Examination of the Measurement of Absorption Using the Reverberant Room Method for Highly Absorptive Acoustic Foam

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ABSTRACT

The absorption coefficient for material specimens are needed to quantify the expected acoustic performance of that material in its actual usage and environment. The ASTM C423-09a standard, “Standard Test Method for Sound Absorption and Sound Absorption Coefficients by the Reverberant Room Method” is often used to measure the absorption coefficient of material test specimens. This method has its basics in the Sabine formula. Although widely used, the interpretation of these measurements are a topic of interest. For example, in certain cases the measured Sabine absorption coefficients are greater than 1.0 for highly absorptive materials. This is often attributed to the diffraction edge effect phenomenon. An investigative test program to measure the absorption properties of highly absorbent melamine foam has been performed at the Riverbank Acoustical Laboratories. This paper will present and discuss the test results relating to the effect of the test materials’ surface area, thickness and edge sealing conditions. A follow-on paper is envisioned that will present and discuss the results relating to the spacing between multiple piece specimens, and the mounting condition of the test specimen.

KEY WORDS: Absorption, absorption coefficient, acoustic energy absorption coefficient, acoustics, acoustic testing, ASTM C423, diffraction edge effect, Eyring absorption, payload fairing acoustics, reverberation room, sabins, Sabine absorption coefficient, Sabine formula.

INTRODUCTION

NASA has an ongoing interest in utilizing melamine acoustic foam for noise reduction in their future launch vehicles. In order to properly design the sound absorption systems used in aerospace, architecture, and other noise control applications, the characterization of the absorption properties of materials is needed. Normal incidence impedance and absorption may be obtained from impedance tube test measurements. However, for many practical applications the measurement of the random incidence absorption coefficient obtained from a reverberant chamber test is desired. Indeed, it is the random incident absorption coefficient, \( a \), also known as the Sabine absorption
coefficient, which is the parameter most available and widely used today in acoustic design to specify the absorption performance of materials.

The reverberant chamber method is a well-established method which utilizes Sabine’s formula (Sabine 1922, Sabine 1964), Equation 1, for the decay of sound for the determination of absorption coefficients within a reverberant room.

\[
RT_{60} = \frac{0.161 V}{A}
\]  

(1)

Here \(RT_{60}\) is the reverberation time (in seconds) for the sound in the reverberant room to decay 60 decibels (dB) once the sound source is turned off, \(V\) is the volume of the reverberant room (in \(m^3\)), and \(A\) is the total area of sound absorption (in \(m^2\), or also denoted as metric sabins), as defined by Equation 2. (Note the English units for sound absorption are sabins, where one sabin was originally described as “1 ft.\(^2\) of open window”.) The 0.161 value is a result of the numerical calculation of \([24 \ln (10)]/c\), where \(c\) is the speed of sound in air (in m/s) at 20° C (Celsius), and \(\ln\) is the natural logarithm.

\[
A = S\bar{a}
\]  

(2)

\(S\) is the total surface area of the reverberant room (in \(m^2\)), and \(\bar{a}\) is the average Sabine absorption coefficient of the reverberant room as defined by Equation 3.

\[
\bar{a} = \frac{s_1a_1 + s_2a_2 + \cdots + s_na_n}{S}
\]  

(3)

Here, \(a_i\) is the Sabine absorption coefficient of the \(i\)th surface, \(s_i\) (in \(m^2\)).

By calculating the total area of sound absorption, \(A\), with and without the test specimen in the reverberant room, a measurement of the absorption of the test specimen can be calculated. The American Society for Testing and Materials (ASTM) C423-09a standard “Standard Test Method for Sound Absorption and Sound Absorption Coefficients by the Reverberant Room Method” provides a method to achieve such results. This reverberant room method, although widely used and rigorously defined by industry testing standards (such as the ASTM C423 and ISO 354 standards), has some conditions and inherent issues that may complicate the interpretation of the measured absorption, including the values of the Sabine absorption coefficient. Some of these considerations will be discussed later in this paper. Nonetheless, the Sabine absorption coefficients have and continued to be used successfully for acoustic design problems. This success is accomplished in spite of the fact that the actual “in-field” applications often take place in non-diffuse fields, and with different surface areas and different diffraction edge effects than what is experienced in the reverberant room test conditions.

For illustration purposes, Figure 1 provides an example of three plots of Sabine absorption coefficients plots as a function of one-third octave band (OTOB) frequency (Hughes and McNelis 2014). Note that values greater than 1.0 for the Sabine absorption coefficient were measured.

Eyring (1930) pointed out that Sabine’s formula is really a special case of a more general equation and should be used when the absorption coefficient is small, i.e. for “live” rooms, but not used for surfaces with large absorption coefficients, i.e. for “dead” rooms. Using the Sabine formulation can result in inaccurate absorption coefficients for highly absorptive materials. Various sources (including Cox 2009, Crocker 1998) suggests that other formulations such as Eyring or Millington be used instead of the Sabine formulation for such cases.
Figure 1. Examples of Sabine Absorption Coefficients for two thicknesses of melamine foam (ML G, with no coversheet and unsealed edges), and fiberglass batting with a coversheet.

ASTM C423 METHODOLOGY (RIVERBANK ACOUSTICAL LABORATORIES)

ASTM C423, “Sound Absorption and Sound Absorption Coefficients by the Reverberation Room Method”, provides a method to calculate the total absorption of a specimen by using the difference in absorption obtained with an empty chamber and with a chamber with the test specimen. This ASTM standard requires the measured frequency range of 100 Hz to 5 kHz (and that is the frequency range of data presented in this paper). The following describes the implementation of this standard test method at the Riverbank Acoustical Laboratories (RAL) located in Geneva, IL. The RAL was founded in 1918 by Wallace Clement Sabine.

Measurements were made in the RAL’s 291.73 m³ (10,302.29 ft³) reverberation chamber (with the following approximate dimensions: length = 8.27 m (27.16 ft.), width = 5.85 m (19.19 ft.), height = 6.03 m (19.77 ft.)). A rotating microphone boom with a 7.98 m (314.17 in) circumferential traverse was placed at a location such that the microphone is always at least 0.75 m (29.5 in) from any surface. The rotating boom was set at 32 seconds per revolution. The temperature (°C), relative humidity (%), and atmospheric pressure (kPa) were recorded and used to correct the measured decay time for air absorption above 1,000 Hz using ANSI S1.26, Method for Calculation of the Absorption of Sound by the Atmosphere.

The reverberation chamber also contains 5 stationary diffuser vanes and 2 rotating diffuser vanes (rotating at 18 seconds per revolution). These large diffusers, scattered over the reverberation room’s walls and ceiling, disrupt any acoustic standing waves and help improve the diffusivity of the room’s acoustic field.
ASTM C423 requires that testing be performed to qualify the reverberation room in the frequency range from 100 Hz to 5 kHz. The RAL reverberation room has been qualified to perform ASTM C423 testing per the Reverberation Room Qualification criteria provided in ASTM C423 Appendix A.3. The diffusivity of the empty RAL reverberation room likely extends even lower than the qualified 100 Hz OTOB, perhaps as low as the 63 Hz OTOB.

With the chamber cleared of all extraneous material (including the test specimen), pink noise (equal sound power per octave) is generated in the chamber until a steady state signal is reached. When the signal noise generator ceases, the decay of the sound pressure level in each frequency band is measured every 0.034 second for 6.8 second (a total of 200 measurement points). This process was repeated 80 times and averaged. ASTM C423 requires a minimum of 50 decays, however RAL uses 80 decays in order to improve their average and minimize uncertainties. The decay measurement is evaluated starting at approximately 100 milliseconds (ms) after the initial decay until the sound pressure level decays 25 dB. The sound absorption of the empty chamber, $A_1$, is then computed using Equation 4.

$$A = 0.921 \frac{Vd}{c}$$

Where, $V$ is the volume of the test chamber ($m^3$), $d$ is the sound decay rate (dB/s), and $c$ is the speed of sound in air (m/s).

The RT$_{60}$ measurement originated with Wallace Clement Sabine’s experiments measuring the practical human dynamic range of the decay of organ pipe sound to inaudibility with his ears and a stopwatch. Today, the RT$_{60}$ measurements are usually extrapolated from shorter, say 25 dB, sound decay measurements. This allows the decay rate to be measured while the decay is linear and still above the background noise levels of the room.

The test specimen is then placed on the floor asymmetrically relative to the test chamber walls at a distance of at least 0.75 m (29.5 in.) from any reflective surface (except the floor surface) and from the microphone traverse. The aforementioned steps are repeated and the sound absorption of the chamber with specimen, $A_2$, is computed using Equation 4. The total sound absorption added to the room by the specimen, $A$, is then calculated as follows:

$$A = A_2 - A_1$$

Where, $A$ is the Sabine absorption of the test specimen ($m^2$), $A_1$ is the Sabine absorption of the empty reverberation chamber ($m^2$), and $A_2$ is the Sabine absorption of the chamber with the test specimen present ($m^2$).

Finally, the Sabine absorption coefficient can be computed by dividing the absorption of the test specimen, $A$, by the test specimen’s surface area, $S$ ($m^2$). Under most normal conditions, $S$ is the top surface area of the material.

$$\alpha = \frac{A}{S}$$

Figure 2 is a photograph of the RAL ASTM C423 sound absorption test setup. This Figure shows the test specimen (standard density Soundfoam® melamine foam, ML G, for this test) on the floor with unsealed edges. Per ASTM C423, the edges of a test specimen are normally sealed off with a mixture of reflective steel beams and Masonite wood strips to avoid any added absorption being contributed by the side edge areas. Figure 2 also illustrates other aspects of the RAL reverberation
room, including the speaker noise source in the corner, the rotating microphone boom, and a partial viewing of a few of the stationary and rotating diffuser vanes.

Figure 2. RAL’s Absorption Test Setup (10.16 cm thick ML G foam with unsealed edges, ASTM-C423 Reverberation Room Method).

Figure 3. Illustration of Reverberation Time Decay.
Figure 3 is an illustration on how the RT$_{60}$ decay times of the RAL reverberant room changes with the introduction of an absorptive test specimen. The RT$_{60}$ times for two measurements of the empty room (with no test specimen) is shown; note that even though these two empty room tests were performed five days apart they are in excellent agreement in all OTOBs. When a “good” test specimen absorber (5.08 cm of melamine foam) is present the RT$_{60}$ times become smaller. When a “better” test specimen absorber (20.32 cm of melamine foam) is present the RT$_{60}$ times become even smaller still, especially at the lower frequencies.

INVESTIGATIVE TEST PROGRAM

As shown in Figure 1, it is possible to get Sabine absorption coefficients greater than 1.0. A number of tests performed for NASA Glenn Research Center at RAL in the past few years on highly absorptive, and relatively thick, melamine foam resulted in several such occurrences (Hughes and McNelis 2014). ASTM C423 and others sources (Cox 2009, Sauro 2009) associate Sabine absorption coefficients greater than 1.0 with the diffraction edge effect phenomenon. That is, diffraction of the sound wave over the edges of the test specimen causes the apparent surface area of the test specimen (“its acoustic footprint”) to be larger than its actual physical surface area. When the test specimen is highly absorptive this can result in Sabine absorption coefficients greater than 1.0.

In an effort to further investigate the diffraction edge effect the authors proposed a test program to explore these issues in a study using highly absorptive melamine foam. The Soundcoat Company Inc. (Irvine, CA) donated their newest melamine ultralight acoustic foam product for this test program. All testing was done using the Soundfoam® ML ULb (melamine ultralight) foam. This foam product is a lightweight, flexible, open-cell acoustic foam, with a mass density of 6.0 kg/m$^3$ (0.375 lb/ft$^3$). Soundcoat’s Soundfoam® ML ULb foam is formulated to have lower formaldehyde emissions, while maintaining similar acoustic properties, than their original ML UL product. The Riverbank Acoustical Laboratories donated the use of their test facility and engineering services for the performance of the ASTM C423 test series for this study. The testing was performed in March – April 2015 at RAL.

The objectives for this test program, relative to measuring the test specimen’s absorption, are:

- **Objective # 1:** Evaluate the effect on absorption of varying the test specimen’s surface area size for a constant 5.08 cm (2 in) thick test specimen.
- **Objective # 2:** Evaluate the effect on absorption of varying an airspace gap between the test specimen and the floor.
- **Objective # 3:** Evaluate the effect on absorption of changing the test specimen’s thickness for a constant surface area of 6.69 m$^2$ (64 ft.$^2$).
- **Objective # 4:** Evaluate the effect on absorption of separating the test specimen into several pieces with air gaps between these pieces.
- **Objective # 5:** Evaluate the effect on absorption of keeping the overall (both top and side edges) surface area constant for two different shape test specimens.
The test matrix is shown in Table 1 (metric units) and Table 2 (English units). The standard sound absorption mounting types are defined in ASTM E795 “Standard Practices for Mounting Test Specimens During Sound Absorption Tests,” but are summarized as follows:

- A-Mount: laid directly against the test surface (floor) with no airspace behind the panel.
- E-400 Mount: 400 mm airspace to resemble suspended grid ceiling.
- F-Mount: laid directly against the test surface, but with a mounting clip that provides a small airspace behind the panel.
- J Mount: as spaced objects distributed throughout the chamber according to the customer’s desired test configuration’s specifications.

**TEST RESULTS AND DISCUSSION**

Testing in support of Objectives # 1, # 3, and # 5 will be discussed in this paper. Testing in support of Objectives # 2 and # 4 will be discussed in a follow-on paper.

**Objective #1:**

Evaluate the effect on absorption of varying the test specimen’s surface area size for a constant 5.08 cm (2 in) thick test specimen.

**Results:**

Test configurations #1 – #7 are all 5.08 cm (2 in) thick sheets of Soundfoam® ML ULb foam. The ASTM C423 standard recommends that the test specimen have an area of 6.69 m² (72 ft.²), with the minimum acceptable area being 5.57 m² (60 ft.²). For our test program however, the surface area (length x width) of these test specimens varied from a high of 10.22 m² (110 ft.²) (the standard size per the ISO 354 standard) to a low of 3.90 m² (42 ft.²). Figures 4 and 5 provide the illustration of this surface area parameter studied in this subset of tests.

**Figure 4.**
Surface Area = 10.22 m² (A15-029),
Maximum Surface Area Tested.

**Figure 5.**
Surface Area = 3.90 m² (A15-036),
Minimum Surface Area Tested.
### Table 1. Test Matrix (metric units)

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<th>Size (m²)</th>
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**Unsealed Edges**
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**Test Objective #**

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**Unsealed Edges**
One might expect that the measured total sound absorption (in m²) would be proportional to the exposed top surface area. If so, then the sound absorption measured in the 10.22 m² configuration would be a factor of 2.62 times (10.22 m² / 3.90 m²) the measured sound absorption for the 3.90 m² configuration. However, per the sound absorption data of Figure 6, it is found that in the 315 Hz to 5 kHz OTOBs frequency range, the ratio is slightly less, being between 2.22 to 2.53. That is, the test specimens with the larger surface area produce sound absorption measurements smaller than what would be predicted purely by scaling absorption levels from the smaller test specimens.

The Sabine absorption coefficient can be computed per Equation 6 and these values are shown in Figure 7. A review of the data in Figure 7 illustrates that although the Sabine absorption coefficient for the 5.08 cm (2 in) thick Soundfoam® ML ULb foam is close for these various test specimens with varying surface areas, they are not the same. Again, the larger surface area test specimens have smaller Sabine absorption coefficients than does the smaller surface area test specimens.

Discussion:
It has been well documented (Bartel 1981, Nelson 1990, Sauro 2009, Cox 2009, and others) that the measured apparent Sabine absorption coefficient will be greater for test specimens with a smaller surface area, compared to the identical material with a larger surface area. This effect is dependent upon the ratio of the specimen’s perimeter to its area, and will vary with both wavelength and with the specific material (i.e., foam will behave differently than fiberglass, wood, and other materials).

Bartel (1981) suggests a linear relationship between the absorption coefficient and the relative edge length of the test specimen as shown in Equation 7.

\[ \alpha = \alpha_0 + \beta E \]  

Here, \( \alpha \) is the apparent Sabine absorption coefficient of a given test specimen as measured by the reverberant room method, \( \alpha_0 \) is the “true” absorption coefficient (i.e. for an infinite size test specimen and thus with no diffraction edge effect), \( \beta \) is a constant (at each particular frequency for a specific material), and \( E \) (m⁻¹) is the ratio of the test specimen’s perimeter (m) to its surface area (m²).

Bartel states that this linear relationship is a better approximation for some materials compared to others. Also, Bartel states that this relationship is approximately true whether or not the side edges are sealed (covered with a reflective material) during testing or not, although varying the sealing condition would result in different values of \( \beta \). Finally, Bartel notes that the extrapolation of this relationship to a value of \( E = 0 \) to obtain \( \alpha_0 \), the true absorption coefficient for an infinite size specimen, may in general not always hold. However, this equation does have merit in using available test measured data to estimate by interpolation or extrapolation the absorption coefficients for an application of the same material with a different (finite) surface area, thereby eliminating the need for additional testing with that new size test specimen.

The Sabine absorption coefficient measured in our testing, was used to produce a plot of Sabine absorption coefficient versus \( E \) for various OTOB frequencies using the method outlined by Bartel. These results are shown in Figure 8. For this Figure, the best linear fit equation was used to fit to the five data points at each OTOB frequency. From this fit, the values of \( \alpha_0 \) (y-intercept) and \( \beta \) (slope) can be derived. This would allow the calculation of the absorption, \( \alpha \), for any size of \( E \).
Figure 6. Sound Absorption as a function of Surface Area.

Figure 7. Sabine Absorption Coefficient as a function of Surface Area.
The test data shown in Figure 8 isn’t as linearly well behaved as the data that Bartel provides, but it does present an example of this method. One can see that this type of plot could be useful to predict Sabine absorption coefficients for the same material of a different surface area size when you already have Sabine absorption coefficient data for that material from other test specimen sizes. By extrapolating the linear equation all the way to E=0 (y-axis intercept), as shown in Figure 8, would in theory give the Sabine absorption coefficient for that material if it were of infinite size (and therein have no diffraction edge effect).

![Figure 8. Sabine Absorption Coefficient as a function of E.](image-url)
**Objective # 3:**

Evaluate the effect on absorption of changing the test specimen’s thickness for a constant surface area.

**Results:**

Test configurations # 16 – 29 all have top surface areas of $2.74 \text{ m} \times 2.44 \text{ m} = 6.69 \text{ m}^2$ (9 ft. x 8 ft. = 72 ft.$^2$). The thickness of the ML ULb foam is varied from a low of 1.27 cm (0.5 in) to a high of 30.48 cm (12 in). Photographs of a few of these test configurations are shown in Figures 9-12.

Acoustic foam is often used in today’s aerospace industry. The inside of the launch vehicle’s payload fairing is lined with foam in order to reduce the amount of the acoustic noise reaching and possibly damaging the spacecraft. The acoustic noise is generated during the liftoff and ascent phases of the flight. Typically such foams are on the order of 5.08 – 10.16 cm (2 – 4 in) in thickness, as stated in launch vehicle payload user guides. Hughes and McNelis (2014) have recently characterized the absorption (and transmission loss) characteristics of even thicker melamine foam materials with the expectation of improving the noise reduction at lower frequencies. Since both weight and the available physical space is important for launch vehicle fairing applications of acoustic foam, knowing how the foam’s absorption varies with thickness is of interest, and thus a wide range of thicknesses were tested.
As the thickness of the foam increases the acoustic performance of the foam typically improves. As the foam thickness increases, the frequency at which the peak absorption occurs becomes lower and the overall magnitude of absorption increases, especially at lower frequencies (Hughes and McNelis 2014, and many others). These trends are illustrated in Figures 13 and 14, for the Sound Absorption and Sabine absorption coefficient, respectively.

![Figure 13. Sound Absorption as a function of the Thickness of the Test Specimen.](image1)

![Figure 14. Sabine Absorption Coefficient as a function of the Thickness of the Test Specimen.](image2)
Discussion:

It is thought that the improvement in absorption seen with increasing thickness is primarily due to the thickness factor itself. Low frequencies have long wavelengths which means the absorbers have to be large to absorb the low frequencies’ wave fronts.

For example, Cox (2009) mentions a rough guideline that a material needs to be at least a tenth of a wavelength thick to cause significant absorption, and a quarter wavelength thick to absorb all the incident sound. Using this guideline, Table 3 lists the acoustic performance of an absorber as a function of frequency, where $c$ is the speed of sound in air (344 m/s; 13,560 in/s) and $h$ is the absorber thickness. On the whole, Table 3 seems to be in general agreement with the test results shown by Figures 13 and 14.

Table 3. Guideline to Frequency of Absorption as a function of Absorber Thickness.

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<th>Absorber thickness, $h$, in cm (in)</th>
<th>Significant Sound Absorption starting at frequency (Hz) $f = \frac{c}{10h}$</th>
<th>“All” Sound Absorbed starting at frequency (Hz) $f = \frac{c}{4h}$</th>
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<td>30.48 (12.0)</td>
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However, there is likely a secondary influence on the results, especially at the lower frequencies. The reverberant room method assumes that a diffuse acoustic field is produced in the reverberant test room. A diffuse acoustic field (per Hodgson, 1996) has waves that are incident from all directions with equal intensity and random phase at any position in the room, and has the same sound field at every position in the room. The size, shape, and aspect ratio of the test room all play a role in determining how diffuse the sound field actual is. Additionally, the very presence of an absorbing material test specimen can produce a non-diffuse field in the locality of the test specimen.

Beyond possibly violating the diffuse field assumption of the reverberant room method, the finite size of the test specimen can cause further influence on the absorption test results from the phenomenon known as the diffraction edge effects. Here, diffraction is the bending of the sound waves around the side edges of the test specimen therein producing additional absorption. Thicker test specimens will create a diffraction edge effect at lower frequencies than thinner test specimens.
Also, lower frequencies diffract to a greater degree than higher frequencies. Therefore, it is surmised that some unknown portion of the absorption observed in Figures 13 and 14 is attributable to diffraction. The observed peaking of the absorption in the 125 Hz OTOB for the test specimens with thickness of 17.78 cm (7 in) or larger may be a sign of this effect, although diffraction edge effects are likely to contribute to the measured absorption for test specimens with even smaller thickness.

There is no doubt that the diffraction edge effect plays a role in increasing the absorption and Sabine absorption coefficients measured in test using the reverberation room method. Cox (2009) states that diffraction at the edges of the test specimen creates excess absorption in the reverberation chamber measurements, and he attributes it to the impedance discontinuity at the specimen’s edges causing the sound to bend into the sample. Nelson (1990) attributes this increased absorption to the test specimen disturbing the diffuse sound field directly above it, thereby drawing the sound energy into itself by diffraction. The end result is that for highly absorptive materials there can be cases when the absorption footprint (in m² or metric sabins) is larger than the physical surface area (in m²), and such the resulting Sabine absorption coefficient will be greater than 1.0. As previously stated the diffraction effects are more prominent at lower frequencies. This diffraction edge effect becomes even more prominent when the test specimen is spread out in an array of pieces as opposed to one continuous piece (Objective # 4).

Objective # 5:
Evaluate the effect on absorption of keeping the overall (both top and side edges) surface area constant for two different shape test specimens.

Results:
As seen in Figures 15 and 16, Test runs A15-053 and A15-054 were two large, very unusual, test specimens. They were tested solely to see how the measured absorption of two test specimens with the same size total surface area, but with different shapes and different top surface area, would compare. As such all the side edges were left exposed (unsealed edges) as shown in the photographs.

The test specimen for Test run A15-053 was 1.22 m (4 ft.) x 2.44 m (8 ft.) x 0.81 m (32 in) high. This resulted in a top surface area of 2.97 m² (32 ft.²) and a side surface area of 5.95 m² (64 ft.²) for a total exposed surface area of 8.92 m² (96 ft.²).

The test specimen for Test run A15-054 was 2.44 m (8 ft.) x 2.44 m (8 ft.) x 0.30 m (12 in) high. This resulted in a top surface area of 5.95 m² (64 ft.²) and a side surface area of 2.97 m² (32 ft.²) for a total exposed surface area of 8.92 m² (96 ft.²).

Thus, the test objective was to observe how or if the measured absorption varied depending upon the orientation of the exposed surfaces (i.e. top surface versus side surfaces).
As can be seen in Figure 17, the total sound absorption were somewhat close, but not the same. The Test run A15-054 test specimen, which had twice the amount of exposed top surface area, has more sound absorption than the Test run A15-053 test specimen. Averaged out over the 100 Hz – 5 KHz OTOBs, it was 10% higher in sound absorption (range of minimum of 4% at 1.6 KHz OTOB to a maximum of 37% higher at 125 Hz OTOB).

Figure 18 shows the comparison of the Sabine absorption coefficient for these two test specimens. Since the Sound Absorption is divided by the top surface area only one would expect that Test run A15-054 test specimen’s Sabine absorption coefficient would be approximately 50% less than the Test run A15-053 test specimen’s Sabine absorption coefficient due to their difference in their respective top surface areas. Thus, Figure 18 is an unfair comparison and should not be considered truly meaningful, but is included here for completeness.

Discussion:
These two large and atypical test specimens were designed and chosen to evaluate the stated objective. However, due to their size and shape they may have violated several underlying assumptions of the reverberant room method. The mere volume of space that they take up, in addition to the very large amount of highly absorbent surface area is likely to have disturbed the diffuse sound field in the test room. There could potentially be blocking or shadowing effects due to the test specimen’s size and location, and the high amount of absorption is likely to have created non-diffuse sound fields around the test specimens therein raising the question of the applicability of the reverberant room method for these particular test specimens. Additionally, one would expect that the diffraction edge effect would play a very significant role in increasing the sound absorption, especially at low frequencies.

Despite all these potential concerns, the sound absorption of the two test specimens was within (on average) 10%. One might surmise that the Test run A15-054 test specimen performed slightly better than its counterpart, Test run A15-053, because its greater surface area contributor was the top surface. One would think that the top surface would have a greater likelihood of “seeing” the reflective sound waves in the room more often, whereas the side surfaces may have somewhat of a less likelihood of this sound energy exchange.
Figure 17. Sound Absorption of Two Test Specimens with Equal Total Surface Areas.

Figure 18. Sabine Absorption Coefficient of Two Test Specimens with Equal Total Surface Areas.
SUPPLEMENTARY DISCUSSION ON EFFECT OF SEALING SIDE EDGES

As stated earlier, ASTM C423 recommends that the side edges of the test specimen be covered with reflective, non-absorptive, material in order to ensure that the side edges do not contribute to the measurement of the absorption. This condition is known as “sealed edges.” For this test series, four Test runs (A15-031, A15-037, A15-042, and A115-050) were performed with “unsealed edges” to evaluate the effects. These four test runs had corresponding identical test specimen configurations that did have “sealed edges” condition (A15-030, A15-036, A15-043, and A115-049). Figures 19 and 20 show such a configuration pair, with and without edge sealing.

Figure 19. Test Specimen with Sealed Edges (A15-030).
Figure 20. Test Specimen with Unsealed Edges (A15-031).

Figure 21 shows a comparison of the sealed versus unsealed conditions for cases with a constant test specimen thickness of 5.08 cm (2 in). There is a sound absorption comparison of a surface area with 3.90 m² (42 ft.²), and another comparison of a surface area for 6.69 m² (72 ft.²) shown in Figure 21. It is observed that the data for the unsealed edges is greater in absorption relative to its corresponding sealed edge data set. This would be expected due to the relative increase in surface area due to the exposed side surfaces in the test. One notes that the absorption at low frequencies is similar for a test configuration pair (say tests # A15-036 and A15-037) before starting to separate around 800 Hz OTOB. This is believed due to the larger wavelengths at low frequency “not seeing” the edge. However, as the wavelength gets smaller the effect of the foam absorber thickness comes into play and differences begin to appear between the sealed and unsealed configurations. For both of the surface area cases with the 5.08 cm (2 in) thick test specimen, the peak difference occurs at the 1600 Hz OTOB frequency. The wavelength at 1600 Hz is 21 cm (8.4 in), so this peak occurs at a frequency corresponding to a wavelength of 4 times the thickness (i.e. test specimen thickness equals one-quarter wavelength).

Figure 22 shows the Sabine absorption coefficient for the same test specimens as Figure 21. Here the Sound Absorption has been divided by the top surface area and one can observe the similar traits as explained above. As previously described in the Test Objective # 3 section, one can also observe the effect of the surface area on absorption, i.e. smaller surface area test specimens give larger Sabine absorption coefficients.

Another set of sealed versus unsealed test data arose from the cases with the same top surface area of 6.69 m² (72 ft.²), but with two test pairs with different test specimen thickness, 10.16 cm (4 in) and 20.32 cm (8 in). This data is shown in Figures 23 and Figure 24 for the Sound Absorption and
Figure 21. Sound Absorption for Edge Sealing Condition for Same Test Specimen Thickness.

Figure 22. Sabine Absorption Coefficient for Edge Sealing Condition for Same Test Specimen Thickness.
Figure 23. Sound Absorption for Edge Sealing condition for Same Top Surface Area.

Figure 24. Sound Absorption Coefficient for Edge Sealing condition for Same Top Surface Area.
Sabine absorption coefficient, respectively. Again, the increase in absorption for the unsealed cases are readily apparent. As before, it is noted that the sealed and unsealed test pair are similar at the lower frequencies, begin to separate and then reach a peak frequency that approximately corresponds to a wavelength of 4 times the test specimen thickness. This would be ~ 800 Hz for the 10.16 cm (4 in) thick test specimen, and ~ 400 Hz OTOB for the 20.32 cm (8 in) thick test specimen. The effect of increasing thickness improving the absorption at low frequencies, as discussed in Test Objective # 1 section, is again observed in this set of data.

SUPPLEMENTARY DISCUSSION ON SABINE AND EYRING ABSORPTION

In the literature Sabine absorption coefficients greater than 1.0 are usually attributed to the diffraction edge effect, sometimes dismissed outright as measurement errors that should be rounded down to 1.0, or even stated to be “just not possible”. This paper has shown that the Sabine absorption coefficient values can go above 1.0 perhaps due to contributions from size effects and the diffraction edge effects, but is there also another reason?

The values of the Sabin absorption coefficient measured by the reverberant room method can often exceed a value of 1.0. Although this may seem impossible, for how can a material absorb more than 100%, it is indeed a valid measurement. It is a result of the derivation of the Sabin acoustic coefficient, whose values are then often further enlarged by the diffraction edge effect for test specimens with significant thickness and high absorptive properties.

The Sabin acoustic coefficient, a product of the Sabine formula and its several underlying approximations and the Reverberant Room Method, has no limiting value, and would reach infinity for a perfect absorber. It is different from the physical mechanism associated with sound absorption at a local boundary (Crocker 1998), defined (Sollner 2015, Young 1959) as the acoustic Energy Absorption Coefficient, ε, which is defined as the ratio of the energy absorbed by a material to the energy incident on that material, as shown in Equation 8.

\[
\varepsilon = \frac{E_a}{E_i} = \frac{E_i - E_r}{E_i} = 1 - \frac{E_r}{E_i} \tag{8}
\]

Here, \(E_i\) is the total acoustic energy incident on a material, \(E_a\) is the energy absorbed by the material, and \(E_r\) is the total reflected part of that energy. Thus a perfect absorber with no reflected energy would have an Energy Absorption Coefficient of 1.0.

The Sabine absorption coefficient derived from the reverberant room method is not the same as this Energy Absorption Coefficient. Young (1959) and Sollner (2015) have stated that the acoustic Sabine absorption coefficient, α, is related to the Energy Absorption Coefficient, ε, by Equations 9 and 10.

\[
\varepsilon = 1 - e^{-\alpha} \tag{9}
\]

\[
\alpha = -\ln(1 - \varepsilon) \tag{10}
\]

Thus, for a perfect absorber (ε = 1), α will approach \(\infty\). Therefore, when using the reverberant room method to compute Sabine absorption coefficients for highly absorptive materials it would
not be unusual to see values exceeding 1.0, as shown in Table 4. A material would only have to have an Energy Absorption Coefficient greater than 63% for its corresponding Sabine absorption coefficient to exceed 1.0.

### Table 4. Numerical Examples of the Relationship between α and ε.

<table>
<thead>
<tr>
<th>α</th>
<th>0.50</th>
<th>1.00</th>
<th>1.50</th>
<th>2.00</th>
<th>4.61</th>
<th>6.91</th>
<th>∞</th>
</tr>
</thead>
<tbody>
<tr>
<td>ε</td>
<td>0.39</td>
<td>0.63</td>
<td>0.78</td>
<td>0.86</td>
<td>0.99</td>
<td>0.999</td>
<td>1.00</td>
</tr>
</tbody>
</table>

Furthermore, Young (1959) goes on to show that the Equations 9 and 10 are the same equations that relate the Sabine absorption coefficient to the Eyring absorption coefficient given in Equations 11 and 12.

\[
\text{Eyring Absorption Coef.} = 1 - e^{-\text{Sabine Absorption Coef.}} \quad (11)
\]

\[
\text{Sabine Absorption Coef.} = -\ln (1 - \text{Eyring Absorption Coef.}) \quad (12)
\]

Figure 25 provides a graphical representation of the relationship between the Eyring and Sabine absorption coefficients. One can see that these two absorptions closely approximate each other for small absorption coefficient values, before deviating from one another around an absorption coefficient value of ~ 0.35.

The Eyring absorption (and its more accurate reverberation formula) takes into account that the decay of sound is not a continuous process, but is instead a stepwise reduction of sound energy whenever a sound wave is incident on a surface, with reflections and absorptions resulting from that surface interaction (Crocker 1998). Every time the sound wave reflects off a surface its energy is reduced by (1-ε), where ε is the Energy Absorption Coefficient (or Eyring Absorption Coefficient).

Young (1959) proposed that the term “sound absorption coefficient” derived from the Sabine reverberation equation and reverberant room method be clarified to “Sabine coefficient” or “reverberation coefficient”. Similarly, in this current paper, the authors have used the term “Sabine absorption coefficient” for the absorption coefficient derived from the reverberant room method.

Young also proposed that reverberation calculations derived from the simple Sabine equation continue within the industry, and that the tabulation of the Sabine absorption coefficients for materials, especially those intended for reverberation and noise control, continue, but with improved clarification of terms. To the extent of the author’s knowledge, the Sabine absorption coefficients produced by the reverberant room method continues to be the primary source for today’s materials’ absorption database. The heritage, familiarity, and success of this type of absorption database, coupled with the industry’s comfort and preference of having the higher α values (as opposed to reporting and using the lower ε values), are the primary reasons that this continues.

The authors of this paper recommend that: (1) the absorption coefficients produced by the reverberant room method be reported as Sabine absorption coefficients, and continue to be used by the noise control industry, and (2) that the acoustic Energy Absorption Coefficient be recognized as the ratio of the energy absorbed to the energy incident. If it is understood that these
two quantities represent different concepts, then the lingering question of why Sabine absorption coefficients values can exceed a value of 1.0 will be answered.

![Comparison of Eyring and Sabine Absorption Coefficients](image)

**Figure 25. Relationship between Eyring and Sabine Absorption Coefficients.**

**SUMMARY**

The reverberation room method, with its foundation in the Sabine formula, is a very useful method to derive the Sabine absorption coefficient of materials. There is a long and successful history of applying the Sabine absorption coefficient material data to real world problems, even in applications where the environment is not diffuse.

Users of the material absorption database should realize however that the Sabine absorption coefficient is not the same as the acoustic Energy Absorption Coefficient. The Sabine absorption coefficient is a product of using Sabine’s formula and the Reverberant Room Method, and therefore it is not surprising that the Sabine absorption coefficient values may exceed a value of 1.0, especially for highly absorptive materials. The acoustic Energy Absorption Coefficient, defined as the ratio of the energy absorbed by a material to the energy incident on the material, is a coefficient that cannot exceed 1.0. The Energy Absorption Coefficient is recognized to be the Eyring absorption coefficient.

Further contributing to high Sabine acoustic coefficients are the effects of the test specimen surface area size, and the diffraction of sound around the side edges of the test specimen. An absorption
investigative test matrix was designed and a test program was implemented to measure these types of effects, and many of its results are presented in this paper.

Test data was presented that showed that test specimens with smaller surface areas result in larger absorption values (Objective # 1). A method of estimating the true absorption for a test specimen with an infinite surface area was demonstrated using this test data set.

The diffraction edge effects for test specimens of varying thickness was presented (Objective # 3). It was observed that as the test specimen’s thickness increases, the frequency of the peak of the absorption becomes lower in frequency and the overall magnitude of the absorption also increases, especially at the lower frequencies. Part of this increase in due to the thickness of the test specimen itself, however a portion of this increase is also attributable to the diffraction of the sound wave over the edges of the test specimen. The diffraction edge effects are more prominent at lower frequencies.

A comparison of two large atypical test specimens with equal total surface area (top and side surfaces) was presented (Objective # 5). Finally, test data showing the effects of sealing or not sealing the side edges of a test specimen was provided.

The effects of the mounting condition (Test Objective # 2), and the effects of spacing out of the test specimen into pieces with various gaps (Test Objective # 4), will be covered in a follow-on paper to this one.

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