FATIGUE LIFE OF POSTBUCKLED STRUCTURES WITH INDENTATION DAMAGE

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Abstract

The fatigue life of composite stiffened panels with indentation damage was investigated experimentally using single stringer compression specimens. Indentation damage was induced on one of the two flanges of each stringer. The experiments were conducted using advanced instrumentation, including digital image correlation, passive thermography, and in-situ ultrasonic scanning. Specimens with initial indentation damage lengths of 32 mm to 56 mm were tested quasi-statically and in fatigue, and the effects of cyclic load amplitude and damage size were studied. A means of comparison of the damage propagation rates and collapse loads based on a stress intensity measure and the Paris law is proposed.

1. Introduction

Composite structures can sustain a high degree of deformation during impact without developing visible cracks, even though the internal substructure is damaged. Thus, the traditional reliance on visual detection to find damage, which worked well for metal skins that dent easily, is inadequate for composite airframes. Therefore, the design and certification of a composite airframe must rely upon a thorough understanding of the strength and life reductions caused by barely visible impact damage (BVID).

The single stringer compression (SSC) specimen was developed by the authors to study the response and the failure of a multi-stringer panel loaded in compression [1, 2]. The SSC specimen represents an intermediate level of complexity between coupon-level specimens and structural components while exhibiting most of the response characteristics of more complex multi-stringer panels. The experimental and numerical advantages of the SSC specimen are the low manufacturing and testing costs and the moderate computational model size requirements, respectively.

The SSC specimen is composed of a skin and a hat-shaped stringer that divides the specimen into two half bays; the dimensions are shown in Fig. 1. The skin consists of an 8-ply quasi-isotropic laminate with a stacking sequence of [45°/90°/-45°/0°]S and a total thickness of 1 mm. The stringer consists of a 7-ply laminate with a symmetric stacking sequence of [-45°/0°/45°/0°/45°/0°/-45°], which results in a total thickness of 0.875 mm. The skin and stringer are co-cured in an autoclave and the material is IM7/8552 prepreg tape.

Carlos G. Dávila, Chiara Bisagni
The test results presented in this paper represent the fourth phase of experimental and analytical investigations to evaluate the effect of defects on the damage tolerance and fatigue life of SSC specimens [2-5]. The first phase of this testing effort, which was conducted in 2009, provided an initial indication of the effect of defect size on the collapse loads of SSC specimens. These test results were also used to validate a shell-based progressive damage finite element model. The second test campaign was performed in 2011 with additional instrumentation that included detailed ultrasonic testing (UT) of the specimens as well as the use of digital image correlation to measure the postbuckling deformations during the test. Fatigue tests were first conducted during the third test phase, which was conducted in 2013, and the instrumentation was expanded to include passive thermography and in-situ UT. The specimens in phases I and II were fabricated at the Politecnico di Milano in two different batches. The specimens for phases III and IV were made in one batch by a well-known aerospace manufacturer of composite structures.

Figure 1. Nominal dimensions of the SSC specimen (in mm).

In contrast with the previous test campaigns, where initial bond defects were introduced by placing a Teflon film between the skin and one of the stringer flanges, the initial damage in the present test campaign (fourth test phase) was induced to the panel by quasi-static indentation. One specimen was subjected to quasi-static loads until collapse, and four specimens were subjected to cyclic loading. The collapse loads of all the specimens tested in phases I through IV are compared in this paper.

2. Indentation Damage

In the present study, damage similar to BVID was induced on the skin side of the panel by quasi-static indentation. The advantages of indentation compared to impact include the simplicity of application, less dependence on boundary conditions, better controllability and repeatability of the imparted damage, and the ability to re-indent at the same location to increase the extent of damage. A hydraulic indenter with a 12.7 mm hemispherical indenter was used.

Five specimens, referred to as SSCS-1 to -5, were tested. The specimens were indented on the skin side at the mid-span of the specimen, as illustrated in Fig. 1. Specimens SSCS-1 and SSCS-5 were indented under the flange termination (edge indent), and the three remaining specimens were indented at the center of the flange. Previous experience using Teflon films as crack initiators [1] indicate that when using rectangular 40-mm-long Teflon inserts, a cyclic load of approximately 80% of the collapse load results in fatigue lives of a few tens of thousands of cycles. With 20-mm Teflon inserts, the cyclic load required for any fatigue damage propagation was found to be too close to the collapse load. Therefore, to avoid fatigue runouts or unintended collapses, a target indentation damage size of approximately 40 mm was selected.

UT images of the induced indentation damage for the five specimens are shown in Fig. 2 with dimensions in mm. The 31-mm damage size initially obtained for specimen SSCS-3 was considered too small for fatigue testing, so it was subsequently re-indented. Upon re-indentation, the damage size extended to 56 mm.

Carlos G. Dávila, Chiara Bisagni
3. Testing Equipment and Instrumentation

Five SSC specimens with indentation damage were tested at the NASA Langley Research Center to study the evolution of damage under quasi-static and cyclic compression loads. A quasi-static test was performed on one of the specimens, and the other four specimens were tested in fatigue by cycling into postbuckling at 2 Hz. The tests were conducted under controlled conditions using a uniaxial test frame, and with instrumentation that allowed a precise evaluation of the postbuckling response and damage. The test frame and the instrumentation used during the tests is shown in Fig. 3. The primary instrumentation for these tests consisted of cameras for digital image correlation, an infrared camera for the passive thermal monitoring, and an in-situ UT scanner. Two back-to-back pairs of strain gauges placed on opposite faces of the skin one inch from the upper loading potting were used to align the upper platen at the start of the test.

![Image](image_url)

**Figure 2.** UT images of damage induced in specimens SSCS-1 to -5 by indenting either at the edge or at the center of the stringer flange.

Digital image correlation was used extensively. Specifically, two three-dimensional digital image correlation (VIC-3D) systems [6] were used to monitor the formation and evolution of the postbuckling deformations and to measure the full-field displacements and strains on the skin and on the stringer sides of the specimen.

Passive thermal monitoring was conducted in real time during the fatigue tests using an infrared camera. Inspection by passive thermography is accomplished without the application of external heat. Instead, the rubbing of matrix cracks and delaminations induces heating that is detectable by the infrared camera. The technique is particularly useful in fatigue because it can track the position of a delamination front during fatigue cycling without stopping the test. The live information from the thermography was used to determine when to stop the fatigue tests at several stages of the damage evolution to allow detailed measurements using a non-immersion in-situ UT scanner [7]. The UT
probe and the UT translation stage were mounted on the load frame and a UT inspection could be performed without removing the specimen from the load frame.

Figure 3. Test frame and instrumentation used to monitor the response and damage propagation.

4. Fatigue Tests

Four SSC specimens were tested in fatigue. These fatigue tests were conducted in stages so that UT scans of the indented area of the panel could be performed at regular intervals. Digital image correlation was used during cyclic loading to monitor the formation and evolution of the postbuckling deformations. Passive thermography and UT were used to track the evolution of damage.

The fatigue test was conducted in stages so that UT of the indented area of the panel could be performed at regular intervals. To illustrate the typical propagation of damage, a sequence of images for SSCS-4 obtained by the UT measurements immediately after indentation and at 12,000, 36,000, and 78,000 cycles are shown in Fig. 4. The images show an extension of the initial skin-stringer separation along the length of the specimen. Collapse of the specimen occurred at cycle 78,135, shortly after the last image was taken.

Figure 4. UT images showing the extent of the damage for specimen SSCS-4 at different cycle counts.

A study was conducted to examine the morphology of the initial indentation damage and to characterize the propagation of the damage under cyclic loading. The scan shown in Fig. 4 for 78,000 cycles was processed and colorized according to “time of flight” to characterize the location through the depth of the various delaminations [7]. The resulting images are shown in Fig. 5, where five cross sections of the skin and stringer flange are examined. The results indicate that the largest delamination
occurs at the +45/-45 interface between the skin and the stringer. Other smaller delaminations are present in the skin at other interfaces closer to the indented surface. It was found that only two delaminations propagate during cyclic loading and that both delaminations propagate together: one interface is at the skin/stringer interface, and the other one is one-ply deep into the stringer flange, at the -45/0 interface.

![Diagram of delamination propagation](image)

**Figure 5.** UT images using “time-of-flight” for location of depth of delaminations.

5. **Comparison of Fatigue Damage Propagation**

The results of the present test campaign are summarized in Table 1. The specimens are grouped according to the location of the indentation: specimens SSCS-1 and -5 were indented at the edge of the flange while specimens SSCS-2, -3, and -4 were indented at the center of the flange. The initial damage length and the length of the damage at different intervals are shown. Specimens SSCS-2 and SSCS-3 were loaded quasi-statically to failure. All of the damage lengths were measured from the UT, except for the last value in the fatigue tests (shown in italic), which was estimated by using the average measured rate of propagation, as described at the end of this section.

One difficulty in performing an exploratory study in fatigue such as this one is that the cyclic loads required for a practical rate of damage propagation is unknown. In the present test campaign, an ideal rate of fatigue damage propagation would result in a collapse of the specimen in 10,000 to 100,000 cycles. However, when considering different damage sizes and other variations between specimens, the ranges of loads that cause collapse and those that cause slow fatigue damage propagation can overlap. Therefore, in several instances, the rate of damage propagation was deemed to be too low and the cyclic load was progressively increased. In the case of specimen SSCS-3, the initial cyclic load was too large and the specimen collapsed during the first loading cycle. Consequently, it becomes difficult to compare the rate of fatigue damage propagation for specimens with different damage sizes, different loads, and possibly different damage morphologies and structural responses. To enable some
means of comparison, the rate of propagation was assumed to depend on a stress intensity measure, $K$, according to the Paris Law:

$$\frac{da}{dN} = C(K)^m = C\left(\sigma\sqrt{a}\right)^m$$ (1)

where $\sigma$ is assumed to be the cyclic load applied to the panel, $a$ is the length of the damage size, and $N$ is the number of cycles. The constants $C$ and $m$ are determined empirically by curve-fitting the experimental results. One set of these constants is assumed for edge indentation, and another for center indentation.

**Table 1. Summary of quasi-static and fatigue test results.**

<table>
<thead>
<tr>
<th>SSCS-1 (Edge)</th>
<th>SSCS-5 (Edge)</th>
<th>SSCS-4 (Center)</th>
<th>SSCS-3 (Center)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cycles $\times 1000$</td>
<td>$a$ (mm)</td>
<td>Load (kN)</td>
<td>Cycles $\times 1000$</td>
</tr>
<tr>
<td>initial</td>
<td>45.0</td>
<td></td>
<td>initial</td>
</tr>
<tr>
<td>12</td>
<td>45.0</td>
<td>29.8</td>
<td>12</td>
</tr>
<tr>
<td>24</td>
<td>45.7</td>
<td>31.1</td>
<td>20</td>
</tr>
<tr>
<td>36</td>
<td>46.7</td>
<td>31.1</td>
<td>30</td>
</tr>
<tr>
<td>48</td>
<td>47.5</td>
<td>31.1</td>
<td>33.623</td>
</tr>
<tr>
<td>$K = 261$</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>60</td>
<td>48.0</td>
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</tr>
<tr>
<td>72</td>
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<td>31.1</td>
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</tr>
<tr>
<td>117.506</td>
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<td>33.8</td>
<td></td>
</tr>
<tr>
<td>$K = 258$</td>
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</tbody>
</table>

The results of the fatigue damage propagation are illustrated in Fig. 6, where the experimental results are represented by the symbols and the lines correspond to the damage lengths calculated with the Paris law. Two sets of parameters $C$ and $m$ were determined by curve fitting: one for edge indentation and a different one for center indentation. The values used are shown in Table 1. As can be observed in Fig. 6, a single set of Paris law parameters provides a good fit to both specimens with edge indentation (SSCS-1 and SSCS-5). This indicates that similar propagation laws characterize the damage growth in both specimens in spite of the differences in initial damage size and cyclic load. It is also apparent that the rate of propagation for center indentation (SSCS-4) is significantly higher than for edge indentation, perhaps because center indentation causes more damage towards the highly loaded web/flange corner than center indentation, as was discussed in Section 2. Specimens SSCS-2 and SSCS-3 were tested quasi-statically.

6. Comparison of Collapse Loads

For any damage size, there is a critical load that causes a collapse of the SSC specimens. It is useful to examine the effect of defect size on the collapse load. The experimental results of the present test campaign are combined with the results of three previous test campaigns in Fig. 7. The tests in phases I and II were exclusively quasi-static, while subsequent ones comprised mixes of quasi-static and fatigue tests. The damage size considered in phases I and II consists of the length of Teflon film (if present) placed between the skin and stringer. In the case of fatigue tests, the defect size consists of an estimate of the damage at the moment of the collapse obtained by adding an incremental extension calculated with the Paris Law to the last measured damage length.
Following the concept used in the previous section, it may be useful to compare the results of different tests according to the stress intensity measure $K = \sigma \sqrt{a}$. Using Fig. 7, it can be observed that the edge indent specimens collapsed at approximately $K = 260 \text{kN} \times \text{mm}^{0.5}$. The center indent specimens failed at $196 \leq K \leq 237 \text{kN} \times \text{mm}^{0.5}$. Other specimens failed at lower values of $K$, which is not surprising considering, for instance, the effect of the postbuckling mode on the collapse load [4, 5, 8]. In particular, one specimen from phase III with a 20-mm Teflon insert failed at $K = 130 \text{kN} \times \text{mm}^{0.5}$, apparently due to a sudden snap-through mode change of the flange at the Teflon insert. Nevertheless, a classification of specimens according to their stress intensity measure provides a useful means to assess different aspects of the response on the damage tolerance of stiffened structures with defects.

7. Summary

A series of static and fatigue tests were performed on single stringer compression specimens. Five specimens were manufactured with a co-cured hat-stringer, and an initial defect was introduced at the
specimen mid-length of the stringer flange by indentation. One of the specimens was tested under quasi-static compressive loading, while the remaining four specimens were tested by cycling in postbuckling. The tests were conducted under controlled conditions and the specimens were monitored throughout the loading with multiple in-situ non-destructive evaluation (NDE) methods to obtain detailed information on deformation response characteristics and damage evolution. Three-dimensional digital image correlation was used to obtain full-field displacement measurements, and in-situ passive thermography and UT were used to track damage evolution.

Using passive thermography with an infrared camera, it was possible to monitor the growth of the initial delamination damage while the specimens were being cycled. The real-time information from the thermography was used to determine stopping points along the fatigue tests to ensure that critical stages of the damage evolution were then recorded with UT scans.

To enable a comparison between different tests, a procedure was proposed based on the concept of a stress intensity measure, which is the product of the applied load and the square root of the damage size. The stress intensity measure provides the means to compare the collapse loads of specimens with different damage types and damage sizes. In addition, the stress intensity measure was applied in a Paris law to compare the damage propagation rates in specimens loaded with different cyclic loads. The empirical measures applied are not intended for use as prediction tools for damage tolerance and fatigue life because they do not account for a number of factors such as the location of the damage, the postbuckling deformation, or the shape of the damage. However, the approach does enable a comparison of different tests and the potential identification of effects that influence the fatigue lives and damage tolerance of postbuckled structures with defects.

References