This paper presents a jig twist optimization study of Mach 0.745 Transonic Truss-Braced Wing (TTBW) aircraft using an in-house developed aero-structural analysis solver VSPAERO coupled to BEAM3D. A vortex-lattice model of the TTBW model is developed, and a transonic and viscous flow correction method is implemented in the VSPAERO model to account for transonic and viscous flow effects. A correction method for the wing-strut interference aerodynamics is developed and applied to the VSPAERO solver. Also, a structural dynamic finite-element model of the TTBW aircraft is developed. This finite-element model includes the geometric nonlinear effect due to the tension in the struts which causes a deflection-dependent nonlinear stiffness. The VSPAERO model is coupled to the corresponding finite-element model to provide a rapid aero-structural analysis. A flight condition corresponding to Mach 0.745 at 42000 ft is selected for the TTBW aircraft jig twist optimization to reduce the drag coefficient. After the design is implemented, the drag coefficient of the twist optimized TTBW aircraft is reduced about 8 counts. At the end, a high-fidelity CFD solver FUN3D is used to validate the design.

I. Introduction

The demand for green aviation is expected to increase with the need for reduced environmental impact of air travel. Most large transports today operate within the best cruise L/D range of 18-20 using the conventional tube-and-wing design. This configuration has led to incremental improvements in aerodynamic efficiency over this past century. In recent years, the use of lightweight materials, such as composites, has been shown to significantly reduce structural weight and trim drag, leading to improved energy efficiency. The Boeing 787 transport is an example of a modern airframe design that employs lightweight structures. High aspect ratio wing design can provide another opportunity for further improvements in energy efficiency.

Research and development of high aspect ratio wing transport designs has placed a greater emphasis on the studies of aeroelasticity and flutter owing to the increase in the wing flexibility as the wing aspect ratio increases. These studies have sought to develop methods and tools for aeroelasticity by laying the foundation for more modern high aspect ratio wing aircraft such as the Transonic Truss-Braced Wing (TTBW). The Subsonic Ultra Green Aircraft Research (SUGAR) TTBW aircraft concept is a Boeing-developed N+3 aircraft configuration funded by NASA Aeronautics Research Mission Directorate (ARMD) Advanced Air Transport Technologies (AATT) project through a NRA (NASA Research Announcement) selection of Boeing Research and Technology as the lead organization. The TTBW aircraft is designed to be aerodynamically efficient by employing an aspect ratio of about 19.55, which is significantly greater than those of conventional aircraft cantilever wings. The main idea is to use truss structures to alleviate the wing root bending moment, so that a significant increase in the wing aspect ratio could be afforded. The main wings are braced at approximately mid-span by two main struts. In addition, two jury struts, one on each wing, provide additional reinforcement. Figure 1 is an illustration of the TTBW aircraft. The additional braced structures will cause some aerodynamic impacts to the wing. The design of a truss-braced wing is a Multidisciplinary Design Analysis and
Optimization (MDAO) process that strives to achieve a delicate balance between aerodynamic and structural efficiencies. The MDAO studies have been conducted at each stage to improve the wing aerodynamics, structural efficiency, and flight performance using advanced N+4 turbofan engines. These MDAO studies have refined the geometry of the wing and configuration layout and have involved trade studies involving minimizing induced drag, profile drag, and wave drag due to the addition of the main strut and jury struts.

Figure 1 Boeing SUGAR Transonic Truss-Braced Wing (TTBW) Aircraft Concept

A typical MDAO process uses a variety of different tools of varying fidelity for many different purposes such as aerodynamic prediction, static aero-structural analysis, and flutter analysis. While there are on-going efforts in developing high-fidelity Reynolds-averaged Navier-Stokes (RANS) computational fluid dynamics (CFD) models of the TTBW for aerodynamic design and performance analysis, these high-fidelity CFD models are typically not coupled to the structure of the TTBW. There is a need to conduct aeroelastic analysis of the TTBW configuration to address flutter requirements and aero-structural coupling which can affect aerodynamics and vehicle stability and control. Thus, aero-structural coupling is an important element of the TTBW development. To enable this analysis capability, one approach is to use a lower-order aerodynamic tool that can still sufficiently capture the transonic and viscous flow effects on the vehicle for coupling to a finite-element model of the TTBW structure. This approach can provide a rapid analysis capability that facilitates vehicle optimization with aeroelastic constraints such as flutter.

This paper presents a jig twist optimization study of Mach 0.745 TTBW aircraft using an in-house developed aero-structural analysis solver VSPAERO coupled to BEAM3D. The VSPAERO models of the TTBW include both a low-fidelity vortex-lattice model and a mid-fidelity panel model for steady-state aerodynamics. Transonic and viscous flow corrections for the steady-state aerodynamics are implemented on the vortex-lattice model using a transonic small disturbance (TSD) code called TSFOIL coupled to an in-house integral boundary layer (IBL) code. In the region near the strut attachment to the wing, the flow involves a considerable degree of interactions between the wing and the strut. A high-fidelity CFD model of the TTBW is developed using FUN3D to investigate the wing-strut interference aerodynamics for the purpose of developing a wing-strut interference aerodynamic correction method applied to the VSPAERO model. The BEAM3D finite-element model of the TTBW is based on a three dimensional beam theory which includes all six degrees of freedom at a node. The VSPAERO model is coupled to the corresponding finite-element model to provide a rapid aero-structural analysis. An aerodynamic optimization program is developed based on the aero-structural analysis solver. The objective is to minimize the drag of the TTBW jig geometry by optimizing the jig twist distribution along the wing spanwise direction. A flight condition corresponding to Mach 0.745 at 42000 ft is selected for the TTBW aircraft jig twist optimization. Finally, a high-fidelity CFD solver FUN3D is used to validate the design.
II. Aerodynamic Model of the Truss-Braced Wing

A. VSPAERO Model

In order to develop a rapid aeroelastic analysis that facilitates a vehicle MDAO process, a lower-fidelity aerodynamic model of the TTBW is necessary. A previous effort in modeling the TTBW using the vortex-lattice code VORLAX based on the aerodynamic superposition principle has shown that low-order aerodynamic tools can provide a reasonably accurate prediction of aerodynamic performance of the TTBW. Due to the limitations of VORLAX in the previous effort, an improved vortex-lattice model as well as a panel model of the TTBW has been developed in VSPAERO. VSPAERO is a solver that includes both the vortex lattice method and the full panel method based on generalized vortex loops. The core VSPAERO solver is based on an agglomerated multi-pole approach, coupled with a preconditioned linear solver, to reduce solution times. Adaptive wakes, time-accurate, unsteady analyses, and propeller modeling are all supported. The latest version of VSPAERO supports a loosely coupled integration of BEAM3D finite-element code to perform steady state, aeroelastic analyses. VSPAERO is part of the OpenVSP design package and is freely available under the NASA open source license.

Two Mach 0.745 TTBW Outer Mold Line (OML) geometries are available: cruise (1g shape geometry), and jig shape geometry. The jig shape geometry is not a flight jig shape that accounts for the wing aeroelastic wash-out twist for the full-scale vehicle at the design flight condition, but is a wind tunnel model jig shape. Wind tunnel tests have been conducted in NASA Ames 11-Ft Transonic Wind Tunnel. Both geometries are modeled in VSPAERO. Figure 2 illustrates one of the TTBW geometries used in the VSPAERO models. The initial mesh for the vortex-lattice model of the TTBW in VSPAERO is shown in Figure 3. The surface triangulation mesh of the panel model is shown in Figure 4.
Figure 4  Surface Triangulation of VSPAERO Panel Model of TTBW

Figure 5 shows the differential pressure coefficient contour at Mach 0.7 and an angle of attack of 4° for the VSPAERO vortex-lattice model. The shed wakes are shown in Figure 5 to illustrate the time-stepping wake capability in VSPAERO. Figure 6 shows the surface pressure coefficient contour computed by the VSPAERO panel model.

Figure 5  Differential Pressure Coefficient Contour of VSPAERO Vortex-Lattice Model of TTBW
The final VLM model discretization is formulated based on an intricate grid convergence study. Each aircraft component is individually analyzed. Components deemed as lifting surfaces by the interpretation standards set within the VLM software package are separated into a number of airfoils comprised of many individual nodes. The airfoils are used to geometrically determine a mean camber line, which the VLM utilizes to analyze the aerodynamic parameters of interest based on prescribed flow conditions. The number of airfoils for each component is specified based on the geometric features of that component. For instance, for the TTBW wing, it is important for cross sections to be located where the sweep changes and where other components, like the pylon, strut, and jury strut join the wing. Juncture regions are most likely to impact the mean camber line, and therefore, the aerodynamic performance of a given component. Beyond these requirements, a maximum relative distance between span stations is established for each component to ensure that all of the geometric intricacies of each component are captured. Ultimately, the combination of these strategies leads to the span station discretization scheme illustrated by Figure 7 which is comprised of 31 individual airfoils separated by a maximum relative spacing of $\Delta \eta = 0.0381$. The strut, meanwhile, is comprised of 44 cross sections to capture the complex variable taper near the root. The horizontal tail is modeled using 13 cross sections, the vertical tail requires 18 due to variable taper near the tip, the jury strut and pylon are comprised of 5 cross sections each, the nacelle uses 24 cross sections, and the fuselage uses 41 cross sections.
For the main lifting surfaces of the TTBW, namely the wing, horizontal tail, and strut, the number of nodes for each airfoil section is determined by increasing the number incrementally until the component lift coefficient converges. Figure 8 includes the grid convergence results for the three main lifting components of the TTBW. The ratio between the sectional lift coefficient, $c_L$, and the mean sectional lift coefficient for the component, $c_{L\text{mean}}$, is plotted as the grid is refined. Convergence is achieved when there is an increase of less than 1% between grid levels. Based on the results of this grid convergence study, 151 points per cross section are used for the wing and strut components, whereas only 75 points are necessary for the horizontal tail.

![TTBW Grid Convergence](image-url)

**Figure 8  TTBW Grid Convergence**

Minor lift-generating surfaces, such as the jury strut, vertical tail, and pylon, for which the component lift is only marginally impacted by the number of nodes per cross section, are similarly discretized into a number of airfoil sections based on a minimum separation distance. The number of nodes per cross section, however, is set to a baseline minimum of 45 nodes in order to fully capture the curvature of the mean camber line without sacrificing additional computation time by adding tedious detail. The nacelle is generated by extracting a single airfoil from the CAD model and rotating the airfoil 360 degrees under an approximate circular symmetry assumption. The number of sections and nodes can then be specified in a similar fashion to other minor lift-generating components. The fuselage, or lone body component, as deemed by the VLM software standards, is treated as a minor lift-generating component for the purposes of discretization.

**B. Transonic and Viscous Flow Correction**

Because of the missing transonic effect in the linear potential flow method, a method for transonic and viscous corrections has recently been developed. In this method, a full-configuration aerodynamic model can be based on the vortex-lattice method. The wing is discretized into several spanwise sections at which the section lift coefficients computed by the potential flow method are used to correct for the transonic and viscous flow effects. The transonic and viscous correction method is an iterative process to compute the incremental section lift coefficient due to transonic and viscous flow by a virtual re-twist of the individual wing sections to account for the accompanied change in the effective local angle of attack. Implementation of the correction begins by initializing the virtual twist angle due to transonic and viscous corrections, $\gamma(y)$, to zero. The effective 2D angle of attack is then calculated for each airfoil using:

$$\alpha_{2D}(y) = \alpha_0(y) + \frac{c_{\lambda_{VLM}}(y)}{c_{\lambda_{\alpha}}} - \gamma(y),$$

(1)
where $\alpha_{2D}$ is the effective airfoil angle of attack, $\alpha_0$ is the zero-lift angle of attack, $c_{l_{VLM}}$ is the sectional lift coefficient obtained via VSPAERO, and $c_{la}$ is the 2D lift curve slope corrected for sweep as follows:

$$c_{la} = \frac{2\pi}{\sqrt{1 - M^2}},$$

Here, $M_\Lambda$ is the Mach number based on the mid-chord sweep angle. Each airfoil is analyzed by the TSD/IBL model at the effective angle of attack. The transonic flow correction is handled by a transonic small disturbance (TSD) code called TSFOIL. This code is loosely coupled to an in-house integral boundary layer (IBL) code to correct for the viscous flow interaction with the transonic shock on an airfoil. Optionally, the correction method can be performed using the 2D Euler CFD code MSES with an integral boundary layer method developed by Mark Drela. The virtual twist angle is then updated for each section according to:

$$\gamma_{i+1}(y) = \gamma_i(y) + \frac{c_{l_{2D_i}}(y) - c_{l_{VLM_i}}(y)}{c_{la}} - c_{l_{\alpha}} ,$$

where $c_{l_{2D_i}}$ corresponds to the sectional lift coefficient calculated by TSFOIL or MSES for iteration $i$.

The coupling and iterative update process is repeated until the VLM section lift and the 2D lift from the TSD/IBL model converge for all sections. Wave and friction drag are calculated by the TSD/IBL model, whereas lift, pitching moment, and induced drag are calculated by the VLM model. The flow chart of the transonic and viscous flow correction method is shown in Figure 9. An extensive validation of the transonic and viscous flow correction method has been performed to compare the method against the RANS CFD solvers. The solution methods agree quite well in terms of key aerodynamic parameters and pressure distribution results. The major advantage of using vortex-lattice method coupled to transonic and viscous corrections is the computational efficiency of the method, which is several orders of magnitude faster than RANS CFD. This computational efficiency becomes highly important when the potential flow solver is coupled to a structural finite-element model for aero-structural modeling.

Figure 9 Transonic and Viscous Correction Flow Chart
C. Wing-Strut Interference Aerodynamic Correction

The transonic and viscous flow corrections using the TSD/IBL method are generally valid for a single-element airfoil. The TTBW configuration is a complex geometry that includes a strut juncture region where the effect of interference aerodynamics can influence the overall aerodynamic performance of the aircraft. As the strut approaches the wing from below, the transonic and viscous flow corrections using the TSD/IBL method are no longer valid due to the interactions between the wing airfoil and strut airfoil.\textsuperscript{13,14} To account for these interference aerodynamics, CFD models of the wing-strut configuration and the wing-alone configuration of the jig shape TTBW geometry are developed using FUN3D, as shown in Figure 10. To isolate the interference aerodynamic effect for the wing and strut, the nacelle, the pylon, and the horizontal tail are removed from the models. Surface pressure coefficients are computed for both configurations at various wing stations. By comparing the wing-strut data to the wing-alone data, it is seen that the presence of the strut induces a suction peak along the lower surface of the wing near the wing-strut juncture.\textsuperscript{13}

![Figure 10 TTBW Geometric Configurations for Interference Analysis](image)

A wing-strut interference correction method is developed to correct the VSPAERO model coupled to the TSD/IBL approach. The correction method is applied to the VSPAERO+TSD/IBL model to update the section lift, drag, and pitching moment coefficient of each wing section.

The interference correction, $\Delta c_{IC}$, that is applied to the model is calculated using the following equation:

$$\Delta c_{IC} = dc_{FUN3D} - dc_{VSPAERO+TSD/IBL},$$

where $c$ represents a key aerodynamic parameter such as $c_L$, $c_D$, and $c_M$, and the equation computes the change in the given parameter between the two geometric configurations.

Figure 11 shows the lift distribution and the sectional lift coefficient correction along the wing span for a Mach number = 0.745, $C_L = 0.4536$, and Reynolds number 3.3 million based on the mean aerodynamic chord for the wind tunnel experiment. The presence of the strut enhances the shock wave on the upper surface of the wing at inboard wing stations, which increases the lift coefficient. There is an abrupt change in the lift coefficient near the wing-strut juncture location, which is caused by the suction peak on the lower surface of the wing. The lift coefficient difference decreases toward the outboard span stations of the wing where the interference effects are diminished. For the implementation of the wing-strut interference correction, piecewise polynomials are used to fit the data for the inboard wing stations. Near the strut and the outboard wing stations, two linear fits are used where the discontinuity occurs at the wing-strut juncture location.

Figure 12 shows the drag distribution and the sectional drag coefficient correction along the wing span for Mach number = 0.745, $C_L = 0.4536$, and Reynolds number 3.3 million based on the mean aerodynamic chord for the wind tunnel experiment. There is an abrupt change in the drag coefficient near the wing-strut juncture location for FUN3D simulation results, which is caused by the suction peak on the lower surface of the wing. The VSPAERO+TSD/IBL model could not capture the change of the sectional drag coefficient near the wing-strut juncture location due to its limitations. In this case, piecewise polynomials are used to fit the drag coefficient correction distribution for the inboard wing stations and near the strut, and a linear fit is used for the outboard wing stations.
Figure 13 shows the pitching moment distribution and the sectional pitching moment coefficient correction along the wing span direction for Mach number = 0.745, $C_L = 0.4536$, and Reynolds number = 3.3 million. The pitching moment is calculated about the quarter chord location. The presence of the wing-strut juncture only changes the pitching moment coefficient near the juncture location because the suction peak on the lower surface of the wing reshapes the pressure distribution on the wing. A piecewise polynomial is used to fit the sectional pitching moment coefficient correction near the strut, and two linear fits are used for the inboard and outboard wing stations.

As can be seen, near the strut juncture region, there is a significant change of the aerodynamic performance. The impact of varying Reynolds number on aerodynamic interference is found to be marginal via FUN3D; therefore, the established relationships are deemed sufficient for all Reynolds numbers investigated.

![TTBW Wing-Strut Interference Effect (M = 0.745, Re = 3.3x10^6, C_L = 0.4536)](image1)

![TTBW Wing-Strut Interference Effect (M = 0.745, Re = 3.3x10^6, C_L = 0.4536)](image2)

![TTBW Wing-Strut Interference Effect (M = 0.745, Re = 3.3x10^6, C_L = 0.4536)](image3)

(a) Lift Coefficient Distribution - FUN3D

(b) Lift Coefficient Distribution - VSPAERO

(c) Lift Coefficient Correction Distribution

**Figure 11** Lift Coefficient and Lift Coefficient Correction Distribution
TTBW Wing-Strut Interference Effect ($M_\infty = 0.745$, $Re = 3.3 \times 10^6$, $C_L = 0.4536$)

(a) Drag Coefficient Distribution - FUN3D

(b) Drag Coefficient Distribution - VSPAERO

(c) Drag Coefficient Correction Distribution

Figure 12 Drag Coefficient and Drag Coefficient Correction Distribution
D. Aerodynamic Analysis of Cruise Shape Geometry

The VSPAERO vortex-lattice model is used for the aerodynamic analysis of the cruise 1g shape TTBW geometry. In addition, a CFD model of the full-configuration cruise 1g shape TTBW geometry is developed in FUN3D. Wind tunnel test data of the cruise shape geometry in NASA Ames 11-Ft Transonic Wind Tunnel are available for validation of the VSPAERO and FUN3D models. Test data from Run 380 at Mach 0.745 and Reynolds number of 2.6 million based on the mean aerodynamic chord (MAC) with full wind tunnel model corrections are used for validation.

Figure 14 shows the plots of the lift and drag coefficients computed by VSPAERO for Mach 0.745 and a Reynolds number of 2.6 million with and without all the corrections as well as FUN3D. These computed results are compared to Run 380 wind tunnel data. While the lift coefficient is somewhat under-predicted, the drag coefficient computed by VSPAERO alone is mostly induced drag, and therefore it is substantially under-predicted. With all the corrections applied to the VSPAERO model for transonic viscous flow and wing-strut interference aerodynamics, the lift and drag coefficients match remarkably well to the wind tunnel data, although there is a small discrepancy in the drag polar at lower lift coefficients.
Figure 14  TTBW Lift Curve $C_L$ vs. $\alpha$ and Drag Polar $C_L$ vs. $C_D$ at Mach 0.745

Figure 15 shows the plot of the computed $L/D$ ratios as a function of the lift coefficient from VSPAERO, FUN3D, and wind tunnel data. All the three curves of $L/D$ ratios are in very good agreement. The excellent agreement between the VSPAERO model, the FUN3D model, and the wind tunnel data thus has validated the aerodynamic modeling approach.

Figure 15  TTBW $L/D$ at Mach 0.745

III. Finite-Element Model of the Truss-Braced Wing

A. BEAM3D Model

BEAM3D is an in-house finite-element code that is used to model a general wing structure using beam, rod, and rigid elements. The code contains a number of analysis modules: a static deflection analysis module, an eigenvalue analysis
module, a flutter analysis module, and an aeroservoelastic flight dynamic simulation module. The static deflection analysis module can be coupled to a flow solver such as VORLAX, VSAPERO, or CART3D to perform aero-structural and static aeroelastic deflection analyses. The eigenvalue analysis module computes the structural dynamic frequencies and the normal mode shapes of a wing structure. The flutter analysis module computes the frequencies and damping of the wing aeroelastic modes and performs a flutter speed search in the frequency domain using the Theodorsen’s theory for unsteady aerodynamics or in the time domain using the R. T. Jones approximation to generate the aerodynamic mass, damping, and stiffness. The aeroservoelastic flight dynamic simulation module provides the capability to couple the dynamic aeroservoelastic state-space model of a wing structure to a nonlinear 6-degree of freedom flight dynamic model of an aircraft to perform time simulations of the aircraft response to atmospheric gust inputs and flight control surface inputs.

Figure 16 illustrates the TTBW finite-element model in BEAM3D. The left wing and main strut are modeled as the major structural elements. The jury strut is neglected in the model as its contribution is marginal. The mass and structural properties of the finite-element model are made available to NASA by Boeing. The stiffness properties and the elastic definition of the wing and strut are included in the structural properties. BEAM3D models the mass and inertia properties as distributed or running mass and inertias. Thus, the point masses and inertias from the NASTRAN model provided by Boeing have to be converted into the equivalent distributed mass and inertias. Fuel weight is also modeled in the BEAM3D model. The full fuel weight corresponds to a take-off gross weight (TOGW) of 138,000 lbs. The inertias of the fuselage and tails are estimated in VSAPERO.

Figure 16  Finite Element Model of the Truss-Braced Wing

The NASTRAN model provided by Boeing Research & Technology can be used to extract equivalent beam stiffnesses and running mass and inertias through individual, uncoupled beam analyses for both the wing and the strut. Cantilever boundary conditions are applied to the interior face of each beam, and four subcases are conducted for each component to isolate motion in the degree of freedom corresponding to each 3D beam stiffness. A force is applied in the spanwise direction to extract the equivalent axial stiffness, $E A$. A moment is applied about the spanwise axis in order to determine the equivalent torsional stiffness, $GJ$. A force is applied in the chordwise direction to determine the equivalent chordwise bending stiffness, $EI_{zz}$. A force is applied in the flapwise direction to determine the equivalent flapwise bending stiffness, $EI_{yy}$. Deflections and loading are extracted at nodes corresponding to key geometric features to discretize beams into n-elements. The elemental deflection and loading data is then used to calculate stiffness data used by BEAM3D. There are 43 elements used for the wing and 32 elements used for the strut. The resulting stiffnesses are used to calculate deflections, and the deflection data are compared to raw NASTRAN deflection output for validation.

BEAM3D includes the nonlinear capability to model the tension-induced stiffening effect of the struts, which contributes to the overall stiffness matrix of the finite-element model. This is expressed as:

$$K_i (x) = K_i^s + K_i^a + K_i^t (x),$$

where $K_i$ is the total element stiffness matrix of the $i$-th element, $K_i^s$ is the element structural stiffness matrix, $K_i^a$ is the element aerodynamic stiffness matrix, and $K_i^t$ is the element nonlinear stiffness matrix due to the strut tension, which is
dependent on the displacement field \( x(t) \) of the structure. The aerodynamic stiffness is computed from Theodorsen’s theory and depends on the dynamic pressure, wing sectional lift curve slope, and other pertinent unsteady aeroelastic parameters.

B. Static Aeroelastic Analysis

For static aeroelastic analysis, an iterative solution method is implemented for the nonlinear tension-induced stiffness, as shown in Figure 17. At each iteration between the VSPAERO model and the BEAM3D model, the iterative solution method iterates on the static deflection until it converges.

A static aeroelastic analysis is performed for the jig shape TTBW geometry. The VSPAERO model of the jig shape TTBW geometry with all the corrections is coupled to the BEAM3D model. Figure 18 shows the linear and nonlinear static aeroelastic deflections of the wings at Mach 0.745 and the design lift coefficient \( C_L = 0.73 \) computed by BEAM3D. Except for a minor discrepancy near the wing root, the linear static solutions of the wing bending deflection computed by NASTRAN and BEAM3D are in excellent agreement. The wing tip deflection at cruise is computed to be 23.3 inches by BEAM3D and 23.2 inches by NASTRAN. The nonlinear static solution of the wing tip deflection is computed to be 22.8 inches. Thus, the nonlinear tension-induced stiffening does not significantly alter the static aeroelastic deflections.

![Figure 17 Iterative Solution for Nonlinear Finite-Element Model of Strut Tension Stiffening](image-url)
Figure 18  TTBW Wing Bending Deflection and Twist at Mach 0.745 and $C_L = 0.73$

The nose-up wing twists about the aircraft pitch axis, or the $y$-axis, computed by BEAM3D and NASTRAN are in general agreement, but discrepancies do exist along the wing span. The wing twist computed by NASTRAN is higher than that computed by BEAM3D by at most $0.3^\circ$ outboard of the wing station $y = 400$ inches. The wing twist computed by NASTRAN is lower than that computed by BEAM3D by at most $0.2^\circ$ inboard of this wing station. These discrepancies could be due to the application of the distributed lift and pitching moment about the elastic axis in NASTRAN not being precisely on the elastic axis but rather along the nearest nodes. The overall nose-up wing twist at the tip is in better agreement between NASTRAN and BEAM3D with the NASTRAN computed value of $-2.39^\circ$ and BEAM3D computed values of $-2.35^\circ$ and $-2.33^\circ$ corresponding to the linear and nonlinear static solutions, respectively.

Figure 19 shows the strut axial displacement and tension as a function of the wing station at the design lift coefficient $C_L = 0.73$. The axial displacement of the struts is almost 0.6 inches and the tension carried by the strut is about 171,000 lbs.15

Figure 19  TTBW Strut Axial Displacement and Tension at Mach 0.745 and $C_L = 0.73$

The VLM model is coupled to the transonic and viscous corrections as well as the FEA model for aero-structural iterations via the panel incidence angle using the following relationship:
\[ \tilde{\alpha}_{inc}(y) = \alpha_{inc}(y) + \phi_y(y) + \gamma(y), \] (6)

where \( \tilde{\alpha}_{inc} \) represents the effective panel incidence angle along the wing span, \( \alpha_{inc} \) is the jig shape incidence angle, and \( \phi_y \) is the elastic twist about the pitch axis. The VLM and FEA models iterate until the tip twist converges. Tip twist convergence typically occurs after 2-5 iterations. If TSD/IBL models iterate until the tip twist converges. Tip twist convergence typically occurs after 2-5 iterations. If TSD/IBL coupling is not present, the virtual twist angle, \( \gamma(y) \), is zero and plays no role in the aero-structural coupling; however, if both aero-structural and TSD/IBL coupling are desired, tip twist convergence is calculated for each TSD/IBL iteration at the new virtual twist angle.

A basic schematic of the full aeroelastic modeling strategy is depicted by Figure 20. This process is used to generate the data presented in Figure 21 which shows the lift and drag coefficients computed by the VSPAERO model of the jig shape TTBW geometry coupled to the BEAM3D model. For comparison, the lift and drag coefficients computed by the VSPAERO model of the cruise 1g shape TTBW geometry and the wind tunnel data are also plotted. The lift and drag coefficients computed by VSPAERO coupled with the BEAM3D model of the jig shape TTBW geometry agree very well with the VSPAERO model of the cruise shape TTBW geometry and the wind tunnel data. The close agreements with wind tunnel data provide confidence in the in-house developed aero-structural analysis solver for the TTBW aircraft design.

![Figure 20 Full Aeroelastic Modeling Scheme](image)

![Figure 21 TTBW Lift Curve $C_L$ vs. $\alpha$ and Drag Polar $C_L$ vs. $C_D$ at Mach 0.745](image)
IV. Flight Jig Twist Optimization Study

A. Flight Jig Twist Optimization

The jig shape OML geometry is not a flight jig shape, which accounts for the wing aeroelastic wash-out twist for the full-scale vehicle at the design flight condition, but is a wind tunnel model jig shape. Thus, the wind tunnel jig shape model is suitable for comparisons to wind tunnel data, but not necessarily suitable for generating a full flight dynamics model. An optimization strategy is developed in order to formulate a flight-optimized jig twist model.

The goal of the optimization scheme is to minimize the drag of the aero-structural model of the jig shape for the TTBW wing. Lift constraints are added to the optimization algorithm, such that $C_L - C_{Ld} < 0.001$, where $C_{Ld}$ is the design lift coefficient, 0.73. A gradient-based optimization scheme utilizing the steepest descent method is used with the cost function as described below:

$$J(\alpha, C) = C_D,$$

where $C_D$ is the aircraft drag coefficient from the aero-structural model of the jig shape geometry and $C = [C_1, ..., C_N]$ is a vector of $C_i$, which are coefficients of a shape function that parameterize the jig twist such that:

$$\theta(y) = \theta_{ini}(y) + \sum_{i=1}^{N}(C_i \cdot \phi_i(y)),$$

where $\theta(y)$ represents the jig twist distribution along the spanwise direction, $\theta_{ini}(y)$ is the initial jig twist distribution along the spanwise direction, corresponding to the wind tunnel optimized twist model, and $\phi_i(y)$ is a shape function of degree $i$. Shape functions are utilized in order to limit the number of design variables for optimization as well as provide a smoother converged optimized jig twist distribution. The steepest descent algorithm for updating the design variables can be represented by the following equations:

$$\alpha_{k+1} = \alpha_k - \epsilon \cdot \frac{\partial J}{\partial \alpha},$$

$$C_{i_{k+1}} = C_{i_k} - \epsilon \cdot \frac{\partial J}{\partial C_i}.$$  

Here, the design variable at iteration $k$ is updated based on the partial derivative of the cost function with respect to the design variable, which is calculated using a small-perturbation, second-order central difference scheme, and $\epsilon$ is a step size weight term.

The optimization procedure begins by initializing both the TTBW geometry and the parameterization of the jig twist. A baseline aero-structural solution is established by first running VSPAERO for the wind tunnel twist optimized model coupled to BEAM3D, and then iterating until the tip twist converges. Once tip twist convergence is achieved, the value of the cost function, or aircraft drag in this case, is updated. The new cost function value is compared to the convergence criteria. If the criteria are not met, small perturbations are applied to the design variables. The design jig twist, $\theta(y)$, is then calculated, and the VSPAERO mesh is deformed based on the updated twist. As before, the VSPAERO model is then coupled to BEAM3D until a converged aero-structural solution is generated. A gradient is established based on the effect of the small perturbations such that the design variables can be updated relative to their respective cost function partial derivatives. This small perturbation iterative procedure is repeated until the cost function converges. A block diagram illustrating the full jig twist optimization framework is shown in Figure 22.
The optimization results can be seen in Figure 23. Initially, a single, continuous shape function is utilized to parameterize twist; however, it is discovered that a piecewise polynomial, such that $\theta$ and $\frac{d\theta}{dy}$ match at the wing-strut juncture location, can provide improved jig twist optimization by accounting for aerodynamic changes at the wing-strut juncture. Of the shape function fitting techniques tested, the piecewise cubic Chebyshev polynomial fit is deemed the optimal solution. Table 1 helps to quantify the main observations for the optimal case.

Table 1 Drag Minimization Jig Twist Optimization Results from VSPAERO Coupled to BEAM3D

<table>
<thead>
<tr>
<th>Model</th>
<th>$\alpha_{trim}$ (deg.)</th>
<th>$C_L$</th>
<th>$C_D$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1g</td>
<td>2.3623</td>
<td>0.7300</td>
<td>0.03435</td>
</tr>
<tr>
<td>Wind Tunnel Jig Twist</td>
<td>1.9982</td>
<td>0.7300</td>
<td>0.03545</td>
</tr>
<tr>
<td>Flight Optimized Jig Twist</td>
<td>2.0113</td>
<td>0.7300</td>
<td>0.03435</td>
</tr>
</tbody>
</table>

Figure 23 Drag Minimization Jig Twist Optimization Candidate
Overall, the ideal optimized twist distribution maintains a significantly different $c_L$ distribution when compared to the 1g shape model, but it achieves the same lift and drag coefficients as the 1g shape, thereby indicating that the jig twist is optimal. This solution produces a reduction in lift-matching error when compared to the wind tunnel twist distribution, and it minimizes drag such that $C_D$ matches the value found for the 1g shape model. This solution also produces a converged twist distribution that is very similar to the wind tunnel optimized twist distribution, which makes it believable. These findings suggest that the model optimized could perhaps be considered a flight jig twist candidate.

B. High-fidelity CFD Validation

To ensure the optimized flight jig twist candidate is valid, a validation study using high-fidelity CFD solver FUN3D is performed. The computational fluid dynamics code used in this study is FUN3D\textsuperscript{16,17} which solves the unsteady three-dimensional Navier-Stokes equations on mixed-element grids using a vertices-centered finite-volume method. Information exchange for flow computation on different partitions using multiple CPUs is implemented through the MPI (Message Passing Interface) protocol. It employs an implicit upwind algorithm in which the inviscid fluxes are obtained with a flux-difference-splitting scheme. At interfaces delimiting neighboring control volumes, the inviscid fluxes are computed using an approximate Riemann solver based on the values on either side of the interface. The Roe flux difference splitting\textsuperscript{18} is used in the current study. For second-order accuracy, interface values are obtained by extrapolation of the control volume centroidal values, based on gradients computed at the mesh vertices, using an unweighted least squares technique. The Venkatakrishnan\textsuperscript{19} limiter is used in the current study to limit the reconstructed values when necessary. In this study the tetrahedral mesh with prism layers are used. In FUN3D, for tetrahedral meshes, the full viscous fluxes are discretized using a finite-volume formulation in which the required velocity gradients on the dual faces are computed using the Green-Gauss theorem. The solution at each time-step is updated with a backwards Euler time-differencing scheme. At each time step, the linear system of equations is approximately solved with either a multi-color point-implicit procedure or an implicit-line relaxation scheme. Local time-step scaling is employed to accelerate convergence to steady-state. To model turbulent flows, the one-equation model of Spalart-Allmaras\textsuperscript{20} (S-A) is used in this study.

The deformed geometry is calculated from in-house developed aero-structural analysis solver VSPAERO coupled with BEAM3D at flight design condition which corresponds to $C_L=0.73$. The deformation is assumed the same for the off-design condition, which might introduce some discrepancy. Figure 24 shows the comparison of the jig and deformed geometries. Figure 25 shows the CFD mesh for the deformed geometry. Figure 26 shows the pressure contour comparison of the wind tunnel jig and flight optimized jig TTBW geometries at the design point, which corresponds to $C_L=0.73$. After design is implemented, the pressure distribution is more uniform, which helps reduce the drag. Figure 27(a) shows the lift curves for the wind tunnel jig and flight optimized jig geometries. The lift slope is very similar for the two cases. Figure 27(b) shows the drag polar curves for the wind tunnel jig and flight optimized jig geometries. Table 2 lists the FUN3D simulation results at the flight design condition. After the design is implemented, the drag coefficient is reduced by 8 counts for the flight optimized jig geometry at the flight design condition compared to the wind tunnel jig geometry. This confirms the optimization results found using the in-house developed tool VSPAERO coupled with BEAM3D. However, the drag is increased when the lift coefficient is above 0.8, which might suggest a multi-point jig twist optimization scheme is required to reduce the drag at a wide range of flight conditions.

<table>
<thead>
<tr>
<th>Model</th>
<th>$\alpha_{trim}$ (deg.)</th>
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<th>$C_D$</th>
</tr>
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<td>Wind Tunnel Jig Twist</td>
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<td>0.0352</td>
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<tr>
<td>Flight Optimized Jig Twist</td>
<td>1.600</td>
<td>0.7300</td>
<td>0.0344</td>
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</table>
Figure 24  Jig and Deformed TTBW Geometries

Figure 25  CFD Mesh for the Deformed TTBW Geometry

Figure 26  Pressure Coefficient Contour on the TTBW Geometry at $M = 0.745$, $Re = 11.9 \times 10^6$, and $C_L = 0.73$
Conclusions

A jig twist optimization study for the TTBW aircraft is performed based on the in-house developed tool VSPAERO coupled with BEAM3D for aero-structural analysis. The lift and drag coefficients predicted by the solver agree well with the wind tunnel data for the TTBW aircraft. A flight condition corresponding to Mach 0.745 at 42000 ft is used as the focal point for the TTBW aircraft jig twist optimization study to reduce the drag. After the design is implemented, the drag coefficient is reduced by 8 counts for the flight optimized jig geometry at the design flight condition compared to the wind tunnel jig geometry. The high-fidelity CFD solver FUN3D simulation results confirm the effect of the optimized jig twist shape. However, the drag is increased when the lift coefficient is above 0.8, which might suggest a multi-point design is required to reduce the drag at a wide range of flight conditions.

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References


