage flow comprises approximately 20-30% of the total loss in a turbine stage. It is therefore important to reduce the leakage across the tip relative to the massflow through the passage. The width-to-height ratio of the tip gap changes as the chord increases from leading edge to trailing edge. This is accompanied by a change in the flow structure in the tip gap. If one is to attempt to control the flow through the tip gap, it is important to take into account the location and extent of the separation bubble, the local flow direction and the mass flow rate per unit chord as a function of the mass flow rate through the passage. A detailed literature review of the basic features of turbine tip flow and heat transfer has been conducted by Bunker (Ref. 1) and Glezser et al. (Ref. 2). Glezer et al. (Ref. 2) describe the primary flow features seen due to tip leakage: the pressure side separation bubble on the tip surface and the tip leakage vortex. The extent of the bubble and its reattachment are contingent on blade thickness, Mach number, Reynolds number and tip height (Refs. 2 and 3). For subsonic flows, the percentage of inlet flow that constitutes the tip leakage is shown to grow linearly with tip gap height. Refs. 1 and 2 highlight the importance of Computational Fluid Dynamics (CFD) in tip flow and heat transfer prediction due to the difficulty of conducting experimental measurements in a rotating tip gap. Ameri et al. (Ref. 4) simulated the GE-EEE (Energy Efficient Engine) high pressure turbine stage and studied the tip flow and heat transfer for a smooth tip and for a recessed tip. The cavity height of the recess was varied. Two primary vortex structures were observed in the recess. It was found that the recess had negligible effect on loss. Another study by Ameri et al. (Ref. 5) investigated the effect of upstream casing recess on tip leakage and heat transfer and found that minimal tip heat transfer occurred for a recess height that is almost equal to tip clearance. They concluded that the recess has little effect on efficiency. Hofer et al. (Ref. 6) state that neglecting the relative casing motion does not significantly alter results citing previous studies like that of Krishnababu et al. (Ref. 7). The latter studied the effect of relative casing motion on tip heat transfer and tip leakage mass flow for two different tip gap heights. They concluded that the effect of relative casing motion is diminished for larger tip gap heights due to dominant inviscid effects. The flow physics in a supersonic tip gap such as one encountered in highly loaded turbine stages is described in Shyam et al. (Refs. 8 and 9) and Wheeler et al. (Ref 10). The importance of choking the tip gap to reduce the relative massflow through the gap is emphasized by both authors.

In the realm of tip leakage mitigation, there are numerous passive and active approaches. Passive approaches involve real-time adjustments to the tip gap geometry or flow that can be varied based on mission conditions. This work deals with steady blowing into the tip gap and thus a brief literature review of relevant passive tip leakage control is presented. Rao et al. (Ref. 11) found through an experiment that injection into the tip of a recessed blade through 4 cooling holes reduced the losses associated with tip leakage. A coolant massflow of 0.6% of the passage massflow injected into the tip was found to be the global optimum as evaluated by averaged pressure loss coefficient in the wake. Couch et al. (Ref. 12) compared CFD to measurements of blowing from purge holes on the turbine blade tip. They found a strong dependence of cooling effectiveness on tip gap height. Studies of film cooling (such as Refs 12, 13, 14) show the dependence of jet behavior on momentum ratio, injection angle, pitch and plenum conditions. Canelli et al. (Ref 14) studied film cooling from holes in the recessed tip of a turbine blade. They simulated 3 holes near the leading edge region along the mean camber line and holes near the suction side further down the axial chord. Holes are generally placed along the mean camber line due to ease of manufacturing. It is clear that along the chord in the tip gap, the blowing ratio would change based on local conditions in the tip gap. There are several unanswered questions related to managing tip leakage using blowing. These relate to the optimal locations at which the coolant holes should be placed, the spacing of the holes, their inclination, the blowing ratio, frequency and the effect of loading (subsonic or supersonic flow) on the leakage control. Frequency is mentioned because it might be possible to modify the loss core with pulsed jets such as those used for separation control by Ibrahim et al. (Refs. 15, 16).
This paper examines the effect of the number of holes along the mean camber line and the effect of leading edge hole inclination on leakage induced losses. While the mean camber line might not be the optimal location for leakage mitigation, the intent is to determine the influence of the holes on the leakage through the tip and on the overall pressure loss through the passage. Cooling holes are usually placed in locations in the tip region where heat transfer is high and to purge dust that might accumulate in sandy environs (Ref. 13). They are also usually inclined at 90° to the tip surface and placed within squealer tips (Ref. 12 and 14). The scope of this paper is to answer the question of global impact of number of holes and of hole inclination on the overall loss across the turbine blade passage. Future investigations will look at heat transfer on the tip and the effect of blowing into the separation bubble as well as varied hole inclination along the tip as a function of chord.

II. Numerical Methods

The numerical simulations were conducted utilizing the finite-volume code ANSYS FLUENT (Ref. 18). For validation, cases were run at different Reynolds numbers. Table 1 shows the cascade parameters. The computational domain was based on Ibrahim et al. (Ref. 15, 16). A correlation-based transition model proposed by Menter et al. (Ref. 18) that is available in ANSYS FLUENT V-12 as Transition-SST (4-equation) turbulence model was selected to model turbulence. Figure 1 shows the computational domain and the boundary conditions applied in this paper. The figure depicts a case with 11 jets at the tip equally spaced between a distance from 0.13 Cx to 0.9 Cx. The number of cells used is 9.2 million with 50 cells packed in the tip gap region in the spanwise direction. The tip gap height is 2% of the span. The grid size used was reached from a grid independence study that was conducted on the same blade. Convergence was established when: 1) residuals reduced below a value of $10^{-5}$, 2) no change was observed in any field results, and 3) the mass imbalance between inlet and exit to the computational domain was less than 0.01 %.

![Figure 1. Computation Domain and Boundary Conditions.](image)

III. Experimental Facility And Measurements

The results of the numerical simulations that were carried out are compared to the data of McVetta et al. (Ref. 17). The data was collected in the NASA Transonic Turbine Blade Cascade facility at the NASA John H. Glenn Research Center. The data includes the midspan total pressure at the exit plane and the exit flow angle at seven inlet flow angles. Reynolds numbers of 85,000 to 683,000 at two isentropic exit Mach numbers of 0.74 and 0.34 are reported. The survey plane at midspan was 8.6% axial chord downstream of the blade trailing edge plane and covered three blade passages. Blade and endwall static pressure distributions were reported for each flow condition. Table 1 shows the relevant parameters used in the cascade experiment of Ref. 17.

<table>
<thead>
<tr>
<th>Axial Chord, $C_x$ [mm]</th>
<th>Pitch, $L_\phi$ [mm]</th>
<th>Span [mm]</th>
<th>Inlet flow angle</th>
<th>Exit flow angle</th>
</tr>
</thead>
<tbody>
<tr>
<td>132.59</td>
<td>132.59</td>
<td>152.4</td>
<td>+29.7°</td>
<td>-65°</td>
</tr>
</tbody>
</table>

Table 1: Cascade parameters

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Figure 2 shows the layout of the experiment in Ref. 17. The turbulence intensities are reported to be between 0.25% and 0.4%.

IV. RESULTS AND DISCUSSION

A. Code Validation and Turbulence Model/Geometry Selection, No Gap

In the validation stage, the blade was assumed to have no tip gap and the results are compared to the data from Ref. 17. A symmetry plane was used at mid-span after comparison to a full span simulation that showed no benefit to the additional computational domain. Shown below are static pressure distributions for two different turbulence models (RSM and SST) at Reynolds numbers, Re, of 85,000, 343,000 and 685,000. Results at spanwise locations of Z = 50%, 75% and 97.5% are presented. The pressure loss coefficient at a location X = 1.086 Cx from the airfoil leading edge and at Z = 50% is also compared to experiment.

1) Re = 85,000

Figures 3a, b, c show the static pressure coefficient plotted against dimensionless axial location, X/Cx for Z = 50%, 75% and 97.5% respectively for Re = 85,000. The following observations were made: 1) The pressure distribution on the pressure surface of the airfoil are in close agreement with the experimental data regardless of the turbulence model used, or the Z location, 2) As for the suction surface the plots show some flow separation in the range of X/Cx from 0.65 to 0.78 after that the flow reattaches, 3) The two turbulence models, RSM and SST, at Z=97.5% showed flow separation as expected (there is no experimental data at that location to verify this although the wake shown in Figure 3d for the experiment shows a wide wake that is indicative of separation.)

Figure 3d shows the total pressure distribution along X/Cx = 1.086 and Z = 50% plotted against y/pitch. The two turbulence models, RSM and SST, showed smaller wake width as compared to the experimental data perhaps indicating that the SST predicted separation is local and the flow reattaches. The RSM model does not show separation and therefore has a narrow wake.

2) Re 343,000

Figures 4a, b, c show the static pressure coefficient plotted against dimensionless axial location, X/Cx for Z = 50%, 75% and 97.5% respectively, for Re = 343,000. The following observations were made: 1) The pressure distribution on the pressure surface and the suction surface of the airfoil are in close agreement with the experimental data regardless of the turbulence model used, or the Z location.

Figure 4d shows the total pressure distribution along X/Cx = 1.086 and Z = 50% plotted against y/pitch. All cases exhibit similar wake size and peak value with SST turbulence model showing slightly better agreement with the experimental data. The absence of separation removes any discrepancies between the models.

3) Re 685,000

Figures 5a, b, c show the static pressure coefficient plotted against dimensionless axial location, X/Cx for Z = 50%, 75% and 97.5% respectively, for Re = 685,000. Figure 5d shows the total pressure distribution along X/Cx = 1.086 and Z = 50% plotted against y/pitch. The results for Re = 685,000 have similar observations shown earlier for Re = 343,000.
Figure 6 shows a plot of the loss coefficient, area averaged defined as:

$$\frac{P_{\text{total,in}} - P_{\text{total,exit}}}{P_{\text{total,in}} - P_{\text{static,exit}}}$$

for different Reynolds numbers comparing experimental data (Ref. 17) with CFD results. Figure 6 shows that both turbulence models underpredict loss at low Reynolds number (Re = 85,000) because of their failure to predict an open separation. At higher Reynolds numbers both models show improved predictions with the SST model doing a better job.

**Summary of code validation**

All cases examined in this section exhibit the following:

1) The static pressure distribution on the pressure surface of the airfoil is in close agreement with the experimental data regardless of the turbulence model used, or the Z (span-wise) location.
2) As for the suction surface, all cases exhibit similar results to the experimental data except at Re = 85,000, where the SST model shows a closed separation and the RSM model shows no separation. The experimental results suggest a wide wake that is not matched by the CFD.
3) As for the total pressure results at a location 1.086 Cx from the leading edge, and Z = 50%, the two turbulence models, RSM and SST, showed good agreement with the experimental data for higher Re (343,000 and 685,000). The wake predictions for Re = 85,000 is not as good for the following reasons: a) Transition is expected and was not simulated well with the turbulence models, b) The simulation did not include the boundary layer in the inlet flow, c) The span of the blade is smaller (approximately equal to the cord length), d) literature review indicates the difficulty in predicting the wake for transitional flows.
4) The overall conclusion is that there are good perdictions of the experimental data especially at higher Re and with the SST model.

In the rest of the paper analyses will be done for Re = 343,000 using the SST turbulence model.

**B. Tip Leakage with Different Jet Configuration**

Different configurations were examined to investigate the effect of various jet configurations on the tip leakage. The gap size is 2% Cx. All jets are located at the mean camber line, 5 mm in diameter and with jet length/diameter ratio of 1.5. Table 2 shows three different jet configurations examined: 1) One jet located at X/Cx = 0.23 measured from the leading edge, 2) Three jets equally spaced over a distance from X/Cx = 0.23 to 0.69 measured from the leading edge, 3) Eleven jets equally spaced over a distance from X/Cx = 0.13 to 0.9 measured from the leading edge. In addition different jet angles were examined: a) 30 degree minus (i.e. aiming towards the suction surface), b) 90 degrees normal to the tip surface, c) 30 degree plus (i.e. aiming towards the pressure surface). The jet inlet pressure was kept equal to the inlet total pressure (=36.942 kPa) for all cases. Accordingly (as will be shown later) the jet blowing ratio (based on jet exit velocity/inlet velocity) will vary from 1.0 to 2.2 depending on the number of jets, jet location and jet orination. This is expected to simulate real life situation where all jets will be supplied from one plenum.

Figures 7a, b, c show the static pressure coefficient, Cp, plotted against dimensionless axial location, X/Cx for Z = 50%, 75% and 97.5% respectively for Re =343,000. The plots show cases with no jet, one jet at +30° and one jet at -30°. The plots do not show any noticeable differences due to the jet on the static pressure and accordingly on the blade loading. The effect on the leakage and the total pressure losses are examined later.

Figures 8a, b, c show the static pressure coefficient plotted against dimensionless axial location, X/Cx for Z = 50%, 75% and 97.5% span respectively for Re =343,000. On the plots shown, cases with no Jet, three jets with 30 degree plus and 30 degree minus and 11 jets with 30 degree plus.

In this section our study will focus of the following cases: 1) No jet, 2) One jet, minus 30 degrees, 3) One jet, 90 degrees, 4) Three jets, plus 30 degrees, and 5) Eleven jets, plus 30 degrees.
Table 2 Parameters of the Jets Configurations

<table>
<thead>
<tr>
<th>Case</th>
<th>1 Jet</th>
<th>3 Jets</th>
<th>11 Jets</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chordwise Location (%Cx)</td>
<td>23</td>
<td>23 – 69 (equally spaced)</td>
<td>13 – 90 (equally spaced)</td>
</tr>
<tr>
<td>Holes Diameter (mm)</td>
<td>5</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>Length to Diameter (L/D) Ratio</td>
<td>1.5</td>
<td>1.5</td>
<td>1.5</td>
</tr>
<tr>
<td>Plenum Pressure (kPa)</td>
<td>36.942</td>
<td>36.942</td>
<td>36.942</td>
</tr>
<tr>
<td>Plenum Temperature (K)</td>
<td>300</td>
<td>300</td>
<td>300</td>
</tr>
</tbody>
</table>

Figure 9a shows the velocity vectors colored by the velocity magnitude, in a plane normal to Z and mid-gap, Re = 343,000, for no jets. The plot shows the flow velocity is very high in the tip gap and in the aft 30% of the blade chord. Figure 9b shows the velocity vectors colored by the velocity magnitude, in a plane normal to Z and mid-gap, Re = 343,000, for one jet, minus 30 degrees. The plot shows how the flow is accelerated due to the presence of the jet. This fact is responsible for having more leakage (as will be shown later). Figure 9c shows the velocity vectors colored by the velocity magnitude, in a plane normal to Z and mid-gap, Re = 343,000, for one jet, 90 degree. The plot shows how the flow is decelerated due to the presence of the jet. However the flow is accelerated upstream and around the jet. This fact is responsible for having more leakage (as will be shown later). Figures 9d and e show the velocity vectors colored by the velocity magnitude, in a plane normal to Z and mid-gap, Re = 343,000, for (3) jets, plus 30 degree and (11) jets, plus 30 degree, respectively. The plots show how the flow is decelerated due to the presence of the jets near the leading edge to 30% chord region while it is accelerated in the aft region of the tip.

Figure 10a shows the velocity magnitude plotted versus X/Cx at two lines: mid-distance between the blade tip and the casing, one on the pressure side (PS) and one on the suction side (SS), Re = 343,000, no jets and one jet, minus 30 degrees. The vertical line shows the location of the jet. For the case of no jet, the velocity magnitude on SS side is higher that than on PS except in the range of X/Cx from 0.38 to 0.48. In the case of one jet, the blowing ratio (jet outlet velocity/inlet velocity) is about 2. The velocity magnitude on PS side did not change much. However on the SS side the signature of the jet is very clear with a slight decrease in the velocity magnitude.

Figure 10b shows the velocity magnitude plotted versus X/Cx at two lines: mid-distance between the blade tip and the casing, one on the pressure side (PS) and one on the suction side (SS), Re = 343,000, no jets and one jet, 90 degrees. The vertical line shows the location of the jet. For the case of no jet, the velocity magnitude on SS side is higher that than on PS except in the range of X/Cx from 0.38 to 0.48. In the case of one jet, the blowing ratio (jet outlet velocity/inlet velocity) is about 2. The velocity magnitude on PS side did not change much. However on the SS side the signature of the jet is very clear with a decrease in the velocity magnitude down to 50%.

Figure 10c shows the velocity magnitude plotted versus X/Cx at two lines: mid-distance between the blade tip and the casing, one on the pressure side (PS) and one on the suction side (SS), Re = 343,000, no jets and (3) jets, plus 30 degrees. The vertical lines show the location of the jets. In the case of (3) jets the blowing ratio (ratio of jet exit velocity to the inlet) of the jets (starting from the upstream) are: 1.14, 1.31 and 1.48 respectively (see Figure 11). The velocity magnitude on PS side changed slightly. However on the SS side the signature of the (3) jets is very clear with decrease in the velocity magnitude down to close to zero.

Figure 10d shows the velocity magnitude plotted versus X/Cx at two lines: mid-distance between the blade tip and the casing, one on the pressure side (PS) and one on the suction side (SS), Re = 343,000, no jets and (11) jets, plus 30 degrees. In the case of (11) jets the blowing ratio of the jets (starting from the upstream) are: 0.79, 1.13,
accomplishing both reductions in the tip leakage flow and the loss coefficient, area averaged would require strategic allocation of: 1) number of jets, 2) jets location, and 3) jet angle. Blowing ratio is expected to play a role but was not included in this study.

Table 3. Summary of leakage and losses for all cases.

<table>
<thead>
<tr>
<th>Case</th>
<th>Tip Leakage Mass Flow</th>
<th>Loss Coefficient, Area Averaged</th>
</tr>
</thead>
<tbody>
<tr>
<td>No Jets</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>One Jet, Minus 30 Degrees</td>
<td>104</td>
<td>76</td>
</tr>
<tr>
<td>One Jet, 90 Degrees</td>
<td>96</td>
<td>67</td>
</tr>
<tr>
<td>(3) Jets, Plus 30 Degrees</td>
<td>95</td>
<td>82</td>
</tr>
<tr>
<td>(11) Jets, Plus 30 Degrees</td>
<td>88</td>
<td>105</td>
</tr>
</tbody>
</table>

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V. Conclusions

The following conclusions are drawn from this investigation:

1) The turbulence model selected (SST) and the grid topology designed showed good agreement in predicting pressure distribution along the EEE blade for a wide range of Re (from 85,000 to 685,000),

2) The study was focused on Re = 343,000 and examining different jet configurations (one, three and eleven) distributed on the camber cord. Different jet angles were examined; 90 degrees, 30 degrees plus and 30 degrees minus.

3) With no jet about 50% of the mass leakage took place in the later 30% of the blade near the trailing edge.

4) Jets with 30 degrees minus increase the mass flow while showing a decrease in loss coefficient, area averaged. This could be attributed to the fact that jets with 30 minus will be in the same direction where the flow leakage occur thus increase the mass flow leaking. However, these jets will be able to break the tip leakage vortex and reducing its strength and thus reduce the losses.

5) On the contrary to the above, 30 degrees plus will reduce the leakage but will increase the losses.

6) A future exercise is to use some jets with 30 plus and others with 30 minus to achieve both leakage reduction as well as loss coefficient reduction.

Acknowledgments

Part of this work was conducted by the lead author while he was a Summer Fellow at NASA GRC and with Dr. Shyam as the NASA colleague. NASA GRC is greatly acknowledged for such support. We greatly appreciate the computer time provided for us by the Ohio Super Computer (OSC). The OSC Computer Cluster has been made available as part of the Center’s mission to support Ohio Universities.

References


270, DOI:10.2514/1.18034.


18ANSYS FLUENT Documentation, 2009.
Figure 3a. Cps comparison, Exp. and CFD, Re = 85,000, Z = 50%, No Gap.

Figure 3b. Cps comparison, Exp. and CFD, Re = 85,000, Z = 75%, No Gap.

Figure 3c. Cps comparison, Exp. and CFD, Re = 85,000, Z = 97.5%, No Gap.

Figure 3d. Cp-total at 1.086 Cx, comparison, Exp. and CFD, Re = 85,000, Z = 50%, No Gap.
Figure 4a. Cps comparison, Exp. and CFD, Re = 343,000, Z = 50%, No Gap.

Figure 4b. Cps comparison, Exp. and CFD, Re = 343,000, Z = 75%, No Gap.

Figure 4c. Cps comparison, Exp. and CFD, Re = 343,000, Z = 97.5%, No Gap.

Figure 4d. Cp-total at 1.086 Cx, comparison, Exp. and CFD, Re = 343,000, Z = 50%, No Gap.
Figure 5a. Cps comparison, Exp. and CFD, Re = 685,000, Z = 50%, No Gap.

Figure 5b. Cps comparison, Exp. and CFD, Re = 685,000, Z = 75%, No Gap.

Figure 5c. Cps comparison, Exp. and CFD, Re = 685,000, Z = 97.5%, No Gap.

Figure 5d. Cp-total at 1.086 Cx, comparison, Exp. and CFD, Re = 685,000, Z = 50%, No Gap.

Figure 6. Loss Coefficient, Area Averaged, for all cases examined, versus Re and RSM and SST turbulence models.
Figure 7a. Cps comparison, CFD, $Re = 343,000$, $Z = 50\%$, No Jet, One Jet, Plus and Minus 30 Degrees.

Figure 7b. Cps comparison, CFD, $Re = 343,000$, $Z = 75\%$, No Jet, One Jet, Plus and Minus 30 Degrees.

Figure 7c. Cps comparison, CFD, $Re = 343,000$, $Z = 97.5\%$, No Jet, One Jet, Plus and Minus 30 Degrees.

Figure 8a. Cps comparison, CFD, $Re = 343,000$, $Z = 50\%$, No Jet, 3 Jets, Plus and Minus 30 and 11 Jets Plus 30 Degrees.

Figure 8b. Cps comparison, CFD, $Re = 343,000$, $Z = 75\%$, No Jet, 3 Jets, Plus and Minus 30 and 11 Jets Plus 30 Degrees.

Figure 8c. Cps comparison, CFD, $Re = 343,000$, $Z = 97.5\%$, No Jet, 3 Jets, Plus and Minus 30 and 11 Jets Plus 30 Degrees.
Figure 9a. Velocity vectors colored by the velocity magnitude, in a plane normal to Z and mid-gap, Re = 343,000, No Jet.

Figure 9b. Velocity vectors colored by the velocity magnitude, in a plane normal to Z and mid-gap, Re = 343,000, One Jet, Minus 30 Degrees.

Figure 9c. Velocity vectors colored by the velocity magnitude, in a plane normal to Z and mid-gap, Re = 343,000, One Jet, 90 Degrees.

Figure 9d. Velocity vectors colored by the velocity magnitude, in a plane normal to Z and mid-gap, Re = 343,000, Three Jets, Plus 30 Degrees.

Figure 9e. Velocity vectors colored by the velocity magnitude, in a plane normal to Z and mid-gap, Re = 343,000, Eleven Jets, Plus 30 Degrees.
Figure 10a. Velocity magnitude versus X/Cx at PS & SS for No jet and One Jet, Minus 30 Degrees.

Figure 10b. Velocity magnitude versus X/Cx at PS & SS for No jet and One Jet, 90 Degrees.

Figure 10c. Velocity magnitude versus X/Cx at PS & SS for No jet and Three Jets, Plus 30 Degrees.

Figure 10d. Velocity magnitude versus X/Cx at PS & SS for No jet and Eleven Jets, Plus 30 Degrees.

Figure 11. Jets velocity magnitude/Inlet velocity versus X/Cx for Three & Eleven Jets, Plus 30 Degrees.
Figure 12a. Contours of the total pressure at 1.086Cx (from leading edge), for No jet(s).

Figure 12b. Contours of the total pressure at 1.086Cx (from leading edge), for One Jet, Minus 30 Degrees.

Figure 12c. Contours of the total pressure at 1.086Cx (from leading edge), for One Jet, 90 Degrees.

Figure 12d. Contours of the total pressure at 1.086Cx (from leading edge), for Three Jets, Minus 30 Degrees.

Figure 12e. Contours of the total pressure at 1.086Cx (from leading edge), for Eleven Jets, Minus 30 Degrees.
Figure 13a. Contours of the static pressure at the blade top and SS, for No jet(s).

Figure 13b. Contours of the static pressure at the blade top and SS, for One jet, Minus 30 Degrees.

Figure 13c. Contours of the static pressure at the blade top and SS, for One jet, 90 Degrees.

Figure 13d. Contours of the static pressure at the blade top and SS, for Three jets, Plus 30 Degrees.

Figure 13e. Contours of the static pressure at the blade top and SS, for Eleven jets, Plus 30 Degrees.
Figure 14. Tip leakage mass flow as % of total inlet mass flow for (6) segments along the suction side of the gap, Re = 343,000, No Jets, One Jet Minus 30 Degrees, One Jet 90 Degree, Three Jets, Plus 30 Degrees, and Eleven Jets, Plus 30 Degrees.

Figure 15. Total tip leakage mass flow as % of the No Jet case, Re = 343,000, No Jets, One Jet Minus 30 Degrees, One Jet 90 Degree, Three Jets, Plus 30 Degrees, and Eleven Jets, Plus 30 Degrees.

Figure 16. Loss coefficient, area averaged at 1.086 Cx as % of the No Jet case, Re = 343,000, No Jets, One Jet Minus 30 Degrees, One Jet 90 Degree, Three Jets, Plus 30 Degrees, and Eleven Jets, Plus 30 Degrees.