The purpose of this article is to explain why the extension of the previously published $C = (S/H_o)\sqrt{J}$ scaling for opposed rows of staggered jets wasn't directly successful in the study by Choi et al. (2016). It is not surprising that staggered jets from opposite sides do not pass each other at the expected value, because $H_o/D$ and $\sqrt{J}$ are much larger than the maximum in previous studies. These, and large $x/D$'s, tend to suggest development of 2-dimensional flow.

Although there are distinct optima for opposed rows of in-line jets, single-side injection, and opposed rows of staggered jets based on $C$, opposed rows of staggered jets provide as good or better mixing performance, at any $C$ value, than opposed rows of in-line jets or jets from single-side injection.

The purpose of this article is to investigate why the extension of the $C = (S/H_o)\sqrt{J}$ scaling in Ref. [1] wasn’t quantitatively successful for the application that motivated Ref. [2].

From the experimental results in Ref. [1], it is apparent that midplane values approach centerplane values (the mean flow becomes more 2-dimensional) as the momentum-flux ratio, $J$, and the dimensionless downstream distance, $x/D = (x/H_o)(H_o/D)$, increase.

2. History and previous usage of the NASA empirical model for confined JIC's

The effect of high momentum-flux ratio and small orifice size can be shown for conditions similar to those in Ref. [2] using the NASA JIC empirical model. This model was used in Refs. [3,4] to represent data obtained in the 1970s and 1980s. The original Applesoft® BASIC code (in Appendixes A and B of Ref. [5]) was subsequently rendered in an Excel® spreadsheet (unchanged – except for correction of known errors) in Refs. [5–8] using the correlation equations in Appendix C of Ref. [5]. (These correlations are the same as those in Ref. [1], but with the curvature effect equations in Ref. [1] deleted). The NASA JIC spreadsheet was also used in...
### Nomenclature

- \( C \) (orifice discharge coefficient = (effective area)/(physical area))
- \( C_d \) orifice discharge coefficient
- \( D \) actual orifice diameter
- \( DR \) jet-to-mainstream density ratio, \( \rho_j/\rho_m \) (for an incompressible flow, and for gases of the same chemical composition, this ratio is approximately equal to the mainstream-to-jet temperature ratio, \( T_m/T_j \))
- \( H_o \) duct height at center of row of holes (called \( H \) in several previous publications)
- \( J \) jet-to-mainstream momentum-flux ratio
- \( MR \) jet-to-mainstream mass-flow ratio
- \( S \) lateral spacing between equivalent locations of adjacent orifices, e.g. between orifice centerplanes
- \( S/D \) ratio of orifice spacing to orifice diameter
- \( T \) local scalar variable
- \( T_j \) jet exit scalar variable
- \( T_m \) unmixed mainstream scalar variable
- \( U_m \) velocity of unmixed mainstream
- \( V_j \) jet exit velocity
- \( x \) downstream coordinate; \( x = 0 \) at center of the row of orifices
- \( y \) cross-stream coordinate
- \( y_c/H_o \) scalar trajectory = location of maximum scalar difference ratio in centerplane, \( y_c \)
- \( z \) lateral coordinate; \( z = 0 \) at centerplane
- \( \theta \) \( (T_m - T_j)/(T_m - T) \)
- \( \theta_c \) maximum scalar difference ratio, defines location of scalar trajectory, \( y_c/H_o \)

### 3. Results

Profile and contour plots from the NASA JIC spreadsheet are shown in Figs. 1–7 for the conditions in Table 1 in the present communication. The conditions for Figs. 3–6 are the same as those in Table 1 in Ref. [2].

The parameter shown in the profile and contour plots is \( \theta = (T - T_j)/(T_m - T_j) \), where \( T_m \) is the mainstream temperature, \( T_j \) is the jet temperature, and \( T \) is the local temperature. Note that \( \theta = 1 \) for pure jet fluid, \( \theta = 0 \) for pure mainstream fluid, and \( \theta = MR/(MR + 1) \) at the fully mixed condition. Although temperature is used here, any conserved scalar is acceptable.

The profile and contour plots in this paper always cover a span of two orifices on each side. Thus, the physical distance shown will vary with orifice spacing.

The conditions for \( C = 1.3 \) in Fig. 1 (column 1) represent an optimum mixer for opposed rows of aligned jets. The results shown in Fig. 1 suggest that the flow becomes 2-dimensional very quickly, which is not surprising given the high \( J \), high \( x/D \), small orifice size, and small orifice spacing.

Nonetheless, the results in Fig. 1 agree with the \( C = (S/H_o)\sqrt{f} \) scaling in Ref. [1]. Although the jets on top and bottom are aligned, results for in-line and staggered jets are indistinguishable for high \( C \) values at the \( C \) value that is optimum for opposed rows of in-line jets.

The conditions in column 2 for \( C = 2.6 \) are nearly optimum for one-side injection, and have been changed from the staggered case in Ref. [2] to one-side injection at the jet-to-mainstream mass-flow ratio used in Ref. [2]. Note that the diameter of the orifices is double that for each row of the single-side jets in column 2 (and Fig. 2) because there are only half as many orifices per row and only half as many rows in the single-side configuration in column 2.

The one-side injection in Fig. 2 is also in approximate agreement with the \( C \) scaling in Ref. [1], but note that the jet penetration also depends significantly on downstream distance.

The results in Fig. 2 are very similar to the results for the upper jets in Fig. 1 when the \( x/H_o \) for single-side injection (Fig. 2) is twice that in opposed rows of in-line jets (Fig. 1) since the “effective” mixing height for opposed rows of in-line jets is \( H_o/2 \). Thus, better mixing is obtained at a specified downstream distance (\( x/H_o \)) with opposed rows of jets.

The results for staggered jets at \( C = 2.6, 3.5, 5.7 \) and 9.4 shown in Figs. 3–6 essentially agree with the results in Ref. [2].

Fig. 3 has the same \( C \) value as Fig. 2 (\( C = 2.6 \)), but the configuration in Fig. 3 is opposed rows of staggered jets. Note that the orifices are smaller than for single-side injection since there are twice as many rows, but the orifice spacing (\( S/H_o \) and \( MR \) are the same.

### Table 1

Parameters for cases calculated with the NASA JIC spreadsheet.

<table>
<thead>
<tr>
<th>C</th>
<th>1.3</th>
<th>2.6</th>
<th>2.6</th>
<th>3.5</th>
<th>5.7</th>
<th>9.4</th>
<th>18.8</th>
</tr>
</thead>
<tbody>
<tr>
<td>DR</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
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<tr>
<td>J</td>
<td>800</td>
<td>800</td>
<td>800</td>
<td>800</td>
<td>800</td>
<td>800</td>
<td>800</td>
</tr>
<tr>
<td>H_o/D</td>
<td>70.6</td>
<td>35.3</td>
<td>49.9</td>
<td>42.4</td>
<td>32.8</td>
<td>24.4</td>
<td>17.3</td>
</tr>
<tr>
<td>S/H_o</td>
<td>0.045</td>
<td>0.091</td>
<td>0.091</td>
<td>0.125</td>
<td>0.200</td>
<td>0.333</td>
<td>0.667</td>
</tr>
<tr>
<td>C_d</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>S/D</td>
<td>3.2</td>
<td>3.2</td>
<td>4.5</td>
<td>5.4</td>
<td>6.6</td>
<td>8.2</td>
<td>11.5</td>
</tr>
<tr>
<td>D/H_o</td>
<td>0.014</td>
<td>0.028</td>
<td>0.024</td>
<td>0.031</td>
<td>0.041</td>
<td>0.058</td>
<td></td>
</tr>
</tbody>
</table>
Fig. 3 shows equivalent mixing to that in Fig. 2 at the $C$ value that is optimum for single-side injection. However, opposed rows of staggered jets fill in the gaps, and are less sensitive to variations in downstream distance.

The profiles and contours in Figs. 4 and 5 show that the jets from opposite sides do not pass each other. Although optimum penetration for opposed rows of staggered jets was expected for $C = 5.7$ (Fig. 5), this probably does not occur because the high $J$ and $H_0/D$ values promote jet interaction and 2-dimensional flow.

The profiles and contours for $C = 9.4$ in Fig. 6 suggest that the jets from opposite sides are trying to pass, as the initial profiles are similar to the initial ones in sequence 18 in the slideshow in the

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**Fig. 1.** Profile and contour plots from NASA JIC Excel® spreadsheet for opposed rows of in-line jets at $C = 1.3$: $DR = 1$, $J = 800$, $H_0/D = 70.6$, $S/H_0 = 0.045$ ($S/D = 3.2$), and $C_d = 1$. 
However, further penetration is masked by 2-dimensional flow. However, the mixing is quite uniform at $x/H_0 = 0.5$.

The conditions for $C = 18.8$ in column (and Fig. 7) are not possible in the facility used in Ref. [2], but are included here to show what might be expected for a further increase in $C$. Here...
$S/H_o = 0.667$ which seems acceptable, but it is unlikely that a jet would spread laterally more than in the direction of jet penetration so care must be taken to insure that $S/H_o \leq 1$.

Fig. 7 shows jets from opposite sides that pass each other, as shown in Fig. 12 of Ref. [7] and Fig. 7 of Ref. [9]. Apparently the high momentum-flux ratio jets are finally spaced far enough apart.
Fig. 4. Profile and contour plots from NASA JIC Excel® spreadsheet for opposed rows of staggered jets at $C = 3.5; \ DR = 1; J = 800, H_o/D = 42.8, S/H_o = 0.125 (S/D = 5.4), \text{ and } C_d = 1.
that jets from opposite sides can pass each other without interacting. Distributions from the JIC spreadsheet are not shown farther downstream than $x/H_o = 0.1$ as the jet trajectory exceeds $H_o$, and significant mass is “lost” (i.e. the profiles are truncated).

Although calculating $S/D = (S/H_o)(H_o/D)$ is straightforward, $S/D$ values are included in Table 1 and the titles of Figs. 1–7 as they highlight the importance of $S/D$ spacing.

No matter what the application is, the absolute minimum spacing that allows staggered jets from opposite sides to pass each other.
is $S/D = 2$, provided that the opposed rows are perfectly staggered and the jets do not diffuse as they proceed downstream. Of course, this won’t happen, and the minimum $S/D$ will increase as $J$ increases.
In the application that motivated Ref. [2], the optimum $S/D$ for opposed rows of staggered jets appears to be approximately $S/D = 10$. Thus, $C = ([S/D]/[H_0/D]) \sqrt{J}$ for $J = 800$; if $H_0/D = 20$, then $C \approx 15$. Note that in Fig. 7 of Ref. [9], $S/D = 8$, $H_0/D = 8$, and $J = 26.4$, so $C = 5.14$, but if $J$ were 800, $C$ would be 28.3 for $S/H_0 = 1$.

4. In Conclusion

Since $H_0/D$ and $\sqrt{J}$ are approximately both 3 times larger than the maximum in previous studies, and these, and large $x/D$'s show 2-dimensional flow, it is not surprising that staggered jets from opposite sides do not pass each other at the expected $C$ value.

There are distinct optima for opposed rows of in-line jets, single-side injection, and opposed rows of staggered jets based on $C$. However, opposed rows of staggered jets provide as good or better mixing performance as opposed rows of in-line jets or jets from single-side injection at any $C$ value.

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Fig. 7. Profile and contour plots from NASA JIC Excel® spreadsheet for opposed rows of staggered jets at $C = 18.8$: $DR = 1, J = 800, H_0/D = 17.3, S/H_0 = 0.667 (S/D = 11.5)$, and $C_2 = 1$. 

(a) $x/H_0=0.029$ $(x/D=0.5)$
(b) $x/H_0=0.05$ $(x/D=0.87)$
(c) $x/H_0=0.1$ $(x/D=1.73)$
References


