Thermal Signature Identification System (TheSIS)
a Spread Spectrum Temperature Cycling Method

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GOALS
1) Prepare for multivariate modern control loop design using detailed models of device and system dynamics, i.e. “thermal signatures”.
2) Capture the maximum thermal performance information in the minimum time.

KEY FEATURES
1) Measure the thermal signatures of optoelectronic components to direct sequence spread-spectrum temperature cycles,
2) Model the thermal signatures, and
3) Select the most likely model per the Akaike Information Criterion (AIC).
4) Analyze parameter variability and develop multivariate Figures of Merit.

Using the AIC-tested model and parameter vectors from TheSIS, one can analyze changes in model parameters, detect subtle reversible shifts in performance, investigate the cause of instabilities or irreversible changes in component or subsystem performance, e.g. aging, and select high-performing components on a multivariate basis, i.e. with multivariate Figures of Merit (FOM). We show examples of the TheSIS methodology for passive and active components and systems, e.g. fiber Bragg gratings (FBGs) and DFB lasers with coupled temperature control loops.
Applications

- EO Component, Subsystem, and System Evaluation (this talk)
- Electronic Component Evaluation
  - e.g. Oscillators, Crystals, Frequency References
- Reliability/Failure Analysis,
  - e.g. modify Thermal Vacuum (TVAC) cycling profiles to include System Identification (SI) via direct sequence spread spectrum “dither”.
- Efficient Thermal cycling and Control Loop SI Problems
  - e.g. Tuning PID or other control loops -> “plant” models
  - e.g. Polymerase Chain Reaction (PCR) control
Three Perfect Barker Codes

Use for: Short Direct Sequence Spread Spectrum

Barker 3: ++ -
Barker 7: + + + - - + -
Barker 11: + + + - - - + - - + -

Each + or – is a “Chip”

Note: the spectrum of the other perfect code, Barker 2 +-, is not shown
Modified Barker 7 Profile
(7 sub-intervals = “Chips”)

Original = (4 6 7)  
Modified = (3.925 5.875 7)

Baseline chip

Baseline chip
Autocorrelation of Barker 7 and Modified Barker 7

Original = (4 6 7)

Modified = (3.925 5.875 7)
Note: Frequency is from Laser Heterodyne method with the reference laser or LO at a higher frequency than the device under test (DUT). Therefore, as displayed here, a frequency increase corresponds to a redshift of the DFB laser.

\[ T_{\text{chip}} = 1 \text{ minute} \]
A Comparison of Autoregressive Moving Average (ARMA) Models of DFB Laser Dynamics using the Akaike Information Criterion (AIC)

$$e^{-(AIC - AIC_{min})/2}$$

is the likelihood of a given model relative to the most likely model.
Pole and Zeros of \((DFB \, Laser \, + \, Laser \, TEC)\)
Response to Mount TEC set point changes

\((AR1MA8; \, one \, of \, the \, seven \, Zeros \, is \, not \, shown; \, (at \, -3.48))\)

Sampling Period, \(T=4.5 \, \text{seconds}\)
1. False Hysteresis
2. Recursive peak finding algorithm
   \[(\lambda_c, \text{Insertion Loss (dB), Reciprocal Bandwidth Squared})\]
3. Modified Barker 7 Cycling
4. FBG AR3MA2 Poles and “thermality zero” for MA2 models
5. Stability of Poles and “thermality zero”, \(Z_T\)
6. Temperature coefficient of center frequency, \(\alpha\).
7. Contrast conventional vs TheSIS temperature cycling
8. Multivariate selection metric
Center Wavelength Deviation

Relative Wavelength (pm) vs Temperature (deg C)

False hysteresis
**Peak Finding Recursion**

MODEL \[
\text{OPM}(\lambda, H_0, \beta, \lambda_c) := H_0 + \beta \cdot (\lambda - \lambda_c)^2
\]

Parabolic "near" the peak, at \(\lambda_c\), \(\beta\) is negative

\[M_j\] are the measured Optical Power values.

\(J\) is the number of samples per spectrum. \(j = 0 \ldots J-1\)

\(M\) spectra collected at \(T=4.5\) second intervals and interpolated to 4 seconds.

\(H_0\) is insertion loss
\(\beta\) is inverse bandwidth squared parameter
\(\lambda_c\) is center Wavelength

Samples of \(M\) can be collected individually, e.g. via laser heterodyne, and in any order.
Peak Finding Recursion

Performance Function: Find $H$, $\beta$, and $\lambda_c$ (not initial values); After at least one iteration, REPLACE initial values $H_0$, $\beta_0$, and $\lambda_c 0$ values with $H$, $\beta$, $\lambda_c$ below; i.e. the program is recursive and, optionally, iterative.

$$P(H, \beta, \lambda_c) := \sum_j \left[ M_j - \left[ H + \beta \left( \lambda_j - \lambda_c \right)^2 \right] \right]^2$$

$$H := \frac{\sum_j \left[ M_j - \beta_0 \left( \lambda_j - \lambda_c 0 \right)^2 \right]}{J + 1} \quad \text{dBm}$$

$$\beta := \frac{\sum_j \left[ \left( M_j - H_0 \right) \left( \lambda_j - \lambda_c 0 \right)^2 \right]}{\text{dBm/pm}^2}$$

$$\lambda_c := \lambda_c 0 - \frac{\sum_j \left[ M_j - H_0 - \beta_0 \left( \lambda_j - \lambda_c 0 \right)^2 \right] \cdot \beta_0 \cdot \left( \lambda_j - \lambda_c 0 \right)}{\sum_j \left[ 2 \beta_0^2 \left( \lambda_j - \lambda_c 0 \right)^2 - \left[ M_j - H_0 - \beta_0 \left( \lambda_j - \lambda_c 0 \right)^2 \right] \cdot \beta_0 \right]} \quad \text{pm}$$

$H \rightarrow \text{Insertion Loss}$, $\beta \rightarrow \text{Bandwidth}^{-2}$, $\lambda_c \rightarrow \text{Center Wavelength}$

(the zero subscript denotes the value of the previous recursion)
A Barker 7 TheSIS Cycle for Fiber Bragg Gratings (FBG)

Temperature (blue) in deg C. AR3MA2 Model (red)

Typical AR3MA2 Parameter Vector

<table>
<thead>
<tr>
<th>AR3</th>
<th>B1</th>
<th>B2</th>
<th>B3</th>
<th>MA2</th>
<th>A0</th>
<th>A1</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1.52548</td>
<td>-0.26380</td>
<td>-0.26980</td>
<td>0.81490</td>
<td>-0.81700</td>
<td></td>
</tr>
</tbody>
</table>

Deviation: Finish-Start (multiple FBGs)

Retest or fail

Expanded Scale

$T_{\text{chip}} = 6.5$ minutes

$T_{\text{sample}} = 4$ seconds
FBG Poles and Zeros

introducing the “thermality zero”, $Z_T$

Context: $T = 4$ seconds/sample, Modified Barker 7 “dither” sequence, Tspan = $60^\circ$C pp.
Dominant FBG Poles and Thermality zero, $Z_T$ (Detail)

z-plane

$Z_T$

Unit circle
Stability of the FBG AR3MA2 Parameters

Abscissa = #Barker 7 (B7) Thermal Cycles

Thermality Zero, $Z_T$

$\text{Re}(z)$

Cycle #
Stability of the FBG Thermality Zero, $Z_T$

- 44 parts-per-million rms
- 0.016% peak-to-peak
FBG Temperature Coefficient, $\alpha$

\[ \alpha = \frac{\sum_{j=1}^{NMA} A_{j-1}}{1 - \sum_{i=1}^{NAR} B_i} \]

- <3\% variation rms (600 kHz/\(^0\text{C}\))
- <9\% variation peak-to-peak (1.9 MHz/\(^0\text{C}\))
Frequency Response Results

Notes:
1) Mapped z plane to Laplace (s) domain via the bilinear transform
2) There is a 4 milliHz peak (4 minute period) to be aware of.
Example Target specification: A perfectly athermal DUT with a parameter vector comprising a specified center wavelength and bandwidth.

Example DUT response: a DUT with a parameter vector comprising center wavelength, temperature coefficient, and bandwidth.

Figure of Merit (FOM), i.e. the expected performance over the observed range of environmental conditions, e.g. temperature deviations.

Note: \( \sigma_T \) represents a vector of parameters of the measured probability density function of temperature.

Note: the Spec and DUT parameter vectors can include insertion loss (IL); i.e. one can penalize deviations from a (IL) specified value.

Given a specification, optimize FOM as a function of any DUT, thermal parameter, or combinations thereof.
Optimum Temperature Coefficient of Wavelength

Example: Asymmetric Temperature Regulation

Probability density of regulated FBG temperature

FOM Surface
(independent variables = wavelength offset and bandwidth)
Summary

Points & Highlights:

Demonstrated the use of spread spectrum temperature cycling to shorten test time.

Tested models using the AICc and extracted parameter vectors suitable for control loop design.

Introduced the idea of the “thermality zero”.

Presented a recursive algorithm that extracts multiple parameters of passive DUTs.

Showed 30 femtometer rms (1σ) precision in measuring the center wavelength of passive optical components (FBGs).

Showed Model stability across multiple Barker 7 cycles: 2.8% rms cycle-to-cycle variation of thermal coefficient of FBGs (MHz/°C )