Molecular-Based Optical Diagnostics for Hypersonic Nonequilibrium Flows

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“Paul, Why are you doing this special session?”

• Multi-purpose:
  – Educate those new to field of laser based measurements (students)
  – Let collaborators from other fields know what is possible to measure
  – Provide some updates and ideas for those already working in measurement technology

• Special session is coordinated with the launch of a new AIAA Progress Series Book
  – Pedagogical treatment
  – Came out of a Fluids TC Working group led by E. Josyula
  – Our chapter: Molecular-Based Optical Diagnostics for Hypersonic Nonequilibrium Flows
Hypersonic Nonequilibrium Flows: Fundamentals and Recent Advances

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About the Book

The high-temperature environment poses an unusual challenge in understanding the basic physics of hypersonic flight. A lack of such understanding can lead to risks and uncertainties in the design of aerospace vehicles. *Hypersonic Nonequilibrium Flows* documents recent, unprecedented scientific advances in the field of nonequilibrium processes for aerospace applications. These advances have been driven primarily by interest in space access and exploration, or in developing military technologies involving hypersonic flight regimes.

In the modeling of hypersonic flows, the last decade has witnessed a reexamination of fundamental principles of kinetic theory and quantum chemistry to describe the kinetic and thermal states, respectively, of the individual gas particles. Modern aerospace programs where nonequilibrium energy transfer processes play a major role may broadly be categorized as exo- and endo-atmospheric. The exo-atmospheric flight programs consist of Earth and planetary reentry programs, as well as access to space programs for applications that include space exploration, flight experiments and demonstrations, missile defense, and the nascent space tourism industry. The endo-atmospheric flight programs are primarily motivated by hypersonic military applications requiring high-precision engagement for tactical, theater and strategic defense, as well as applications involving intelligence, surveillance, and reconnaissance.

The nonequilibrium processes considered in this volume are generally associated with flight Mach numbers between 7 and 25, where the shock-layer temperatures range from 3000 to 25,000 K.

*Hypersonic Nonequilibrium Flows* includes fundamental governing equations of nonequilibrium fluid transport and computational approach to calculation of rates and cross-sections in quantized energy states; DSMC approach; radiative heat transfer; a CFD perspective; surface chemistry, with additional chapters on high enthalpy facilities and the associated diagnostic techniques.
Hypersonic Nonequilibrium Flows: Fundamentals and Recent Advances
Edited by Eswar Josyula

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Introduction and Application Considerations for Optical Diagnostics in Hypersonic Nonequilibrium Flows

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Introduction and Application Considerations for Optical Diagnostics in Hypersonic Nonequilibrium Flows

- Temperature, equilibrium and nonequilibrium
- Characteristics of hypersonic nonequilibrium flow
  - What needs measuring?
- Advantages of spectroscopic measurement
- Aspects of a good measurement technique
- Choosing which measurement technique to use.
Temperature and Equilibrium

• Temperature
  – Classical thermodynamics
    • Heat flowing from object A to B $\rightarrow T_A > T_B$
  – Statistical thermodynamics
    • Describe by Boltzmann distribution
    • e.g. Maxwellian Velocity Distribution
      width $\sim \sqrt{T}$

• Equilibrium
  – Classical thermodynamics
    • Thermal equilibrium: $T_A = T_B$
  – Statistical thermodynamics
    • One temperature can describe all the different energy modes (via Boltzmann)
  – Chemical equilibrium:
    • Reactants and product concentrations don’t further change with time
Energy Modes

- Translation
- Rotation
- Vibration
- Electronic

These can all be described by a temperature:

- $T_{\text{trans}}$, $T_{\text{rot}}$, $T_{\text{vib}}$, $T_{\text{elec}}$

- Thermal equilibrium: these $T$’s are all equal
Nonequilibrium

• Thermal Nonequilibrium:
  – Different energy modes described by different $T$’s
    • e.g.: $T_{rot} \neq T_{vib}$
  – Or, the distribution of population can’t be described by Maxwell-Boltzmann statistics (“non-thermal” distribution)

• Chemical Nonequilibrium:
  – Products and reactants are in a state of change
  – If held at those conditions ($P$, $T$) the composition will change.

• Equilibrium occurs via \textit{collisions}
Hypersonic Flows and Noneq.

• Hypersonic vehicles fly at high altitude (low $P$) and high speed ($M > 5$) resulting in gas and vehicle heating (high $T$)
  – Collisions rate scales as $P/\sqrt{T}$
  – *Low collision rate causes nonequilibrium*
  – At STP for $O_2$: Trans: 10; Rot: 10; Vib: 20,000; Dissoc: 200,000 collisions to equilibrate!
    • 10 coll. ~ 1 ns; 20,000 coll. ~ 2 μs at STP

• Hypersonic flows are also characterized by:
  – Steep gradients (shocks, boundary layers, expansions)
  – Combustion (in scramjets)
  – Dissociation / recombination
Some Hypersonic Nonequilibrium Flows

• Shock wave:

\[ T_{\text{trans}} = T_{\text{rot}} = T_{\text{vib}} \]

thermal equilibrium

\[ T_{\text{trans}} = T_{\text{rot}} = T_{\text{vib}} \]

thermal non-equilibrium

• Expansion:

\[ T_{\text{trans}} = T_{\text{rot}} = T_{\text{vib}} \]

thermal, chemical equilibrium

Low \( P, T \), High \( V, M \)

thermal, chemical non-equilibrium

• We can measure, quantify these!
Parameters to measure

• Typical parameters of interest in Hypersonic Nonequilibrium Flows:
  – Velocity, Pressure, Density, Temperatures, Species
    • Non-thermal population distributions
  – How is energy in flow partitioned in terms of:
    • thermal energy \((T)\)
    • chemical energy \((\text{species})\) and
    • kinetic energy \((V)\)?

(O and N atom LIF at NASA ARC)
Some advantages of Spectroscopic Measurement Techniques

• Non-intrusive
  – No probes, particles perturb the flow

• Remote detection
  – Can be used in hostile environments

• Can measure multiple parameters, states:
  – Sometimes simultaneously
  – Can be instantaneous (<10 ns) and high freq. (MHz)
  – Can be precise, accurate, high spatial res. (2D, 3D)

• But...
  No one measurement technique can meet all requirements
  – Can have more complicated theory, expensive and complex equipment, more difficult data analysis
  – May require seeding of (sometimes toxic) gases, more expertise, slower data acquisition, analysis
Scope of the Content

• Content focuses on molecular based, quantitative, mostly spectroscopic measurement techniques previously applied in or *may be applicable to* non-equilibrium flows. Many examples in equilibrium.
  – Content of lectures and manuscript are not exhaustive. Not all the ‘first’ or ‘most important’ references are given. Instead they there is an emphasis on describing how the techniques work and how they can be used to measure.
  – Also there is an admitted bias towards the authors’ own work.

• *Content excludes the many relevant particle-based* (PIV, LDV), *probe-based and surface-based measurement techniques that could be used to study non-equilibrium flows; mostly no ‘flow vis’. (No schlieren.*)*
What makes a good measurement technique?

• A reliable measurement system matched with well-understood physics to make a quantified measurement that meets a customer’s requirements.

Explore each of these...
Typical Measurement System

- Need to understand equipment and physics of process to make a measurement
  - Emission, Abs., LIF, Rayleigh, Raman, CARS, etc.
Measurement System: Lasers

- **Lasers**: pulsed vs. continuous wave (cw)
  - Continuous wave: lower power (mW to Watt)
  - Pulsed:
    - 10 ns, picosecond, femtosecond all commercially available
    - ‘Freeze’ the flow
    - Much higher power vs cw (MWatt-GWatt, even TWatt)
    - Frequency conversion (useful in linear techniques such as Raman, Rayleigh, LIF)
    - Provide high powers for nonlinear techniques (CARS)
    - Repetition rate: 10-100 Hz, 16 kHz, 1 MHz, 80 MHz...

- **What colors of laser light do we need?**
• Many different colors can be useful for spectroscopy
• As energy increases, more modes can be excited
  – LIF: can see electronic, vibrational and rotational structure
Measurement System 2

• **Detectors:**
  – Single point detectors:
    Photomultiplier tubes (PMT) and photodiodes
  – Camera technology is rapidly evolving:
    • CCDs provide ‘scientific grade’ (low noise, linear, etc.)
    • CMOS cameras are faster
    • Commercially available cameras at up to 10’s, 100’s of kHz steady streaming or MHz for short bursts or few pix
  – Fiber optics and fiber-optic bundles often used for either transmitting laser or collecting signal

• **Processing:**
  – Some data processing codes are available (CARSFT, LIFBASE) but many are proprietary.
What makes a good measurement technique?

• A reliable measurement system matched with well-understood physics to make a quantified measurement that meets a customer’s requirements.

Explore each of these...
Quantified Measurements

• Accuracy and precision of a measurement must be quantified to be useful, for example when comparing to a code
  – Qualitative measurements (flow vis) can be useful

• Quantified measurement:
  – Accuracy and precision are well characterized

  – Accuracy: compared to a ‘standard’ or ‘accepted’
  – Precision: $1\sigma$ of large sample of measurements
    • Averaging reduces precision’s contribution to uncertainty
    • High precision required to quantify fluctuations (turbulence)

(from Wikipedia, “accuracy and precision”)

Accurate but not precise

Precise but not accurate
Customer Requirements

Interview the customer... (sometime the customer is you!)

- Simultaneous measurements to obtain correlations: T’u’, ρu’v’
- Time resolution (< μsec), and frequency response (> MHz)
- Spatial resolution: near walls; smallest scales in shear layer
- Where are the measurement to be made?
  - Inflow to establish B.C., exit, near walls?
  - Point, line, plane, volume?
- Accuracy and precision requirement?
- What quantity of data is required? Uncertainty required?
- When is the data needed? Is “real-time” data required?
- What type of optical access is available?
- Can (toxic) seed gases be introduced? Will they influence the properties being measured? Can particles be used?
- What is the ordered priority of the above requirements?
What makes a good measurement technique?

- A reliable **measurement system** matched with **well-understood physics** to make a **quantified measurement** that meets a **customer’s requirements**.

- Now the lectures will focus on different measurement systems, introducing the physics.
  - How’s the basic physics of the method work?
  - Can the measurements be made instantaneously (aka. single-shot) at high frequencies?
  - What accuracy and precision can be obtained?
Customer Requirements

• Consider a customer with arbitrary measurement requirements:
  – Would like a particular parameter measured
  – Would like the measurement at some conditions \((P, T)\)
    • Many measurement technique signals scale as \(P_{\text{static}} T_{\text{static}}\)

• Parameters to be measured:
  – Velocity, temperature, density, pressure, species
    (concentration or mole fraction)

• Can base choice of measurement technique (in part) on prior success by others:
  – We compiled past work into graphics that show static pressure and temperature of demonstrated measurements
  – Use these charts to find appropriate measurement methods
Backup Charts
Explanation of Parameter Charts

Overview:
This appendix shows the static conditions (temperature and pressure) at which various measurement techniques have been successfully demonstrated. When planning a new experiment to occur at a specified temperature and pressure, these graphs might be useful to see what measurements have previously been demonstrated at those conditions. The numerals used as data points indicate the reference in the attached reference list. The different measurement techniques are denoted by the colors indicated. Pressure is plotted on a logarithmic axis while temperature is on a linear axis.

Caveats:
• The data includes both references contained in the manuscript as well as additional works.
• The reference numbers in the manuscript are different from those in this appendix.
• This study is not meant to be exhaustive; it provides a partial sampling of the data available in the literature.
• Some data points overlap. This is particularly true at room temperature and atmospheric pressure. Some data has been omitted to avoid overlaps.
• For temperatures greater than 3500 K, the reference number is plotted to the right of the chart with the static temperature in parentheses.
• “Species” includes either species concentrations or species mole fraction measurements.

(Not included in AIAA Progress Series manuscript)

Temperature

![Temperature Diagram]
Velocity

Temperature vs. Pressure Diagram

- Emission
- Absorption
- Fluorescence
- Rayleigh
- Raman
- CARS
- Holography

Points: 3, 2, 2, 3, 10, 23
Pressures: 33, 33, 34, 19, 19, 39
Temperatures: 11, 11, 21 (12000 K)
Density

![Graph showing the relationship between pressure and temperature, with various points and labels indicating different methods of measurement such as Emission, Absorption, Fluorescence, Rayleigh, Raman, CARS, and Holography.](image-url)
Species
References


Intro to Optical Emission Spectroscopy for Hypersonic Nonequilibrium Flows

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PICA at NASA Ames (SPRITE)

Shot 35 (Blue) - 8.53 km/s, 0.098 torr

EAST shock tube (NASA Ames)
Outline:

• Introduction to emission spectroscopy
• Excitation of Atoms and Molecules (electronic, vibrational, rotational)
• Line broadening
• Spatial resolution
• Application examples of emission spectroscopy
Applications of emission spectroscopy

- **Astronomy !!!** - composition and velocity of celestial bodies
- **Diagnostics for gases at high temperatures**
  - re-entry (ground test and flight)
  - electric propulsion characterization
  - plasma processing (coating, edging, ...)
  - combustion (though temperatures might be too low)
  - material analysis (laser ablation of surface material → radiation)
- **Radiation transport in gases at high temperatures**
  - re-entry radiation heat flux to the spacecraft (ground test and flight)
  - radiation transport within the flow field (source term in energy equation)
    → particular importance of VUV radiation

Goals:
- **Identification of elements**
- **Radiation heat flux determination**
- **Temperature determination**
  - ratios of atomic lines (**electronic** excitation temperature)
  - rotational and vibrational temperature of molecules
    (line ratios or comparison with spectral simulation)
  - translational temperature from line broadening (Doppler effect)
  - glowing surfaces (Planck blackbody radiation)
- **Chemical composition (usually under equilibrium conditions)**
Each particle in a gas has a specific undirected velocity and, therefore, a kinetic energy.

Definition of translational temperature: for the sum of all particles, a statistic distribution function can be formulated (Maxwellian velocity distribution):

\[
f(v) = \frac{dN}{N} = \frac{4}{\sqrt{\pi}} \left( \frac{1}{2RT} \right)^{\frac{3}{2}} e^{-\frac{v^2}{2RT}} dv
\]

Similar distribution functions can be formulated for other energies such as vibrational, rotational and electronic excitation (i.e. Boltzmann distributions).

Energy is constantly exchanged through collisions.

Electrons are lighter and more movable than heavy particles \(\rightarrow\) more collisons possible \(\rightarrow\) possibly different energy distribution \(\rightarrow\) distinctive temperature.

For each form of energy, a temperature can be defined which controls the corresponding energy distribution \( (T_{\text{vib}}, T_{\text{rot}}, T_{\text{elec}}, \ldots) \).

For many plasmas, the distribution parameters (i.e. temperatures) might all be different \(\rightarrow\) \( T_{\text{trans}} \neq T_{\text{el}} \neq T_{\text{rot}} \neq T_{\text{vib}} \rightarrow\) non-equilibrium.
Emission of Atoms and Molecules

- **Line position**
- **Line strength/intensity**
- **Line shape**

from $\Delta E = E_{\text{upper}} - E_{\text{lower}} = h \nu$, 
$\Rightarrow \nu$ or $\lambda$ for known energy levels

valid in general (atoms and molecules)

$$\varepsilon_{21} = \frac{h\nu}{4\pi} A_{21} n_2$$

one photon/transition 
$\Rightarrow$ depends on energy difference

In equilibrium, the density $n_k$ is related to $n$ through the Boltzmann distribution:
Emission of Atoms: Electronic Excitation

- Line position
- Line strength/intensity
- Line shape

from $\Delta E = E_{\text{upper}} - E_{\text{lower}} = h\nu$, 
$\to \nu$ or $\lambda$ for known energy levels
valid in general (atoms and molecules)

$\varepsilon = \frac{h\nu}{4\pi} A_{ki} n_k$

Population density of the excited state $k$

$n_k = \frac{g_k}{U(T_{ex})} n_0 \exp\left(-\frac{E_k}{kT_{ex}}\right)$

Partition function

$U(T_{ex}) = \sum_i g_i \exp\left(-\frac{E_i}{kT_{ex}}\right)$

Total density of the species under consideration

In equilibrium, the density $n_k$ is related to $n$ through the Boltzmann distribution:
Emission of Atoms: Electronic Excitation

- Line position
- Line strength/intensity
- Line shape

from $\Delta E = E_{\text{upper}} - E_{\text{lower}} = h \nu$,
$\rightarrow \nu$ or $\lambda$ for known energy levels

valid in general (atoms and molecules)

$$\varepsilon = \frac{h \nu}{4 \pi} A_{ki} n_k$$

$$= \frac{h \nu}{4 \pi} A_{ki} \frac{g_k}{U(T_{ex})} n_0 \exp \left( - \frac{E_k}{kT_{ex}} \right)$$

for electronic excitation in equilibrium

In equilibrium, the density $n_k$ is related to $n$ through the Boltzmann distribution:

information on the transition (from quantum mechanics, e.g. from tables)

information about the thermodynamic condition of the plasma
Theoretically, the ratio of two lines would be sufficient to determine the excitation temperature, but it is often in doubt if the electronic excitation is in equilibrium.

\[
\ln \left( \frac{I_{ki}}{\nu A_{ki} g_k} \right) + \text{const} = -\frac{E_k}{kT_{ex}}
\]

→ Plot \( \ln \left( \frac{I_{ki}}{\nu A_{ki} g_k} \right) \) vs \( E_k \) → straight line with slope \( 1/-kT \) (Boltzmann Plot)

If points are indeed on a straight line → Boltzmann valid → \( T \) can be determined

BUT: Even if Boltzmann seems valid, the apparent excitation temperature might not be an equilibrium temperature:
Theoretically, the ratio of two lines would be sufficient to determine the excitation temperature, but it is often in doubt if the electronic excitation is in equilibrium.

\[
\ln \left( \frac{I_{ki}}{A_{ki} g_k} \right) + \text{const} = -\frac{E_k}{kT_{ex}} 
\]

\[\Rightarrow \text{Plot } \ln \left( \frac{I_{ki}}{A_{ki} g_k} \right) \text{ vs } E_k \Rightarrow \text{straight line with slope } 1/-kT \text{ (Boltzmann Plot)}
\]

If points are indeed on a straight line \(\Rightarrow\) Boltzmann valid \(\Rightarrow\) \(T\) can be determined

BUT: Even if Boltzmann seems valid, the apparent excitation temperature might not be an equilibrium temperature:

**Recombining plasma**
- high energy states will be populated through recombining ions
  \(\Rightarrow\) flat distribution
  \(\Rightarrow\) high excitation temperature

**Ionizing plasma**
- high energy states will be depopulated through ionizing neutrals
  \(\Rightarrow\) steep distribution
  \(\Rightarrow\) low excitation temperature
Emission from Molecules

Molecule emission shows some shape but looks like a continuum

- Ratio of the different vibrational systems governed by $T_{\text{vib}}$
- Ratio within one vibrational transition (e.g. $0-0 \rightarrow V_u=0, V_l=0$) governed by $T_{\text{rot}}$

High spectral resolution → Single lines like atoms but more ...

→ rotation and vibration

Emission from Molecules

Radiation of molecules is caused by changes of the electronic level, the vibrational level, and the rotational level of excitation, often simultaneously.

\[ \tilde{\nu} = \frac{1}{hc} \left( \Delta E_{el} + \Delta E_{vib} + \Delta E_{rot} \right) \]

Born-Oppenheimer approximation: The total energy is the sum of the different excitations which can be computed separately.

Electronic excitation works similar to the atoms ...
Emission from Molecules

• For diatomic molecules, **rotation** and only **one vibrational mode** need to be accounted for.
• Already for tri-atomic molecules, several vibrational modes are possible.

- **Diatomic molecules**

  - Rotation and vibration energies are discrete and not continuous and are obtained from solutions of the Schrödinger equation.
  - For diatomic molecules, each energy is characterized through one quantum number (J for rotation, V for vibration).
  - In addition, molecules may be electronically excited (same process as for atoms).

- **Linear triatomic molecules**
  - Symmetric stretch mode
  - Asymmetric stretch mode

- **Triatomic molecules**
  - Different modes for linear and non-linear molecules
  - Symmetric stretch
  - Asymmetric stretch

Main vibrations occurring in liquid water
(http://www1.lsbu.ac.uk/water/water_vibrational_spectrum.html)
Each electronic level of a molecule is described by a potential curve in terms of energy vs. internuclear distance.

Different vibrational energies appear as lines of constant energy on these potentials.

Excitation of the levels can happen through collisions (one major partner are electrons) or absorption of radiation.

From one upper level, transitions to different lower levels are possible, each one resulting in a different emission line.

Usually, rotational energy changes in the same transition, possibly electronic excitation does, too, therefore contribution to the transition energy and the line position.
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Vibrational Excitation of diatomic molecules
Each electronic level of a molecule is described by a potential curve in terms of energy vs. inter nuclear distance. From one upper level, transitions to different lower levels are possible, each one resulting in a different emission line. Usually, rotational energy changes in the same transition, possibly electronic excitation does, too, therefore contribution to the transition energy and the line position.

**Vibrational Excitation of diatomic molecules**

- Different vibrational energies appear as lines of constant energy ion these potentials
- Excitation of the levels can happen through collisions (one major partner are electrons) or absorption of radiation.
- From one upper level, transitions to different lower levels are possible, each one resulting in a different emission line.
Emission from Molecules

- Rigid Rotator and Harmonic Oscillator
  - simple model, mainly to be used to account for rotational and vibrational energies in CFD codes → energy conservation
  - not suitable (at least the harmonic oscillator for spectral simulation)
  - The harmonic oscillator, however, does not describe real molecules:
    - for \( r \sim \infty \) → \( E = \) dissociation energy
    - for \( r \sim 0 \) → \( E \sim \infty \).

**Morse Potential**

\[
U(x) = D_e \left(1 - e^{-\beta x}\right)^2
\]

- \( x \): distance to \( r_e \)
  (re: equilibrium distance between the nuclei)
- \( D_e \): Well depth of the potential
  (dissociation energy- energy at minimum)

\[
\beta = 1.2177 \cdot 10^{-7} \omega_e \sqrt{\frac{\mu_A}{D_e}}
\]

- \( \mu_A \): reduced mass of the molecule

vibrational energy increment from \( V \) to \( V+1 \) now decreases with \( V \):

\[
G(V) = \omega_e \left(V + \frac{1}{2}\right) - \omega_e x_e \left(V + \frac{1}{2}\right)^2
\]
• Separation of rotational and vibrational excitation is not completely possible.
• In fact, the whole molecular potential changes shape with rotational quantum number.
• For rotationally highly excited states, only low vibrational excitation possible $\rightarrow V_{\text{max}}(J)$
• Or: limiting rotational quantum numbers different for each vibrational state $\rightarrow J_{\text{max}}(V)$

Molecular potential with rotational excitation

- limiting case: no more potential well $\rightarrow$ not stable
- will be different for each electronic state

Emission from Molecules

Theoretical Simulation of Molecule Radiation

- Intensity of one emission line:

\[ \varepsilon = \frac{N' A_{\lambda} \Delta E}{4\pi} = \frac{16\pi^3 c V^4}{3} \left( R \left( \vec{r}_{V'V''} \right) \right)^2 q_{V'V''} \frac{S_{J''}}{2J''+1} \]

  - Particle density in the level \( e' V' J' \)
  - Electronic transition moment
  - Hönl London Factor

Assumption of Boltzmann distributions

\[ \frac{N_{e'V'J'}}{N_{total}} = \sum_{e'V'J'} \frac{Q_{el} e' Q_{vib} e' Q_{rot} e'Q_{e'V'J'}}{Q_{el} e' Q_{vib} e' Q_{rot} e'Q_{e'V'J'}} \]

with the total partition function:

\[ Q = \sum_{e'V'J'} Q_{el} e' Q_{vib} e' Q_{rot} e'Q_{e'V'J'} \]

\[ N_{e'V'J'}(T_{el}, T_{vib}, T_{rot}) = N_{total} g_e' \frac{(2J' + 1)}{Q} \exp \left( -\frac{E_{el} e'}{kT_{el}} \right) \exp \left( -\frac{E_{vib} e' e'}{kT_{vib}} \right) \exp \left( -\frac{E_{rot} e' e'}{kT_{rot}} \right) \]

- Electronic
- Vibrational
- Rotational

\[ Q_{el} = g_e e' \exp \left( -\frac{E_{el} e'}{kT_{el}} \right) \]

\[ Q_{vib} = e' e' \exp \left( -\frac{E_{vib} e' e'}{kT_{vib}} \right) \]

\[ Q_{rot} = (2J' + 1) \exp \left( -\frac{E_{rot} e' e'}{kT_{rot}} \right) \]
Emission from Molecules

Theoretical Simulation of Molecule Radiation

- Intensity of one emission line:

\[ \varepsilon = \frac{N' A_{\Delta E\rightarrow''}}{4\pi} = N' \frac{16\pi^3 c \bar{V}^4}{3} \left( R_e (\bar{r}_{V''V'}) \right)^2 q_{V''V'} \frac{S_{J''\Lambda''}}{2J'+1} \]

Particle density in the level e’ V’ J’

Electronic transition moment

Hönl London Factor

- The electronic transition is fast in comparison to the motion of the nuclei during vibration.

→ The position of the nuclei relative to each other will not change during the transition.

→ The higher the overlap between the upper and lower potential, the higher the probability of the transition.

→ If wave functions are analyzed, this probability can be expressed in the electronic transition moment containing the Franck-Condon factor.

Molecular Band Structure

- Transition energies with the same difference in vibrational quantum number $\Delta \nu$ are similar
  - The different vibrational transitions tend to group for the same $\Delta \nu$.
- $\Delta \nu = 0 : \ 0-0, 1-1, 2-2, 3-3, \ldots$

![Graph showing molecular band structure with transitions marked for different $\Delta \nu$ values.](image-url)

Molecular Band Structure

- Transition energies with the same difference in vibrational quantum number $\Delta v$ are similar → The different vibrational transitions tend to group for the same $\Delta v$.
- $\Delta V = 1 : 1-0, 2-1, 3-2, 4-3, \ldots \rightarrow$ higher $\Delta E \rightarrow$ lower $\lambda$.

\[ \Delta V = 2, 1, 0, -1, -2, \ldots \]

\[ \Delta v = 2 \rightarrow \Delta V = -1 \]

\[ \Delta v = 1 \rightarrow \Delta V = -2 \]

\[ \Delta v = 0 \rightarrow \Delta V = -3 \]

\[ \Delta v = -1 \rightarrow \Delta V = -4 \]

\[ \Delta v = -2 \rightarrow \Delta V = -5 \]

\[ \Delta v = -3 \rightarrow \Delta V = -6 \]

Molecular Band Structure

• Transition energies with the same difference in vibrational quantum number $\Delta v$ are similar
  → The different vibrational transitions tend to group for the same $\Delta v$.

• $\Delta V = -1 : 0-1, 1-2, 2-3, 3-4, \ldots$  → lower $\Delta E$  → higher $\lambda$

$\Delta V = -1$ : transition energy higher than $\Delta V = 0$

$\Delta V = -1$ : transition energy lower than $\Delta V = 0$
Emission from Molecules

Temperature determination from molecular radiation

• Within one vibrational transition, a large number of rotational lines is present → rovibrational lines (may shift to lower or higher wavelengths, depending on B)

• Similar to the atoms, a Boltzmann plot can be performed to determine $T_{\text{rot}}$.

$$Q_{\text{rot}}^{e'v'J'} = (2J'+1) \exp \left( -\frac{E_{\text{rot}}^{e'v'J'}}{kT_{\text{rot}}} \right)$$

emission spectroscopy is a line of sight method → only integrated data, no spatial resolution

Abel integral equation:

\[
I(z) = 2 \int_{r=z}^{R} \frac{r}{\sqrt{r^2 - z^2}} \varepsilon(r) \, dr
\]

Typically, integrals along the line of sight are measured → the local emission is desired.

\[
\varepsilon(r) = -\frac{1}{\pi} \int_{z=r}^{\infty} \frac{dI}{dz} \frac{dz}{\sqrt{z^2 - r^2}}
\]

Solving this equation is usually only possible in special cases (e.g. a constant local distribution \( \varepsilon(r) = \text{const.} \) yields and elliptical profile in \( I(z) \))

Under the assumptions of rotational symmetry and optically thin medium, local emission values can be obtained from an Abel-Inversion.
Approximate Abel-Inversion

→ Different radial/vertical positions are to be measured
→ A matrix can be built that gives a relation between integrated and local emission

→ The matrix simplifies significantly if only few measurement positions are taken into account. Constant local intensity in each ring assumed
→ A very simple system of linear equations can be obtained and solved recursively

\[ I_{3, \text{int}}(Z_3) = \varepsilon(r_3) * L_3(r_3) \]
\[ I_{2, \text{int}}(Z_2) = \varepsilon(r_3) * L_2(r_3) + \varepsilon(r_2) * L_2(r_2) \]
\[ I_{1, \text{int}}(Z_1) = \varepsilon(r_3) * L_1(r_3) + \varepsilon(r_2) * L_1(r_2) + \varepsilon(r_1) * L_1(r_1) \]
\[ I_{0, \text{int}}(Z_0) = \varepsilon(r_3) * L_0(r_3) + \varepsilon(r_2) * L_0(r_2) + \varepsilon(r_1) * L_0(r_1) + \varepsilon(r_0) * L_0(r_0) \]
The matrix simplifies significantly if only few measurement positions are taken into account. Constant local intensity in each ring assumed. A very simple system of linear equations can be obtained and solved recursively.

\[
\begin{align*}
I_{3,\text{int}}(Z_3) &= \varepsilon(r_3) \cdot L_3(r_3) \\
I_{2,\text{int}}(Z_2) &= \varepsilon(r_3) \cdot L_2(r_3) + \varepsilon(r_2) \cdot L_2(r_2) \\
I_{1,\text{int}}(Z_1) &= \varepsilon(r_3) \cdot L_1(r_3) + \varepsilon(r_2) \cdot L_1(r_2) + \varepsilon(r_1) \cdot L_1(r_1) \\
I_{0,\text{int}}(Z_0) &= \varepsilon(r_3) \cdot L_0(r_3) + \varepsilon(r_2) \cdot L_0(r_2) + \varepsilon(r_1) \cdot L_0(r_1) + \varepsilon(r_0) \cdot L_0(r_0)
\end{align*}
\]

Application examples

Measurements in an atmospheric, inductively coupled plasma torch
( C. Laux, Stanford University, now Ecole Centrale, Paris)

- Equilibrium plasma at up to 6000 K → chemistry well defined
- Used for the development of radiation models
- Excellent agreement between experiment and simulation can be achieved.
- After equilibrium characterization, used for non-equilibrium investigation.

Comparison of free stream spectra at high condition with LTE simulation (VIS/NIR):

- Spectra dominated by emission of N2 B-A (1st Pos.)
- Thermodynamic quantities from CFD solution used as input for NEQAIR
- Spectra integrated along the line of sight

- Simulation and experiment do not even agree qualitatively
- If individual vibrational states are computed separately, the spectrum can be fitted by scaling these upper populations
  → massive overpopulation of the high vibrational levels peaking at $v_{upper} = 13$

Application examples

level crossing with $N_2 B^3\Pi_g$ at $v$ between 10 and 13

→ Population of the excited state is not caused by thermal excitation of the ground state but by recombination of atoms in an excited $N_2$ state

→ Molecule emission can be used to determine atom ground state densities.

- Observed radiation comes from the 1st Pos. System $(N_2 B^3\Pi_g \rightarrow A^3\Sigma_u^+)$ with electronic excitation energies around 8eV to 10eV.

Harry Partridge, Stephen R. Langhoff, and Charles W. Bauschlicher, Jr., and David W. Schwenke, "Theoretical study of the $A^6S_g^+$ and $C^6P_u$ states of $N_2$: Implications for the $N_2$ afterglow," J. Chem. Phys. 88 (5), 1 March 1988. Figure reproduced with permission from the authors.

Quantify radiation loads to spacecraft during atmospheric entry in impulse facilities

EAST shock tube (NASA Ames):
- reproduction of flight conditions
- no model testing
- 130nm – 8μm in various intervals
- simultaneous measurements with 4 spectrometers possible
- one dimension resolves spectrally, the other spatially

Goals:
- quantify radiation from shock and post shock
  → radiation heat flux from the plasma upstream of the spacecraft after spectral integration
  → empirical correlation for radiation heat flux

Application examples

Monitoring of ablation species through optical methods

Testing of PICA at NASA Ames (SPRITE) showed the appearance of ablation products in emission spectra inside the boundary layer:
- CN, OH, NH, Ca, (Na, K)

Combination of pyrolysis products themselves and interactions with the plasma.

Remote recession measurements of ablating TPS material

- Tracer element (Coating/paint)
- Tracer plug (e.g. PICA)

Conclusions

- Optical emission spectroscopy is a useful tool to access information on thermal characteristics and composition of a plasma.

- Applications for which the assumption of equilibrium is rather uncritical:
  - identification of species;
  - total radiation flux (in the wavelength covered and if properly calibrated);
  - quantities from line broadening (e.g. Doppler temperature, electron density);
  - identification of thermal non-equilibrium.

- Applications for which the assumption of equilibrium is rather crucial:
  - determination of particle densities from thermal excitation;
  - measurement of excitation temperatures from line ratios.

- Proper calibration is imperative.

- Comparison with simulation (non-equilibrium chemistry and excitation, e.g. though collisional radiative models) seems the best approach as soon as these models are validated.

Thanks for your attention! Open for

Questions?
Selection of Simulation Codes (Line-by-Line)

• **NEQAIR (Non Equilibrium …)** - NASA Ames  
  FORTRAN, non-eq. (QSS + multi T), air and CO$_2$ plasma related species + H, radiation transport capabilities  

• **HARA (…) – NASA Langley**  
  FORTRAN, non-eq. (QSS + multi T), air and CO$_2$ plasma related species, radiation transport capabilities  

• **SPRADIAN/RADIPAC – Japan/South Korea**  
  available on request to JAXA  
  FORTRAN, non-eq. (QSS + multi T), air + ablation related species, radiation transport capabilities  

• **PARADE – European Space Agency ESA**  
  available on request to ESA  
  FORTRAN, non-eq. (QSS + multi T), air + CO$_2$ plasma related species, rad. transport capabilities (HERTA)  

• **SPECAIR – Ecole Centrale Paris**  
  Windows version available by download  
  air, multi T, no radiation transport  

• **LIFBASE - Stanford Research Institute SRI** Windows version available by download  
  LIF related diatomic molecules (CH, NH, OH, CO, NO, …), no radiation transport  
Intensity Calibration – How?

- Calibration with an integrating sphere (halogen bulbs - UV-VIS-NIR) and a Deuterium lamp (UV) both calibrated to spectral radiance in $\mu$W/(cm$^2$ sr nm)
- Correction factor: ratio of factory calibration value and measurement of calibration lamp
- Deuterium lamp (UV) can not easily be used for absolute calibration → scaling of Deuterium correction factor to the I-Sphere in overlapping region.
- Best calibration: place the calibration lamp at the location of the measured plasma → all set-up influences are covered and direct calibration is possible.
  - Lamp area must be larger than measurement spot !!!

Intensity Calibration – How?

VIS: direct

\[ I_{pl, cal}(\lambda) = corr(\lambda) I_{pl, meas}(\lambda) \]

UV: scaled

\[ I_{pl, cal}(\lambda) = \text{corr}_{BB} \text{ corr}_{Deut} \Delta \lambda_{\text{scaling}} \frac{I_{BB, theory}(\lambda)}{I_{BB, meas}(\lambda)} \]

\[ = \frac{I_{BB, theory}(\lambda)}{I_{BB, meas}(\lambda)} I_{pl, meas}(\lambda) \]

\[ \rightarrow \text{Correction factor } corr(\lambda) \text{ which is the inverse sensitivity of the set-up.} \]

\[ \rightarrow \text{Use of Deuterium lamp only for qualitative calibration} \]

\[ \text{followed by scaling (cross calibration) through halogen lamp/black-body.} \]

Emission of Atoms: Electronic Excitation

\[ \mathcal{E} = \frac{h \nu}{4\pi} A_{ki} n_k = \frac{h \nu}{4\pi} A_{ki} \frac{g_k}{U(T_{ex})} n_0 \exp\left(-\frac{E_k}{kT_{ex}}\right) \]

- For low temperatures, only the first energy levels are populated.
- With temperature going to infinity, all levels would be populated according to \( g_k/U \).
Electronic Excitation of Hydrogen

\[ \mathcal{E} = \frac{h\nu}{4\pi} A_{ki} n_k = \frac{h\nu}{4\pi} A_{ki} \frac{g_k}{U(T_{ex})} n_0 \exp \left( -\frac{E_k}{kT_{ex}} \right) \]

Balmer spectrum of hydrogen

normalized line emission \( \varepsilon_k \),

- wavelength, nm

H I, Balmer
Electronic Excitation of Hydrogen

\[ \varepsilon = \frac{h \nu}{4\pi} A_{ki} n_k = \frac{h \nu}{4\pi} A_{ki} \frac{g_k}{U(T_{ex})} n_0 \exp \left( - \frac{E_k}{kT_{ex}} \right) \]

- Emission increases by 60 orders of magnitude between 1000K and 8000K
- Ratio of different lines in the Balmer series changes with temperature (hard to see on log scale).
- To illustrate the ratios, we normalize the spectrum to the H\(_\alpha\) line.
Electronic Excitation of Hydrogen

\[ \varepsilon = \frac{h \nu}{4\pi} \quad A_{ki} \quad n_k \quad = \quad \frac{h \nu}{4\pi} \quad A_{ki} \quad \frac{g_k}{U(T_{ex})} n_0 \exp \left( - \frac{E_k}{kT_{ex}} \right) \]

Ratio of two states:

\[ \frac{n_{i,n}}{n_{i,m}} = \frac{g_{i,n}}{g_{i,m}} e^{-\frac{E_{i,n} - E_{i,m}}{kT}} \]

Spectrum normalized to H\(\alpha\) to illustrate the influence on the line ratios:
Line Broadening

Emission and absorption lines can be broadened through different processes:

- **natural broadening (Heisenberg uncertainty principle)**
- **Doppler broadening (thermal motion)**
- **Collision broadening**
  - Van-der-Waals: collisions with neutrals
  - Resonance: collisions with the ‘like’ species particles (perturber’s state connected by an allowed transition to the upper or lower state of the transition under consideration)
  - Stark for interactions with ions or electrons, specific for each transition/line
- **(Zeeman effect - interaction with magnetic fields)**

  - Each of these processes is actually a line shift for one photon.
  - The integration over many photons with different shifts produces a broadening.

  $\rightarrow$ distributing the transition energy over a certain wavelength/wavenumber range

- Depending on the physical effect, the final line shape will follow a Gauss or a Lorentz profile.
- Usually, the broadening is described by the line width at its half maximum (full width FWHM, or half width HWHM).
- Half widths of Lorentz profile can be summed up linearly.
- Half widths of Gauss profiles can be combined quadratically through

$$FWHM_{G,\text{total}} = \sqrt{FWHM_{G,1}^2 + FWHM_{G,2}^2}.$$
Emission of Atoms and Molecules

Line Broadening

Collision broadening (Lorentz)

\[ \kappa_\eta = \frac{S}{\pi} \frac{b_c}{(\eta - \eta_0)^2 + b_c^2}, \quad S = \int_{\Delta \eta} \kappa_\eta \, d\eta, \]

HWHM decreases with T

\[ b_c = b_{cu} \left( \frac{p}{p_0} \right) \sqrt{\frac{T_0}{T}}, \]

Doppler broadening (Gauss)

\[ \kappa_\eta = \sqrt{\frac{\ln 2}{\pi}} \left( \frac{S}{b_D} \right) \exp \left[ -\ln(2) \left( \frac{\eta - \eta_0}{b_D} \right)^2 \right] \]

HWHM increases with T

\[ b_D = \frac{\eta_0}{c_0} \sqrt{\frac{2kT}{m}} \ln 2. \]

Lorentz:
- 90% of the transition energy within 6 HWHM
- 99% is reached after \(~ 50 \) HWHM

Gauss:
- 99% in 2 HWHM
Emission from Molecules

The Anharmonic Oscillator – Higher Order Potentials

• Higher order potentials
  Lippincott – 3 parameter fit
  Hulbert-Hirschfelder – 5 parameter fit
• may provide better agreement with experimental data

Morse Potential

\[ U(x) = D_e \left(1 - e^{-\beta x}\right)^2 \]

• \( x \): distance to \( r_e \)
  (re: equilibrium distance between the nuclei)
• \( D_e \): Well depth of the potential
  (dissociation energy- energy at minimum)

\[ \beta = 1.2177 \cdot 10^{-7} \sqrt{\frac{\mu_A}{D_e}} \]

• \( \mu_A \): reduced mass of the molecule

vibrational energy increment from \( V \) to \( V+1 \) now decreases with \( V \):

\[ G(V) = \omega_e \left( V + \frac{1}{2} \right) - \omega_e x_e \left( V + \frac{1}{2} \right)^2 \]
Emission from Molecules

Higher Order Approximations - Dunham Expansion

• Vibrational energy expressed as a polynomial function of V
• For small quantum numbers equivalent to Morse

\[ G(V) = \omega_e \left( V + \frac{1}{2} \right) - \omega_e x_e \left( V + \frac{1}{2} \right)^2 + \omega_e y_e \left( V + \frac{1}{2} \right)^3 + \omega_e z_e \left( V + \frac{1}{2} \right)^4 + \ldots \]

• Rotational energy contains higher orders of J
• coupling constants now depend on V

\[ F_V(V, J) = B_V J(J + 1) - D_V J^2 (J + 1)^2 + \ldots \]

\[ B_V = B_e - \alpha_e \left( V + \frac{1}{2} \right) + \gamma_e \left( V + \frac{1}{2} \right)^2 + \ldots \]

\[ D_V = D_e + \beta_e \left( V + \frac{1}{2} \right) + \delta_e \left( V + \frac{1}{2} \right)^2 + \ldots \]

• Different sets of constants given in literature

Dunham, J: The energy levels of a rotating vibrator, Phys. Rev. 41, 721, 1932.
Intensity Calibration – How?

\[ I_{\text{plasma,cal}}(\lambda) = \text{corr}(\lambda) \times I_{\text{plasma, measured}}(\lambda) = \left[ \frac{I_{\text{lamp, theory}}(\lambda)}{I_{\text{lamp, measured}}(\lambda)} \right] \times I_{\text{plasma, measured}}(\lambda) \]

- Best calibration: place the calibration lamp at the location of the measured plasma → all set-up influences are covered and direct calibration is possible.
- **Lamp area must be larger than measurement spot !!!**
• Deuterium lamp (UV) uses a hydrogen discharge to produce high radiation in VUV-VIS
• Usually, only the continuum emission from UV down is used for calibration.
• Although calibrated to radiance in $\mu W/(cm^2 \cdot sr \cdot nm)$, the dimensions of the discharge are small (~1mm) $\rightarrow$ measurement spot usually larger
• Discharge shows gradients $\rightarrow$ additional uncertainties introduced.

$\rightarrow$ **Use of Deuterium lamp only for qualitative calibration followed by scaling (cross calibration) through halogen lamp/black-body.**
Wavelength Calibration

• Compare measured line positions (pixel) with known line positions (e.g. Hg lamp):
  - scanning spectrometer: typically linear with time → at least 2 lines needed;
  - CCD measurement: typically binomial → at least 3 lines needed.
• additional lines may serve as a calibration check …

\[ \lambda (\text{pixel}) = C_1 \cdot \text{pixel}^2 + C_2 \cdot \text{pixel} + C_3 \]
The emission coefficient is integrated along the line of sight

\[ I_{ki} = \int \varepsilon(x) dx = \frac{h \nu}{4\pi} A_{ki} n_k l \]

follows:

\[ \ln \left( \frac{I_{ki}}{\nu A_{ki} g_k} \right) + \text{const} = -\frac{E_k}{kT_{ex}} \]

Theoretically, the ratio of two lines would be sufficient, but it is often in doubt if the electronic excitation is in equilibrium.

→ Boltzmann Plot:

\[ \ln \left( \frac{I_{ki}}{\nu A_{ki} g_k} \right) \text{ vs } E_k \]

→ Straight line with slope 1/-kT

If points are indeed on a straight line
→ Boltzmann valid
→ T can be determined
Molecular Band Structure

• Transition energies with the same difference in vibrational quantum number $\Delta v$ are similar.
  $\rightarrow$ The different vibrational transitions tend to group for the same $\Delta v$.

• $\Delta V = -1 : 0-1, 1-2, 2-3, 3-4, \ldots \rightarrow$ lower $\Delta E \rightarrow$ higher $\lambda$.
Intensity of one emission line:

\[
\varepsilon = \frac{N' A_{\Delta E}}{4\pi} = N' \frac{16\pi^3 c \bar{V}^4}{3} (R_e (\bar{r}_{VV''}))^2 q_{VV''} \frac{S_{JJ''}^{1/2}}{2J'+1}
\]

- There are \((2J+1)\) allowed rotational states (rotational multiplicity)
- The selection rules allow for \(\Delta J = -1, 0, 1\)
- The Hönl London Factor controls how the \((2J+1)\) states are distributed among the branches
Line Broadening

Emission and absorption lines can be broadened through different processes:

- **natural broadening (Heisenberg uncertainty principle)**
- **Doppler broadening (thermal motion)**
- **Collision broadening**
  - Van-der-Waals: collisions with neutrals
  - Resonance: collisions with the ‘like’ species particles (perturber’s state connected by an allowed transition to the upper or lower state of the transition under consideration)
  - Stark for interactions with ions or electrons, specific for each transition/line
- **(Zeeman effect - interaction with magnetic fields)**

  - Each of these processes is actually a line shift for one photon.
  - The integration over many photons with different shifts produces a broadening.
  - Distributing the transition energy over a certain wavelength/wavenumber range

- **Temperature measurement** (low pressures, high temperatures)

- **Electron density measurement** (lines with large Stark coefficients, e.g. H\(_\alpha\) or H\(_\beta\))
Emission of Atoms and Molecules

Line Broadening

Emission and absorption lines can be broadened through different processes:

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- **Doppler broadening (thermal motion)**
- Collision broadening
  - Van-der-Waals: collisions with neutrals
  - Resonance: collisions with the ‘like’ species particles (perturber’s state connected by an allowed transition to the upper or lower state of the transition being studied)
  - Stark for interactions with ions or electrons, specific for each transition/line
- (Zeeman effect - interaction with magnetic fields)

**Lorentz:**
- 90% of the transition energy within 6 HWHM
- 99% is reached after ~ 50 HWHM
- Half widths are added linearly.

**Gauss:**
- 99% in 2 HWHM
- are combined as the geometric sum

\[
FWMH_{G,total} = \sqrt{FWMH_{G,1}^2 + FWMH_{G,2}^2}
\]

- 99% in 2 HWHM
- are combined as the geometric sum

\[
FWMH_{G,total} = \sqrt{FWMH_{G,1}^2 + FWMH_{G,2}^2}
\]
Intro to Absorption Spectroscopy in Nonequilibrium Hypersonic Flows

Craig Johansen, The University of Calgary, Canada
Sean O’Byrne, University of New South Wales, Canberra, Australia

Outline

• Introduction & Background
• Velocity measurement
• Temperature:
  – Translational
  – Rotational
  – Vibrational
• Tomography and Hyperspectral
• Flight Application
Absorption is described by the Beer-Lambert Law:

$$-dI_v = I_v k_s(\nu)dx$$

where $k_s(\nu)$ is the spectral absorption coefficient.

This leads to exponential decay of laser intensity:

$$I_{v,x} = I_{v,0} e^{-k_s(\nu)x}$$

Measure $I_v$, know $x$, directly measure $k_s(\nu)$

$k_s(\nu)$ contains information about temperature, concentration, velocity of gas.
TDLAS: Strengths and Weaknesses

• **Strengths**
  - Can probe non-luminous flows and ground-state populations
  - Simple, rugged optical arrangements with no moving parts
  - Comparatively inexpensive
  - Fast wavelength scanning capability (wavelength agile)
  - Can provide quantitative multi-parameter measurement with a single instrument
    - No systematic errors due to quenching

• **Weaknesses**
  - Path-integrated technique
    - Distributions can be determined tomographically, but time consuming and analysis can be complex
  - Spatial and temporal flow nonuniformity can produce bias errors in measurements unless the freestream is well characterized
  - Some important diatomics (eg N$_2$) do not have a dipole moment and do not have a direct absorption spectrum
Broadening Mechanisms

• Spectral shape of \( k_s(\nu) \) is from “broadening”
• Pressure (Homogeneous) Broadening

\[
g_H = \frac{\Delta \nu_H}{2\pi} \left( \frac{1}{(\nu - \nu_0)^2 + (\Delta \nu_H/2)^2} \right)
\]

– Caused by collisions with other atoms/molecules, a high-pressure effect causing a Lorentzian shape
– Generates a broadening

\[
\Delta \nu_c = P \sum_i (\chi_i^2 \gamma_i)
\]

and a shift in the transition

\[
\Delta \nu_s = P \sum_i (\chi_i \delta_i)
\]

If temperature can be independently determined, pressure can be measured from these quantities
Broadening Mechanisms

• Doppler (Inhomogeneous) Broadening
  – Due to thermal motion of absorbing particles towards or away from laser

\[ g_D = \frac{2\sqrt{\ln 2}}{\pi^{1/2} \Delta \nu_D} e^{\left[-\frac{4(\ln 2)(\nu-\nu_0)}{\Delta \nu_D^2}\right]} \]

  – \( \Delta \nu_D \) is the full-width at half-maximum of the measured peak, and is given by

\[ \Delta \nu_D = 2\nu_0 \sqrt{\frac{2kT_{\text{trans}}}{(MW)c^2}} \ln 2 \]

  \( \nu_0 \) is the transition center
  \( k \) is the Boltzmann constant
Voigt Profile

- The Voigt profile is a convolution of the two previous broadening effects

\[
V(a, x) = \frac{a}{\pi} \int_{-\infty}^{\infty} \frac{e^{-y^2}}{a^2 + (x - y)^2} \, dy
\]

\[
a = \sqrt{\ln 2} \frac{\Delta V_H}{\Delta V_D}, \quad x = 2\sqrt{\ln 2} \frac{(\nu - \nu_0)}{\Delta \nu_D}
\]
Laser Sources

• In 1970s, dye lasers were often used in visible and NIR absorption studies, and Pb salt for IR. Now mostly replaced with:

• Diode laser sources
  – Distributed feedback (DFB) lasers
    • Tune over ~0.1 nm
    • Robust and well tested in telecoms
    • Very spectrally narrow (1-30 MHz)
  – Vertical cavity surface-emitting lasers (VCSELs)
    • Tune over 1 nm
    • Tune very rapidly
    • Spectrally narrow (<30 MHz)
  – Quantum cascade lasers (QC)
    • High-power pulsed source operating in the IR
Detection Schemes

• **Direct absorption**
  – Simple, direct measurements, but poor use of dynamic range

• **Difference amplification**
  – Removes intensity modulation, but only when perfectly balanced

• **Log-ratio detection**
  – Simple circuit, and cancels common-mode electronic and laser noise very efficiently
  – Can be autobalanced, to remove offset caused by mismatch in reference and signal intensities
    • M.G. Allen *et al.* *Applied Optics* 34.18 (1995): 3240-3249
  – Bandwidth decreases as photocurrent decreases
Detection Schemes

• **Wavelength modulation**
  – Removes DC offset from signal
  – Signal proportional to the derivative of the input intensity
  – Phase-sensitive detection at a multiple of the modulation frequency can reduce \(1/f\) noise in the signal
  – Traditionally required careful calibration to samples under controlled conditions, but recent innovation using the ratio of second-harmonic (\(2f\)) and first-harmonic (\(1f\)) signals to account for the laser intensity

• **Cavity-based methods**
  – Useful for measurements of trace quantities, but practical challenges in hostile environments.
Detection Schemes
Detection Schemes

• E.g. Goldenstein et al.
  – Measured spectra of water vapor in UVa scramjet test facility
  – Small amplitude of second feature limits signal-to-noise ratio for direct absorption
  – $2f/1f$ ratio measurement provided consistently better signal-to-noise ratios, but both methods consistent with computational predictions

## Detection Schemes

<table>
<thead>
<tr>
<th>Operation Mode</th>
<th>Expected Value</th>
<th>DA</th>
<th>WMS</th>
</tr>
</thead>
<tbody>
<tr>
<td>11% Steam</td>
<td>700–1000 K</td>
<td>776 ± 10 K</td>
<td>742 ± 9 K</td>
</tr>
<tr>
<td>(Combustor Entrance)</td>
<td>11.4 ± 0.2% H₂O</td>
<td>10.9 ± 0.1% H₂O</td>
<td>10.8 ± 0.1% H₂O</td>
</tr>
<tr>
<td>9% Steam</td>
<td>700–1000 K</td>
<td>860 ± 30 K</td>
<td>831 ± 9 K</td>
</tr>
<tr>
<td>(Exit Plane)</td>
<td>9 ± 0.2% H₂O</td>
<td>9.1 ± 0.2% H₂O</td>
<td>9.1 ± 0.1% H₂O</td>
</tr>
<tr>
<td>12% Steam</td>
<td>700–1000 K</td>
<td>875 ± 50 K</td>
<td>850 ± 6 K</td>
</tr>
<tr>
<td>(Exit Plane)</td>
<td>12 ± 0.2% H₂O</td>
<td>12.1 ± 0.5% H₂O</td>
<td>11.5 ± 0.1% H₂O</td>
</tr>
<tr>
<td>H₂-Air Combustion</td>
<td>1800–2200 K</td>
<td>1802 ± 94 K</td>
<td>1765 ± 41 K</td>
</tr>
<tr>
<td>φ = 0.33</td>
<td>13% H₂O</td>
<td>12.8 ± 0.5% H₂O</td>
<td>13.3 ± 0.3% H₂O</td>
</tr>
</tbody>
</table>

Velocity Measurements

• Simplest quantity to measure in a high-speed flow
  – Measured through Doppler shift between beams with velocity components in two different directions relative to the flow

\[ U = \frac{c \Delta \nu_{Dopp}}{\nu_{Source}} \]

– Shift in the peak position relatively insensitive to amplitude noise.
– Shift typically calibrated to etalon measurements
Velocity Measurements

- *E.g. Lyle et al.*, mass flux sensor based on measurements of density and velocity using oxygen A-band near 760-nm.
- Measured speed with time-averaged precision of 0.25 m/s.

Translational Temperature

- Can be determined through the Doppler width, but as \( T_{\text{trans}} \propto \left( \frac{\Delta v_D}{v_0} \right)^2 \), small errors in Doppler width have a significant effect on \( T \)

\[
\frac{\Delta T}{T} = \frac{2\Delta (\Delta v_D)}{\Delta v_D}
\]

- E.g. An uncertainty in width measurement of 1.5% for a Doppler-broadened transition in the oxygen A-band will cause an uncertainty of 3% in temperature
- Uncertainty further increased in the presence of pressure broadening
- Measuring \( T \) through linewidth has the advantage of only requiring 1 transition for a measurement
Translational Temperature

- E.g. Measurements of temperature in an arcjet facility using an AR I line at 811.531 nm
- 12% uncertainty in width translated to 30% uncertainty in $T_{\text{trans}}$ over 2000–1000 K

• *E.g.* Measurements of NO translational temperature at 5.44 μm in the LENS I facility, using direct absorption

• Fit temperature of 290 K significantly different to the predicted temperature of 563K

Rotational Temperature

- Typically measured using the ratio of integrated absorbance \( a \) over two lines with different linestrength variations with \( T \)
  \[
  a_j = P \chi_i LS_j
  \]
  - for transition \( j \) of an absorbing species \( i \)
  - \( L \) is the path length and \( S_j \) is the linestrength of the transition
- All quantities other than \( S_j \) are common to the two lines and divide out
  \[
  \frac{a_1}{a_2} = \frac{S_1}{S_2} = \frac{S_1(T_0)}{S_2(T_0)} e^{\frac{hc\Delta E_{rot}}{k} \left( \frac{1}{T_{rot}} - \frac{1}{T_0} \right)}
  \]

Rotational Temperature

• *E.g. Wehe et al.* measured H$_2$O rotational and translational temperature in the 10 MJ/kg Calspan 96-inch hypersonic shock tunnel freestream

• ν1 + ν3 band near 1396 nm (λ$_2$) and 1400 nm (λ$_1$)

• 8 kHz scan rate

• $T_{rot}$ uncertainty of ±2.3 % compared with $T_{trans}$ uncertainty of ±2.7 % and ±6.4 % for the $T_{trans}$ measurements on the two lines

E.g. Brandt and Roth measured $T_{vib}$ and $T_{trans}$ in CO in a reflected shock tube, using a lead salt laser operating at 2100-2200 cm$^{-1}$, at 20 kHz scan rate.

TDLAS Tomography

• Major limitation of TDLAS: path-averaged
  – Can do tomography

– 15x15 grid provides data at 225 points (36 mm grid)

TDLAS Tomography

- General Electric J85 gas turbine engine
  - University of Tennessee Space Institute (UTSI)

- Measure water and temperature at 50 kHz rate

TDLAS Tomography Results

• Measurement is over ~0.5 meter square
  – Time resolution is 20 µsec (50 kHz)
  – Spatial resolution is ~36 mm

Using Spectral Information

- Many hypersonic environments (flight vehicles, test facilities) have limited optical access for tomography
  - Can use spectral information to infer spatial variations of temperature.

Extracting Line-of-Sight Temperatures

- Example: Temperature in a tube furnace using a single VCSEL line of sight
  - The ‘distribution technique’ assumes *a priori* knowledge of the distribution shape.

TDLAS Hyperspectral Tomography

- Using hyperspectral sources, can gain spectral images over many lines, reducing number of projections

Flight-Testing TDLAS Systems

- Small size and power requirements have allowed TDLAS systems to be used in hypersonic flight tests.


Conclusions

• TDLAS is a reliable and well established nonintrusive measurement technique, capable of precise path-averaged measurements of velocity, density and trans/rot/vib temperatures
• Availability of telecoms lasers and detectors makes it comparatively economical
• Path-averaging disadvantages can be mitigated using tomography or additional spectral information
• Particularly valuable for flight-test applications and time-resolved online facility monitoring
• Rapid development in mid-IR sources and detectors will significantly expand applications
Intro to Planar Laser-Induced Fluorescence for Hypersonic Nonequilibrium Flows

Brett Bathel, NASA Langley Research Center, Virginia, USA
Paul Danehy, NASA Langley Research Center, Virginia, USA
Craig Johansen, The University of Calgary, Canada

Planar Laser-Induced Fluorescence (PLIF)

Tunable Laser

Laser sheet excites molecules

Excited molecules fluoresce

CCD camera detects

LIF $\sim n_{\text{NO}}$
PLIF can probe nonequilibrium

- Commonly used in equilibrium environments
- Useful probe for thermal non-equilibrium:
  - Translational temperature
  - Rotational temperature
  - Vibrational temperature (often $T_{\text{vib}} \neq T_{\text{rot}} \approx T_{\text{tran}}$)
  - Species specific:
    - Different species can have different temperatures (especially vibrational temperatures)
- Can measure, quantify species in chemical non-equilibrium (eg. NO in shock tunnels)
LIF Theory (Two-Level Model)

Energy of absorbing species at excited state (2)

Energy of absorbing species at ground state (1)

Assumptions:

A. There are only two important states to consider (ground state and excited state). Other levels (rotational and vibrational) are ignored.

B. Prior to excitation, population of absorbers in excited state is negligible ($N_2=0$)
Two-Level Model Theory

An incident photon from the light source (e.g. laser) is absorbed and sends some of the ground state population to the excited state.

\[ \frac{dN_1}{dt} = -N_1 W_{12} \]

\[ \frac{dN_2}{dt} = N_1 W_{12} \]

Population rate equations (incomplete at this point)

\[ W_{12} = \text{Stimulated Absorption} \]
The excited state population is further increased by collisional excitation.

\[
\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12})
\]

\[
\frac{dN_2}{dt} = N_1(W_{12} + Q_{12})
\]
Two-Level Model Theory

Some of the excited state population returns to the ground state through stimulated emission

\[
\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12}) + N_2 W_{21}
\]

\[
\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2 W_{21}
\]
Some of the excited state population returns to the ground state through collisions (self or with other atoms/molecules)

\[
\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12}) + N_2(W_{21} + Q_{21})
\]

\[
\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2(W_{21} + Q_{21})
\]
The excited state population gets depleted through dissociation and ionization (without returning to the ground state)

\[
\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12}) + N_2(W_{21} + Q_{21})
\]

\[
\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2(W_{21} + Q_{21} + Q_{\text{pre}} + W_{\text{ion}})
\]
Finally, some of the excited population return to the ground state via spontaneous emission and emit a photon (fluorescence)

\[
\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12}) + N_2(W_{21} + Q_{21} + A_{21})
\]

\[
\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2(W_{21} + Q_{21} + Q_{\text{pre}} + W_{\text{ion}} + A_{21})
\]
Fortunately, for many applications, $Q_{12}$, $W_{21}$, $Q_{\text{ion}}$, and $Q_{\text{pre}}$ are negligible.

\[
\frac{dN_1}{dt} = N_2(W_{21} + Q_{21} + A_{21}) - N_1(W_{12} + Q_{12})
\]

\[
\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2(W_{21} + Q_{21} + Q_{\text{pre}} + W_{\text{ion}} + A_{21})
\]
Two-Level Model Theory

Simplification of rate equation:
\[
\frac{dN_1}{dt} = -\frac{dN_2}{dt} = N_2(Q_{21} + A_{21}) - N_1W_{12}
\]

Conservation of mass for absorbing species:
\[
N_1 + N_2 = N_s = \chi_s f_B N_T
\]

Number density of the absorbing species in the ground state prior to excitation

Boltzmann fraction

Mole fraction of absorbing species

Total number density
Steady State Two-Level Model

- Steady state assumption (e.g. continuous wave laser): \[ \frac{dN_1}{dt} = -\frac{dN_2}{dt} = 0 \]

- Solve for \( N_2 \): \[ N_2 = \frac{\chi_s f_B N_T W_{12}}{W_{12} + Q_{21} + A_{21}} \]

- Weak excitation assumption: \( W_{12} \ll (Q_{21} + A_{21}) \)

- Integrate spontaneous emission rate:

\[ \int_0^{t_{det}} N_2 A_{21} dt = N_2 A_{21} t_{det} \]

- Include the optics of detection to get LIF signal:

\[ S_{LIF} = \chi_s f_B N_T W_{12} \left( \frac{A_{21}}{Q_{21} + A_{21}} \right) t_{det} V \frac{\Omega}{4\pi} \eta \]

- Steady state assumption (e.g. continuous wave laser):

\[ \frac{dN_1}{dt} = -\frac{dN_2}{dt} = 0 \]

- Solve for \( N_2 \):

\[ N_2 = \frac{\chi_s f_B N_T W_{12}}{W_{12} + Q_{21} + A_{21}} \]

- Weak excitation assumption:

\[ W_{12} \ll (Q_{21} + A_{21}) \]

- Integrate spontaneous emission rate:

\[ \int_0^{t_{det}} N_2 A_{21} dt = N_2 A_{21} t_{det} \]

- Include the optics of detection to get LIF signal:
\[ S_{\text{LIF}} = \chi_s N_T f_B W_{12} \Phi t_{det} V \frac{\Omega}{4\pi} \eta \]

- To first order, \( S_{\text{LIF}} \) is proportional to the concentration of the absorbing species.
- Qualitative PLIF visualization often used to show the spatial distribution of absorbing species.
- (see the text for measurement strategies for quantitative concentration)
Boltzmann Fraction

\[ S_{LIF} = \chi_s N_T f_B W_1 \Phi t_{det} V \frac{\Omega}{4\pi} \eta \]

- Rotational Boltzmann fraction
  \[ f_B = \frac{g_j e^{-E_j/k_BT}}{\sum_j g_j e^{-E_j/k_BT}} \]
  - a function of temperature only
  - Peak at 300 K is \(~3\%\) for \(N = 7\) \((J = 7.5)\)

- Vibrational and electronic Boltzmann fractions
  - Most molecules in ground state for \(T < 2000\) for atoms, diatomics

Computed using LIFBASE (J. Luque, SRI International)
Stimulated Absorption

\[ S_{LIF} = \chi_s N_T f_B W_{12} \Phi t_{det} V \frac{\Omega}{4\pi} \eta \]

\( W_{12} \) is the probability of an absorption transition per sec

\[ W_{12} = B_{12} I \int Y_v L_v dv \]

- laser irradiance
- absorption lineshape function
- laser spectral profile
- Einstein B coefficient
- spectral overlap integral
Fluorescence Yield

\[ S_{LIF} = \chi_s N_T f_B B_{12} IG \Phi t_{det} V \frac{\Omega}{4\pi} \eta \]

The fluorescence yield is affected by collisional quenching

\[ \Phi = \frac{A_{21}}{Q_{21} + A_{21}} \]

Probability of a quenching collision per second

Collisional quenching is hard to predict since it depends on many factors

\[ Q_{21} = N_T \sum_i \chi_i \sigma_{s,i} v_{s,i} \]

\[ N_T = P/k_B T \]

\( \chi \) is mole fraction
\( \sigma \) is quenching cross section
\( v \) is mean relative velocity
Steady State $S_{\text{LIF}}$ dependencies

$S_{\text{LIF}} \propto \chi_s f_B(T) B_{12} IG(\chi_s, P, T, U) \Phi(\chi_s, \chi_i, P, T) t_{\text{det}}$

– LIF signal is sensitive to $T, P, U, \chi_s, \chi_i$
  • Can potentially measure these parameters
  • Complicates measurement of a single parameter

– Making quantitative measurements with LIF involves finding a way to make measurement sensitive only to the parameter being measured
Time Dependent $S_{\text{LIF}}$ Solution

$$S_{\text{LIF}}(t) = S_{\text{LIF}}(t_{\text{laser}}) e^{-\frac{(t-t_{\text{laser}})}{\tau_{\text{LIF}}}}, \quad t > t_{\text{laser}}$$

- Laser pulse length is typically ~10 ns
- LIF lifetimes can be a few ns to 100’s of ns or longer
  - If you can measure lifetime, you can measure Q!
  - Can measure velocity from long lived decay (MTV)
More Complicated LIF Models

• More complete LIF theories and phenomena:
  – Saturation effects (see manuscript)
  – Line shapes
    • overlap integral, G, to be discussed below
  – Multi-level LIF models
    • 2 photon absorption
    • 3, 4, 5 level models
  – Predissociation
  – Rotational energy transfer
  – Vibrational energy transfer

• For further reference:

A real molecule: NO

- NO is a diatomic molecule
  - Electronic
  - Vibration
  - Rotation
    - Not shown
- Absorption and fluorescence take place between electronic states
  - Show rotational and vibrational structure

Figure A2.1. Selected potential energy curves that show the electronic structure of NO. In this experiment, we probed transitions in the A-X band of NO [adapted from (Sheingraber and Vidal, 1985)].
LIFBASE Simulation of NO

- LIF Excitation Scan between 226.6-227 nm, 1 atm, 300 K
  - Lines all have band names (O, P, Q, R, S) and N’s or J’s (rot quant #)

LIFBASE freeware by J. Luque, SRI International
lifbase@yahoo.com
LIF Temperature Measurements

- Rotational Temperature
  - Ratio of 2 or more rotational lines
  - Describe general case
  - Example in a turbulent base flow

- Vibrational Temperature
  - Ratio of 2 or more vibrational lines
  - Example of freestream characterization
    - Boltzmann plot, where more than 2 lines used

- Translational Temperature
Rotational Lines of NO, 300 K

- LIF Excitation Scan between 225-227 nm, 1 atm, 300 K
Rotational Lines of NO, 600 K

- LIF Excitation Scan between 225-227 nm, 1 atm, 600 K
LIF: Rotational Temperature, $T_{rot}$

- Recall:

$$S_{LIF} \propto \chi_s f_B(T) B_{12} I G(\chi_s, P, T, U) \Phi(\chi_s, \chi_i, P, T) t_{det}$$

- Obtain LIF or PLIF on two different rotational lines of a molecule: $i$ and $j$. Take ratio, $R$:

$$\frac{S_{LIF,i}}{S_{LIF,j}} = R = C \frac{B_{12,i} E_i (2J_i+1) \exp[-F_{J,i}/k_B T_{rot}]}{B_{12,j} E_j (2J_j+1) \exp[-F_{J,j}/k_B T_{rot}]}$$

- Where:
  - $C$ is a constant
  - $E$ is the laser energy (in mJoules)
  - $J$ is the rotational quantum number
  - $F_{J}$ is the energy of the state
  - $k_B$ is Boltzmann’s constant
  - $\Omega, \chi_s, \eta, G, V, N_T$ and $\Phi$ (including $Q_{21}$) cancel out!
LIF: Rotational Temperature, $T_{rot}$

- Solve for $T_{rot}$:

$$T_{rot} = \frac{-\Delta E_{rot}}{k_B \ln \left( \frac{C R B_{12,j} E_j (2J_j+1)}{B_{12,i} E_i (2J_i+1)} \right)}$$

- Where:

$$\Delta E_{rot} = (F_{J,i} - F_{J,j})$$

- Temperature sensitivity:

$$\frac{\delta T_{rot}}{T_{rot}} = k_B T_{rot} \frac{\delta R}{\Delta E_{rot} R}$$

- Suggests to maximize $\Delta E_{rot}$ (as long as signals still strong) to minimize error in temperature, $\delta T_{rot}$
  - Should choose widely separated states: e.g. $J = 3.5$ & $35.5$
Typical Strategies for $T_{rot}$

- Typically two approaches:
  - Steady laminar flow
    - Obtain images on one J, then scan laser to another J
    - Ratio images, determine temperature
  - Turbulent flow
    - Two lasers, two cameras (Cumbersome! Expensive!)
    - Acquire two images nearly simultaneously, different J’s
    - Need to do this because ratio is a nonlinear function of temperature:
      \[
      \frac{S_{\text{LIF},i}}{S_{\text{LIF},j}} = R = C \frac{B_{12,i}E_i (2J_i+1)\exp[-F_{J,i}/k_BT_{rot}]}{B_{12,j}E_j (2J_j+1)\exp[-F_{J,j}/k_BT_{rot}]}
      \]
    - Typical single-shot temperature measurement precision is $\sim20\%$ at flame temperatures (Seitzman, 1994)
    - If you use 1 laser/1 camera, $\rightarrow$ bias errors in turb. Flows
      - Average many measurements to reduce uncertainty
Single laser/camera for $T_{rot}$ in turbulent flow

- Lachney and Clemens (1998) used 1 laser / 1 camera to map mean $T_{rot}$ in a base flow.
- NO seeded $N_2$ at Mach 3
- Chose: $J = 8.5$ and $J = 10.5$
Single laser/camera for $T_{rot}$ in turbulent flow

- Lachney and Clemens (1998):

Turbulent supersonic wake flow temperature measurement
Agreed with temperatures inferred from probe measurements to within 11%

Vibrational Bands of NO

• Three vibrational bands: $T = 1000 \text{ K}$
  – Vibrational bands have quantum number, $v$

$v''=0$  
$v''=1$  
$v''=2$
Vibrational Bands of NO

• Three vibrational bands: $T = 2000$ K
Vibrational Temperature \( T_{vib} \) Measurement

- A similar approach can be made to obtain vibrational temperature measurements
  - Typically excite the same rotational line (\( J \)) in 2 or more vibrational bands (\( F_j \approx \text{constant} \))
  - Can do 2 line measurements as before
  - Can use a Boltzmann Plot:
    - Graph:
      \[
      \ln \left[ \frac{S_{\text{LIF},i}}{B_{12,i}E_i(2J_i+1)\exp[-F_{J,i}/k_BT_{\text{rot}}]} \right] \]
    - Slope is:
      \[-1/(k_BT_{vib})\]

If \( F_j \approx \text{constant} \) then \( T_{vib} \) can be determined independent of \( T_{\text{rot}} \)
Vibrational Temperature $T_{vib}$ Measurement

- Vibrational temperature measured in a nozzle exit flow verifying vibrational nonequilibrium ($T_{vib} \neq T_{rot}$)

$T_{rot} \approx 400 \text{ K and decreasing with distance}$

Translational Temperature

• Can measure $T_{\text{trans}}$ (and $P$) from width and shapes of spectral lines

• Spectral lines have a shape
  – Molecular motion leads to:
    • **Doppler Broadening** (inhomogeneous)
    • Gaussian shape
    • FWHM: $\Delta \nu_D = \frac{\nu_0}{c} \sqrt{\frac{8\ln(2)k_BT}{m}}$
  – Collisions lead to:
    • **Pressure Broadening** (homogeneous)
    • Lorentzian shape
    • FWHM: $\Delta \nu_P = \frac{P}{101,325} \left[ 2\gamma \cdot \kappa_i \cdot \left( \frac{295}{T} \right)^{0.75} \right] + ...$
  – Combination is: **Voigt**
    • Convolution (if $\Delta \nu_P, \Delta \nu_D$ comparable)
    • Formulas in manuscript

Translational Temperature

- If using a very narrow linewidth laser...
  \[ \Delta \nu_L \ll \Delta \nu_P, \Delta \nu_D \]
  ...can neglect laser width
  - Semiconductor diode laser
- Scan laser frequency across a transition
  - Argon atom at 810.4 nm
  - Turbulent inductively coupled plasma (ICP) torch
- Fit measured LIF spectrum
  - Have homogeneous (Stark) and Doppler broadening
  - Determine \( n_e \) and \( T \)

Species Concentrations

• Problem: How to deal with unknown $Q_{21}$?

• Solutions:
  – Saturated LIF: $(W_{12} + W_{21}) \gg (Q_{21} + A_{21})$
    • $Q_{21}$ is negligible compared to $W$’s
    • Hard to achieve
  – Predissociation
    • $Q_{pre} \gg Q_{21}$
  – Measure $\tau_{\text{LIF}}$
    • Determine $Q_{21}$ from $\tau_{\text{LIF}}$
  – Measure other species present and predict $\tau_{\text{LIF}}$
    • Raman/Rayleigh/LIF (Sandia and DLR)
  – Counter-propagating beams, take ratio (Versluis, 1997)

• Potential problems: absorption, rad. trapping
LIF Advantages/Disadvantages

• Advantages
  – Relatively easy to make planar measurements (PLIF)
  – Provides flow visualization simultaneously
  – Relatively easy to perform
  – Can probe many different parameters (T, V, concentration)
    • Velocity measurements (MTV) can have with 1-2% precision

• Disadvantages
  – Precision of single-shot temperature measurements (~20%) is not good compared to CARS (2-3%) or LITA (1%)
  – Difficult to do quantitative concentration measurements, especially planar
LIF Theory: Atoms

- Two level model
  - e.g. Hydrogen atom
- Photon energy = $h\nu$
  - $c = \lambda\nu$; wavenumbers $= \bar{\nu} = 1/\lambda$ cm$^{-1}$

Hydrogen atom energy levels
(from Wikipedia, “hydrogen spectral series”)
http://creativecommons.org/licenses/by-sa/3.0/deed.en

$\lambda = 656$ nm
$\nu = 4.6\times10^{14}$ Hz
$\bar{\nu} = 15,240$ cm$^{-1}$
Introduction to LIF Velocimetry Techniques for Hypersonic Nonequilibrium Flows

Brett Bathel, NASA Langley Research Center, Virginia, USA
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Craig Johansen, The University of Calgary, Canada

U-Velocity (m/s)

NASA and The Australian National University

Texas A&M
Outline: Velocimetry Techniques

• LIF-Based Velocimetry Techniques
  – Doppler shift
    • Based on laser frequency relative to absorption line
  – Molecular tagging velocimetry (MTV)
    • aka Flow tagging velocimetry
    • Time of flight
    • Single-laser method requires lifetime long enough for flow to move while light is being emitted
  – Summary

• Other Techniques
  – Particle: Particle Image Velocimetry (PIV), Laser Doppler Velocimetry (LDV)
  – Interference/Scattering: Laser-Induced Thermal Acoustics (LITA)
  – Schlieren: Density Tagging Velocimetry (DTV)
  – Scattering: Rayleigh
Doppler Shift Velocimetry
Doppler Shift Velocimetry

• The Doppler shift:
  \[ \Delta \nu = \frac{U}{c} \nu_0 \]

• Can be used to measure velocity with LIF
  • Relative shift between laser and absorbing molecules
  • Angle of detection does not matter for LIF

• The overlap integral, \( G \), which describes the overlap of the laser’s spectrum with a line
  • \( L_\nu \) is laser’s spectral shape, typically modeled as Gaussian or Lorentzian
  • \( Y_\nu \) is the transition’s absorption line shape, can be shifted by Doppler shift
    \[ G = \int L_\nu Y_\nu d\nu \]

Wikipedia “Doppler Shift”
http://creativecommons.org/licenses/by-sa/3.0/deed.en
Doppler-based LIF Velocimetry

- Direct laser sheet into the flow
- Acquire images or signal at different laser frequencies
  - Choose frequencies near an absorption line
  - Measure absorption lineshape at each point
  - Reference data acquired simultaneously
- Measure from two different directions to get two different velocity components
- Do need to consider pressure shift

R. Hruschka, S. O’Byrne, and H. Kleine, “Two-component Doppler-shift fluorescence velocimetry applied to a generic planetary entry probe model,” Experiments in Fluids, 48, pp. 1109-1120, 2010
Doppler-based LIF Velocimetry

- **Self-referenced tuning Doppler velocimetry**
  - Does not require reference cell measurement
  - \( v_0 = \frac{v_f + v_r}{2} \) \( \rightarrow U = \frac{c}{\cos \theta} \cdot \frac{(\Delta v/2)}{([v_f + v_r]/2)} \)
  - Laser passed through measurement volume, followed by a delay line that returns beam along original path
  - Requires high-speed measurement device (e.g. photomultiplier tube) to resolve forward and return signals

- **Fixed frequency (single-shot)**
  - Potential for time resolved velocity
  - Less accurate – estimating Doppler shift with few measurements

---


Doppler Shift Velocimetry

• Benefits
  – Capable of providing 1- or 2-component velocity maps
  – Relatively easy to implement

• Drawbacks
  – Typically not time resolved
  – Typically requires reference measurement
  – Spectral shift resulting from increased pressure needs to be accounted for
  – Requires a gas ‘seed’ to either be naturally present or introduced into the flow
Molecular Tagging Velocimetry
Single-Laser MTV

- Biacetyl (Hiller et al, 1984; Koochesfahani, 2007)
- Acetone (Lempert, 2002)
- NO (Danehy, 2003; Hsu, 2009; Bathel, 2011)
- I₂ (Balla, 2013)
- N₂ using FLEET (*Femtosecond laser electronic excitation tagging*) (Michael, 2011)
  - Does not require seeding
  - Does require an expensive fs laser

- LIF lifetime must be long enough so molecules still emit light after (slightly) moved
LIF Molecular Tagging Velocimetry (MTV)

Single-laser LIF MTV

- Boundary layer: slow moving gas near surface
  - Important: heat transfer, drag, separation, etc.
- Instantaneous measure of 1 velocity component
  - Can be extended to 2 or 3 components

MTV: Delayed Images

- Measurements performed on successive tunnel runs

Single-laser MTV

**Tunable Laser**

Sheet-forming lenses

Lens array

\[ V = \frac{\Delta x}{\Delta t} \]

Flow Direction

Molecules move, fluoresce

Camera captures image

Gas flow

Ground state

Excited state

LIF ~ \( n \) NO

\( \lambda \) and \( \lambda_0 \)

Flow Direction

\( t_{E1} \), \( \Delta t_{D2} \), and \( t_{E2} \)
**Single-laser MTV**

- **Velocity Measurement**
  - Instantaneous (<1 μs), single-component measure of 25 profiles simultaneously
  - Developed thorough uncertainty analysis methodology
  - Data used in subsequent CFD study by Iyer et al. of Univ. of Minnesota (AIAA 2011-566)

Single-laser MTV

• **Analysis**
  - Uncertainties in mean: as good as 3% of freestream (~1000 m/s) for 38 images
  - Modeled error from intensity decay, exposure duration, motion blur
  - Error from velocity component parallel to MTV profiles quantified

• **Study conclusions**
  - Velocity gradients can bias measurement
  - Scatter off of the model surface limited proximity of measurement to the wall
  - Limited to low-pressure conditions
  - Need higher pressure capability for higher Reynolds number required to study laminar-to-turbulent transition at least on this short model

Errors up to ~15% of measured mean velocity
Single-laser MTV: FLEET

• Simple principle:
  – Works with N$_2$ seed
  – Femtosecond laser is focused down to a line or spot
  – Gas glows for 10’s of μs

• Originally developed at Princeton:
  – Air jet at room temperature, atmospheric pressure
  – Non-linear process

• Recently applied to transonic cryogenic flow at NASA Langley
  – Tracking of spot provided 2-D velocimetry
  – ~1 m/s accuracy and precision


Single-laser MTV

• Benefits
  – Instantaneous measurement
  – Capable of providing velocity information along a line (1-component) or at grid points (2-component)
  – ‘Seedless’ methods available
  – Relatively simple to setup

• Drawbacks
  – Reduced spatial resolution compared to Doppler shift approach
  – Operational limits often dictated by fluorescence lifetime
  – Potential for model damage
  – Potential for altering thermodynamic state of gas
Multilaser MTV

• Typically, one laser generates a line, series of lines or a grid pattern by, ionization (LEI\textsuperscript{126-128}), vibrational excitation (RELIEF\textsuperscript{129-131}), photolysis, bleaching or other process. Additional laser(s) read out pattern.
  – Example: Excimer laser at 193 nm+N\textsubscript{2}+O\textsubscript{2} \rightarrow NO
  – \textit{Air Photolysis and Recombination Tracking (APART)}
    • Dam et al, Optics Letters, 26 (1), pp. 36-38 2001

• A list of partner species used in the photolysis writing and reading process includes:
  \[ \text{H}_2\text{O}-\text{OH}_\cdot\text{N}_2\text{O}-\text{NO}, \text{O}_2-\text{O}_3, \text{N}_2/\text{O}_2-\text{NO}, \text{NO}_2-\text{NO} \]

• Method can use air constituents (\text{N}_2/\text{O}_2, \text{O}_2, \text{N}_2) or can be seeded (\text{H}_2\text{O}, \text{N}_2\text{O}, \text{NO}_2, \text{Na}, etc.).
  – We have used NO\textsubscript{2} \rightarrow NO to study transition
Multilaser MTV

• NO to NO Photolysis
• NO LIF excitation

(for details of velocimetry method, see Bathel et al, AIAA-2011-3246 and others incl. TAMU\textsuperscript{149}, OSU\textsuperscript{150}, etc.)
Velocimetry: 1-mm Tall Trip (centerline)

- Transition-to-turbulence study (Bathel et al. AIAA-2011-3246)
  - Reynolds number requirement necessitated higher operating pressures
  - Signal lifetime too short for single-laser NO LIF MTV
3 laser MTV: measure \( u, v, T \)

- Texas A&M has used 3 laser technique with crossed beam pattern for 2-component velocity and temperature in an underexpanded \( \text{N}_2 \) jet flow with \( \text{NO}_2 \):
  - VENOM: vibrationally excited nitric oxide monitoring
  - Excite to \( v' = 1 \) state

Multilaser MTV: Unseeded

- **Air Photolysis And Recombination Tracking (APART)**
  - Nitric oxide generated in unseeded air via dissociation by UV excimer laser beam
  - NO then probed with LIF excitation wavelengths

- **Raman Excitation and Laser-Induced Electronic Fluorescence (RELIEF)**
  - $O_2$ vibrational excitation via Raman pumping
  - UV Excimer laser used to probe 1$^{st}$ vibration state of oxygen
  - Works for flows where $T < \sim 750 \text{ K}$

---

Multi-laser MTV

• Benefits
  – Capable of providing instantaneous velocity along a line (1-component) or at grid points (2-component)
  – Several ‘seedless’ methods available
  – Not limited by fluorescence lifetime (works in high \( P \))

• Drawbacks
  – Reduced spatial resolution compared to Doppler shift approach
  – More complicated setup – requires multiple lasers
  – Potential for model damage
  – Altering thermodynamic state of gas
Summary
Velocimetry Techniques

• Introduced three fluorescence-based techniques
  – Doppler shift velocimetry
  – Single-laser molecular tagging velocimetry
  – Multi-laser molecular tagging velocimetry

• Provided representative examples for each of the techniques

• Discussed benefits and drawbacks for each approach

• Following presentation will provide a more in-depth discussion of laser-induced fluorescence used for many of these MTV techniques.
Backup Charts
Experimental Setup: Top View

Velocity ~ 3000 m/s; Mach Number = 7, laminar boundary layer

T2 Free Piston Shock Tunnel, ANU

- Thermometry laser sheet: 5 mm wide, 0.7 mm thick
- Velocimetry laser sheet: 3 mm wide, 0.2 mm thick

Dimensions:
- 120 mm
- 80 mm
- 50 mm
- 15 mm
Average of Single-Shot Measurements

- Freestream velocity is uniform at 3035±60 m/s.
- 95% boundary layer thickness is 1.4±0.1 mm.
- Single shot measurement precision: ~60 m/s out of ~3000 m/s (2%)
  - spatially averaged uncertainty (freestream region) ~100 m/s (3%)
Three-Laser MTV (NO$_2$ → NO velocimetry)

(for details of velocimetry method, see Bathel et al, AIAA-2011-3246 and others incl. TAMU$^{149}$, OSU$^{150}$, etc.)

NO$_2$ + 355 nm → NO

Write lines of NO into NO$_2$ seeded in the flow
Flow Visualization: No trip

- Flow appears laminar when no trip is present

\[ PA = 20^\circ \]

\[ \text{mid-Re} \]

\[ M_e \approx 4.2 \]
Velocimetry: 1-mm Tall Trip (centerline)

- Velocity profile is full near flat plate with a deficit near edge of BL
  - Note: 2x lower flowrate in this run compared to no-trip case previously shown.
- U’ data has increased to peak ~250 m/s (3x larger than laminar case).
- Shape of U’ profile changes slightly with distance downstream.
Velocimetry: No Trip

Data formatting:
- Center of the data point is mean velocity; Width is uncertainty in mean
- Standard deviations shown in red (instrument error ~2% of max U was subtracted)

Blasius-like boundary layer profiles observed (to within 100 μm of wall)
- Deficit near edge is likely caused by seeding in zero velocity gas into BL (see Johansen et al)
- $U' \sim 80$ m/s at maximum. Peak $U'$ is ~ 0.7 mm above surface.
• 4.5 mm profiles show profiles most different from laminar
• Flow becomes more laminar far from centerline (similar to flow vis)
  – U’ drops back to ~80 m/s
Comparison of $U$ for different trip heights

- No Trip
- 0.53-mm Trip
- 1.0-mm Trip

- $0.53$ mm trip profile is between no and 1-mm but no inflection point.

Re$_{kk} \approx 400$

Re$_{kk} \approx 2000$
Comparison of $U'$ for different trip heights

- **No Trip**
- **0.53-mm Trip**
- **1.0-mm Trip**

- 0.53 mm trip $U'$ peak much closer to plate.
Three-laser MTV: uncertainty & design

• **Analysis**
  - Uncertainty for high s/n data
    - **Mean**: 1% of edge velocity (~1300 m/s) in 200 images
    - **Single-shot**: 1-2% of edge velocity
  - Measurement within 100 μm from wall

• **Tradeoffs for experiment design**
  - Accuracy and precision improve with probe delay
  - Spatial resolution worse with longer probe delay
    - Can use longer delay for slow flow
  - Current configuration requires relatively large blowing rates for adequate signal-to-noise
    - May be significant wall-normal velocity component

Data obtained at static, low pressure conditions
Intro to Rayleigh and Raman Spectroscopy for in Hypersonic Nonequilibrium Flows

Paul Danehy, NASA Langley Research Center, Virginia, USA
Rayleigh and Raman Scattering

• When light passes through a gas:
  – LIF is a *resonant* absorption/emission process
  – Mie, Rayleigh and Raman are *scattering* processes
    • Mie Scattering: $d \geq \lambda$ (\(d\) is the particle size)
    • Spontaneous Rayleigh and Raman scattering: $d \ll \lambda$
• Will explain Rayleigh and Raman two ways
  – Physical interpretation
  – Classical description
  – (Not going to discuss quantum treatment)
Rayleigh Scattering

• Rayleigh scattering:
  – Electric field causes electron cloud to oscillate with respect to the nucleus: induced dipole

http://www.timkelf.com/Research/ResearchSERS.html

– An oscillating dipole acts like an antenna: radiates!
  • Radiation is perpendicular to oscillation
Many Particle Scattering

- A plane-wave perturbs many particles: they radiate
  - Interfere constructively in direction of propagation
  - Interfere destructively in other directions

- If exact same number of particles everywhere in gas, destructive interference would give no side scatter
  - But random statistical variation in particle concentration: deconstructive interference is incomplete: Rayleigh Scattering!

Rayleigh Scattering

• Very weak process
  – 1 photon in 0.1 million scatters / meter at STP
• Wavelength dependence: $1/\lambda^4$

• Causes blue sky and red sunsets
  – Mie scattering from aerosols also contributes

Rayleigh scattering in the atmosphere after sunset, picture taken over the ocean, at 500m altitude. [http://ms.wikipedia.org/wiki/Selerakan_Rayleigh](http://ms.wikipedia.org/wiki/Selerakan_Rayleigh)
Raman Scattering

- Similar to Rayleigh scattering but molecules gain or lose energy during scattering process
- Raman x1000 lower probability than Rayleigh

Energy Level Diagrams:

- Energy stays same
- Molecule gains energy
- Molecule loses energy
Raman Scattering

- Raman scattering results in a frequency shift
  - Molecule vibrating at frequency $\nu_{\text{mol}}$
Rayleigh and Raman Scattering

- **Energy level diagram:**
  - **Stokes Raman:** energy absorbed by molecule
  - **anti-Stokes Raman:** energy lost by molecule

- **Initial state must not have been a ground state**
Rayleigh and Raman Spectra

- Rayleigh: near laser’s wavelength
- Raman: frequency shift depends on molecule, state (sensitive to concentration and temperature)
  - Rotational Raman
  - Vibrational Raman
Scattered intensity, \( I \), is proportional to the square of the induced dipole moment, \( \vec{\rho} \) :

\[
\vec{\rho} = \varepsilon_0 \alpha \vec{E}
\]

where \( \varepsilon_0 \) is the permittivity of free space, \( \alpha \) is the molecular polarizability and \( \vec{E} \) is the incident electric field given by:

\[
\vec{E} = \vec{E}_0 \cos(\omega_0 t)
\]

where \( \vec{E}_0 \) is the amplitude of the electric field, \( \omega_0 \) is the frequency of the laser light and \( t \) is time.
Rayleigh and Raman Theory 2

• Polarizability, $\alpha$, depends on internal structure
  – varies with time during vibrational oscillations at the natural frequency of the molecule, $\omega_v$
  
  \[ \alpha = \alpha_0 + \left( \frac{\partial \alpha}{\partial Q} \right)_0 dQ \]

  where $dQ$ is small displacement about equilibrium positions which occurs during normal vibration

  \[ dQ = Q_0 \cos(\omega_v t) \]
Rayleigh and Raman Theory 3

• Substituting previous equations into \( \hat{p} = \varepsilon_0 \alpha \vec{E} \):

\[
\hat{p} = \left[ \alpha_0 + \left( \frac{\partial \alpha}{\partial Q} \right)_0 Q_0 \cos(\omega_v t) \right] \varepsilon_0 \vec{E}_0 \cos(\omega_0 t)
\]

• Expanding and using trig identity:

\[
\hat{p} = \alpha_0 \varepsilon_0 \vec{E}_0 \cos(\omega_0 t) + \frac{1}{2} \left( \frac{\partial \alpha}{\partial Q} \right)_0 \varepsilon_0 Q_0 \vec{E}_0 \left[ \cos(\omega_0 - \omega_v) t + \cos(\omega_0 + \omega_v) t \right]
\]

• Resulting induced dipole moment (and scattering) is at three frequencies

• Amplitude is usually determined empirically:

\[
\left( \frac{\partial \sigma}{\partial \Omega} \right)_{zz} \equiv \frac{I_{zz}^\Omega}{NI}
\]

Differential Cross Section

(varies by molecule and with I but not with P, T)

(zz indicates polarization of laser and detection)

\[
I_{zz}^\Omega = \left( \frac{\partial \sigma}{\partial \Omega} \right)_{zz} NI
\]

scattered power per solid angle
diff. cross section
number density
laser irradiance
• Selection Rules: Raman Activity
  – Not every molecule or vibrational mode produces Raman
  \[ \vec{p} = \alpha_0 \varepsilon_0 \vec{E}_0 \cos(\omega_0 t) + \frac{1}{2} (\frac{\partial \alpha}{\partial Q})_0 \varepsilon_0 Q_0 \vec{E}_0 [\cos(\omega_0 - \omega_v) t + \cos(\omega_0 + \omega_v) t] \]
  – Amplitude of Raman is proportional to the magnitude of: \( (\frac{\partial \alpha}{\partial Q})_0 \)
  – Polarizability, \( \alpha \), must change during vibrations to be Raman active
  – Raman active:
  – Raman inactive:
Rayleigh and Raman Theory 5

- Rayleigh Scattering is at or near the laser’s wavelength.
  - Doppler broadened ($\sim T^{1/2}$)
  - Can be Doppler shifted ($\sim V$)
  - Signal proportional to $N$ ($\sim \rho$)
- Can potentially measure these simultaneously
  - Requires high spectral resolution

$$I_{zz}^\Omega = \left( \frac{\partial \sigma}{\partial \Omega} \right)_{zz} NI$$
Rayleigh and Raman Examples

- Rayleigh
  - Velocimetry, multi point
  - $V, T, \rho$, single point
  - $V, T, \rho$, imaging
  - $\rho$ measurement (and infer $T$)

- Raman
  - Concentration
  - Temperature
Rayleigh Velocimetry

• Rayleigh scattering velocimetry can measure selected velocity components
  – Measured component is bisector between incident laser and collection optics

  \[ V_1 = \frac{k_{laser} + k_{signal}}{2} \]

  \[ V_2 = \frac{k_{laser} - k_{signal}}{2} \]

  Wave vector:
  \[ k = \frac{2\pi}{\lambda} \]

– Can measure multiple velocity components by adding additional detection angles or laser beams

Rayleigh Velocimetry

- Rayleigh scattering velocimetry has been performed different ways, always requiring a high resolution device to resolve the Doppler shift
  - $I_2$ filter in front of CCD
    - Imaging capability
    - Limited dynamic range
  - Fabry Perot etalon
    - PMT based (faster)
    - CCD based (multi-point)
  - Combined $I_2$ filter and Fabry Perot etalon

- See manuscript for references
Rayleigh Velocimetry using Fabry-Perot Etalon

- Velocimetry using a Fabry Perot Interferometer (FPI) with CCD camera

Rayleigh Velocimetry using Fabry-Perot Etalon

measurement volume

collection optics

one-component system

reference

F-P Etalon is two planar, separated mirrored surfaces

Spatial and Spectral Info

Reference Frequency

CCD Camera

Rayleigh Scattering Image Processing


• Significant image processing is required
Rayleigh Scattering Velocity Results

- Rayleigh scattering in a large scale (6 cm diameter) Mach 1.6 $H_2$-air combustion heated jet operating at Mach 5.5 enthalpy at NASA Langley

Velocity precision of ~40 m/s out of 1200 m/s, (3%)
The dynamic range of the instrument was ~3000 m/s
- precision 1% of dynamic range

Rayleigh Scattering: T, V, ρ

- Continuous laser excitation
  - 10 W at 532 nm
- Fiber optic collection
- Data rate: 10 kHz
- Single point measurement

Rayleigh Scattering: T, V, ρ

- Heated, 2” (50 mm) diameter axisymmetric near-sonic jet at NASA Glenn Research Center

Rayleigh Velocimetry ($I_2$ filter)

- Instead of an etalon, use $I_2$ filter $\rightarrow$ 2D imaging

- Gas cell, filled with low-pressure $N_2$ plus some $I_2$ crystals; control temperature to determine absorption
- Scan Nd:YAG laser frequency (or fixed)


Rayleigh Imaging of $T$, $V$, $\rho$ (or $P$)

- Direct YAG laser sheet into a Mach 2 jet

- Scanned laser frequency, determine $T$, $V$, $\rho$ (report $P$) based on measured spectrum at each pixel

- Same method can be used for velocimetry from particles (usually fixed frequency, multiple detection angles)
  - Planar Doppler Velocimetry (PDV) or Doppler Global Velocimetry (DGV)

Rayleigh Scattering: $\rho$

- Rayleigh scattering has a spectrum:
  - Sensitive to $T$, $V$, $\rho$
  - Prior examples used Fabry Perot Etalon or $I_2$ cell to observe spectrum
  - These devices reject signal, making them less sensitive detectors of $\rho$.
- Collect all of the scattering
  - Less equipment/less setup/simpler
  - Bigger signal
  - Can do single point or imaging
  - Only sensitive to $\rho$.
    - (If you know $P$ and composition you can convert $\rho$ to $T$.)

Using a UV laser (e.g. ArF at 193 nm) allows measurements to be made at low pressures (e.g. 1/300 atmospheric density)

Raman Spectroscopy

- Raman spectrum obtained in a CH$_4$-air flame:
  - Average of 500 pulses using stretched 0.5 J/pulse, 532 nm
  - Stretch 10 ns pulse to 500 ns to avoid laser-induced breakdown

- Can measure species (N$_2$, CO, CO$_2$, H$_2$, H$_2$O) from such spectra & temperature from Stokes/anti-Stokes

Figure courtesy of Jun Kojima, NASA Glenn Research Center (Jun.J.Kojima@nasa.gov)
Raman Concentration Measurement
(and Rayleigh Temperature and LIF concentration)

• Example of Raman concentration measurements in a subsonic turbulent CH₄/air flame at Sandia National Laboratories, California
  – 4 Nd:YAG lasers at 532 nm to produce 1.8 Joules/pulse, focused to a point

\[ \chi_i \text{ precision } \sim 0.7\% \text{ to } 7.5\% \]
\[ T \text{ precision } \sim 0.75\% \]

• Raman/Rayleigh/LIF line imaging (\( \sim 10 \) pixels / mm along the 6-mm-long probe volume)
  – N₂, O₂, CH₄, CO₂, H₂O and H₂ from Raman, CO from 2 photon LIF
  – Temperature from Rayleigh density measurement (idea gas law)

Raman Temperature Measurement

- Several ways to measure temperature with Raman
  - none as precise as CARS (3%)

- Rotational Temperature from pure-rotational Raman

- Vibrational temperature measurements
  - Only good above 700 K
  - Stokes / anti-Stokes vibrational Raman
    - Low resolution, so can measure concentrations at same time
    - ~20% precision in measurements along a line (Wehrmeyer, 1996)
  - Spectrally resolved vibrational band (Sharma et al, 1993)

(see Kojima, 2008)
Raman Temperature Measurement

- Raman temperature measurement from spectrally resolved vibrational N\textsubscript{2} band.
  - Excited with KrF Excimer laser 0.25 J at 248 nm (25 ns pulse)

- Single shot precision \(\sim 5\%\) (not explicitly stated)
  - More precise than Stokes/anti-Stokes but cannot measure species concentrations with same instrument.

Rayleigh Scattering: $\rho$

- When precise measurements are required, high S/N is needed
  - Use high powered lasers, focused to a point
    - If too high: laser-induced breakdown
- Sandia, Livermore, Calif.:
  - Raman/Rayleigh/LIF line imaging at $P = 1$ atm
  - 4 double-pulse Nd:YAG lasers: 1.8 J/pulse
  - Camera images Rayleigh along line
    - ~10 pix / mm along 6-mm-long probe volume
  - $N_2$, $O_2$, $CH_4$, $CO_2$, $H_2O$ and $H_2$ from Raman
  - CO from 2 photon LIF
  - Temperature from Rayleigh density, $\rho$,
    - Need composition to determine $\left(\frac{\partial \alpha}{\partial Q}\right)_0$
    - If known $P$, idea gas law give $T$
    - $T$ precision reported: ~0.75%
    - ($\rho$ precision is probably same)
  - Cutting edge MHz laser: 40x lower energy (Jiang, 2011)
Advantages and Disadvantages: Rayleigh & Raman

• **Advantages:**
  – No seeding required
  – Only one color of laser used (simplicity)
  – Multiple properties measured at once
    • $T, V, \rho$ for Rayleigh
    • $T$, many species for Raman
    • Can do Raman and Rayleigh together and with LIF

• **Disadvantages:**
  – Weak signal:
    • Requires very high power laser
      – stretched to avoid laser induced breakdown
    • Requires large windows, big, close collection optics
    • Usually single point or line measurements
  – Temperature less accurate & precise than CARS
Intro to Coherent anti-Stokes Raman Spectroscopy (CARS) for Hypersonic Nonequilibrium Flows

Andrew Cutler, The George Washington University, USA
Paul Danehy, NASA Langley Research Center, Virginia, USA
Outline

• Brief introduction to nonlinear optics
• Introduction to CARS and basic theory
• NASA / GWU CARS System
  – Temperature and composition measured in UVa dual mode scramjet
  – Thermometry shows vibrational nonequilibrium
• CARS in a non-thermal plasma
• Concluding remarks
Nonlinear Optics

• First, a few words about nonlinear optics
  – Conservation of energy
  – Conservation of momentum
  – Wave equation from Maxwell’s equations

• Second Harmonic Generation as an Example
  – $2^{\text{nd}}$ order nonlinearity (solid)
  – CARS is a $3^{\text{rd}}$ order nonlinearity (gas)
– **Second Harmonic Generation (SHG)**

- 1064 nm → 1064 nm
- **Second-order non-linear crystal** → 532 nm

– Solved using the Wave Eqn:

\[
\nabla^2 E - \frac{1}{c^2} \frac{\partial^2 E}{\partial t^2} = \mu_0 \frac{\partial^2 P_{NL}}{\partial t^2}
\]

– Assume SVEA and 1st Born Approx:

\[
I_{\omega_2} \propto \frac{d^2 P_{\omega_1}^2 L^2}{A^2}
\]

– *d* is a coefficient, *P* is power, *L* is length, *A* is area
Non-linear Susceptibility

- Non-linear effects: Intense electric fields of one frequency can generate a $P$ at another

Phase Matching

• What is Phase Matching?
  – *Ensuring that the light wavefronts ‘match up’.*

  • Dispersion causes deconstructive interference
  • New photons generated are out of phase with previous ones: resulting in loss
  • For SHG there are tricks to make it phase matched

• Conservation of momentum: phase matching
• Conservation of energy: $\omega_2 = 2\omega_1$
What is CARS?

Broadband N₂ CARS

Spectrally-broad red beam  +  Spectrally-narrow green beams  =  Single-shot blue CARS spectrum
• Lasers: 2 Green (532 nm) and 1 Red (607 nm)
  – Frequency difference between Green and Red
    Probes $N_2$ vibrational Raman Shift

  $N_2 \uparrow \omega_{P1} \downarrow \omega_S \uparrow \omega_{P2} \downarrow \omega_{A-S}$

• Result: Blue signal beam at 473 nm.
  – Spatially, spectrally, temporally filter this signal
    • Good technique for luminous flows
  – Send to spectrometer equipped with CCD camera
  – Measured CARS spectra is best fit to a library of
    theoretical spectra on a single-shot basis (10 ns)
It is straightforward to compute the CARS phase matching angles:

\[ k_{p1} + k_{p2} = k_S + k_{A-S} \]

<table>
<thead>
<tr>
<th>N2 cars</th>
<th>adjust input</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>lambda</td>
</tr>
<tr>
<td>stokes</td>
<td>607</td>
</tr>
<tr>
<td>pump 2</td>
<td>532</td>
</tr>
<tr>
<td>pump 1</td>
<td>532</td>
</tr>
<tr>
<td>anti stokes</td>
<td>473.4956</td>
</tr>
</tbody>
</table>

Different molecules require different angles (can get multiple signals at different spatial locations: Dual-Stokes)

N2 Raman = 2322.528 cm⁻¹
(nominal N2 = 2330 cm⁻¹)
CARS Phase Matching Geometries

- **Collinear CARS:**
  - Poor spatial resolution

- **(Planar) BoxCARS:**

- **Folded BoxCARS:**
  - Best spatial resolution (1.5 mm x 0.1 mm x 0.1 mm) but lower signals and affected by beam steering from turbulence
CARS Theory 1

- **Non-linear effects:**
  - Intense electric fields of one frequency can generate a $P$ at another
  
  $$ P = \varepsilon_0 (\chi E + \chi^{(2)} E^2 + \chi^{(3)} E^3 + \ldots) $$

  - $\chi^{(2)} = 2$nd order susceptibility
    • Only media lacking a centre of symmetry (ie, no gases, liquids)

  - $\chi^{(3)} = 3$rd order susceptibility
    • All dielectric media

  - Generally ($\chi E \gg \chi^{(2)} E^2 \gg \chi^{(3)} E^3$)

CARS Theory 2

• Polarization generated at CARS signal frequency:
  \[ P^{(3)}(\omega_{\text{signal}}) = \varepsilon_0 \chi_{\text{CARS}} E(\omega_{\text{pump}}) E(\omega_{\text{Stokes}}) E(\omega_{\text{probe}}) \]

• Substitute into the wave equation. Result:
  \[ I_{\text{signal}} \propto I_{\text{pump}} I_{\text{Stokes}} I_{\text{probe}} |\chi_{\text{CARS}}|^2 L^2 \]

• To obtain large signals, want long \( L \), high laser power (tight focus) and strong resonance

\[ \chi_{\text{CARS}} = \sum_j \frac{K_j \Gamma_j}{2\Delta \omega_j - i \Gamma_j} + \chi_{\text{nr}} \text{ where } K_j \propto N \Delta_j \left( \frac{\partial \sigma}{\partial \Omega} \right)_j \]

• \( \Gamma_j \) is damping coefficient, \( N \) is number density, \( \Delta_j \) is the population difference
  – \( N \rightarrow \) concentration; \( \Delta_j \rightarrow \) Temperature sensitivity
CARS Theory 3

- Instructive to graph example N$_2$ spectra:

- N$_2$ is commonly probed with CARS because it is often present and spectroscopy is well known.

- CARS spectrum at 1 atm., 1400 K, v” = 0 band.
  - N$_2$ Q-branch ($\Delta v$=+1, $\Delta J$=0)
  - CARS signal spectrum is convolved with lasers used...
CARS Theory 4

- Effects of temperature (left) and composition (right):

Vibrational “hot band” becomes populated above 700 K

CARS spectra are sensitive to the gas composition through resonant and nonresonant parts
Multi-Species Measurement: Dual-Pump CARS

Conventional Broadband CARS

Dual-Pump CARS (Lucht and co-workers)
Dual-Pump CARS: N$_2$, O$_2$, H$_2$

- Green and Red Probe N$_2$ Raman Shift
- Red and Yellow Probe O$_2$ Raman Shift

Result: Two different spectral regions of Raman Shift appear coincident in the 490 nm CARS beam.

- ‘self calibrating’ compared to other methods
- H$_2$ pure rotational Raman lines present

O’Byrne et al AIAA Journal v. 45, 2007
Typical Dual-Pump CARS Spectra and Fits

- Single-shot spectra obtained in combustor shown with best fit
- Absolute measurement of rotational, vibrational temperature, N\textsubscript{2}, O\textsubscript{2}, and H\textsubscript{2} mole fractions

Measurement obtained:
- In UVa Scramjet (Conf C)
- \(\phi=0.18\), Plane 2, \(z/H=0\)
- in 10 ns (instantaneous)
- at 20 Hz repetition rate
- Measurement volume = 1.7 x 0.2 x 0.2 mm\textsuperscript{3}
NASA/GWU Mobile CARS System

→ Simplifies/speeds set up in facility

Set up in basement below DCSCTF
Features of NASA/GWU Mobile CARS System

- YAG laser plus 2 dye lasers on single cart
- Transmission and receiving optical stages
- Can put system on a truck and moved to facilities
- Measures $T_{\text{rot}}$, $T_{\text{vib}}$, $N_2$, $O_2$, $H_2$ mole fractions at 20 Hz.
  - Quantified accuracy, precision
- Fully automated data acquisition
  - Remote operation of system
  - X-Y (-Z) probe volume traverse capability
  - Input test matrix; then system acquires and automatically saves data for hours until complete
  - Laser power automatically adjusted to prevent saturation effects (detector saturation, Stark broadening, Raman pumping)
  - Beam alignment monitors; remote control alignment
- Beam shaping capability to maintain alignment measurement in turbulent/vibration flows
  - 10x improvement compared to USED CARS
Setup at UVa: Optical System 1

Laser cart

Nd:YAG laser (green)
Broad-band dye laser (red)
Narrow-band dye laser (yellow)

Transmission

Collection

Flame/Facility

Optics focus and cross beam

Optics separate and collimate signal

Beam Relay System
Translates the measurement point
Setup at UVa: Optical System 2

- Detection
- From Laser Cart
- Signal beam
- Transmission
- Exhaust
- X-motion
- CARS windows
- Z-motion
- Y-motion
- Dual-mode Scramjet
- Collection
Transmission stage and test section at UVa
Electrically heated clean air, nominal $T_t = 1200 \text{ K}$, $M = 2$ nozzle
Long test times allow large data sets at steady inflow conditions
Highly turbulent flowfield
Good optical access
Nonequilibrium: CARS $T_{\text{rot}}$ and $T_{\text{vib}}$

$\varphi=0.18$

$T_{N_2\text{vib}}$ observed to be 600 K higher than $T_{\text{rot}}$ in facility freestream; not anticipated before experiment

**Vibrational Temperature**

CARS vibrational $O_2$ and $N_2$ temperatures “lumped” together and used to validate the vibrational nonequilibrium model implemented in VULCAN code by R. Baurle (NASA).


**H$_2$ fuel, Config. C**

**Temperature Mean, Standard Deviation**

**Rotational Temperature**

- $\varphi=0.18$
- $\varphi=0.49$

$T_{\text{rot}}$ higher in free stream for $\varphi=0.49$ due to ram mode

**Standard deviation**

- $\varphi=0.18$
- $\varphi=0.49$
Contours of Mole Fraction $N_2$

- Since inert shows overall mixing

View from right looking upstream
CARS compared with CFD (LES from NC State)

- CARS provides valuable quantitative comparison data
  - *The comparisons are not always this good!*

![Image of CARS and CFD comparison](image_url)

**Figure 9.** Comparison between CARS and O₂ concentrations and RMS fluctuations for ‘0.17’ equivalence ratio.
CARS for nonthermal plasma

- 100 Torr pulsed discharge at Ohio State

- CARS can measure individual state populations for model validation.

Additional Thoughts on CARS

• CARS is a relatively accurate and precise high-temperature and species measurement technique in reacting and nonequilibrium flow
  – Temp. Accuracy 2-3%; Precision 2-3% (Magnotti, 2012)
• CARS can be performed through small windows or slots but need access on 2 sides.
• It is a relatively complicated technique, theoretically and experimentally, though seedless.
  – Takes months to analyze data carefully.
• Is being extended to much faster measurements ~10 kHz with fs CARS
  – Very recently: 2 beam CARS, CARS imaging (Sandia)
• Has been performed using optical fibers to deliver the laser beams, both in ns and ps regimes
Conclusion

• Variety of different molecular-based measurement technologies are available for measuring hypersonic nonequilibrium flows.
  – Can measure temperature, density, velocity, species concentrations, etc.
  – Which is best? Which technique to use?
• Must start measurement campaign with an interview of “customer” to determine the requirements
  – How do different measurement technique capabilities satisfy the requirements?
Conclusion

- Variety of different molecular-based measurement technologies are available for measuring hypersonic nonequilibrium flows.
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  - Which is best? Which technique to use?
- Must start measurement campaign with an interview of “customer” to determine the requirements
  - How do different measurement technique capabilities satisfy the requirements?
    - Also consider practical issues:
      - Experience of the research team
      - Available equipment / budget
      - Schedule, difficulty of method, etc.
  - Rarely a perfect match, but a match can provide the data needed to advance or validate theory or computations
The interview: prior to getting started

- What parameter(s) need to be measured?
- Must multiple parameters be obtained simultaneously to determine correlations?
- What spatial resolution is required?
- Is imaging required or are single-point or line measurements sufficient?
- What temporal resolution is required? (e.g. time required for a single measurement)
- Do measurements need to be time resolved? (e.g. a continuous sequence of data)
- What accuracy is needed?
- What precision is needed?
- What quantity of data is required?
- When is the data needed? Is instant (real-time) data required?
- Where in the flow are measurements required? (inflow, exit, near walls, etc.)
- What type of optical access is available?
- Can (toxic) seed gases be introduced? Will they influence the properties being measured?
- What is the ordered priority of the above requirements?