Habitable Exoplanet Observatory (HabEx) Telescope: Systems Engineering and STOP Modeling

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Abstract — The Habitable Exoplanet Observatory Mission (HabEx) is one of four missions studied for the 2020 Astrophysics Decadal Survey. Its goal is to directly image and spectroscopically characterize planetary systems in the habitable zone around nearby sun-like stars. Additionally, HabEx will perform a broad range of general astrophysics science enabled by 115 to 1700 nm spectral range and 3 x 3 arc-minute FOV. Critical to achieving its science goals is a large, ultra-stable UV/Optical/Near-IR (UVOIR) telescope. The baseline HabEx telescope is a 4-meter off-axis unobscured three-mirror-anastigmatic, diffraction limited at 400 nm with wavefront stability on the order of a few 10s of picometers. This paper summarizes the opto-mechanical design of the baseline optical telescope assembly, including a discussion of how we applied science driven systems engineering to derive the telescope’s engineering specifications from the mission’s science requirements, and presents analysis that the baseline telescope structure meets its specified tolerances.

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1. INTRODUCTION

“Are we alone in the Universe?” is maybe the most compelling science question of our generation. Per the 2010 New Worlds, New Horizons Decadal Report [1]: “One of the fastest growing and most exciting fields in astrophysics is the study of planets beyond our solar system. The ultimate goal is to image rocky planets that lie in the habitable zone of nearby stars.”

In this spirit, the Habitable Exoplanet Observatory Mission (HabEx) has three goals: to seek out nearby worlds and explore their habitability; to map out nearby planetary systems and understand the diversity of the worlds they contain; and, to carry out observations that open up new windows on the universe from the UV through near-IR. The

HabEx Science and Technology Definition Team has selected ‘Architecture A’ a 4-meter telescope with four science instruments (coronagraph, star-shade instrument, UV-NIR imaging multi-object slit spectrograph, and a high resolution UV spectrograph; and a 52-m external star-shade occulter. [2]

Section 2 describes the process used to design the HabEx baseline telescope. Section 3 reviews how the HabEx Optical Telescope Assembly (OTA) specifications are derived from the HabEx science requirements. Section 4 describes the baseline opto-mechanical OTA design, its key components and design features. Section 5 summarizes detailed performance analysis of the baseline opto-mechanical design which shows that the design, using proven technology and engineering practice, can achieve the specifications necessary to perform HabEx science. Section 6 shows how STOP (structural thermal optical performance) model performance predictions are used to construct an error budget. The baseline 4-m off-axis HabEx opto-mechanical telescope design ‘closes’ for its line-of-sight (LOS) and wavefront error (WFE) stability specifications. The only external assumptions is that the mission is launched in an SLS 8.4-m fairing and uses low disturbance micro-thrusters for pointing control.

2. DESIGN PROCESS

Telescope design is an iterative process. The HabEx OTA design team followed a science-driven systems-engineering design method. Design element specifications were derived from science requirements (Table 1). And error budgets created for each specification.

| Table 1: Specification flow-down from Science Requirements |
|---------------------------------|-----------------|-----------------|
| Science                        | Performance     | Design           |
| TWA                            | PSF             | Unobscured Aperture |
|                                |                 | 4-m Aperture Dia  |
|                                |                 | 400 nm Diffraction Limit |
| Raw Contrast                   | Polarization    | Mechanical Stability |
|                                | Stable Wavefront| Thermal Stability |
|                                |                 | 0.3 mas LOS Jitter |
| WFOV Imaging                   | 3 x 3 arc-min   | TMA Design       |

Point designs were created for the telescope structure as primary mirror assembly and evaluated for compliance with the error budget using STOP modeling. The point designs were then iterated and refined.

3. OTA Specifications

Aperture Architecture and Size

Exoplanet science drives the off-axis architecture, aperture diameter and primary mirror F/#. General astrophysics drives spectral range and requires a three mirror anastigmatic (TMA) design to enable a 3 x 3 arcmin field of view (FOV) (Figure 1).

Imaging habitable zone exoplanets using a coronagraph requires a telescope ‘system’ that can produce a $10^{-10}$ ‘dark hole’ with as small of an inner working angle (IWA) as possible and as large of an irradiance throughput as possible. IWA is the minimum angular distance (on the sky) where the ‘dark hole’ begins – the location when the coronagraph can block $10^{10}$ of the host stars light (Figure 2). The smaller the IWA and the larger the throughput, the greater the number of habitable zones that can be searched. The ability to achieve a small IWA depends upon the telescope’s ability to produce a stable point spread function (PSF) with a compact stable encircled energy (EE). The smaller the EE, the smaller the IWA. It is common knowledge that the larger a telescope’s aperture, the smaller its PSF and EE. But, what is often overlooked is that an unobscured (off-axis) telescope always has a more compact EE (better IWA) than an on-axis telescope with a central obscuration, because diffraction from the central obscuration broadens the PSF. To be specific, an unobscured circular aperture has 82.8% EE at $\lambda/D$. And, a telescope with a 10% central obscuration has 82.5% EE at 1.4 $\lambda/D$ (and for a 20% obscuration, 82% EE is at 1.63 $\lambda/D$). [7] Thus to achieve the same IWA performance as an unobscured 4-m telescope, an on-axis telescope with 10% central obscuration would need to be at least 5.6-m and one with 20% obscuration would need to be at least 6.5-m. Additionally, diffraction from secondary mirror spider obscurations distort the PSF and broaden the EE. A 1 to 2% wide spider can increase EE diameter (IWA) by 5 to 10% [7] – requiring a 5 to 10% larger on-axis telescope. Of course the problem is even worse for a segmented aperture primary mirror.

Throughput is the percent of the exoplanet’s PSF core irradiance transmitted through the coronagraph as a function of angular separation between the host star and planet. Figure 3 shows the core throughput for three different coronagraphs – vector-vortex charge 4 (VVC4), charge 6 (VVC6) and hybrid Lyot (HLC) – all with the HabEx baseline 4-meter off-axis unobscured telescope; and, the throughput for a 6-m on-axis segmented primary mirror telescope (i.e. JWST) with an apodized pupil Lyot coronagraph (APLC). [8-9]

Regarding aperture and diffraction limit, the specification is based on a design reference mission yield estimate for an off-axis-telescope/coronagraph combination. [10] Threshold science occurs when the telescope PSF core radius ($\lambda$/$D$) is < 25 mas. This is accomplished with a > 3.7-m off-axis monolithic telescope with a 400 nm diffraction limit.

Regarding F/#, to minimize polarization cross-talk in the coronagraph, a slow PM F/# is required. An optical design similar to Exo-C with an F/2.5 primary mirror and the science instruments located on the anti-Sun side of the telescope [11] was selected. Benefits of this configuration are that it minimizes the need for high angle of incidence reflections that produce unwanted polarization effects and isolates the coronagraph from thermal disturbances. But, it results in a physically long OTA. The baseline 4-m design has a primary to secondary mirror separation of ~9-m.

Diffraction Limited Performance Specifications

Diffraction Limited is driven by both general astrophysics and coronagraphy because, along with aperture diameter, diffraction limit directly relates to the performance parameters of PSF size, EE and Strehl ratio. To have a 400 nm diffraction limited telescope requires a system wavefront error (WFE) of approximately 30 nm rms. Contributors to telescope WFE are the primary mirror (PM), secondary mirror (SM) and tertiary mirror’s (TM) surface figure errors, and the ability to attached the PM and SM to the structure and accurately align them to the TM, and maintain that alignment on-orbit. Because the telescope has a laser metrology system that establishes and maintains PM and SM alignment to the TM with high precision, the majority of the telescope’s WFE budget can be allocated to the mirrors. And, because the PM is larger and less stiff than the SM or PM, it gets the largest allocation.
Two sources of LOS instability are thermal and mechanical. LOS drift occurs when the telescope is slewed relative to the Sun. Temperature change causes the telescope structure to expand or contract resulting in rigid-body motions of the optical components relative to each other. Fortunately, thermal effects are slow and can be corrected. HabEx is baselining a laser-truss system to sense and correct slow LOS drift. LOS jitter is more important. Jitter is produced by mechanical disturbance accelerations (from sources such as reaction wheels, cryo-coolers, etc.) exciting modes in the telescope structure causing rigid body motions of the primary, secondary and tertiary mirrors. To correct ‘slow’ jitter (i.e. < 10 Hz), HabEx is baselining a low-order Zernike Wavefront Sensor (ZWFS) similar to the WFIRST low-order wavefront sensor (LOWFS) that can sense and correct LOS jitter on the order of 2.5 mas to less than 0.3 mas per axis. But, given that the ZWFS cannot correct ‘fast’ jitter at frequencies above 10 Hz, to be conservative, the telescope design is specified to meet the uncorrectable jitter specification of 0.3 mas per axis.

To design the telescope, it is necessary to convert LOS stability specification into an engineering tolerance, i.e. maximum allowed optical component rigid body motions. Zemax tolerance analysis of the baseline optical design provides the LOS and WFE sensitivity to rigid body motions of the primary and secondary mirrors relative to the tertiary mirror for the baseline F/2.5 optical design [3]. From these sensitivities, an LOS error budget can be allocated for each rigid body degree of freedom (DOF) to keep the on-sky LOS jitter < 0.3 mas per axis specification. Figure 5 shows one potential error budget allocation.

**Wavefront Error (WFE) Stability Specification**

WFE stability specification is driven by the coronagraph. Any temporal or dynamic change in WFE can result in dark-hole speckles that produce a false exoplanet measurement or mask a true signal. Figure 6 outlines a method for creating a wavefront stability error budget based on the total allowable coronagraph contrast leakage which enables the detection, at a defined signal to noise ratio, of an exoplanet with a given flux ratio relative to its host star by a coronagraph with specific noise properties. [8-9] For the case illustrated in

Figure 4 shows how the nominal PM WFE engineering specification flows into an error budget which must be achieved by the PM fabrication process. Surface figure error allocation is set to what is demonstrated on WFIRST. Metrology error is set to what was demonstrated on JWST.

General astrophysics and exoplanet science drive the primary mirror surface specification as a function of spatial frequency. General astrophysics is most sensitive to the shape and stability of the PSF – which is driven by low-spatial frequency errors. And, exoplanet science high-contrast imaging is most sensitive to mid- and high-spatial frequency errors. Mid-spatial frequency errors blur or spread the core. And high-spatial frequency errors and surface roughness scatter light out of the core and over the entire PSF. Thus, per Table 2, the total PM surface figure specification is further divided into low-, mid- and high-spatial frequency bands.

This specification assumes computer controlled polishing for spatial frequencies to 30 cycles (50 nm minimum tool size) to correct quilting error and a -2.5 PSD slope for high spatial frequencies. The 100-cycle boundary between mid and high spatial error is defined assuming that the coronagraph uses a 64 x 64 deformable mirror (DM). A 64x64 DM can theoretically correct spatial frequencies up to 32 cycles (or half the number of DM elements). This could create a ‘dark hole’ with an inner working angle (IWA) of λ/D and an outer working angle (OWA) of 32λ/D. The system engineering consideration is that primary mirror spatial frequency errors up to 3X beyond what can be corrected by the DM can scatter energy back into the ‘dark hole’. Therefore, the primary mirror needs have a surface figure as smooth as possible for spatial frequency errors from 30 cycles up to 100 cycles. [12-13]

**Line of Sight (LOS) Stability Specification**

 LOS instability is important for both general astrophysics and coronagraphy because it causes PSF smearing that degrades spatial resolution and IWA. A typical specification for LOS error is less than 1/10th the PSF radius. For a 400 nm diffraction limited 4-m telescope, the on-sky PSF radius is ~20 mas. Thus, the specification should be < 2 mas. But, the coronagraph requires a LOS stability better than 0.3 mas per axis. The reason is that LOS error causes beam-shear on the SM and TM, as well as other mirrors in the optical train, which introduces WFE that result in contrast leakage.

![Figure 4: Primary Mirror Specification Allocation](image-url)
Figure 6, the exoplanet is detectable as long as WFE instability produces < 40 ppt of contrast leakage. But, to be conservative, the HabEx study assumed 30 ppt. The next step is to calculate the coronagraph’s contrast leakage for each Zernike polynomial. Then, using this sensitivity, allocate the 30 ppt on an RSS basis between each Zernike term to produce an error budget tolerance specification.

Figure 6: Wavefront Stability Error Budget Development Method

Figure 7 shows this process for the Vector Vortex Charge-6 Coronagraph (VVC-6). The first data column shows the contrast leakage sensitivity to each Zernike term. As is evident, the VVC-6 is insensitive to lower order error up to spherical and very sensitive to trefoil and higher errors. The next column shows a completely arbitrary RSS allocation of 30 ppt of contrast. Multiplying these allocations by the sensitivity yields an initial wavefront error budget. But, these errors must be sub-allocated to the actual physical mechanisms by which they arise: LOS Jitter, Inertial Deformation and Thermal. For purposes of initial analysis, we did a simple uniform allocation.

LOS WFE instability occurs when LOS jitter or drift causes beam-shear on the secondary and tertiary mirrors. Because they are cones, beam shear manifests itself as low-order astigmatism and coma (shear of spherical aberration is coma and sub-aperture coma appears to be astigmatism). Inertial WFE instability occurs when the primary mirror is accelerated, by mechanical disturbances, causing it to react (i.e. bend) against its mounts. The shape of this error is similar to the mirror’s static (X,Y,Z) gravity sag (i.e. bending of the mirror when it is exposed to a 1G acceleration in the X,Y,Z directions). Therefore, the shape of the inertial instability can be tailored by adjusting the geometry of the mirror mount design, i.e. 3 vs 6 vs 9-point mount, and location of mounts, i.e. edge vs 70% radius.

Thermal WFE instability occurs when the primary mirror’s bulk temperature or temperature gradient changes. If the mirror’s coefficient of thermal expansion (CTE) is completely homogeneous and constant, then a bulk temperature should only result is a defocus error. But any inhomogeneity in the mirror’s CTE will result in a temperature dependent WFE. Additionally, because CTE is itself temperature dependent, any change in the mirror’s thermal gradient will also result in a WFE. Unlike mechanical WFE which is mostly low-spatial-frequency, thermal WFE can have significant high-spatial-frequency content. Therefore, the best mitigation strategy is to minimize thermal disturbances. This can be done either by passive isolation or active sense and control.

4. OPTO-MECHANICAL DESIGN

The ‘baseline’ telescope (Figure 8) consists of the primary mirror assembly, secondary mirror assembly, secondary mirror tower with integrated science instrument module, and stray-light tube with forward scarf. The 40 deg scarf angle determine the closest angle of observation to the sun. The tower and baffle tube are the optical bench which maintains alignment between the PMA, SMA and TMA. The OTA is physically separate from the spacecraft which includes the solar array sunshield. The size of the solar arrays on the bottom are driven by thermal power requirements during anti-sun pointing. Instead of reaction wheels, thrusters are used for slewing the observatory and micro-thrusters are used for fine pointing control during science observations. The OTA and spacecraft connect only at the interface ring. This ring is also the interface between the payload and the

<table>
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Figure 7: Allocation of WFE Stability between LOS, Inertial and Thermal Sources.
Space Launch System (SLS). Not shown is the forward door. It is closed for launch to prevent contamination and provide additional stiffness. Additionally, launch locks connect the spacecraft solar panels to the tube for launch.

The Baseline Observatory is designed for the SLS Block IB mass and volume capacities, and launch environment. [14] The payload fits inside the SLS 8.4-m fairing with no deployments. The projected total mass (with 30% reserve) of 14-mt has significant margin against the SLS Block-2 capacity of 44 mt to SE-L2. The telescope and spacecraft structure are designed to have a first mode higher than 10 Hz and to survive a 3.5g axial and 1.5g lateral launch load.

The structure is the foundation for the entire telescope. It is the optical bench to which the optical components and science instruments are attached. It has the critical function of placing the primary, secondary and tertiary mirrors at the locations specified by the optical design and keeping them at those locations with sufficient stability to meet the required performance specifications. This is accomplished by making the structure as stiff as possible and by minimizing the disturbances to which the structure is exposed. Given that the optical design is a TMA and that three of the four science instruments share a common tertiary mirror. The TM location is fixed, and the primary and secondary mirror alignments are adjusted relative to the TM. STOP modeling predicts that the baseline structure meets the LOS Jitter and LOS WFE stability specification for a specified micro-thruster disturbance profile.

The Baseline Observatory design team conducted multiple trade studies with literally hundreds of variations to optimize the stiffness, mass and gravity sag of candidate open-back Zerodur® and closed-back ULE® primary mirrors. Design parameters traded included facesheet thickness, mirror thickness, core wall thickness, core pocket size, core geometry, and mount geometry (i.e. edge mount R = 100% vs R = 80% or 67%). [15-19] Zerodur® was selected as the baseline material because Schott has demonstrated a routine ability to fabricate 4.2-m diameter Zerodur® substrates and turn them into lightweight structures via their extreme-lightweight Zerodur® Mirror (ELZM) machining process.

And, because a 1.2-m Zerodur® ELZM mirror owned by Schott and tested at NASA MSFC showed better thermal stability than a 1.5-m ULE® mirror manufactured as part of the AMTD project. [20] Part of Zerodur’s CTE advantage over ULE is that the mirror is fabricated from a single boule of material, thus a Zerodur® mirror has a more homogeneous CTE distribution than a mirror assembled from multiple ULE® components.

The baseline Zerodur® mirror assembly provides an excellent balance between mass and stiffness. The substrate has a flat-back geometry with a 42 cm edge thickness and mass of approximately 1400 kg. The mirror’s free-free first mode frequency is 88 Hz. And, its mounted first mode frequency is 70 Hz. Mass is important because it provides thermal capacity for a thermally stable mirror. Additionally, mass allows for local stiffening of the substrate to minimize gravity sag. [15] The mirror substrate geometry and hexapod mount designs were optimized to produce as uniform as possible XYZ gravity sag deformation. The mirror is attached at three edge locations to a hexapod mount system. This geometry was selected to allow defocus and minimize spherical gravity sag based on vector coronagraph aberration sensitive.

The primary mirror thermal control system is critical to the telescope’s ability to achieve science required diffraction limited performance and wavefront stability. The function of the thermal control system is to uniformly set the primary mirror’s front surface to the desired operating temperature and keep it at that temperature regardless of where the telescope points on the sky relative to the sun. Control system accuracy impacts diffraction limit performance, signal to noise and spectral throughput. And, the precision to which the system can maintain temperature determines wavefront stability. Any gradient or bias error in the mirror’s bulk temperature will introduce a static ‘cryo-deformation’ wavefront error. And, any temporal variation in the mirror’s temperature will introduce instability.

Similar to Hubble, HabEx is cold biasing the primary and secondary mirrors and heating them to their operating temperature. The operating temperature is constrained by
two competing requirements. Near-IR science requires cold mirrors to minimize in-field thermal noise. But, UV science requires the mirrors to be free of any contamination such as a monolayer of water ice or other out-gassed molecules to maximize spectral throughput. HabEx has selected an operating temperature of 270K for its mirrors because it is above the sublimation temperature for water ice. The amount of cold bias is also constrained by competing engineering requirements. The greater the bias, the easier it is to control the mirror temperature; but the more electrical power required to achieve that control. The minimum amount is one where the mirrors are cold biased for all potential sun orientation angles. Cold bias is produced by thermal isolation around the telescope.

HabEx plans to use a thermal control system with radial and azimuthal heater zones behind and around the perimeter of the primary mirror. The radial heater zones compensate for the view factor radial gradient to create a uniform front surface temperature. And, the azimuthal heater zones compensate for changes in the lateral thermal gradient as a function of pointing angle.

The baseline HabEx active radial thermal control concept is an engineering scale-up of systems built by the Harris Corporation. Zonal active thermal control of primary mirrors is currently TRL-9 with systems currently flying on the Harris Corporation commercial 0.7-m and 1.1-m Spaceview™ telescopes. These systems enable on-orbit focus adjustment for optimal image quality. [21, 22] Additionally, under the Astrophysics Division funded Predictive Thermal Control Study (PTCS), Harris Corporation has built and delivered to NASA, for testing with candidate mirror assemblies, a 1.5-m system with 37 thermal control zones (Figure 9). [23] This system has 6 azimuthal heater zones in each of 5 radial and circumferential zones. Additionally, there are heater zones on each mirror strut and the support structure. The test article is fully instrumented to quantify radiative and conductive heat flow.

5. STOP MODEL ANALYSIS

Integrated Model

To evaluate if the baseline HabEx telescope meets its performance requirements, integrated thermal and finite element models (FEM) were constructed of the telescope and spacecraft bus then merged into an observatory model. An observatory level model was required because the telescope’s thermal and mechanical performance is strongly influenced by the spacecraft. These models were used to perform structural thermal opto-mechanical performance (STOP) analyses.

The integrated observatory FEM was created using the MSC Patran pre-processor and geometry created in Pro-Engineer CAD. The primary and secondary mirror FEMs were created independently using the NASA MSFC developed Arnold Mirror Modeler. Using the integrated NASTRAN model, analyses were performed to ensure strength/stability and stiffness requirements were satisfied in accordance with NASA-STD5001B and the launch vehicle payload users guide (ULA - Delta IV Heavy). Additionally, the integrated finite element model was used to perform dynamic response, and thermal analysis.

The integrated observatory thermal model was created in Thermal Desktop using the geometry created in Pro-Engineer CAD. The Thermal Desktop model has 20K elements and calculates telescope’s structure and mirror temperature distribution at 10K nodes. The temperature distribution for each node is mapped onto the NASTRAN FEM and the deflections created by each node’s coefficient of expansion (CTE) is calculated using NASTRAN Solution 101. Rigid body motions (RBM) and mirror surface deformations are calculated from the NASTRAN deflections using SigFit. The primary and secondary mirror’s mesh grids were sized to enable SigFit to fit thermally induced surface figure error (SFE) to higher order Zernike polynomials.

Dynamic mechanical errors (LOS jitter, LOS WFE stability, inertial WFE stability, and impulse ring-down) are caused by structural response to mechanical stimuli. To minimize the source of such stimuli, the baseline HabEx observatory architecture does not use reaction wheels for slewing and pointing. Instead it uses thrusters and micro-thrusters. Thrusters slew and point the telescope. They are then turned off and micro-thrusters maintain pointing for the duration of a science exposure. The noise on their thrust is the only source of mechanical stimuli. Micro-thrusters run...
continuously with variable thrust proportional to applied current. Figure 10 shows a measured noise PSD for a single colloidal micro-thruster emitter. The data indicates that micro-thrusters have a maximum noise of about 0.05 μN/√Hz with a roll-off after about 2 Hz. [24] But, because the data is noisy and has not been measured beyond 5 Hz, HabEx is assuming for its dynamic STOP analysis that each micro-thruster head has a flat or ‘white’ noise spectrum of 0.1 micro-Newton. Because the aft modules have twice as many emitter heads as the forward modules, each forward module is specified to have a flat noise spectrum of 0.4 μN/√Hz and each aft module is specified to have 0.8 μN/√Hz.

Dynamic thermal errors (LOS drift, LOS WFE, and thermal WFE stability) are caused by structural and optical component response to thermal stimuli. To predict thermal performance, a 250 hour design reference mission (DRMs) was analyzed in Thermal Desktop. The calculated temperature distribution is mapped onto the NASPAN FEM and the deflections of each node calculated. Rigid body motions and surface figure errors (SFE) of the primary and secondary mirrors were calculated from the NASPAN deflections using SigFit.

The DRM starts by pointing the telescope at a reference star to dig the dark hole. The analysis assumes that the telescope reaches a steady state thermal condition at this sun orientation. Next, the telescope is pointed at the science star. To make the analysis worst-case, it is assumed that this requires a ±θ degree pitch away from the sun. To facilitate speckle subtraction, the telescope is rolled ±Φ degrees about the science star vector.

**Predicted LOS Stability Performance**

Mechanical LOS stability performance, the rigid-body motion of the primary and secondary mirrors relative to the tertiary mirror were calculated as a result of the structure’s response from 0 to 350 Hz to the micro-thruster noise specification applied to the structure from 0 to 10 Hz (Figure 10). The specification provides at least a 2X margin at low frequencies and more margin at higher frequencies. Additionally, a MUF of 2 was applied for a total margin of ~4X. Typically the results of this analysis would be presented as a plot of displacement vs frequency because all previous space telescopes used reaction wheels which operate over a range of frequencies. But, HabEx is using microthrusters which are always on and simultaneously excite the structure over the entire frequency range. Therefore, it is necessary to take an extra step and RSS the individual components into a running sum. Figures 11 and 12 shows the cumulative rigid body displacement and rotations for the primary and secondary mirrors.

Table 3 lists the maximum amplitude for each rigid body motion (with MUFs). Collectively, these motions predict an LOS jitter of approximately 0.03 mas which provides a ~10X performance margin against the 0.3 mas (> 10 Hz) specification.

<table>
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<tr>
<th>DOF</th>
<th>Δx (nm)</th>
<th>Δy (nm)</th>
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To predict thermal LOS stability performance, the rigid-body motions of each mirror was calculated for the 250-hr DRM. Figures 13 and 14 show the XYZ rigid body residual displacements of the primary and secondary mirrors, i.e. the amount of thermal rigid body motion that is not corrected by the laser metrology system that senses and controls the optical alignment of the primary and secondary mirrors.

Taking the maximum uncorrectable motion for each rigid-body degree of freedom of the primary and secondary
mirrors predict an LOS thermal drift of less than 0.2 mas (i.e., ~12.5X margin) against the 2.5 mas (< 10 Hz) specification. In this case, no MUF is applied.

**Predicted WFE Stability Performance**

Predicted WFE stability from LOS Jitter as a function of Zernike polynomial is calculated from the predicted PM and SM motions. As expected, the largest LOS errors are tilt, power and astigmatism. But these errors are not significant to the VVC-6. The most significant are trefoil and secondary astigmatism. But, because the LOS jitter is so small, the predicted amplitudes for these errors have >100X margin relative to their error budget allocation (Figure 15).

Inertial WFE instability occurs when the PM is accelerated by mechanical disturbances causing it to react (i.e. bend) against its mounts. Figures 16 illustrate how the mirror bends as it reacts against the hexapod mount for the rocking and bouncing modes.

![Figure 16: Mirror bending from (left) 49.5 Hz Rocking Mode; (right) 50 Hz Bouncing Mode](image)

NASTRAN calculated the displacement of PM surface nodes from 0 to 350 Hz as a function of the micro-thruster noise specification applied to the structure from 0 to 10 Hz. To eliminate rigid body displacements, the node displacements were calculated relative to a fixed surface reference point. The WFE produced by these displacements were fit to Zernike polynomials using SigFit. And, because the microthrusters excite all modes simultaneously, the individual frequencies were RSSed to yield a total accumulated WFE for each Zernike term (Figure 17).

Consistent with mass dampening (i.e., where the mirror has a smaller response at higher frequency accelerations), the non-linear analysis predicts an astigmatism WFE that is 3X smaller, a focus error that is 4X smaller, and a trefoil WFE that is 5X smaller than the simple linear gravity sag scaling approach. Figure 18 shows how the calculated inertial WFE of the primary mirror compares with its simple error budget allocation. As expected Trefoil is the dominant term, but still has 1.6X margin.

Thermal WFE instability was predicted by applying the 250 hr DRM to the integrated model. Thermal Desktop calculated the temperature distribution as a function of time. With this distribution, NASTRAN calculated surface deformations which were then used by SigFit to decompose the temporal WFE into Zernike polynomials as a function of time. Figure 19 shows the predicted change in primary mirror surface figure error decomposed into Zernike polynomials. As symmetric errors, power and trefoil’s changes are caused by the DRM pitch angle, which changes the total solar load on the telescope. And as an asymmetric error, astigmatism’s change is caused by the DRM roll which shifts thermal load from one side to the other.
Total DRM wavefront error was calculated by RSSing the PM and SM Zernike terms as a function of time and selecting the maximum amplitude for each. This analysis has a 3X MUF. Figure 20 shows each Zernike compared to the simple error budget. Obviously, trefoil is a problem. Fortunately there is a solution. Reallocation the error budget.

6. Final Performance Error Budget

The initial error budget (Figure 7) assumed a simple uniform distribution of high-order contrast leakage. But, because some Zernike terms are more likely to occur than others, it is permissible to reallocate contrast leakage from the less likely terms to the more likely terms. Figure 21 shows an optimized error budget for the VVC-6 where the majority of the contrast leakage is allocated to trefoil. The first three data columns input the predicted STOP performance for each error source with its MUF (4X on LOS Jitter and LOS wavefront stability, 2X on inertial WFE stability and 3X on thermal WFE stability). These are RSSed to yield a total RMS WFE for each Zernike term. The VVC-6 Sensitivity column gives how many parts-per-trillion of Raw Contrast error leaks through the VVC-6 coronagraph for a pico-meter of Zernike WFE. The Raw Contrast column gives the predicted leakage for the STOP predicted Zernike WFE. The Allocation column normalizes and redistributes the 30 ppt of allowed raw contrast to maximize the amount allocated to Trefoil. The WFE Tolerance column is the new error budget. This error budget provides a margin of 4.1X for all Zernike. Please note that this error budget is ONLY for the baseline ZeroEdr primary mirror. A different mirror substrate or mount design will require a different error budget. And, the error budget will need to be adjusted for the ‘as-built’ mirror. Also, active WFE control via the ZWFS may add margin.

7. Summary

The Habitable Exoplanet Observatory Mission (HabEx) was studied for the 2020 Astrophysics Decadal Survey. Its goal is to image and spectroscopically characterize planetary systems in around nearby sun-like stars. Critical to achieving the HabEx science goals is a large, ultra-stable UV/Optical/Near-IR (UVOIR) telescope. The desired telescope is a 4-meter off-axis unobscured three-mirror-anastigmatic, diffraction limited at 400 nm with wavefront stability on the order of a few 10s of picometers. The baseline HabEx telescope is designed using standard engineering practice and its design ‘closes’. The telescope’s predicted Structural Thermal Optical Performance (STOP) meets with margin its specified performance error budget allocations for Line of Sight Jitter, LOS Wavefront Error, Inertial WFE and Thermal WFE. Key to meeting its LOS and Inertial specifications is the choice to use micro-thrusters for pointing control instead of reaction wheels. The baseline observatory design fits with margin within the mass and volume constraints of the SLS Block-2 8.4-m fairing.

Acknowledgements

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Figure 20: Estimated PM/SM Thermal WFE.

<table>
<thead>
<tr>
<th>Index</th>
<th>Predicted Performance Amplitude (pm rms)</th>
<th>Total WFE</th>
<th>VVC-6 Sensitivity</th>
<th>Raw Contrast</th>
<th>Allocation</th>
<th>WFE Tolerance</th>
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Figure 21: Optimized Error Budget for VVC-6.
REFERENCES


BIography

H. Philip Stahl, senior optical physicist at NASA MSFC, was the telescope design lead for the HabEx mission concept study. And leads studies to mature mirror technologies for potential large-aperture space telescopes. Previous assignments include developing JWST mirror technology. He is a leading authority in optical metrology, optical engineering, and phase-measuring interferometry. He is a Fellow of OSA, Fellow of SPIE and was SPIE 2014 President. He earned his PhD in optical science at the University of Arizona, Optical Sciences Center in 1985.