MIXING AND HEAT TRANSFER OF AN ARGON ARCJET
WITH A COAXIAL FLOW OF COLD HELIUM

by

Jerry Grey, Peter M. Williams, and David B. Fradkin

prepared for

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

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PRINCETON UNIVERSITY

Department of
Aerospace and Mechanical Sciences
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FINAL REPORT

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I. SUMMARY

The mixing of a subsonic, one-centimeter-diameter argon arcjet with a coaxial flow of cold helium in a 3-inch-diameter duct has been studied visually by schlieren photography and quantitatively with a 0.075-inch-diameter calorimetric and sampling probe. Measurements of temperature, velocity and composition of the mixing field were made for an initially laminar argon jet having a mass flow of 0.3 g/sec, an exit plane peak temperature of 20,000°R., and an exit plane peak velocity of 600 ft/sec. The effects of cold coaxial helium flow velocities of 0, 0.27, and 2.7 ft/sec on jet mixing characteristics were studied, as well as the effect on the flow field of varying the argon jet flow from 0.2 to 1.4 grams per second at a fixed coaxial helium velocity of 0.27 ft/sec.

The data have been correlated with previous experimental and theoretical investigations for a free argon arcjet at similar initial conditions, mixing with stagnant helium at 1 atmosphere. The results are in excellent agreement with this earlier work. The principal effect of the controlled ducted coaxial flow has been to hasten mixing by causing earlier transition of the arcjet to turbulence. The dominant mixing process for both the free and ducted jets was found to be the inflow of helium into the argon jet, the effects of radiation and ionization being negligible. This results from the high specific heat and high diffusion coefficient of helium at arcjet temperatures. In cases where turbulence is present, the dominant mixing process is still the inflow of helium, although the rate of this inflow
is substantially augmented by turbulence.

The experiments with variable argon mass flow showed that at increased argon mass flows the rate of mixing of the jet is retarded, a phenomenon commonly observed in other types of jets.

The results indicate potential feasibility of the coaxial gaseous-core nuclear rocket. The observed mechanism of jet cooling and mixing, which consists principally of an inflow of light helium atoms rather than the dispersion of the heavier argon atoms, is consistent with the requirements for retention of gaseous nuclear fuel in this concept. In the rocket, however, the coaxial light gas velocity is substantially greater than the core velocity, and it is this case which will be investigated in future work with the object of determining whether the light-gas inflow mechanism will continue to be observed under these conditions.

II. INTRODUCTION

A. Purpose

The purpose of this program, as defined in Reference 1, was "to investigate the mixing and heat transfer characteristics of a hot, high-molecular-weight gas jet injected into a bounded annular flow of a surrounding cool, low-molecular-weight gas. Of specific interest are the axial pressure distribution, the effect of outer-stream turbulence on transition of the inner jet, and the effect of heat-release via ion recombination in the inner jet."
In detail, again quoting from Reference 1,

"1. Data from measurements...are for use with an analysis made at NASA Lewis. The system is basically a plasma jet injected into an outer, room-temperature gas.

2. The outer gas shall be of low molecular weight (helium) and the plasma of high molecular weight (argon).

3. The light gas shall be contained within a channel whose diameter is approximately five times that of the plasma.

4. The plasma shall be injected into the light gas at velocities down to the same as that of the light gas, as limited by experimentally obtainable conditions.

5. The results shall be presented as measured values of concentration, temperature, and velocity taken at various radial positions. These radial profiles shall be measured at various distances downstream from the point of injection of the inner gas.

6. The above measurements shall be made over a range of gas flow rates such that Reynolds numbers of the inner stream shall be between 100 and 1,000, and the Reynolds numbers of the outer stream shall be between 50 and 10,000, as limited by experimentally obtainable conditions."

B. Background

Knowledge of the nature of the flow processes occurring in the coaxial-geometry gaseous-core nuclear rocket is required in order to properly evaluate the feasibility of this propulsion concept. Although analytical models and analyses
have been formulated for both laminar\(^3\) and turbulent\(^4,5\) flows, it was necessary to obtain some experimental indication of their validity. The equipment previously developed at Princeton\(^6,7\) for more generalized studies of high-temperature, partly-ionized gas interactions\(^8,9\) appeared to be well suited to this purpose, and with comparatively minor additions and modifications, was adaptable to the purposes described above.

III. DESCRIPTION OF TEST PROGRAM

A. Apparatus

The entire experimental apparatus is diagrammed in Figure 1. It consists of a plasma generator mounted so as to eject a partly-ionized gas jet horizontally into a test chamber, the test chamber itself forming part of a 1,000-gallon tank. For the purposes of these tests, a series of ducts could be mounted which permitted the injection of a coaxial flow of cool gas, concentric with the plasma jet axis. Instrumentation consisted of a schlieren system for visual studies, a calorimetric probe\(^6\) and drive systems suitable for pressure, composition and enthalpy mapping of the entire duct interior, and miscellaneous instrumentation related to the arc generator and duct. Details of each major component are described in the ensuing paragraphs.

1. Plasma Generator

The initial visual studies, as originally planned, were made with a Plasmaflame Model F-80 Arcjet manufactured by Thermal Dynamics, Inc., (Figure 2). This generator
was available at Princeton, and for the purpose of these tests utilized a 3/8"-diameter straight-bore water-cooled nozzle, whose exterior was tapered so as to provide smooth-entry mixing with the annular light-gas flow (Figure 3).

The torch was powered by a marine diesel generator driving four Westinghouse RA-2 rectifiers, one of which was provided with remote current adjustment, having a total DC capacity (after power factor and lead losses) of approximately 75 kw. A water-cooled, copper-tipped prod was used for torch starting, and operation was controlled from a modified Thermal Dynamics console. The torch, nozzle and leads were cooled with 300 psi water from a Pesco gear pump. Calorimetric measurement of the rate of heat extraction from the torch by the coolant was available.

As described below, it was later found visually that the laminar jet obtained with the Thermal Dynamics torch was too unstable for probe profile measurements. A new plasma generator was procured for use in a complementary Air Force research program. This new generator, (Figure 4) manufactured by Creare, Inc., was adaptable to the existing power supply, ducts, and test chamber. Its principal advantages were (a) micrometer adjustment of radial and axial cathode position; (b) a sectioned straight-line nozzle consisting of a series of thin insulated segments, one of which could be grounded so that the anode arc contact point could be pre-selected and maintained. This generator provided excellent
laminar stability under nearly all operating conditions, and was used to collect the probe test data described later.

An adapter and light-gas injection plate compatible with the duct were designed and installed for this generator (Figure 5). The injection plate, which covered the entire duct inlet, was uniformly drilled with small holes to provide approximately uniform flow of the light gas.

The test gases used were argon for the hot gas and helium for the cool gas. Several test runs were also made using nitrogen for the cool gas for reasons to be discussed later.

2. Duct and Test Section

The test section consisted of a rectangular parallelepiped 18" square by 3 feet long, opening into a 1,000-gallon commercial gasoline tank internally braced for vacuum operation (see Figure 6). The test section was equipped with quartz windows for viewing either the open plasmajet exhaust or the duct. The plasma generator and duct were mounted on opposite sides of the test section endplate, as shown in Figure 6, with the duct fully contained within the test section. Two conventional mechanical vacuum pumps connected to the tank could provide test section pressures down to about 1" Hg absolute. The tank pressure was prevented from exceeding one atmosphere (absolute) by a large flapper. A telescope mounted in the far end of the tank, opposite the duct and arcjet, provided capability for viewing the arc during operation.
Three different ducts were used for this test program. A cylindrical Vycor duct (Figure 7) was first constructed to provide visual indication of the nature of the jet mixing region. Although this was suitable for direct viewing, the curvature of the Vycor precluded the use of schlieren photography. Consequently, a metal duct of square cross-section having approximately the same dimensions (3") and fitted with flat quartz windows (Figure 8) was used for photographic recording of the mixing region, as will be described in Section III-B. Correlation between the two ducts is also described later.

Detailed flow-parameter surveys were made in a brass calorimetric duct (Figure 9) designed to provide two-dimensional coverage of the entire duct interior by the calorimetric probe. This duct was water-cooled, permitting measurement of the overall heat transfer to the duct walls.

3. Instrumentation

The two unique items of instrumentation required for the subject program were the schlieren system and the calorimetric probe. Other more or less standard items, which included those necessary for measurements of arcjet power, gas flow rates, tank pressures, etc., are not described in detail here.

(a) Schlieren System

In order to establish the general nature of the flow within the duct (i.e., length of laminar core, location of transition, structure and stability of the laminar core flow,
etc.), the existing schlieren system of Figure 10 was used, together with the flat-sided duct of Figure 8. The system was of standard design, employing parabolic mirrors instead of lenses in order to gain light-path length, and utilizing a BH-6 microsecond spark source with an open-shutter camera in order to obtain sufficient illumination to provide transparency of the intensely luminous arcjet.

The system was adequate to yield good schlieren photographs when the hot argon jet issued into cold nitrogen. The quality was barely adequate, however, when the jet was cooled by helium, since the density of the hot argon was sufficiently close to that of the coaxial helium so that the density gradients were at the limits of the systems resolution.

(b) Calorimetric Probe

The calorimetric probe is an instrument which measures enthalpy, stagnation pressure, and composition of gases at temperatures up to at least 25,000°F. It has been used for some time in arcjet diagnosis, and since it has been described in detail elsewhere, only its general nature is outlined here.

The probe configuration and its associated instrumentation are diagrammed in Figures 11 and 12, respectively. The construction of the probe itself is of copper, with a brass base. Cooling water from a high-pressure source (up to 1,000 psi) enters through the mounting block, passes through the outer
channel to the tip, and leaves via the inner channel. Sheathed, ungrounded thermocouple junctions are located where the probe cooling water flow enters and leaves the sampling tube. A steady flow of sample gas can be drawn by a vacuum pump from the probe tip, through the central tube past a thermocouple junction located in the tube, and then through the support shaft to valving and instrumentation.

The flow of the hot sample gas in the central tube causes the probe cooling water to rise in temperature a greater amount than when the gas sample flow is not permitted to flow through the tube. A flowmeter measures the probe coolant flow and a critical orifice measures the gas flow. These measurements are sufficient to compute the enthalpy of the gas sample at the point where it enters the probe.

The composition of the two-component gas sample is determined by measuring its thermal conductivity in a carefully calibrated commercial cell, and stagnation pressure is measured when the gas sample is not flowing by simply diverting, through appropriate valving, the gas sample line from the vacuum pump to a water manometer. Enthalpy can be converted to temperature, once the gas composition is known, from an equilibrium theory such as the Saha equation. The measured stagnation pressure is converted to velocity using the Bernoulli equation, since the gas Mach number is less than 0.1.

The sensitivity and calibration of the probe under similar experimental conditions have been described elsewhere.
In previous work, energy and mass balances showed that the probe's accuracy (standard deviation from the mean) was about 3 per cent.  

B. Conduct of Tests
1. Visual Studies

The visual studies were undertaken with the dual objective of (a) establishing the general character of the jet mixing as a guide to the ensuing probe measurements, and (b) establishing that the jet was sufficiently stable and uniform that worthwhile and reproducible probe data could be obtained. Findings in accordance with this latter objective resulted in postponing the probe measurements until the new Creare plasma generator could be installed, as was described previously. The majority of the visual experiments were made with the Thermal Dynamics torch, and although the flame was not sufficiently steady for detailed probing, it was satisfactory from the standpoint of establishing the general nature of the flow.

The first series of visual studies was made in the round Vycor duct, and data were obtained using both helium and nitrogen as the coaxial gas. The conduct of the experiments was generally the same for both gases. The test chamber and the 1000-gallon exhaust tank were evacuated to about 1/5 atmosphere, since it was found experimentally that longer laminar flames, and thus greater flame length differences, could be obtained at reduced pressure. It was believed that this would not invalidate the visual data, since the purpose
of the visual study was only to establish trends to be later verified by probe measurements at one atmosphere.

Once the proper test chamber pressure was established, the plasma generator was started and adjusted to produce as long a laminar flame as possible. Most of these tests were run with an argon flow of about 100 SCFH at a net plasma generator power of about 19 kw.

With the arcjet thus adjusted, observations were made of the character of the jet for different coaxial gas velocities. The typical observation procedure was to first observe the flame with no coaxial gas flow, and record the full length of the laminar portion of the jet. The coaxial flow was then initiated, and the new length of the laminar portion of the jet was observed, together with the flow rate of the coaxial gas. Observations were continued at increasingly higher coaxial flows until the laminar jet disappeared and turbulence was observed at the nozzle exit plane.

These visual observations were made with the aid of schlieren photography, to define as nearly as possible the exact length of the laminar jet. Figure 13 is a schlieren photograph illustrating a typical laminar arcjet and its transition to turbulence in a free environment. Figure 14 is a schlieren photograph of laminar and turbulent jets taken through the windows of the square three-inch duct. Although the quality of these latter photographs is not as good as for the free jet, the difference between laminar and turbulent flows can be clearly distinguished. Note from
Figure 14 that turbulence can exist right at the nozzle exit plane.

As stated previously, schlieren photographs could not be taken through the round duct. The photographs taken in the square duct were therefore used to confirm the round-duct visual observations. Data were taken with both helium and nitrogen coaxial flows, in both round and square ducts, and also with a free jet in nitrogen.

2. Detailed Surveys

The probe measurements were conducted in the calorimetric duct of Figure 9. Radial profile measurements were taken at the exit plane at quarter-inch intervals to the point at which the jet had become fully turbulent and full mixing of the arcjet with the coaxial gas flow had been completed.

Profile data were taken under the following initial conditions for the argon jet:

- Plasma generator power: 14 kw
- Argon Mass Flow Rate: 0.323 qm/sec
- Jet Temperature at Nozzle Exit*: 20,000°R
- Initial Jet Velocity*: 600 ft/sec
- Coaxial Helium Velocity: 0, 0.27, and 2.7 ft/sec

A second series of runs was taken at an axial station 1 inch downstream from the nozzle with a coaxial

*Typical centerline values. Profile data given later provide exact initial condition.
helium flow of 0.27 ft/sec and a variable argon flow between 0.24 and 1.34 gm/sec.

IV. DISCUSSION OF RESULTS

A. Visual Studies

The quantitative results of the visual studies are summarized in Figures 15 and 16, in which the length of the laminar jet is plotted against Reynolds number and velocity, respectively. The region of interest in these figures was originally concentrated on axial locations greater than six inches, because transition to turbulence was not expected to occur much upstream of this location, and the calorimetric probe, which was used to diagnose the jet in the region near the nozzle exit, is a more reliable measurement. This was particularly true in the case of coaxial helium flow, since the high luminosity of the first few inches of the jet precludes precise visual observations.

It is quite apparent from the visual results that the laminar arcjet is very easily disturbed by the coaxial flow, with the laminar jet being shortened to less than six inches at coaxial velocities of only one foot per second. Although some disturbance of the jet by the coaxial flow had been anticipated, it had not been expected that such small velocities would be so significant. This led to closer investigation of the coaxial gas character, and it was observed that the coaxial gas was introduced with considerable initial turbulence, as shown in schlieren photograph of Figure 17.
The quantitative effect of this initial turbulence on producing transition in the laminar jet is discussed later (Section IV-C) in connection with results of the calorimetric probe measurements.

B. Detailed Mapping of Flow Field

Verification of the general nature of the visual study results, as well as quantitative mixing characteristics, were established with the calorimetric probe, covering the region from the nozzle exit plane to the downstream point at which the initial jet had become fully turbulent. Results are summarized in Figures 18 through 21, which show jet centerline values of temperature, velocity, composition, and enthalpy respectively, and in Figures 22 through 27, illustrating radial temperature, velocity, and composition profiles at various axial stations. Also shown on certain of these figures are both theoretical and experimental data on the mixing of a free jet. (The free jet work was performed under the Air Force contract identified previously, but the results reported here are helpful as an aid to the understanding of the duct mixing.)

From the centerline data of Figures 18, 19 and 20, it can be seen that the rapidity of mixing, as evidenced by the rate of decay of the centerline values of temperature, velocity and composition, is strongly influenced by the velocity of the coaxial gas flow, as was indicated by the visual studies discussed above. When the coaxial gas flow was 2.7 ft/sec, mixing was fully accomplished at one inch, or about three jet diameters downstream. At a velocity of 0.27 ft/sec, complete mixing was not accomplished for three inches, or eight diameters downstream.
In the case of no coaxial flow in the duct, as well as in the unbounded jet, mixing was still not completed six inches (about 20 diameters) downstream.

In the case of the free jet, as well as in that for the ducted jet with no coaxial flow (except for Figure 20, which is discussed below), not only did the data indicate confirmation of the visual observations, (i.e., that the jets remained laminar in the region surveyed by the probe) but there was also rather close agreement with laminar mixing theory. These results are in good agreement with studies of laminar mixing of a free arcjet completed recently\(^{10}\). With the free laminar jet it was found that the flow of helium into the jet was the dominant mechanism for jet cooling and mixing, and that the effects of radiation and ionization were negligible. This experimental result, accurately predicted by the laminar mixing theory, is attributed to helium's high specific heat and high diffusion coefficients at arcjet temperatures. This mechanism was also experimentally indicated in the coaxial studies, and accounts for the similarity between the free and ducted cases at 0.27 ft/sec coaxial flow in the laminar flow region within one or two diameters (1/2 to 1 inch) of the nozzle exit plane.

Direct similarities in this region between the free jet (or the no-coaxial-flow ducted case) and the high-coaxial-flow case (2.7 ft/sec) were, on the other hand, not observed, obviously because of the early transition to turbulence indicated by Figures 15, 18, 19, and 20.
The large difference in helium concentration data between the no-coaxial-flow ducted case and the others, as shown in Figures 20, 22, 23, etc., also has a simple explanation. In this case, the equilibrium concentration of cold helium in the duct is less than 20 per cent (see Figures 22, 23, 24) because most of the helium originally present is very swiftly swept out with the argon jet, and the ambient conditions are therefore substantially different than for the free jet or the higher coaxial-flow ducted cases. On the other hand, helium concentration data for the 0.27 ft/sec ducted coaxial flow, before turbulence is initiated, were found to be essentially similar to those of the free jet case because an ample supply of cold helium was always available at the jet boundary.

Considerable insight into the mechanism of mixing is obtained by consideration of enthalpy rather than temperature decay. Although the various cases differ widely in terms of temperature, velocity and species concentration, a plot of centerline enthalpy (Figure 21) indicates that the basic mixing process is the same in all cases. In this figure, it is shown that the centerline enthalpy decay coincides closely for all coaxial gas flows. Thus it is necessary to conclude that radiation and ionization effects are negligible, since reference to Figure 18 shows that at even small distances from the nozzle, the jet temperatures differ by many thousands of degrees. For example, at one inch from the nozzle, the
temperatures of the jets which were still laminar were about 11,000°R, while that of the turbulent jet, in which mixing was substantially complete, was only 1,000°R; still, the enthalpies at the centerline were nearly equal. Clearly, if radiation and ion recombination effects were important mechanisms for jet power loss, the higher-temperature jets should show lower enthalpies. Furthermore, if there were substantial dispersion of the argon jet, the centerline enthalpy of the well-mixed case should be substantially less.

The results of Figure 21 therefore indicate that the principal mechanism for energy transfer (jet cooling) is the inflow of coaxial helium rather than either the direct loss of energy (by radiation or recombination) or the outflow of argon from the core jet.

It may be concluded that while turbulence (of the degree present in these experiments) substantially increases the rate of jet mixing, the effect of the turbulence is to aid the inflow of coaxial helium and not to disperse the argon jet itself.

C. Effects of Turbulence

The very large effect of turbulence on the rate of mixing, in that an apparently small disturbance can cause the jet to lose its initially laminar characteristics, is a prominent result of the experimental program.

Unfortunately, understanding of turbulent jet mixing and the factors causing arcjet turbulence, like all turbulent phenomena, suffers from the fact that present theories of
turbulence are inadequate, and most information on turbulence is empirical. The general character of the observed behavior is consistent with other forms of turbulent-flow experience, however, as is indicated by the summary of results (observed from both the visual and probe studies) in Table I. In this table, Reynolds numbers more than one diameter downstream are based on the length of jet at the point of observation rather than on the jet diameter. The initial Reynolds number (at the nozzle exit) is based on jet diameter, and is 450 for all cases.

Table I shows that transition to turbulent flow did not occur in the free jet until a Reynolds number of 10,000 was reached, while very small disturbances, such as convective currents resulting from the simple presence of the duct* or from very small coaxial flows, caused transition at Reynolds numbers of 4,000 and 3,000 respectively. Furthermore, a coaxial flow of only 2.7 feet per second of helium produced transition in less than one jet diameter from the exit plane at a Reynolds number of only 450.

*The convective turbulence caused simply by the presence of the duct was evidenced by visually-observed motion of dust particles, and has also been observed in combustion experiments where the flow conditions were similar.11
TABLE I

Effect of Test Conditions on Reynolds Number at Transition

<table>
<thead>
<tr>
<th>TEST CONDITIONS</th>
<th>APPROXIMATE LAMINAR JET LENGTH, INCHES</th>
<th>APPROXIMATE REYNOLDS NUMBER AT TRANSITION</th>
</tr>
</thead>
<tbody>
<tr>
<td>Free jet, 1 atm, no coaxial flow</td>
<td>18</td>
<td>10,000</td>
</tr>
<tr>
<td>Ducted jet, 1 atm, no coaxial flow</td>
<td>5</td>
<td>4,000</td>
</tr>
<tr>
<td>Ducted jet, 1/5 atm, no coaxial flow</td>
<td>18</td>
<td>4,000</td>
</tr>
<tr>
<td>Ducted jet, 1 atm, 0.27 ft/sec coaxial He</td>
<td>2</td>
<td>3,000</td>
</tr>
<tr>
<td>Ducted jet, 1 atm, 2.7 ft/sec coaxial He</td>
<td>1/2</td>
<td>450</td>
</tr>
</tbody>
</table>

It should be remarked that only by basing the Reynolds number on a linear dimensional quantity can transition data be obtained which are consistent with the general range in which it is usually observed. Reynolds numbers based on the jet diameter remained nearly constant at about 500 for all types of flow observed, and therefore are not useful as a guide to transition predictions.

On the basis of the above results, it is believed that in any practical propulsion device it would be impossible to maintain laminar flow for more than a few nozzle diameters. These devices should therefore be designed to operate in the turbulent mode.
D. Variation of Mass Flow in Core Jet

Figures 27 through 29 are profiles of temperature, velocity, and composition respectively at one inch downstream from the nozzle exit plane when the argon jet mass flow was varied from 0.24 to 1.34 g/sec while the coaxial helium flow was maintained at 0.27 ft/sec. It can be concluded from the general shape of the profiles that spreading and mixing were little affected, although a wide variation of mass flow was experienced. The plasma generator efficiency is significantly augmented by increased mass flows, and this results in the higher temperatures and velocities observed at the high mass flows. The plots do not indicate which profiles represent laminar flows and which represent turbulent flows, but based on visual observations the profiles at the higher mass flows are likely to be turbulent. It is a tentative conclusion, which must be examined by additional work, that high mass flow rates tend to reduce jet mixing over a given distance, even though turbulence may be present. This is, of course, similar to the phenomena observed in more familiar types of jets.

V. CONCLUSIONS

1. Up to about three jet diameters downstream from the nozzle exit plane there is little difference between the experimental laminar mixing characteristics of a free jet and a bounded jet when the coaxial flow of helium in the duct is sufficient to provide similar ambient helium con-
centrations, but not so large as to disturb the laminar character of the jet. In this region a theoretical analysis for a laminar free jet is also applicable to a similar ducted jet.

2. Very low velocities of an initially turbulent coaxial flow were sufficient to cause transition in an initially laminar core jet, and increases in coaxial gas velocities produced earlier transition to turbulence.

3. Mixing of the jet was very rapid once turbulence was initiated, and in one case (the highest coaxial velocity tested) complete mixing of the jet was accomplished in less than three jet diameters from the nozzle exit.

4. With increased core-jet mass flow, mixing of the jet at three diameters downstream was diminished, even though the jet may have become turbulent. This is, of course, similar to the phenomena observed in more familiar types of jets.

5. The most significant process in the mixing of either a free or a ducted laminar argon arcjet was found to be the flow of helium into the jet, the effects of radiation and ionization being negligible. This behavior results from helium's high specific heat and high diffusion coefficient at arcjet temperatures. The principal effect of turbulence, in the scale studied in the present experiments, was to cause augmentation of the helium inflow rather than dispersion of the jet.

6. An arcjet Reynolds number based on length rather than diameter was most useful in correlating the onset of turbulence, in accordance with conventional laminar free-jet practice.
7. Owing to the difficulty of obtaining and maintaining stable laminar jets, turbulent models should be used in the design of practical propulsion devices.

8. The results indicate potential feasibility of the coaxial flow, gaseous-core nuclear rocket concept, since it was found that the argon arcjet decayed as a result of inflow of cool coaxial helium rather than dispersion of the argon core, even when turbulent mixing was significant. Before this conclusion can be applied to the coaxial gaseous-core rocket, however, it will be necessary to examine the mixing mechanism for coaxial gas velocities up to one or more orders of magnitude greater than the core jet velocity. This study is planned under a subsequent NASA contract.
REFERENCES


FIGURE 1

DIAGRAM OF APPARATUS

KEY

T = TEMPERATURE
P = PRESSURE
m = MASS FLOW RATE
k = THERMAL CONDUCTIVITY
V = VOLTAGE
A = CURRENT

VACUUM PUMP

1000-GALLON LOW-PRESSURE TANK

PROBE COOLANT SYSTEM

PROBE DRIVE

STEEL VIEWING CHAMBER

TORCH

TORCH COOLANT SUPPLY

40 V 3000 AMP DC POWER

ARGON SUPPLY

HELIUM SUPPLY

VACUUM PUMP

JET
FIGURE 2

THERMAL DYNAMICS F-80 ARCJET TORCH WITH SWIRL PLATE AND CATHODE
FIGURE 3

TORCH BODY

NOZZLE RETAINING NUT

NOZZLE

30°

ANODE REGION

WATER COOLANT

.375"

.540"

NOZZLE-ANODE USED WITH F-80 ARCJET TORCH
FIGURE 7

VIEW OF ROUND VYCOR DUCT USED FOR VISUAL COAXIAL-FLOW TRANSITION STUDIES
FIGURE 8

VIEW OF SQUARE DUCT USED FOR COAXIAL-FLOW TRANSITION STUDIES BY SCHLIEREN PHOTOGRAPHY
VIEW OF CALORIMETRIC DUCT USED FOR DETAILED COAXIAL-FLOW MIXING AND HEAT TRANSFER MEASUREMENTS
FIGURE II

DIAGRAM OF CALORIMETRIC PROBE

WATER IN

THERMOCOUPLE LEADS

GAS SAMPLE TO FLOWMETER

WATER OUT

WATER IN THERMOCOUPLE

PROBE BASE

"GAS SAMPLE OUT" THERMOCOUPLE

HOT (UNKNOWN) GAS

.075"

WATER OUT THERMOCOUPLE

FIGURE II
FIGURE 12

Diagram of instrumentation used with tare-measurement calorimetric probe to measure enthalpy, velocity and gas composition.

- Gas Sample Tube
- Water Manometer
- Manometers
- Hot Gas Probe
- Valves
- Test Environment
- Laboratory Environment
- Choked Orifice
- Vacuum Pump
- Constant Temperature Oil Bath
- Gas Composition Analysis (Steady Flow)

Note: Probe thermocouples and probe coolant flowmeter not shown (see Fig. 11).
LAMINAR AND TRANSITION

SCHLIEREN PHOTOGRAPHS OF A FREE ARGON ARCJET IN NITROGEN

FIGURE 13
SCHLIEREN PHOTOGRAPHS OF ARGON ARCJET IN NITROGEN IN 3 INCH SQUARE DUCT (3/8" DIAMETER NOZZLE - 1 ATMOSPHERE)

FIGURE 14
FIGURE 15

VISUAL LENGTH OF LAMINAR ARCJET VERSUS COAXIAL-FLOW REYNOLDS NUMBER

REYNOLDS NUMBER OF COAXIAL GAS

NOTE: REYNOLDS NUMBER BASED ON ANNULUS DIMENSION

NITROGEN, 3 in. SQUARE DUCT
NITROGEN, NO DUCT
NITROGEN, 3 in. ROUND DUCT
HEL IUM, 3 in. ROUND DUCT

VISUAL LENGTH OF LAMINAR JET FROM NOZZLE EXIT PLANE, (INCHES)
FIGURE 16

VISUAL LENGTH OF LAMINAR ARCJET VERSUS COAXIAL-FLOW VELOCITY

VELOCITY OF COAXIAL GAS FLOW, FT/SEC

VISUAL LENGTH OF LAMINAR JET FROM NOZZLE EXIT PLANE, INCHES

NITROGEN, 3 IN ROUND DUCT

HELIUM, 3 IN ROUND DUCT
SCHLIEREN PHOTOGRAPHS SHOWING SCALE OF TURBULANCE
IN COAXIAL HELIUM FLOW
(HELIUM VELOCITY 0.6 FT/SEC)

FIGURE 17
FIGURE 20

CENTERLINE HELIUM CONCENTRATION VERSUS AXIAL POSITION
FIGURE 21

CENTERLINE ENTHALPY VERSUS AXIAL POSITION

HELium VELOCITY = 0.27 FT/SEC

HELium VELOCITY = 2.7 FT/SEC

ZERO HELIUM VELOCITY

DISTANCE FROM NOZZLE EXIT PLANE, INCHES

CENTERLINE ENTHALPY' BTU/LB

5000
4000
3000
2000
1000
0
Temperature, velocity and composition profiles at nozzle exit plane

Figure 22
TEMPERATURE, VELOCITY AND COMPOSITION PROFILES AT 1/2 INCH DOWNSTREAM FROM NOZZLE EXIT PLANE

FIGURE 23
TEMPERATURE, VELOCITY AND COMPOSITION PROFILES AT 1 INCH DOWNSTREAM FROM NOZZLE EXIT PLANES

FIGURE 24
TEMPERATURE, VELOCITY AND COMPOSITION PROFILES AT 2 INCHES DOWNSTREAM FROM NOZZLE EXIT PLANE
TEMPERATURE, VELOCITY AND COMPOSITION PROFILES
AT 3 INCHES DOWNSTREAM FROM NOZZLE EXIT PLANE

FIGURE 26
TEMPERATURE, VELOCITY AND COMPOSITION PROFILES AT 5 INCHES DOWNSTREAM FROM NOZZLE EXIT PLANE

FIGURE 27
TEMPERATURE PROFILE AT ONE INCH DOWNSTREAM FROM NOZZLE EXIT PLANE FOR VARIABLE ARGON FLOW (HELIUM VELOCITY = 0.27 FT/SEC)

FIGURE 28
ARGON FLOW RATES
(gm/sec)

- 0.365
- 0.405
- 0.283
- 0.323
- 0.242
- 0.565
- 1.34

VELOCITY PROFILE AT ONE INCH DOWNSTREAM FROM NOZZLE EXIT PLANE FOR VARIABLE ARGON FLOW
(HELIUM VELOCITY = 0.27 FT/SEC)

FIGURE 29
FIGURE 30

COMPOSITION PROFILE AT ONE INCH DOWNSTREAM FROM NOZZLE EXIT PLANE FOR VARIABLE ARGON FLOW
(HELIUM VELOCITY = 0.27 FT/SEC)
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