A low-NO\textsubscript{x} aircraft gas turbine engine combustion concept was developed and tested. The concept is a second generation swirl-venturi lean direct injection (SV-LDI) concept. LDI is a lean-burn combustion concept in which the fuel is injected directly into the flame zone. Three second generation SV-LDI configurations were developed. All three were based on the baseline 9-point SV-LDI configuration reported previously.\(^1\) These second generation configurations had better low power operability than the baseline 9-point configuration. Two of these second generation configurations were tested in a NASA Glenn Research Center flametube; these two configurations are called the flat dome and 5-recess configurations. Results show that the 5-recess configuration generally had lower NO\textsubscript{x} emissions than the flat dome configuration. Correlation equations were developed for the flat dome configuration so that the landing-takeoff NO\textsubscript{x} emissions could be estimated. The flat dome landing-takeoff NO\textsubscript{x} is estimated to be 87–88% below the CAEP/6 standards, exceeding the ERA project goal of 75% reduction.

I. Introduction

For more than 40 years, NASA has sustained programs to reduce the environmental effects of aviation. A major focus of these programs has been reducing the emissions of nitrogen oxides (NO\textsubscript{x}) while simultaneously reducing emissions of carbon monoxide (CO), unburned hydrocarbons, and smoke and meeting other combustion design requirements including operability and durability. NO\textsubscript{x} emissions increase smog and ozone in the lower troposphere and decrease the protective ozone layer in the stratosphere.\(^2\)

Currently, the Environmentally Responsible Aviation (ERA) project aims to reduce the engine specific fuel consumption by 15% and the emissions of NO\textsubscript{x} by 75%; these goals apply to N+2 concepts that will enter service by 2025. In order to reduce specific fuel consumption, engines will need to increase the operating pressure ratio, thus increasing the combustor inlet pressure and temperature. However, NO\textsubscript{x} formation rates increase with higher temperatures. To decrease NO\textsubscript{x} by 75% while simultaneously reducing specific fuel consumption, improved low-NO\textsubscript{x} combustor technologies need to be developed. Under an ERA project contract with NASA, Woodward FST, has developed a low-NO\textsubscript{x} N+2 combustor concept.

In order to reduce NO\textsubscript{x} emissions, NASA has investigated several combustion concepts. These concepts fall into two categories: rich-front-end and lean-front-end. Rich-front-end combustors are similar to traditional combustors in that the primary combustion zone is fuel-rich—only part of the combustion air
enters through the fuel/air mixers; the rest enters downstream through a set of primary and dilution jets to complete combustion to be completed and meet exit temperature quality requirements including profile and pattern factor. All modern rich-front-end combustors entering revenue service since 1995 use rich-burn-quick quench-lean-burn (RQL) combustion techniques to simultaneously minimize NOx and smoke emissions.3–5

In contrast, lean-front-end combustors operate fuel-lean throughout: All of the combustor air except that used for liner cooling enters through the combustor dome. Lean -front-end combustion concepts include lean, premixed, prevaporized (LPP), lean partially premixed, and lean direct injection (LDI) combustion.1,3,6–10 This paper focuses on a LDI combustion concept.

As the name implies, in LDI the combustor operates fuel-lean without a rich front end. All of the combustor air except that used for lining cooling enters through the combustor dome. Like other lean burn combustion concepts, LDI reduces NOx emissions by minimizing flame temperature, since NOx is an exponential function of temperature. To eliminate local hot spots that produce high levels of NOx, lean burn combustion concepts rely on the fuel and air being well-mixed before burning occurs. Thus, LDI requires rapid fuel vaporization and uniform fuel-air mixing. LDI achieves this by using a multi-element concept with small fuel/air mixers.

Several fuel-air mixing strategies have been studied for LDI fuel/air mixers. There are several ways an individual fuel/air mixer (the fuel injector) can be constructed. On the air side, a radial,1,7 or discrete jet swirler9 may be used. A venturi can be placed downstream of the air swirler, or the venturi can be omitted. On the fuel side, a simplex or air assist atomizer can be used. For a simplex atomizer, flow number (i.e., effective flow area) can be varied. In addition, once a fuel/air mixer design has been chosen, the size and number of the mixer elements can be varied.

The LDI design that has been studied most extensively is the 9-point swirl-venturi LDI (SV-LDI) design.1,7,10 This baseline design consists of 9 identical fuel/air mixers arranged in a 3x3 grid with a 76.2-mm by 76.2-mm square cross section. Each fuel/air mixer consists of a simplex fuel injector and an air passage with an axial air swirler followed by a converging-diverging venturi section. The baseline 9-point SV-LDI design was initially developed under the High Speed Research (HSR) program in the 1990s, and it showed a substantial reduction in NOx emissions compared to the then-current state-of-the-art. However, the NOx emissions were not low enough to meet the most stringent ERA requirement of 75% NOx reduction. In addition, the baseline 9-point SV-LDI did not perform well at low power conditions. Good operation at low power conditions is required for ERA combustor concepts.

Therefore, to meet the ERA goals of 75% NOx reduction and good low power operation, Woodward developed a second-generation SV-LDI concept. Although this design is based upon the baseline 9-point concept, it includes advanced features designed to reduce NOx emissions and improve low power operation; these advanced features included airblast tips and a pilot fuel/air mixer.

Three distinct second-generation SV-LDI configurations were developed. Two of these configurations were tested at flametube facilities at Woodward FST, and NASA Glenn Research Center; these two configurations are described in section IIC below. Testing was done at inlet pressures up to 1790 kPa and inlet temperatures up to 855 K.

This paper presents emissions results from the NASA Glenn flametube testing of this second-generation LDI design. Emissions results from each configuration are shown and compared to each other and to emissions correlations based on the baseline 9-point SV-LDI design.

II. Experimental Facilities and Hardware

A. Experimental Facilities and Data Analysis

These tests were done in NASA Glenn’s flametube combustion test rigs. A sketch of a flametube is shown in Fig. 1. This facility can supply nonvitiated air preheated to 865 K at pressures up to 3.1 MPa. The flametube can be configured to use different test sections with varying cross-sectional area. For the baseline 9-point SV-LDI experiments previously described in R. Tacina et al,1 the flametube test section was configured to have a 76.2-mm × 76.2-mm square cross section that could handle pressures up to 3.1 MPa. For the second-generation LDI experiments described in this paper, the flametube test section was configured to have a 114.3-mm × 114.3-mm square cross section that could handle pressures up to 1.9 MPa at an inlet air temperature of 825 K or 1.7 MPa at an inlet air temperature of 865 K. Both flametubes had ceramic liners downstream of the dump plane. A 5-hole probe is used to measure gaseous emissions.

The test rig supports up to three fuel circuits. The fuel used in typically JP-8. However, an alternative
 jet fuel (e.g., a biofuel) can also be used. JP-8 and the biofuel can be mixed on-the-fly during testing.

The test rig is equipped with a standard gas bench to measure CO$_2$, CO, O$_2$, NO$_x$, and unburned hydrocarbons so that emissions can be measured according to the SAE Aerospace Recommend Practice (ARP) 1256. More details on NASA Glenn’s flametube combustion test rigs can be found in Bianco. More details on NASA Glenn’s flametube combustion test rigs can be found in Bianco.12

Emissions measurements are analyzed according to SAE ARP 1533.13 Adiabatic flame temperatures are calculated using the Chemical Equilibrium for Applications (CEA) equilibrium code.14

### Table 1: Combustion conditions: inlet temperature, $T_3$, and pressure, $p_3$

<table>
<thead>
<tr>
<th>$T_3$ (down)</th>
<th>0.7 MPa (100 psia)</th>
<th>1.0 MPa (150 psia)</th>
<th>1.4 MPa (200 psia)</th>
<th>1.7 MPa (250 psia)</th>
<th>1.6 MPa (230 psia)</th>
<th>1.8 MPa (260 psia)</th>
</tr>
</thead>
<tbody>
<tr>
<td>535 K (500 F)</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>650 K (700 F)</td>
<td></td>
<td>x</td>
<td>x</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>755 K (900 F)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>825 K (1020 F)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>860 K (1090 F)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>x</td>
<td></td>
</tr>
<tr>
<td>810 K (1000 F)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>x</td>
</tr>
</tbody>
</table>

### B. Testing Strategy

Testing parameters were varied as systematically as was possible with the limited testing time and facility capabilities. Most testing was done at four inlet temperatures: 535 K (500 F), 650 K (700 F), 755 K (900 F), and the maximum normal operating temperature 825 K (1020 F). At each of these inlet temperatures, we went tested at three inlet pressures. At lower inlet temperatures, corresponding to lower inlet pressures, the lowest inlet pressure was 0.7 MPa (100 psia); at higher inlet temperatures, it was 1.0 MPa (150 psia). Some data was also taken at the maximum operating pressure of 1.8 MPa (260 psia) at a temperature slightly below the maximum (1000 F instead of 1020 F). In addition, during the flat dome testing we were able to increase the maximum operating temperature to 860 K (1090 F) at the cost of reducing the maximum...
pressure to 1.6 MPa (230 psia). A grid of the test conditions is shown in Table 1.

During the flat dome test, we had enough testing time to vary the dome pressure drop \( \Delta p/p \); we used 3%, 4%, and 5%. However, there was no time to vary the pressure drop in 5-recess test; during this test, we tested with alternative fuel in addition to JP-8, but the testing time was not increased. As a result, the dome pressure drop was kept fixed at 3%.

C. LDI Hardware

The current second-generation SV-LDI configurations were based upon the initial baseline 9-point SV-LDI concept developed under NASA’s HSR and UEET programs. Therefore, the baseline concept will be described before the current second-generation SV-LDI hardware is described.

As shown in Fig. 2, a SV-LDI fuel/air mixer consists of a fuel injector and an air passage with an axial air swirler followed by a converging-diverging venturi section. The fuel injector is inserted through the center of the air swirler, with the tip typically located at the venturi throat.

As shown in Fig. 3, the baseline 9-point configuration consists of 9 SV-LDI fuel/air mixers arranged in a 3 \( \times \) 3 grid with a 76.2-mm \( \times \) 76.2-mm square cross-section. The center-to-center distance between fuel/air mixers is 25.4 mm. The air swirlers each have 6 helical blades, with a blade angle of 45°, 52.5°, or 60°; the blades can have either a clockwise or counterclockwise orientation. The fuel injector is a simplex injector and the injector tip sits at the venturi throat. Except for possible differences in air swirler angle and orientation, each fuel/air mixer is identical. The measured effective area of the 9-point configuration is 955 mm\(^2\) for 45° swirlers, 925 mm\(^2\) for the 52.5° swirlers, and 870 mm\(^2\) for the 60° swirlers.

Results from the baseline configuration guided the design of the second-generation SV-LDI hardware. One major concern was operability. Although baseline results showed that reducing the swirler angle typically reduced NO\(_x\) emissions, reducing the swirler angle also reduced operability.\(^1\) The baseline configuration with the 45° swirlers would have met the ERA NO\(_x\) emissions goals, but the operability would have been unacceptable. In addition, limited experiments showed that fuel staging did not significantly extend low-power operability; this lack of success in fuel staging was attributed to mixing between adjacent fuel-air mixers.\(^1\)

Like the baseline configuration, the second-generation SV-LDI configurations consists of multiple SV-LDI fuel/air mixers: 13 fuel/air mixers arranged in a 114.3 mm \( \times \) 114.3 mm square cross-section. However, unlike in the baseline configuration, the fuel/air mixers are not identical. First, to address operability concerns, a
Pilot stage was added. The pilot stage was a single fuel/air mixer that was slightly larger than the fuel/air mixers used in the main stage. It was larger in part because the diverging section of the venturi was extended; this venturi extension limited mixing with the adjacent main stages. In addition to adding the pilot stage, the main stage was subdivided into three parts, called main 1, main 2, and main 3. Each of these main stages consisted of four fuel/air mixers, for a total of 12 main fuel/air mixers. These twelve fuel/air mixers had the same venturi geometry (e.g., the venturi throat and exit diameters were the same for all 12 main fuel/air mixers). In addition, for a given stage, each fuel/air mixer was identical. However, the fuel/air mixers were configured differently for each stage: both the fuel injector type (simplex or airblast) and the air swirler angle(s) differed.

Two second-generation SV-LDI configurations were tested: these configurations are called the flat dome configuration and the 5-recess configuration. Both are shown in Fig. 4 and some important parameters are given in Table 2. The configurations are similar in many respects. For both, the main 1 fuel injectors are simplex and the main 2 and 3 fuel injectors are airblast. In addition, the swirler angles for the main stages are the same, although the orientations are different. The effective areas are also similar, 1284 mm$^2$ for the

![Figure 4: Second generation SV-LDI hardware: (a) flat dome and (b) 5-recess configurations.](image)

**Table 2:** Second Generation SV-LDI configurations. For each stage, the table gives the type of fuel injector and the air swirler angle(s). (OAS: outer air swirler, IAS: inner air swirler, cw=clockwise, ccw=counterclockwise)

<table>
<thead>
<tr>
<th>Configuration</th>
<th>Pilot Injector</th>
<th>Pilot Swirler</th>
<th>Main 1 Injector</th>
<th>Main 1 Swirler</th>
<th>Main 2 Injector</th>
<th>Main 2 Swirler</th>
<th>Main 3 Injector</th>
<th>Main 3 Swirler</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flat Dome</td>
<td>Simplex</td>
<td>55$^\circ$ ccw</td>
<td>Simplex</td>
<td>45$^\circ$ ccw</td>
<td>Airblast</td>
<td>OAS: 45$^\circ$ cw</td>
<td>Airblast</td>
<td>IAS: 45$^\circ$ cw</td>
</tr>
<tr>
<td>5-Recess</td>
<td>Airblast</td>
<td>IAS: 57$^\circ$ cw</td>
<td>Simplex</td>
<td>45$^\circ$ cw</td>
<td>Airblast</td>
<td>OAS: 45$^\circ$ ccw</td>
<td>Airblast</td>
<td>IAS: 45$^\circ$ ccw</td>
</tr>
</tbody>
</table>
flat dome configuration and 1318 mm² for the 5-recess configuration. However, the configurations differ in two respects. First, the pilot fuel injector is a simplex for the flat dome configuration and an airblast for the 5-recess configuration. Second, the dome geometry is different: in the 5-recess configuration, the pilot and main 1 stages are recessed from the dump plane.

Note that each configuration has 4 stages, a pilot stage and three main stages. However, the test cell only supports three fuel circuits. Therefore, the fuel lines for two stages needed to be ganged together. For the flat dome configuration, the main 2 and main 3 fuel lines were ganged together. For the 5-recess configuration, the pilot and main 2 fuel lines were ganged together; this resulted in the pilot stage being slightly richer than the main 2 stage.

III. Results

Lean blowout tests conducted at Woodward showed that the second generation SV-LDI designs had improved low power operability, with a lean blowout occurring at fuel-air ratios below 0.006.

The rest of this paper concentrates on NOₓ emissions at higher power. First, we compare the NOₓ emissions from the second generation SV-LDI configurations to each other. Then, we consider the effect of combustor inlet conditions for both second generation configurations and of dome pressure drop for the flat dome configuration. After that, we compare the NOₓ emissions when an alternative fuel is burned to the NOₓ emissions when burning JP-8; this is done for the 5-recess configuration. Finally, we develop correlation equations for the flat dome configuration, calculate the landing-takeoff NOₓ emissions for this configuration, and compare the flat dome NOₓ emissions to NOₓ emissions predicted by the first-generation SV-LDI correlation equations.

Although fuel staging was investigated, this paper only presents results where each stage had the same fuel-air ratio. This excludes all data at idle and near-idle conditions (e.g., 535 K = 500 F); during these low power conditions, some of the stages were turned off. It also excludes higher power points where all stages were on but the stages did not have equal fuel-air ratios; for example, cases where the pilot stages was made leaner than the other stages to see if this would reduce the NOₓ. (It turned out that making the pilot more fuel-lean did not help: the NOₓ emissions were generally lowest when all stages had the same fuel-air ratio.)

Most of the results are presented as plots of the NOₓ emissions index vs. adiabatic flame temperature, T_ad. Presenting the results instead as plots of NOₓ emissions index vs. the equivalence ratio φ would not affect the conclusions. This can be seen by comparing Fig. 5 and 6. These figures plot NOₓ emissions at a constant inlet pressure as functions of adiabatic flame temperature and equivalence ratio, respectively. Comparing these two figures show that similar conclusions can be reached by examining either figure: the shape of the NOₓ vs. φ curves are qualitatively similar to the shapes of the NOₓ vs. T_ad curves. As neither the adiabatic flame temperature nor the equivalence ratio collapse the data, there is no advantage to plotting the NOₓ emissions as a function of equivalence ratio. Moreover, plotting the NOₓ emissions as a function of flame temperature will minimize the effect that small deviations in inlet temperature have on the plots. Therefore, in subsequent plots the NOₓ emissions are plotted against the adiabatic flame temperature.

A. Comparison of Second-Generation SV-LDI Configurations

Figures 6 and 7 compare NOₓ emissions from the flat dome configuration to those of the 5-recess configuration. The pressure drop ∆p/p is 3.%. Figure 6 shows results at a constant inlet pressure and Fig. 7 shows results at a constant inlet temperature. In all three figures, flat dome results are plotted with open symbols and dashed lines and 5-recess results are plotted with closed symbols and solid lines.

The results show that the NOₓ emissions from the flat dome configuration are typically either the same or higher than those from the 5-recess configuration. However, whether the emissions are the same or higher does not appear to be a simple trend of inlet temperature, inlet pressure, equivalence ratio, or adiabatic flame temperature.

When the NOₓ vs. T_ad (or φ) curves for the 5-recess configuration are compared with the corresponding curve for the flat dome configuration, four general trends emerge. First, the NOₓ emissions from both configurations are nearly the same at all flame temperatures (or equivalence ratios). This occurs at three combustor inlet temperature, pressure pairs: (650 K, 0.7 MPa), (755 K, 1.4 MPa), and (825 K, 1.4 MPa). Second, the NOₓ emissions are higher for the flat dome configuration but the slopes of the log NOₓ vs. T_ad curves are similar for both configurations. This occurs at two inlet conditions: (650 K, 1.4 MPa) and (650
Third, the flat dome configuration has higher NO\textsubscript{x} emissions at lower flame temperatures but the slope for the flat dome configuration is also flatter; then, when the log NO\textsubscript{x} vs. T\textsubscript{ad} curves for both configurations intersect, the curves converge so that the NO\textsubscript{x} emissions at flame temperatures higher than the intersection point are similar for both configurations. This occurs at inlet conditions of (725 K, 1.7 MPa) and (825 K, 1.7 MPa). It may also occur at two more inlet conditions: (755 K, 1.0 MPa) and (825 K, 1.0 MPa). However, for these latter two conditions, a fourth trend may be happening instead: the flat dome log NO\textsubscript{x} vs. T\textsubscript{ad} curve is nearly flat even at high flame temperatures, which results in the flat dome configuration having lower NO\textsubscript{x} emissions than the 5-recess configurations at high flame temperatures. Distinguishing between these two possibilities requires additional measurements at higher flame temperatures for the flat dome configuration.

**B. Effect of Inlet Temperature and Pressure**

Figures 6–8 show the effect of inlet temperature and pressure on NO\textsubscript{x} emissions. In Fig. 6–7, results are shown from both the 5-recess and flat dome configurations at a pressure drop \( \Delta p/p \) of 3%; the 5-recess results are shown by closed symbols and solid lines and the flat dome results by open symbols and dashed lines. In Fig. 8, only flat dome results are shown. However, the results are shown at three pressure drops, 3%, 4%, and 5%; results for 3% pressure drop are shown by closed symbols and solid lines; results for 4% pressure drop by open symbols and dashed lines; and results for 5% pressure drop by yellow-filled symbols and dotted lines.

Figures 5 and 6 show that NO\textsubscript{x} emissions consistently increase as combustor inlet temperature increases. Figures 7 and 8 show that NO\textsubscript{x} emissions generally increase as pressure increases. One exception to this trend occurs at an inlet temperature of 650 K for the 5-recess configuration; here, as shown in Fig. 7a, NO\textsubscript{x} emissions do not depend on inlet pressure.

A second exception occurs for the flat dome configuration at inlet temperature of 755 K and inlet pressure of 1.0 MPa and a pressure drop of 3%. Figure 7b and 8b show NO\textsubscript{x} vs. T\textsubscript{ad} curves at 755 K. As shown in these figures, at a flame temperature of 1500 K, the NO\textsubscript{x} emissions are the same regardless of whether the pressure is 1.0 or 1.7 MPa. Near 1600 K, the NO\textsubscript{x} emissions are higher for 1.0 MPa. By 1780 K, the NO\textsubscript{x} emissions are lower for 1.0 MPa.

In fact, Fig. 7b and 8b show the the log NO\textsubscript{x} vs. T\textsubscript{ad} curve has an unexpected shape at inlet conditions of 755 K and 1.0 MPa. This is true for pressure drops of both 3% and 4%. Both the 3% and 4% \( \Delta p/p \) are relatively flat; the NO\textsubscript{x} emissions index changes by less than 1.0 between flame temperatures of 1500 and 1700 K. In addition, for both curves, there are conditions when an increase in flame temperature leads to a slight decrease in NO\textsubscript{x} emissions. This is unexpected but does seem to be repeatable: after finishing the \( \phi \)
sweep at 3% $\Delta p/p$, we went back and repeated a few points—the NO$_x$ emissions did not change.

A relatively flat slope of the log NO$_x$ vs. $T_{ad}$ curve may indicate that burning occurs before the fuel is fully vaporized and well-mixed with the combustion air. This should be investigated using optical diagnostics and/or CFD calculations.

C. Effect of Dome Pressure Drop

Figure 8 shows the effect of dome pressure drop on NO$_x$ emissions for the flat dome configuration. Results for 3% pressure drop are shown by closed symbols and solid lines; results for 4% pressure drop by open symbols and dashed lines; and results for 5% pressure drop by yellow-filled symbols and dotted lines.

The results show that increasing the pressure drop generally decreases NO$_x$ emissions. This is expected because the increased pressure drop $\Delta p/p$ is caused by an increase in the cold flow bulk velocity; this in turn decreases the residence time.

There are some exceptions to this trend. At 650 K and 1.4 MPa, NO$_x$ emissions are similar for pressure drops of 3% and 4%. In addition, there are exceptions at 1.0 MPa for inlet temperatures of 755 K and 860 K. Also note that, even for the majority of cases where NO$_x$ emissions decrease with increasing pressure drop, the amount of the NO$_x$ decrease is not consistent. Both the exceptions to the trend and the inconsistent decreases NO$_x$ emissions could also be caused by the change in the cold flow bulk velocity. A change in cold flow velocity will cause a change in the fuel atomization; this change in fuel atomization will cause a change in fuel vaporization and mixing. Again, optical diagnostic measurements and CFD simulations could help to explain the results.

D. Effect of Alternative Fuel

For the 5-recess configuration, an alternative fuel was used in addition to JP-8 to study the effect of alternative fuel on NO$_x$ emissions. The alternative fuel chosen was made from the Camelina sativa plant. This fuel has properties very similar to JP-8. Table 3 and Fig. 9 compare the properties of the Camelina biofuel to samples of JP-8 taken during (4/25/13) and just after (4/29/13) the testing of the 5-recess configuration. The differences between JP-8 and Camelina are small; the most important difference is that Camelina has a slightly higher H/C ratio, 2.0 vs. 1.9 for JP-8.

This small difference in fuel properties is reflected in the NO$_x$ emissions results. Figure 10 shows NO$_x$ emissions as a function of flame temperature for three different combustor inlet conditions. At each inlet condition, results are shown for at least three mass-based alternative fuel percentages, ranging from 0% alternative fuel (i.e., 100% JP-8) to 100% alternative fuel. For all three inlet conditions, NO$_x$ emissions are
Figure 7: NO\textsubscript{x} emissions as a function of equilibrium flame temperature $T_\text{ad}$ at constant $T_3$: (a) 650 K, (b) 755 K, and (c) 810–825 K. The pressure drop $\Delta p/p$ is 3%.

Table 3: Comparison of JP-8 and alternative fuels.

<table>
<thead>
<tr>
<th>Fuel</th>
<th>Carbon % mass</th>
<th>Hydrogen % mass</th>
<th>Sulfur ppm mass</th>
<th>H/C</th>
<th>Lower Heating Value (MJ/kg)</th>
<th>Fuel Density (20 C) kg/m$^3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>JP-8 4/25/13</td>
<td>85.83</td>
<td>13.62</td>
<td>344</td>
<td>1.89</td>
<td>43.2</td>
<td>809</td>
</tr>
<tr>
<td>JP-8 4/29/13</td>
<td>85.91</td>
<td>13.81</td>
<td>219</td>
<td>1.92</td>
<td>43.0</td>
<td>802</td>
</tr>
<tr>
<td>Camelina</td>
<td>85.31</td>
<td>14.42</td>
<td>81</td>
<td>2.01</td>
<td>43.3</td>
<td>778</td>
</tr>
</tbody>
</table>
Figure 8: Flat dome configuration. NO\textsubscript{x} emissions as a function of equilibrium flame temperature $T_{ad}$ at constant $T_3$: (a) 650 K, (b) 755 K, and (c) 810–825 K, and (d) 860 K.
independent of alternative fuel concentration. In other words, using the Camelina biofuel in place of JP-8 does not affect NO\textsubscript{x} emissions. Since the properties of JP-8 and Camelina are similar, this is not surprising.

**E. NO\textsubscript{x} Correlation Equations and ICAO NO\textsubscript{x} Emissions**

In this section, correlation equations are developed for the flat dome configuration. Correlation equations are used to estimate NO\textsubscript{x} emissions at conditions that were not tested. Since the NASA flametube could not reach the inlet conditions needed for high power operation, the correlation equations are needed to estimate the landing-takeoff NO\textsubscript{x} emissions.

Since the second generation SV-LDI hardware was based on the baseline SV-LDI hardware, the flat dome NO\textsubscript{x} emissions are first compared to the emissions predicted by baseline correlation equations. Then, correlation equations are developed for the second generation flat dome configuration. Finally, the correlation equations are used to estimate the ICAO landing-takeoff NO\textsubscript{x} emissions.

1. **Comparison with the baseline correlation equations**

Since the second generation SV-LDI configurations are based on the original baseline 9-point SV-LDI configuration, the second generation correlation equations will be based on the baseline correlation equations developed in R. Tacina et al.\textsuperscript{1} The baseline correlations are given in equations 1–3 below, where $T_3$ is in Kelvin, $p_3$ is in kPa, and $\Delta p/p$ is in \%:

\[
EI-NO_x = a_1 p_3^{0.50} c^{T_3/230} \phi^{b_1} \left( \frac{\Delta p}{p} \right)^{-0.60}
\]

\[
EI-NO_x = a_2 p_3^{0.59} c^{T_3/194} \phi^{b_2} \left( \frac{\Delta p}{p} \right)^{-0.56}
\]

\[
EI-NO_x = a_3 p_3^{0.50} c^{T_3/230} c^{\text{ad}}/b_3 \left( \frac{\Delta p}{p} \right)^{-0.60}
\]

The correlation equations described by equations 1, 2, and 3 will be referred to as Fit 1, Fit 2, and Fit 3, respectively. The coefficients $a$ and $b$ are given in Table 4 for two baseline 9-point SV-LDI configurations: the configuration with a 60\degree swirler angle and co-rotating swirlers and the configuration with a 45\degree swirler angle and co-rotating swirlers. The coefficient of determination, $R^2$, for each correlation is also given. The correlation equations capture the trends in the baseline NO\textsubscript{x} emissions quite well: the $R^2$ value for each correlation are above 0.9 (1.0 would indicate a "perfect fit") and Fig. 11 shows that the NO\textsubscript{x} predicted by the correlation equations is close to the measured NO\textsubscript{x}.

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**Figure 9: Comparison of JP-8 and Camelina fuels.**
Figure 10: Effect of alternative fuel. For all cases, $\Delta p/p = 3.2\%$

Table 4: Baseline and flat dome correlation equations.

<table>
<thead>
<tr>
<th>Configuration</th>
<th>Fit 1</th>
<th>Fit 2</th>
<th>Fit 3</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$a_1$</td>
<td>$b_1$</td>
<td>$R_1^2$</td>
</tr>
<tr>
<td>Baseline, 60°</td>
<td>0.06</td>
<td>1.60</td>
<td>0.97</td>
</tr>
<tr>
<td>Baseline, 45°</td>
<td>0.4</td>
<td>4.82</td>
<td>0.98</td>
</tr>
<tr>
<td>Flat Dome</td>
<td>0.106</td>
<td>2.82</td>
<td>0.63</td>
</tr>
</tbody>
</table>
Figure 11: Correlation equations for the baseline 9-point SV-LDI design with (a) 60° co-rotating swirlers and (b) 45° co-rotating swirlers. From R. Tacina et al.¹

Before finding the coefficients $a$ and $b$ for the flat dome configuration, the NO$_x$ emissions for the flat dome configuration were first compared to the predictions from the baseline correlation equations. This was done to check that the correlation equations give reasonable results for the flat dome configuration. The swirler angles for the flat dome configuration were all between 45° and 60°, so it is expected that the flat dome NO$_x$ emissions will fall between the NO$_x$ emissions predicted for the baseline configuration with 45° swirlers and that for 60° swirlers.

Before comparing the flat dome NO$_x$ emissions to the baseline 45° and 60° curve fits, the baseline curve fits will be compared to each other. This will be done by taking the ratio of each curve fit for the 45° swirlers to the corresponding curve fit for the 60° swirlers. These ratios will be called $r_1$, $r_2$, and $r_3$. For example, $r_1$ is the ratio of Fit 1 for the 45° swirlers to Fit 1 for the 60° swirlers. Taking these ratios shows that the ratios of Fits 1 and 2, $r_1$ and $r_2$, are functions only of the equivalence ratio and that the ratio of the Fit 3s, $r_3$, is a function only of the equivalence ratio. This is shown in equations 4–6 below; in these equations the $a$ and $b$ values for each fit come from Table 4.

\[
\text{Fit 1: } 45° \text{ NO}_x/60° \text{ NO}_x: \quad r_1 = \frac{a_{1,45°} \phi^{b_{1,45°}}}{a_{1,60°} \phi^{b_{1,60°}}} = \frac{0.4\phi^{4.82}}{0.06\phi^{1.60}} \quad (4)
\]

\[
\text{Fit 2: } 45° \text{ NO}_x/60° \text{ NO}_x: \quad r_2 = \frac{a_{2,45°} \phi^{b_{2,45°}}}{a_{2,60°} \phi^{b_{2,60°}}} = \frac{0.11\phi^{5.07}}{0.013\phi^{1.69}} \quad (5)
\]

\[
\text{Fit 3: } 45° \text{ NO}_x/60° \text{ NO}_x: \quad r_3 = \frac{a_{3,45°} e^{T_{ad}/b_{3,45°}}}{a_{2,60°} e^{T_{ad}/b_{3,60°}}} = \frac{10^{-6} e^{T_{ad}/178}}{0.0014 e^{T_{ad}/520}} \quad (6)
\]

Calculating these ratios according to equations 4–6 indicates that the NO$_x$ emissions from the 45° baseline configuration will be less than those from the 60° configuration at low equivalence ratios and flame temperatures. However, as the equivalence ratio and flame temperature increase, the 45° configuration will have higher NO$_x$ emissions; this will occur at $\phi > \sim 0.55$ and $T_{ad} > \sim 1950$. This result is consistent with the measurements reported in R. Tacina et al.¹

Since the swirler angles for the flat dome configuration were all between 45° and 60°, the flat dome configuration is expected to have higher NO$_x$ emissions than the 45° baseline curve fits at low equivalence ratios but similar or lower NO$_x$ emissions at higher equivalence ratios. Similarly, the flat dome configuration is expected to have lower NO$_x$ emissions than the 60° baseline curve fits at low equivalence ratios but similar or higher NO$_x$ emissions at higher equivalence ratios.

The results show that this is what happens. Figure 12 shows the measured flat dome NO$_x$ emissions compared to the baseline correlation equations. The color of each symbols indicates the equivalence ratio $\phi$ at that point, with blue symbols at the lowest equivalence ratios and red symbols at the highest equivalence
Figure 12: Comparison of the measured NO\textsubscript{x} emissions from the flat dome SV-LDI design to the emissions predicted by the baseline 9-point SV-LDI design with (a) 45° and (b) 60° swirlers.

ratios. Figure 12a compares the flat dome NO\textsubscript{x} emissions to the baseline 45° correlation equations. As expected, at low equivalence ratios (blue symbols), the flat dome NO\textsubscript{x} emissions are higher than predicted by the correlation equation, but at high equivalence ratios (red symbols), the NO\textsubscript{x} emissions are lower. Figure 12b compares the flat dome NO\textsubscript{x} to the baseline 60° correlation equations. Again as expected, the flat dome NO\textsubscript{x} emissions are lower than the predicted by the 60° correlations at low equivalence ratios, but about the same or slightly higher than predicted at high equivalence ratios.

These results show that baseline correlation equations give reasonable results when compared to the measured flat dome NO\textsubscript{x} emissions. Therefore, Fits 1–3 will be used as a basis for developing the flat dome correlation equations. This is done in the next section.

2. Flat dome correlation equations

Since the baseline correlation equations produced reasonable results when compared to the flat dome NO\textsubscript{x} emissions data, these correlation equations were used as a basis for developing correlation equations for the flat dome configuration. First, multiple regression was used to find the coefficients a and b for Fits 1–3. This regression was done only on points where the fuel-air ratio was the same for each stage. The coefficients a and b for each of Fits 1–3 are given in Table 4. However, results show that Fits 1–3 do not adequately describe the NO\textsubscript{x} emissions data: the $R^2$ values were all below 0.7. The poor quality of the correlation from Fits 1–3 can also be seen in the plots in Fig. 13a.

In Fits 1–3, the effect of $p_3$, $T_3$, and $\Delta p/p$ were fixed at the values used for the baseline correlation equations. To see if the correlation equations would better describe the data if the effects of these variables were changed, two new correlation equations were developed, called Fits 4 and 5. For these equations, the exponents of $p_3$ and $\Delta p/p$ and the divisor of $T_3$ were allowed to vary. Multiple regression on data points with equal fuel staging was again done. The results are given in the equations for Fits 4 and 5 below:

Fit 4: \[
\text{EI-NOx} = 0.255 p_3^{0.462} e^{T_3/314} \phi^{2.31} \left( \frac{\Delta p}{p} \right)^{-0.695}, \quad R^2 = 0.67 \] (7)

Fit 5: \[
\text{EI-NOx} = 0.0008 p_3^{0.460} e^{T_3/757} e^{T_{ad}/355} \left( \frac{\Delta p}{p} \right)^{-0.647}, \quad R^2 = 0.77 \] (8)

Although Fits 4 and 5 described the data slightly better – $R^2$ was a bit higher – they still did not describe the data well. $R^2$ was below 0.8 for both Fit 4 and 5, and plots of the measured NO\textsubscript{x} vs. the NO\textsubscript{x} calculated from Fits 4 and 5 show that these fits did not collapse the data. See Fig. 13b.
An explanation for why Fits 1–5 do not adequately describe the flat dome NO\textsubscript{x} emissions can be found by comparing the flat dome SV-LDI geometry to the baseline 9-point geometry. For the baseline 9-point configuration, all fuel/air mixers were identical in fuel injector type, swirler angle, and venturi geometry. However, the fuel/air mixers for the flat dome configuration were not identical: they differed in fuel injector type, swirler angle, and venturi geometry. These differences in fuel/air mixer could result in each type of fuel/air mixer following a different correlation; the CFD results of Ajmani et al\textsuperscript{15} show that this is indeed the case. Therefore, Fits 1–4 were modified to have a term for each stage in which the fuel-air ratio could be varied independently. Since the fuel lines for main stages 2 and 3 were ganged together, this results in a term for the pilot, a term for main 1, and a term for mains 2 and 3. The total NO\textsubscript{x} emissions are found by adding the three terms together. In other words,

\[ \text{NO}_x = (\text{NO}_x)_{\text{pilot}} + (\text{NO}_x)_{\text{main 1}} + (\text{NO}_x)_{\text{mains 2 & 3}} \] (9)

This results in the modified correlation equations Fits 1n–5n, as given below:

- **Fit 1n**: \( E\text{I-NO}_x = p_0^{0.50} e^{T_3/230} \left( \frac{\Delta p}{p} \right)^{-0.60} \sum_{i=1}^{3} a_{1n,i} e^{T_{ad} b_{1n,i}} \) (10)
- **Fit 2n**: \( E\text{I-NO}_x = p_0^{0.59} e^{T_3/194} \left( \frac{\Delta p}{p} \right)^{-0.56} \sum_{i=1}^{3} a_{2n,i} e^{T_{ad} b_{2n,i}} \) (11)
- **Fit 3n**: \( E\text{I-NO}_x = p_0^{0.50} e^{T_3/340} \left( \frac{\Delta p}{p} \right)^{-0.60} \sum_{i=1}^{3} a_{3n,i} e^{T_{ad} b_{3n,i}} \) (12)
- **Fit 4n**: \( E\text{I-NO}_x = p_0^{0.46} e^{T_3/314} \left( \frac{\Delta p}{p} \right)^{-0.695} \sum_{i=1}^{3} a_{4n,i} e^{T_{ad} b_{4n,i}} \) (13)
- **Fit 5n**: \( E\text{I-NO}_x = p_0^{0.46} e^{T_3/757} \left( \frac{\Delta p}{p} \right)^{-0.647} \sum_{i=1}^{3} a_{5n,i} e^{T_{ad} b_{5n,i}} \) (14)

where \( i = 1 \) indicates the pilot stage, \( i = 2 \) indicates the main 1 stage, and \( i = 3 \) indicates the main 2 and 3 stages.

Multiple regression was again done, this time including results where the fuel-air ratio was not the same for each stage. Fits 1n–5n capture the data much better, with \( R^2 \) values typically above 0.9. Examining the plots of measured vs. calculated NO\textsubscript{x} emissions showed that Fits 1n and 2n appear to capture the data best; this is shown in Fig. 14. The coefficients \( a_{1n,i} \) and \( a_{2n,i} \) and the \( R^2 \) value for Fits 1n and 2n are shown...
in Table 5. Since these two fits capture the data well, they will be used to calculate the landing-takeoff NO\textsubscript{x} emissions.

3. Landing-takeoff NO\textsubscript{x} emissions

The landing-takeoff NO\textsubscript{x} emissions were calculated for the flat dome configuration. The Pratt & Whitney ERA cycle conditions were used, and we assumed 20% liner cooling. For the lower power conditions, the flametube measurements were used to find the NO\textsubscript{x} emissions. For the higher power points, correlation equations Fit 1\textsubscript{n} and Fit 2\textsubscript{n} were used. The flat dome NO\textsubscript{x} emissions were 87–88% below the CAEP/6 standards. This exceeds the ERA project goal of 75% NO\textsubscript{x} reduction.

IV. Future Work

There are five areas where future work will be done. 1) The third second generation LDI configuration developed by Woodward will be tested in NASA’s flametube test rig. 2) A active combustion control scheme developed by Woodward will be tested in the NASA flametube. 3) Measurements when the fuel-air ratios were different for each stage will be further analyzed and reported. 4) The measurements taken at near-idle conditions will be reported. 5) The dynamic pressure measurements will be further analyzed and reported.

V. Summary

Three second generation SV-LDI configurations were developed. All were based on the baseline 9-point SV-LDI configuration reported previously\textsuperscript{1}. These second generation configurations had better low power operability than the baseline 9-point configuration. Two of these second generation configurations were tested in a NASA Glenn Research Center flametube; these two configurations are called the flat dome and 5-recess configurations. Results show that the 5-recess configuration generally had lower NO\textsubscript{x} emissions than the flat dome configuration. Correlation equations were developed for the flat dome configuration so that the landing-takeoff NO\textsubscript{x} emissions could be estimated. The flat dome landing-takeoff NO\textsubscript{x} is estimated to be 87–88% below the CAEP/6 standards, exceeding the ERA project goal of 75% reduction.

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References


Figure 14: Correlation equations for the flat dome SV-LDI design.


